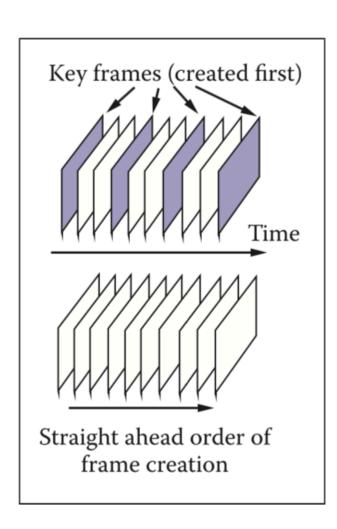
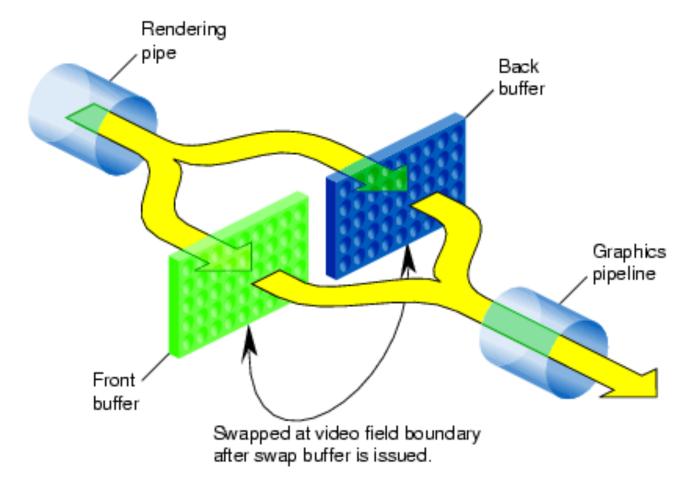
## **Keyframe Animation**

- Idea: Draw a subset of important frames (called key frames) and fill in the rest with in-betweens
- In hand-drawn animation, the head animator would draw the poses and the assistants would do the rest
- In computer animation, the artist draws the keys and the computer does the inbetweening
  - Interpolation is used to fill in the rest!



## Double Buffering

- If you draw directly to video buffer, the user will see the drawing happen
- Particularly noticeable artifacts when doing animation



### Controlling geometry conveniently

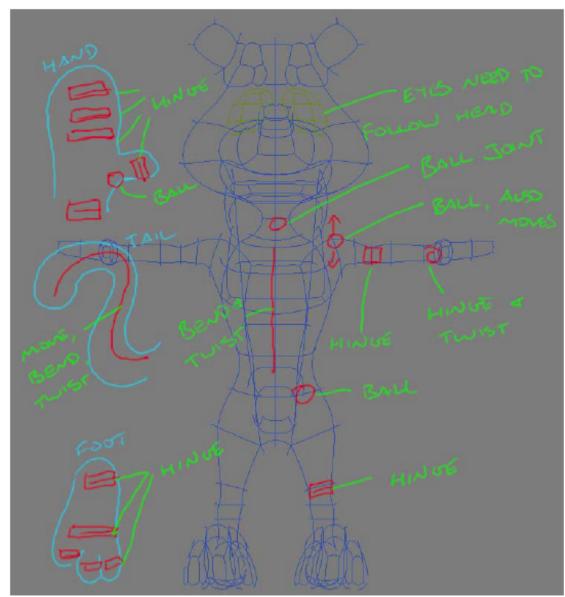
- Manually place every control point at every keyframe?
  - labor intensive
  - hard to get smooth, consistent motion
- Animate using smaller set of meaningful degrees of freedom
  - modeling DOFs are inappropriate for animation
     e.g. "move one square inch of left forearm"
  - animation DOFs need to be higher level
     e.g. "bend the elbow"

### Controlling shape for animation

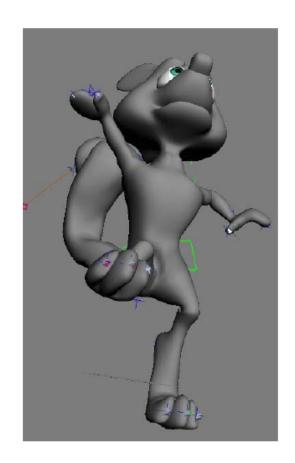
- Start with modeling DOFs (control points)
- Deformations control those DOFs at a higher level
  - Example: move first joint of second finger on left hand
- Animation controls control those DOFs at a higher level
  - Example: open/close left hand
- Both cases can be handled by the same kinds of deformers

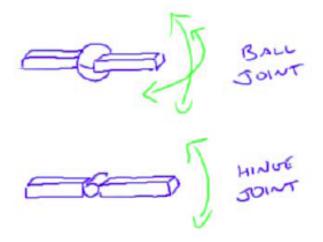
# [Greenberg/Pellacini | CIS 565]

#### **Character with DOFs**

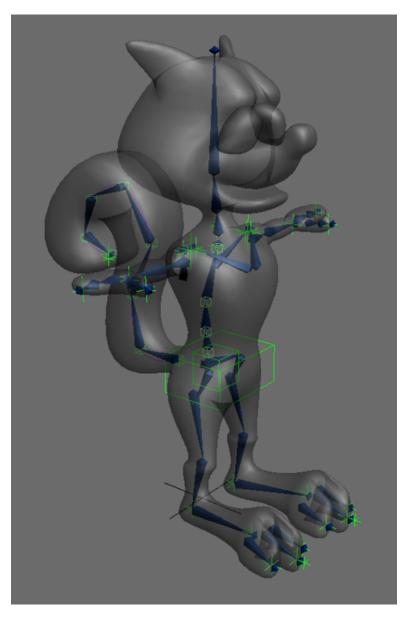


A visual description of the possible movements for the squirrel





## Rigged character



- Surface is deformed by a set of bones
- Bones are in turn controlled by a smaller set of controls
- The controls are useful, intuitive DOFs for an animator to use

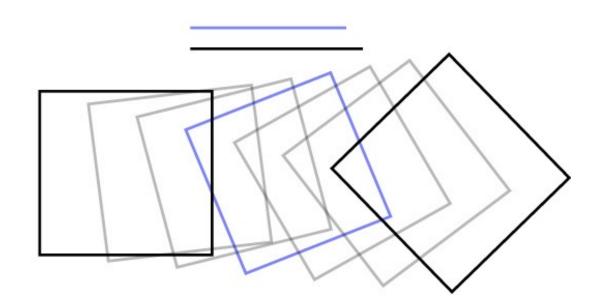
## Interpolating Rotations

#### The most basic animation control

- Affine transformations position things in modeling
- Time-varying affine transformations move things around in animation
- A hierarchy of time-varying transformations is the main workhorse of animation
  - and the basic framework within which all the more sophisticated techniques are built

### Interpolating transformations

- Move a set of points by applying an affine transformation
- How to animate the transformation over time?
  - interpolate the matrix entries from keyframe to keyframe?
     this is fine for translations but bad for rotations



## Interpolating Rotations

$$\frac{1}{2} \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$
90° CCW

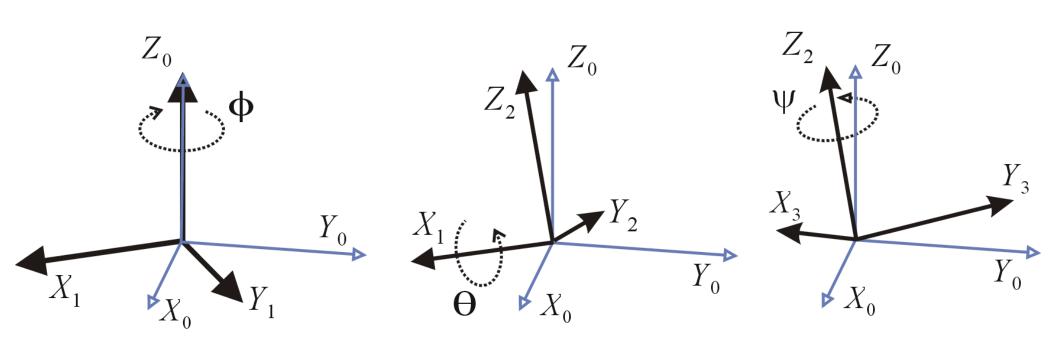
Not a rotation matrix!

#### Interpolating transformations

- Linear interpolation of matrices is not effective
  - leads to shrinkage when interpolating rotations
- One approach: always keep transformations in a canonical form (e.g. translate-rotate-scale)
  - then the pieces can be interpolated separately
  - rotations stay rotations, scales stay scales, all is good

Issues occurs when the source and target angles are not close to each other

## Could Instead Decompose Rotation by Euler Angles

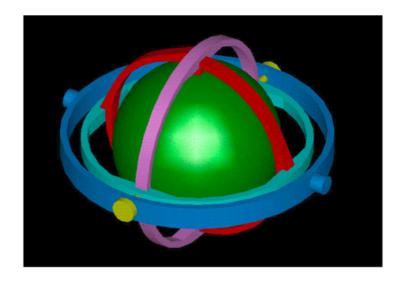


## Parameterizing rotations

#### Euler angles

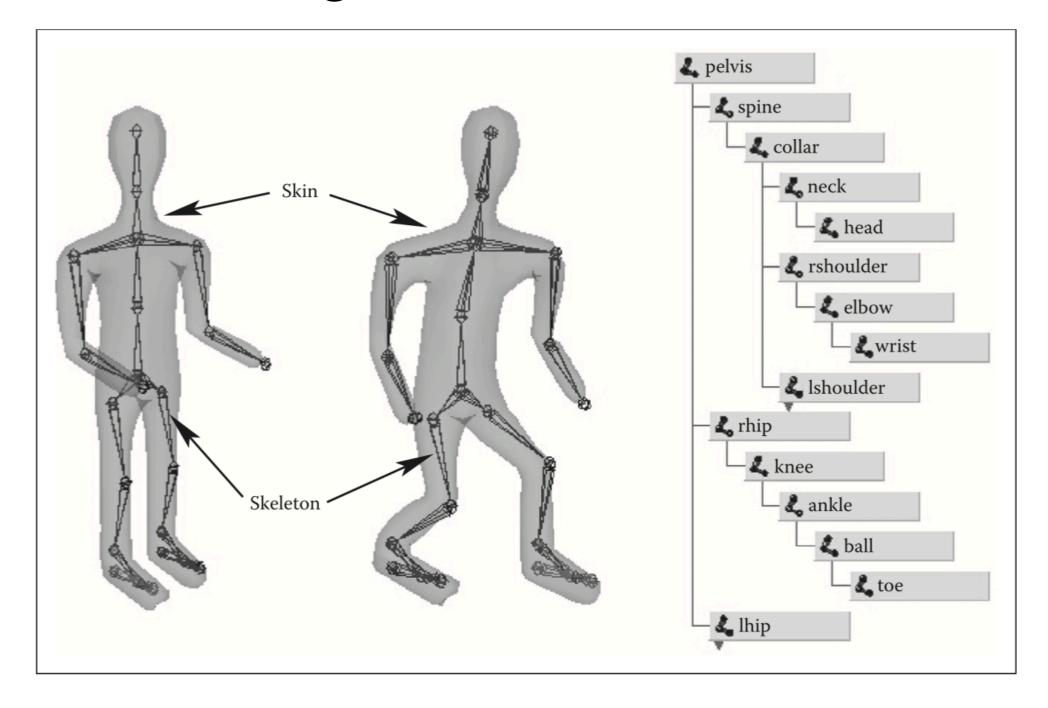
- rotate around x, then y, then z
- nice and simple

$$R(\theta_x, \theta_y, \theta_z) = R_z(\theta_z) R_y(\theta_y) R_x(\theta_x)$$

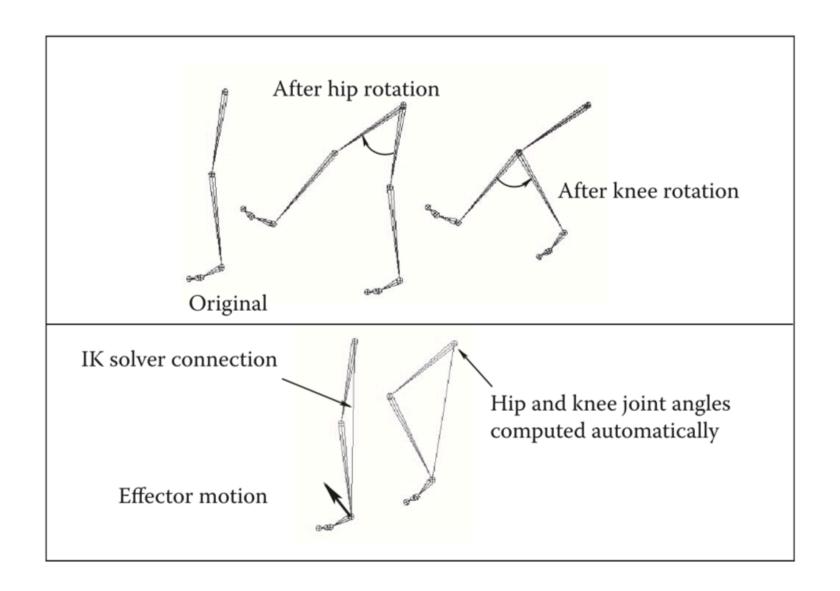


## **Character Animation**

## Animating w/ Skeletal Hierarchies



## Forward vs. Inverse Kinematics



## Inverse Kinematics Solves for all Intermediate Constraints

