

Answer the questions in the spaces provided on the question sheets. If you run out of room for an answer, continue on a separate sheet of paper.

1. Using set-builder notation, give formal descriptions of the following sets:

(a) The set of positive integers that are even.

(b)  $\{ -2, -1, 0, 1, 2 \}$

(c)  $\{ 3, 6, 9, 12, \dots \}$

(d)  $\{ -3, -1, 1, 3, 5, 7, 9 \}$

(e)  $\{ 0, 10, 20, 30, \dots, 1000 \}$

\*(f) The power set of  $X$ , denoted  $P(X)$ .

2. State the cardinality of the following sets:

(a) Question 1, part (a)

(b) Question 1, part (b)

(c) Question 1, part (d)

(d) Question 1, part (e)

(e) Question 1, part (f)

Consider the following sets:

$$A = \{ 2, 4, 6, 8 \}$$

$$B = \{ x \in \mathbb{Z} : x \% 2 = 0 \wedge 0 < x < 10 \}$$

$$C = \{ x \in \mathbb{Z} : x \% 2 = 0 \wedge 0 < x \leq 10 \}$$

3. Indicate whether each statement about the sets  $A$ ,  $B$  and  $C$  is true or false.

(a)  $A \subseteq B$

(b)  $A \subset B$

(c)  $A \subseteq C$

(d)  $A \subset C$

(e)  $C \subseteq B$

(f)  $A = C$

(g)  $A = B$

4. Using roster notation, give formal descriptions of the following power sets:

(a)  $P(A)$

(b)  $P(B)$