Performance analysis

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Performance analysis

- how do we reason about parallel algorithms?
- how can we compare two algorithms and determine which is better?
- how do we measure improvement?

Performance metrics

- execution time (T_p)
- speedup (S)
- efficiency (E)
- cost (C)

Execution time

Serial (T_s)

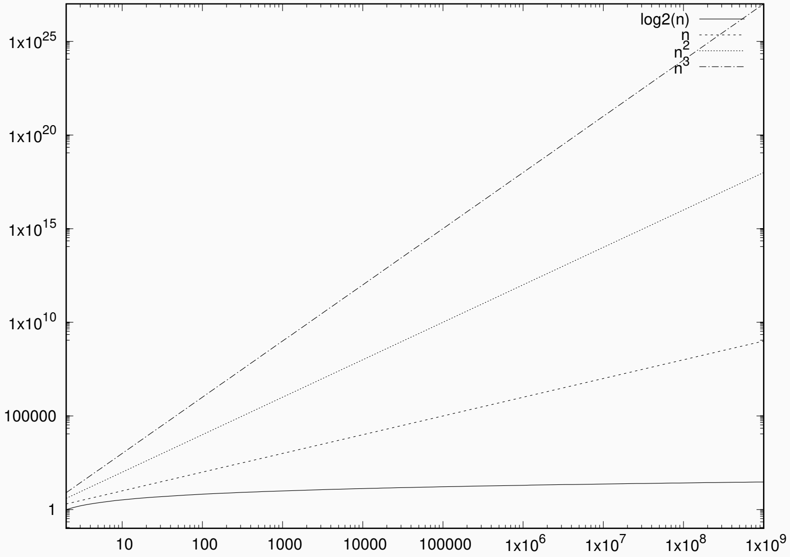
- time elapsed between beginning and end of execution

Parallel (T_p)

- time elapsed between beginning of execution and the moment the last processing element finishes execution

- Adding numbers
- Dot-product
- Matrix-vector multiplication
- Matrix-matrix multiplication

Execution time



Speedup

Speedup ($S = T_s/T_p$)

- the ratio of time taken to solve a problem on a single processing element to the time required to solve the same problem on a parallel computer with p processing elements

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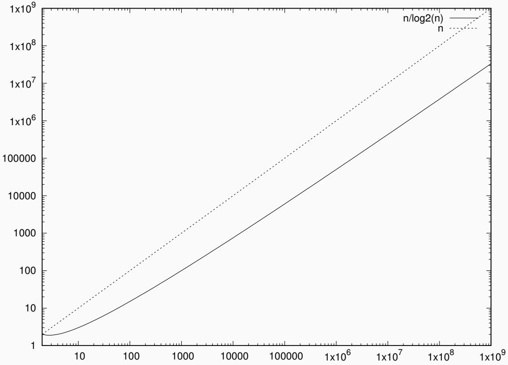

Efficiency

Efficiency ($E = S/p$)

- the ratio of speedup to the number of processing elements — the fraction of time for which a processing element is usefully employed

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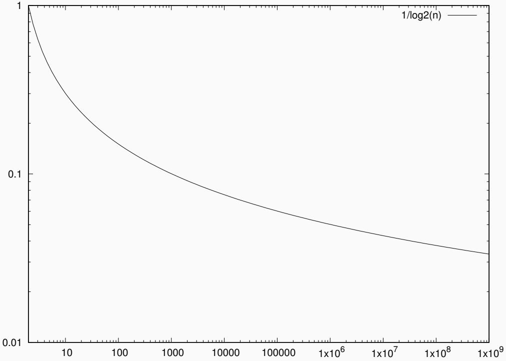

Cost

Cost ($C = pT_p$)

- the sum of the time spent by all processing elements solving the problem
- *cost optimal* if $C = T_s$

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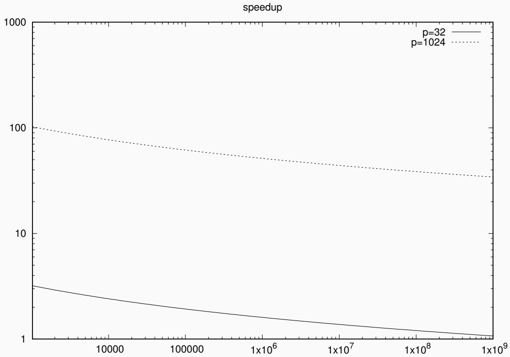
speedup
1x10^6
1x10^7
1x10^8
1x10^9
p=32
p=1024