

# Adapting the Chumbley Score to Bullet Striations

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# Objective and Motivation

- ▶ Same Source Matching of Bullet lands
- ▶ Evaluate performance of Chumbley Score method when used for Bullet Striations
- ▶ Bullet striations have curvature, not present in toolmarks
- ▶ Identify Error rates and effect of different parameters on them  
(In short finding the best error rates possible )

## Structure

- ▶ Data being used
- ▶ What is the Chumbley Score Method?
- ▶ Identifying Best parameter Settings for Bullets
- ▶ Modifications to the Algorithm
- ▶ Results using Hadler and Morris [2017] method and results using Modified method

# Variations of Chumbley score method and Error Rates for toolmarks

Research paper	Method	Data Source	False Positives	False Negatives
<b>Faden et al. [2007]</b>	Maximized Correlation	Screwdrivers	-	-
<b>Chumbley et al. [2010]</b> (Same-Surface Same-Angle)	Randomized Chumbley Score	Screwdrivers	2.3%	8.9%
<b>Grieve et al. [2014]</b>	Randomized Chumbley Score	Slip-joint	-	-
<b>Hadler and Morris [2017]</b> (Same-Surface Same-Angle)	Deterministic Chumbley Score	Screwdrivers	0%	6%

Table 1: Error Rates for Toolmarks using variations of the chumbley score method

# Digitized Striation Marks

- ▶ Data
  - ▶ Ruger P85s Bullet Lands, or Hamby scans (Hamby et al. [2009]) provided by NIST (85,491 comparisons)
  - ▶ Bullet striation marks  $\approx 2\text{mm}$
  - ▶ Screwdriver marks  $\approx 7\text{mm}$  (all chumbley score papers)
- ▶ Let  $x(t_1)$ ,  $t_1 = 1, 2, \dots T_1$  and  $y(t_2)$ ,  $t_2 = 1, 2, \dots T_2$  be two digitized marks (where  $T_1$  and  $T_2$  are not necessarily equal).
- ▶  $T_1$  and  $T_2$  are the final pixel indexes of each marking. Therefore give the respective lengths of the markings.
- ▶ Signatures/ Profiles (NIST- Hamby)  $\approx 1200$  pixels (2 mm)  
Screwdriver toolmarks (Chumbley Papers)  $\approx 9000$  pixels (7 mm)

# Chumbley Score

## Step 0 : Defining a coarseness parameter

- ▶ Used to remove drift and (sub)class characteristics from individual markings
- ▶ Lowess or Loess fit residuals = Signatures
- ▶ Removes topographic structure (curvature)
- ▶ Improve the signal to noise Ratio

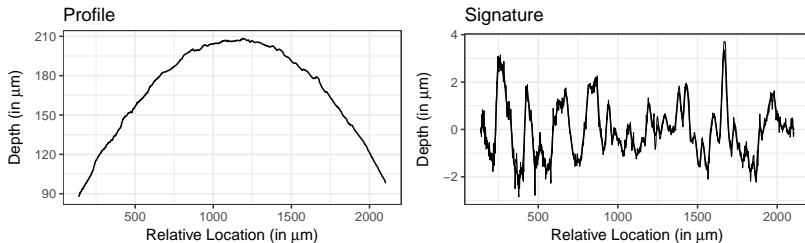


Figure 1: Bullet land profile (left) and the corresponding signature (right).

# Algorithm

- ▶ Two steps: Optimization (1<sup>st</sup>) and Validation (2<sup>nd</sup>).
- ▶ Windows  $\implies$  short segments of the markings
  - ▶ Have *predefined sizes*. ( $T_1$  or  $T_2 \gg w_o$  &  $w_v$ )
    1.  $w_o$  used in the Optimization step
    2.  $w_v$  used in the Validation step

## Optimization step

- ▶ **Goal** :Align markings horizontally as best as possible
- ▶ Correlation Matrix of all possible windows of size  $w_o$  between  $x(t_1)$  and  $y(t_2)$  computed
- ▶ *Identify lag for horizontal alignment*

Window Pair with maximized correlation  $\implies$

Optimal vertical (in-phase) shift of  $t_1^o - t_2^o$

- ▶ For aligning the two markings.

$$(t_1^o, t_2^o) = \arg \max_{1 \leq t_1 \leq T_1, 1 \leq t_2 \leq T_2} \text{cor}(x^{w_o}(t_1), y^{w_o}(t_2))$$

where  $t_1^o, t_2^o$  are the respective starting points of  $w_o$  in  $x(t_1)$  and  $y(t_2)$

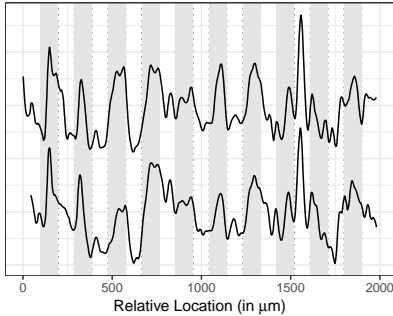
- ▶ Let  $t_1^*$  and  $t_2^*$  be relative optimal locations, where  $t_i^* = t_i^o / (T_i - w_o)$  for  $i = 1, 2$ , such that  $t_1^*, t_2^* \in [0, 1]$ .
- ▶ Once (sub-)class characteristics are removed, these locations have uniform distribution in  $[0, 1]$

## Validation Step

- ▶ Two sets of windows of size  $w_v$  chosen from both markings (see Figure 2)
- ▶ First set or **Same Shift**
  - ▶ pairs of windows are extracted from the two markings using the optimal vertical shift.  $t_1^o - t_2^o$
- ▶ Second set or **Different Shift**
  - ▶ the windows are extracted using a different (out-of-phase) shift.

# In-phase and Out-of-phase

In-phase sample



Out-of-phase sample

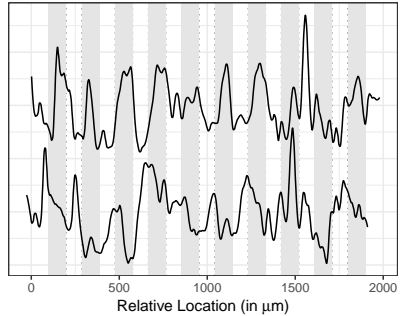


Figure 2: Two markings made by the same source. For convenience, the markings are moved into phase on the left and out-of phase on the right. In-phase (left) and out-of-phase (right) samples are shown by the light grey background. The Chumbley-score is based on a Mann-Whitney U test of the correlations derived from these two sets of samples.



- ▶ Both same- and different-shift pairs correlations between the markings are calculated.
- ▶ For Same-Source markings, correlations
  - ▶ for the in-phase shift should be high
  - ▶ for out-of-phase shift should be low.
    - ▶ Provide a measure for the base-level correlation to which in-phase shift correlations can be compared.
- ▶ The Chumbley score is the Mann Whitney U statistic computed by comparing between in-phase sample and out-of-phase sample.

# Block Diagram

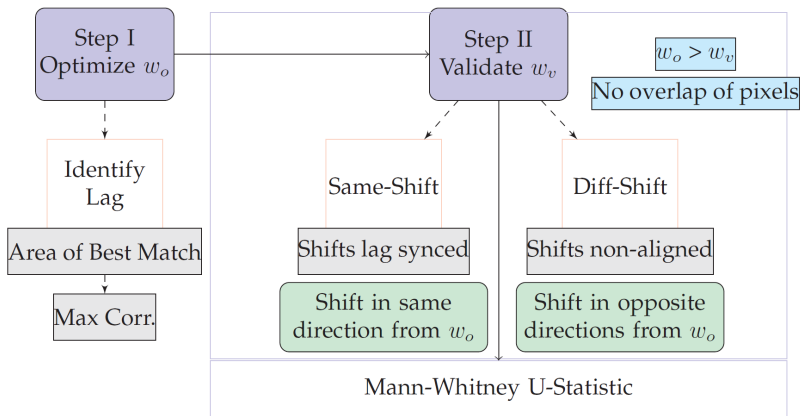


Figure 3: An overview of the adjusted chumbley score method as given by Hadler and Morris [2017]

## Starting Points

More precisely, let us define starting points of the windows of validation  $s_i^{(k)}$  for each marking  $k = 1, 2$  as

$$s_i^{(k)} = \begin{cases} t_k^* + iw_v^* & \text{for } i < 0 \\ t_k^* + w_o^* + iw_v^* & \text{for } i \geq 0, \end{cases} \quad (1)$$

for integer values of  $i$  with  $0 < s_i^{(k)} \leq 1 - w_v^*$

# The Hadler and Morris [2017] method (CS1)

- ▶ Same-shift pairs of length  $w_v$  are all pairs that start in:

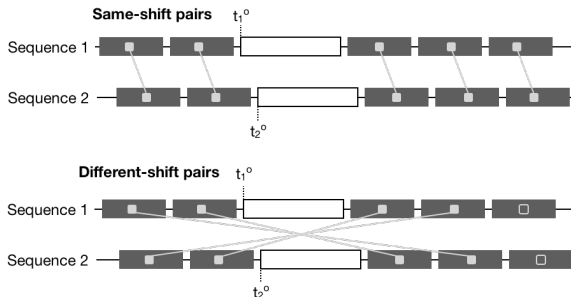
$$(s_i^{(1)}, s_i^{(2)}) \quad \forall i \in \mathbb{Z}$$

for which both  $s_i^{(1)}$  and  $s_i^{(2)}$  are defined.

- ▶ Different-shift pairs are defined as

$$(s_i^{(1)}, s_{-i-1}^{(2)}) \quad \forall i \in \mathbb{Z}$$

where both  $s_i^{(1)}$  and  $s_{-i-1}^{(2)}$  are defined (see fig. 4).



# Failed Tests

- ▶ By definition (equation 1), some number of tests fail to produce a result
- ▶ Either because the number of eligible same-shift pairs is 0, or the number of different-shift pairs is 0.
- ▶  $t_1^o, t_2^o$  not necessarily independent
  - ▶ **same-source:** Assume high dependence,  $\text{corr}(t_1^o, t_2^o) \approx 1$ 
    - ▶ Example:  $w_o = 120$ , coarseness ( $c$ ) = 0.3,  $\text{corr}(t_1^o, t_2^o) = 0.85$
  - ▶ **diff-source:** Assume independence of  $t_1^o, t_2^o$ 
    - ▶ Example:  $w_o = 120$ , coarseness ( $c$ ) = 0.3,  $\text{corr}(t_1^o, t_2^o) = 0.12$

## Failure Rate

$$P\left(t_1^o < w_v \cap t_2^o > T_2 - w_o - w_v\right) + \\ P\left(t_1^o < T_1 - w_o - w_v \cap t_2^o < w_v\right).$$

# Same-shift failure

- ▶ Same-source  $\approx 0$
- ▶ Different-source  $\approx 2 P(t_i < w_o)^2 = \frac{2w_v^2}{(T_1 - w_o)(T_2 - w_o)}$

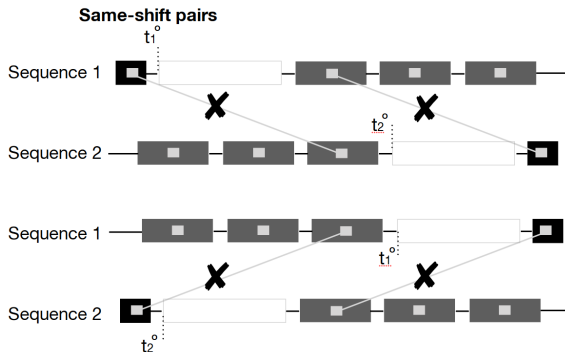


Figure 5: Sketch of same-shift pairings (top) when the lag is too large to accomodate a a vaildation window in either of the two signatures

# Different-Shift Failure

► Same-source (Assuming  $t_1^o \approx t_2^o \approx 2w_v/(T_i - w_o)$ )

$$P(t_1^o < w_v \cap t_2^o < w_v) + P(t_1^o < w_v \cap t_2^o < w_v) = 2P(t_o^1 < w_v)$$

► Different-source  $\approx 2P(t_i < w_o)^2 = \frac{2w_v^2}{(T_1 - w_o)(T_2 - w_o)}$

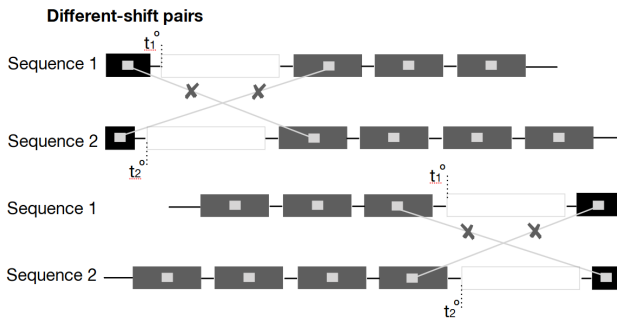


Figure 6: Sketch of diff-shift pairings (top) when the number of diff-shift computations is likely to 0

# Proposed Modification

- ▶ Failures due to missing Same-shift pairs unavoidable
- ▶ Failures due to missing different-shift pairs preventable

Define same-shift pairs identical to Hadler and Morris [2017] as pairs

$$(s_i^{(1)}, s_i^{(2)}) \quad \forall i \in \mathbb{Z}$$

where the boundary conditions of both sequences are met simultaneously.

- ▶ Let us assume that this results in  $I$  pairs.
- ▶ Let  $s_{(j)}^{(k)}$  to be the  $j$ th starting location in sequence  $k = 1, 2$ ,  
i.e.  $s_{(1)}^{(k)} < s_{(2)}^{(k)} < \dots < s_{(I)}^{(k)}$ .



We then define the pairs for different-shifts as

$$\left(s_{(j)}^{(1)}, s_{(l-j+1)}^{(1)}\right) \text{ for } j = \begin{cases} 1, \dots, l & \text{for even } l \\ 1, \dots, (l-1)/2, (l-1)/2 + 2, \dots, l & \text{for odd } l \end{cases} \quad (2)$$

- ▶ For an odd number of same-shift correlations
  - ▶ We skip the middle pair for the different-shift correlations (see fig. 7).
- ▶ This pairing ensures that the number of different-shift pairings is the same or at most one less than the number of same-shift pairings in all tests.

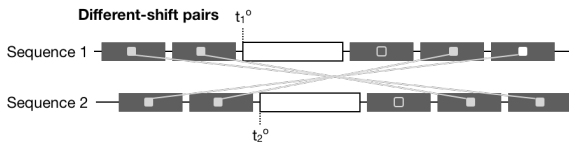


Figure 7: Sketch of adjusted different-shift pairings. At most one of the same-shift pairings can not be matched with a different-shift pair.

# Case where CS1 fails but CS2 does not fail

**CS1** Hadler and Morris [2017] algorithm

**CS2** the suggested modified algorithm

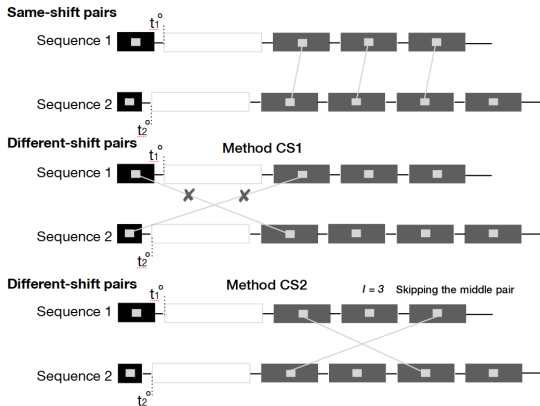


Figure 8: Sketch of a case where CS1 fails but CS2 does not fail

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