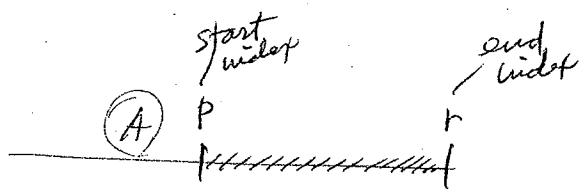


algo

$\text{mergeSort}(A, p, r)$



{ if ($p < r$)

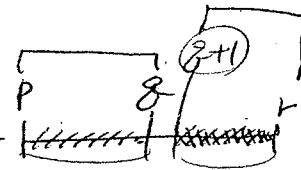
$q \leftarrow \lfloor (p+r)/2 \rfloor$;

$\text{mergeSort}(A, p, q)$;

$\text{mergeSort}(A, q+1, r)$;

$\text{merge}(A, p, q, r)$;

}



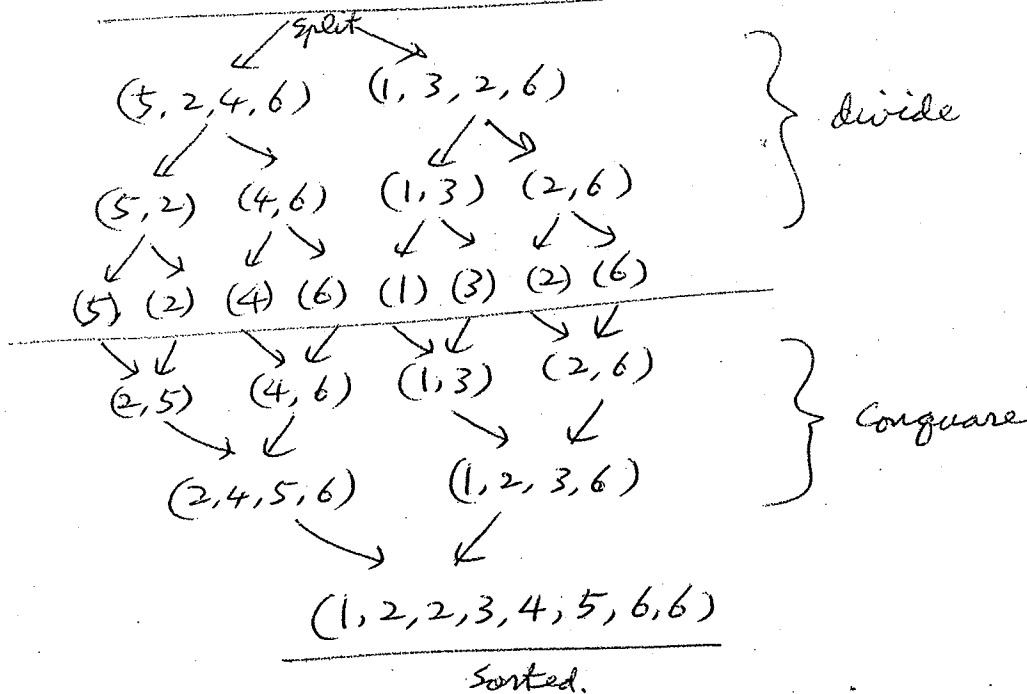
combine

Sorted $p \sim q$ and

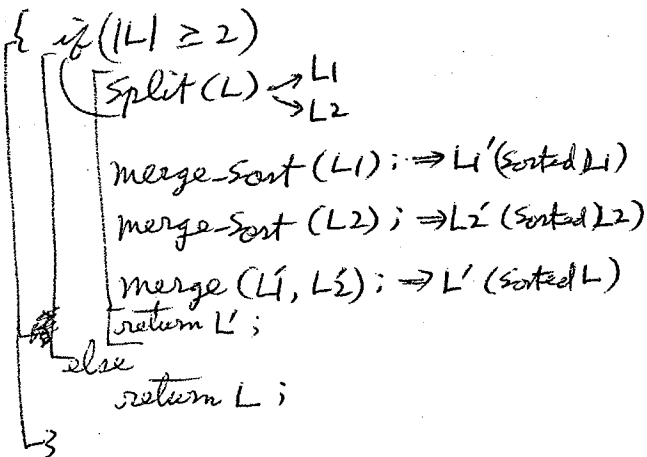
Sorted $q+1 \sim r$

merge sort in scheme

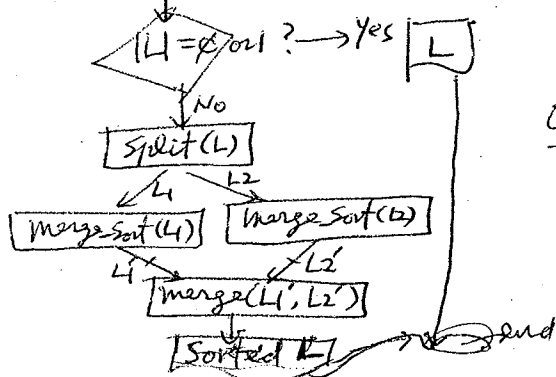
24) (5, 2, 4, 6, 1, 3, 2, 6)



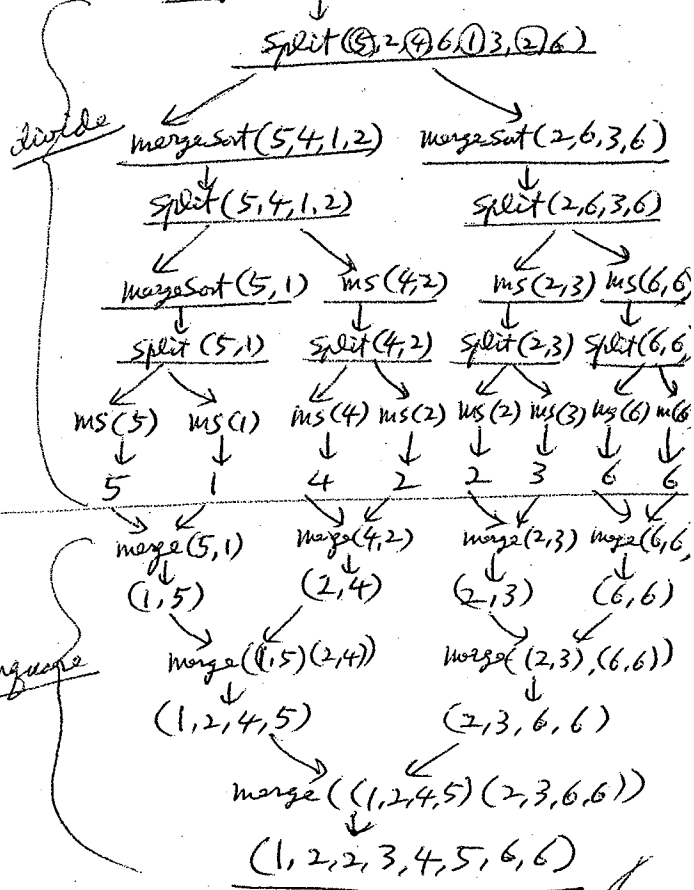
mergeSort(L)



mergeSort(L)



mergeSort(5, 2, 4, 6, 1, 3, 2, 6)



merge (X, Y)

Pseudo-code

```

{
  if (X is null), return Y;
  else if (Y is null), return X;
  else if (1st-ele. of X ≤ 1st-ele. of Y)
    construct ( 1st-ele. of X, merge (P, Q) )
    cons
  else
    construct ( 1st-ele. of Y, merge (P, Q) )
}

```

(P is X without 1st ele.)
 (Q is Y without 1st ele.)

merge-sort (X)

```

{
  if (X is null), return X; — ( ) ⇒ ( )
  else if (X is 1-ele. list), return X; — (1) ⇒ (1)
  else
    return merge ( merge-sort (P), merge-sort (Q) )
}

```

(P is 1st part from Split (X))
 (Q is 2nd part from Split (X))
 (P is (car (split X)))
 (Q is (cdr (split X)))

Split (X) — (1 3 2 4) ⇒ ((1 2) 3 4)

```

{
  if (X is null), construct ( ( ) ); — (cons '() '())
  else if (X is 1-ele. list), construct ( (1) ); — (1) → ((1))
  else
    (1 3 2 4) ⇒ ((1 2) 3 4) or ((1 3) 2 4) } either is ok.

```