## Pathfinding with BFS

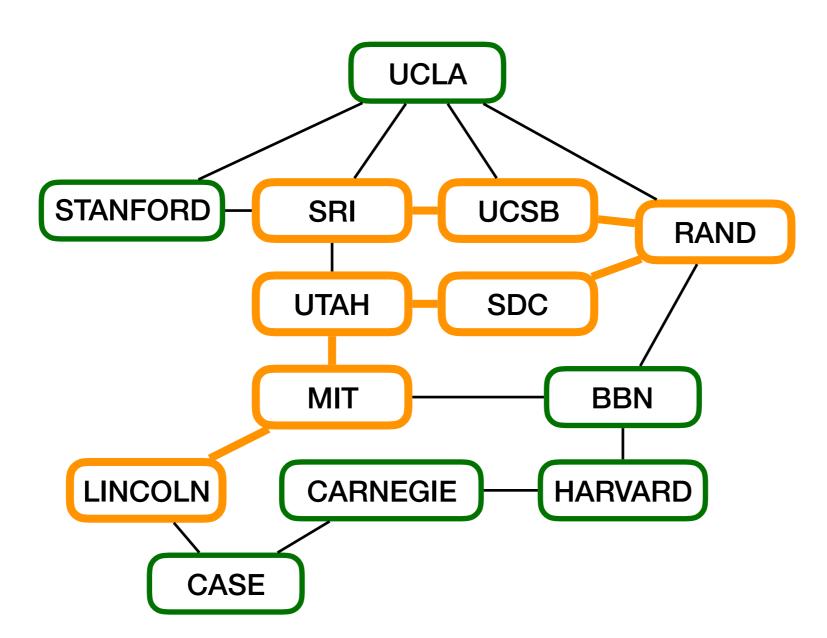
#### Lecture Question

## Task: Find the distance between two nodes in a graph

- In the Graph class
  - Write a method named distance that takes two node indices (Ints) and returns the distance between the two nodes
  - You may assume the two input nodes are connected

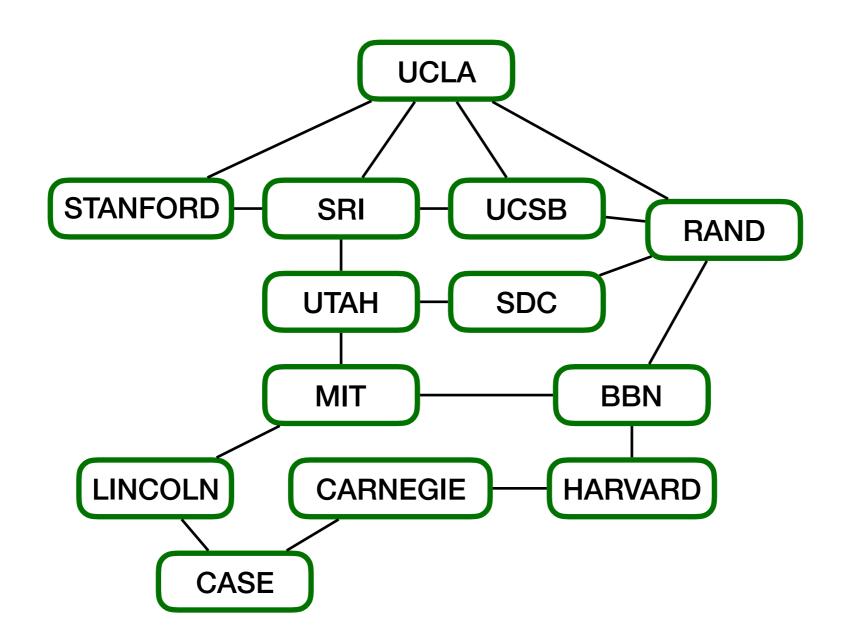
#### Paths

- Path: A sequence of nodes with each adjacent pair of nodes connected by an edge
- The length of a path is the number of edges it contains (number of nodes 1)
- [LINCOLN, MIT, UTAH, SDC, RAND, UCSB, SRI] <-- Path of length 6</li>



#### Distance

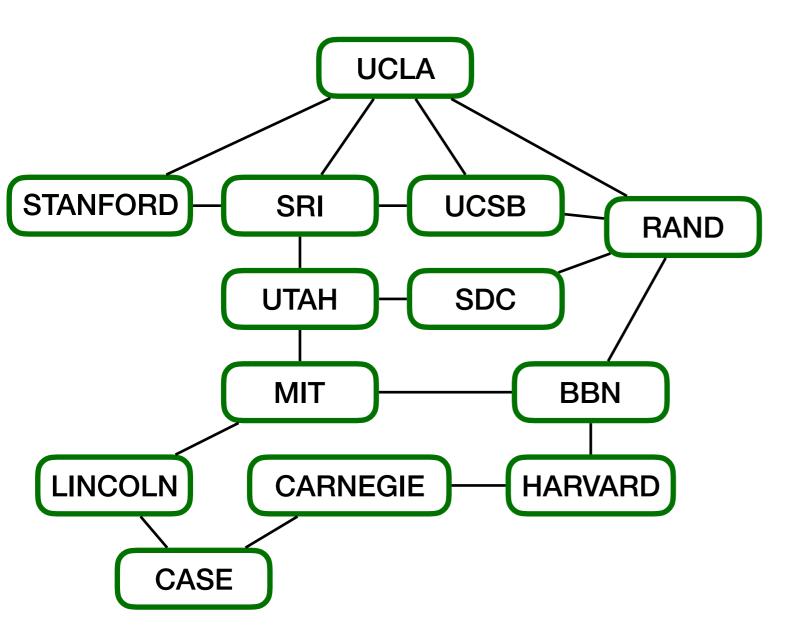
- Distance between two nodes: The length of the shortest path between the nodes
- Distance between LINCOLN and SRI == 3
- Distance between RAND and BBN == 1



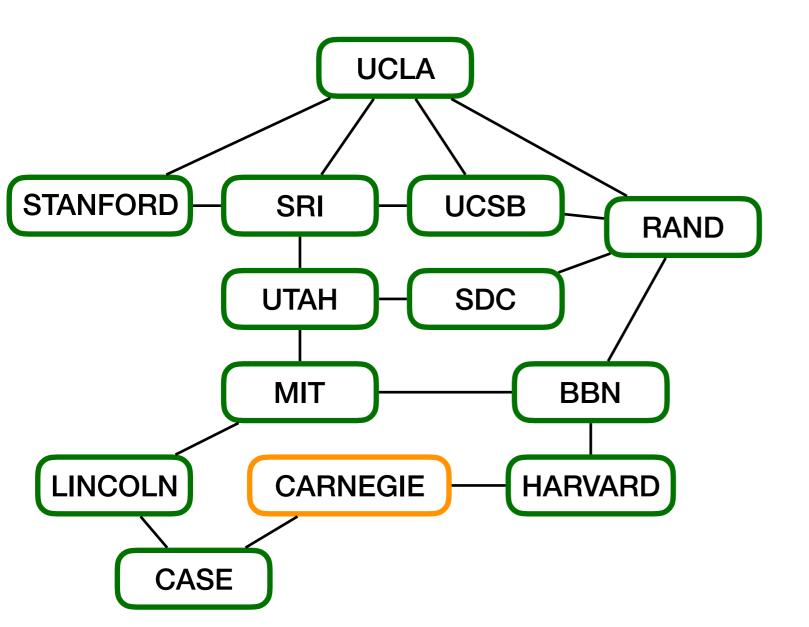
## Use BFS to find the distance between nodes

Track the shortest path for pathfinding

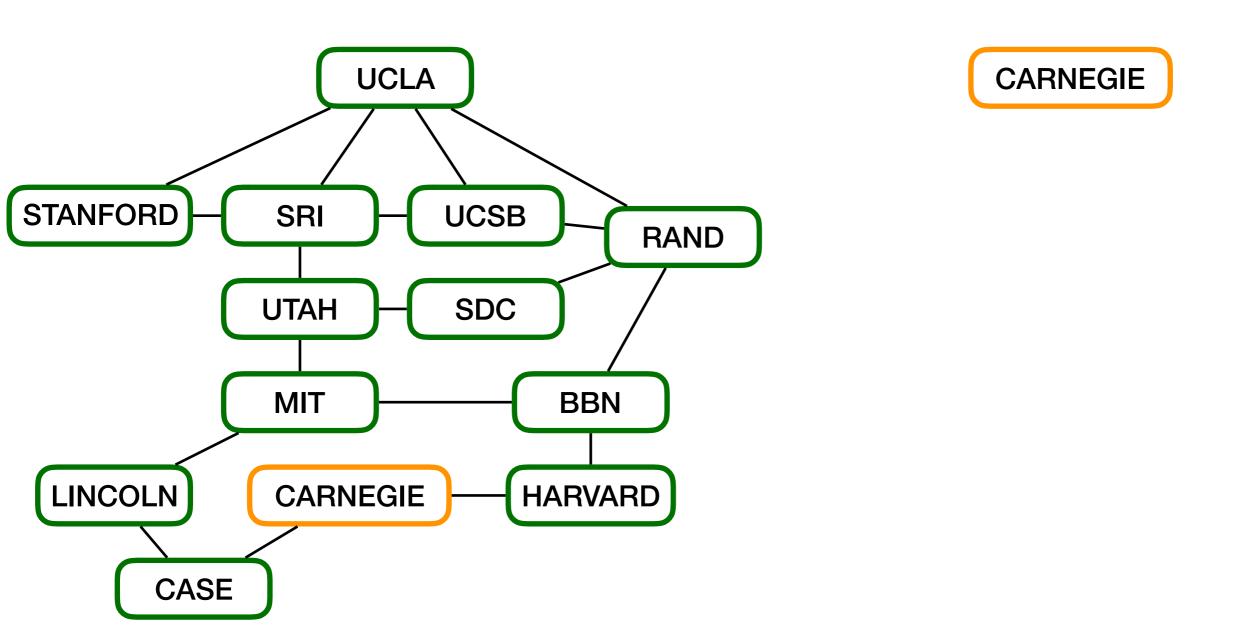
- Let's run through BFS again
  - Instead of just finding the connected component, let's track the paths taken to explore each node



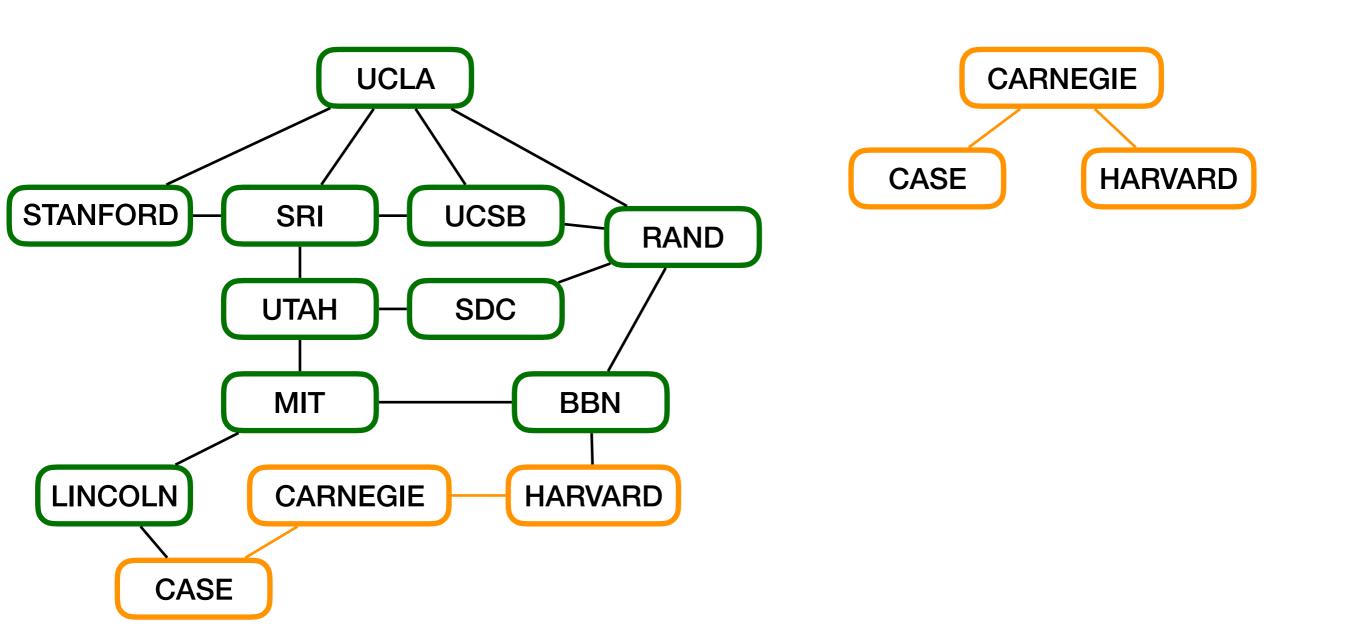
- Start at CARNEGIE this time
  - Just for variety



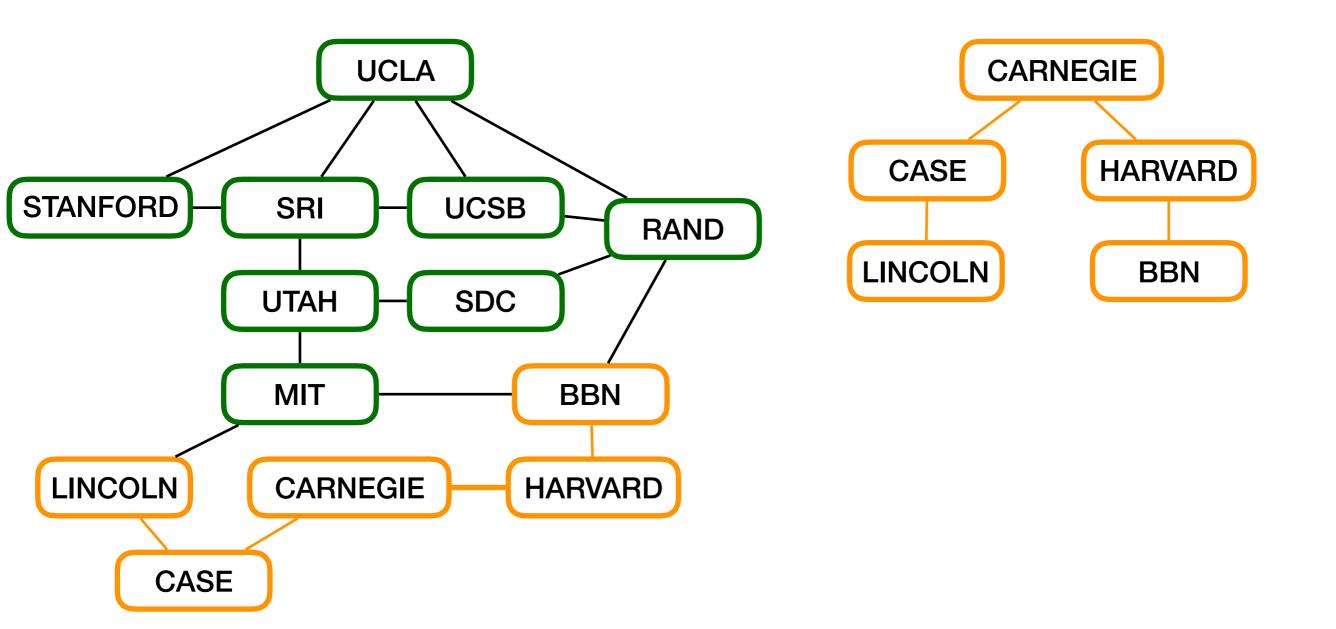
- Keep track of all edges used to explore new nodes
- Redraw the graph with only these edges



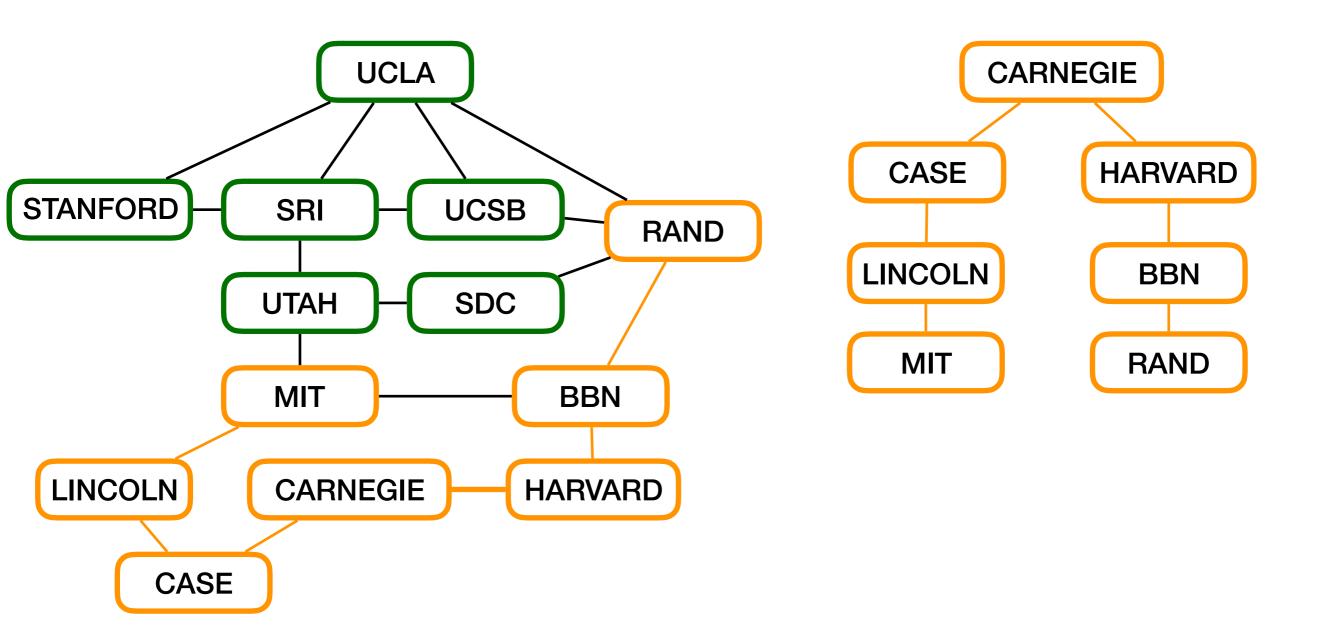
Explore all neighbors of the starting node



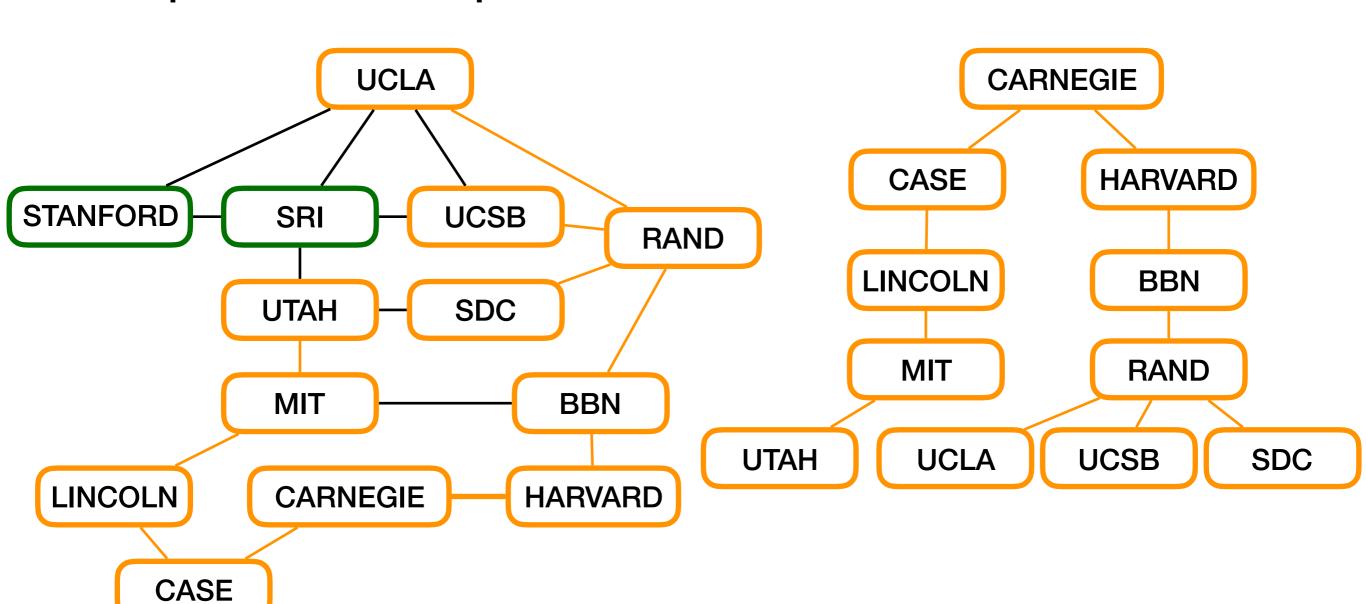
 Explore all neighbors of the nodes explored in the last step



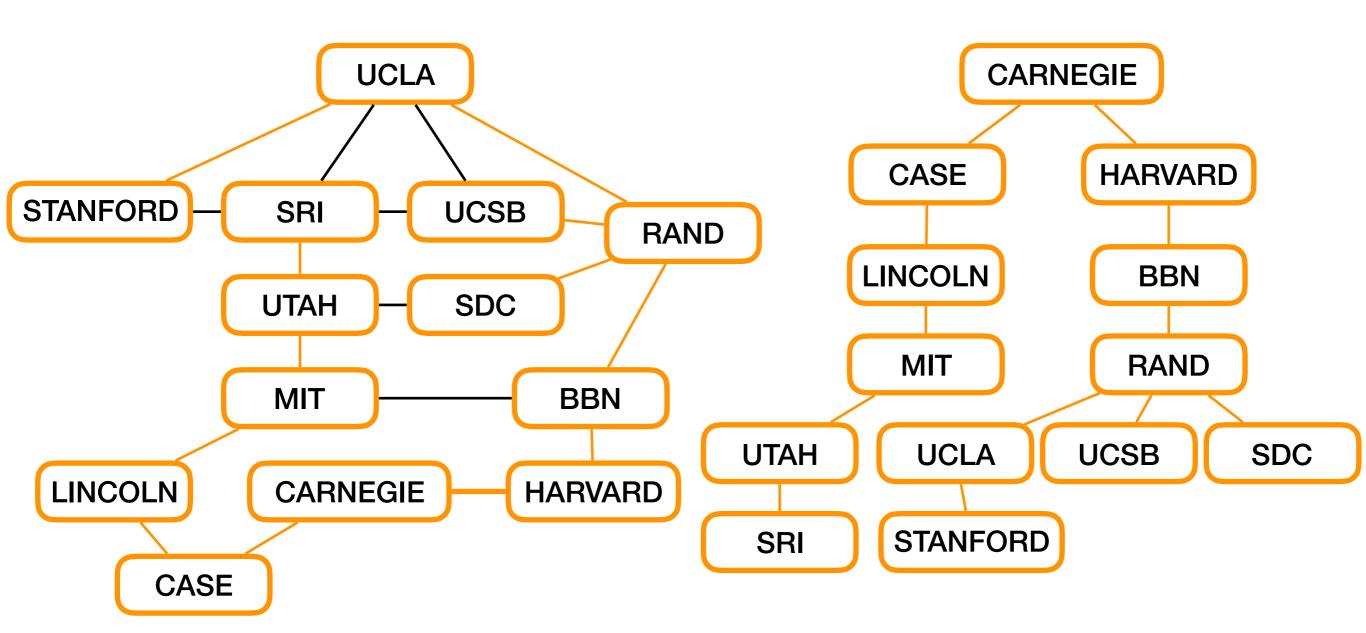
- Repeat
- Choose edge to use for MIT arbitrarily



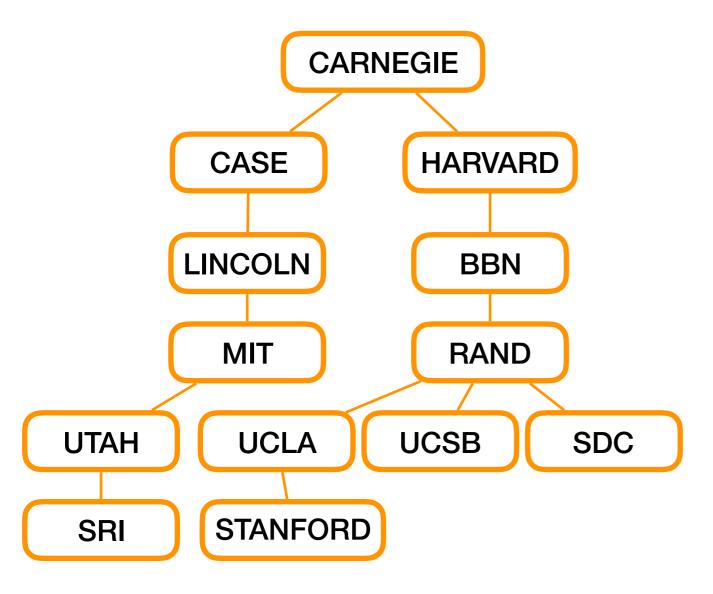
 Each step we explore all nodes that can be reached from the nodes added in the previous step



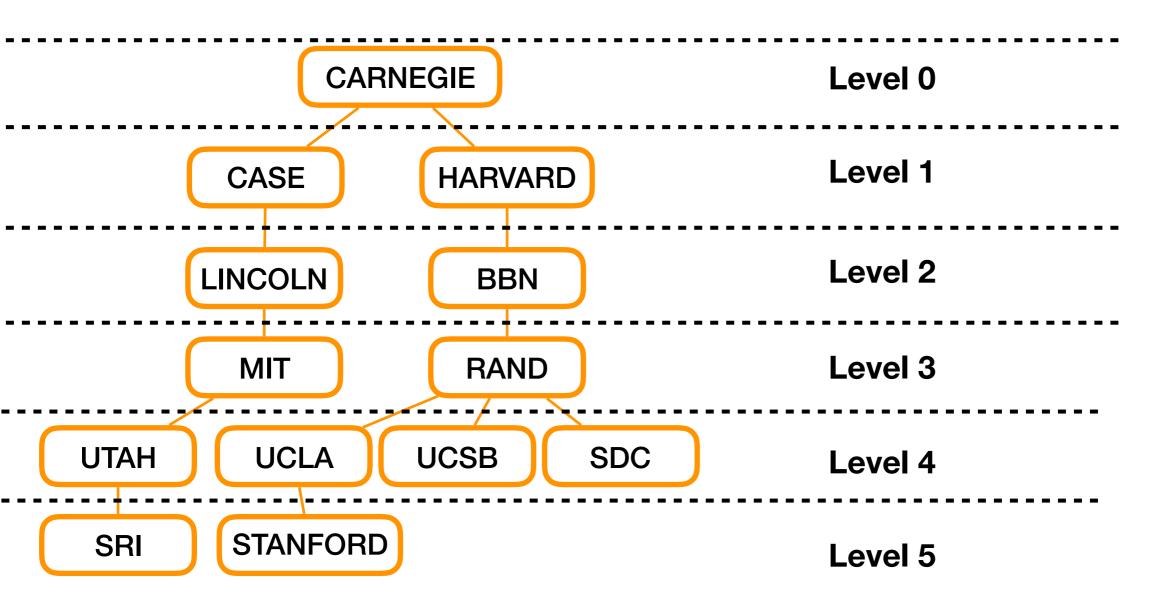
 Each step we explore all nodes that can be reached from the nodes added in the previous step



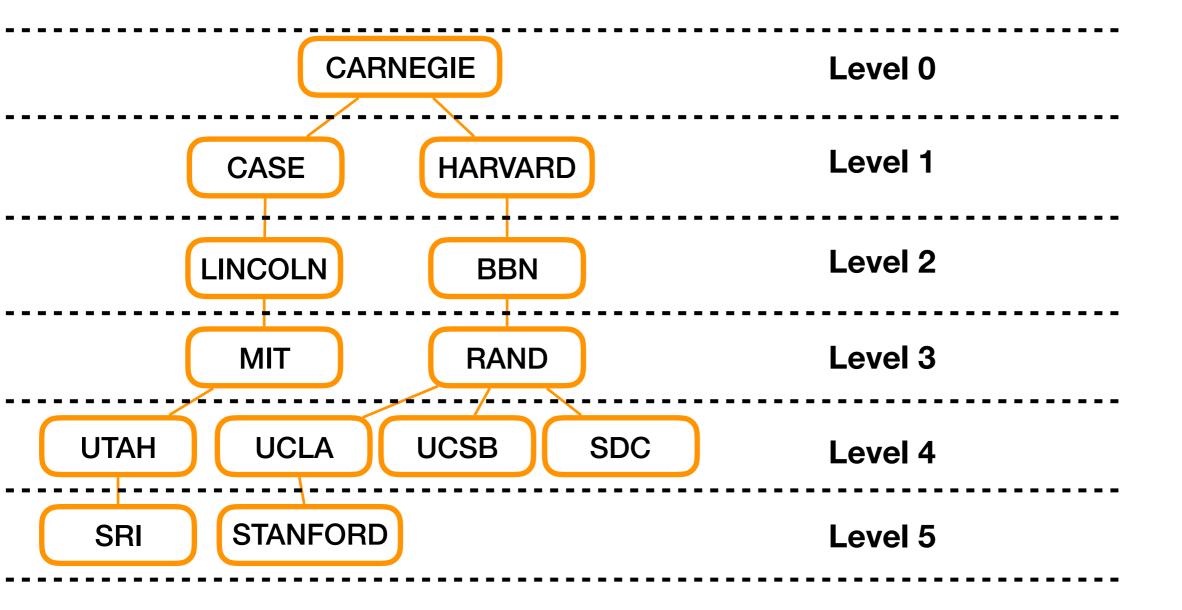
- We have a new graph with a few edges removed
- This graph is a tree (no cycles)



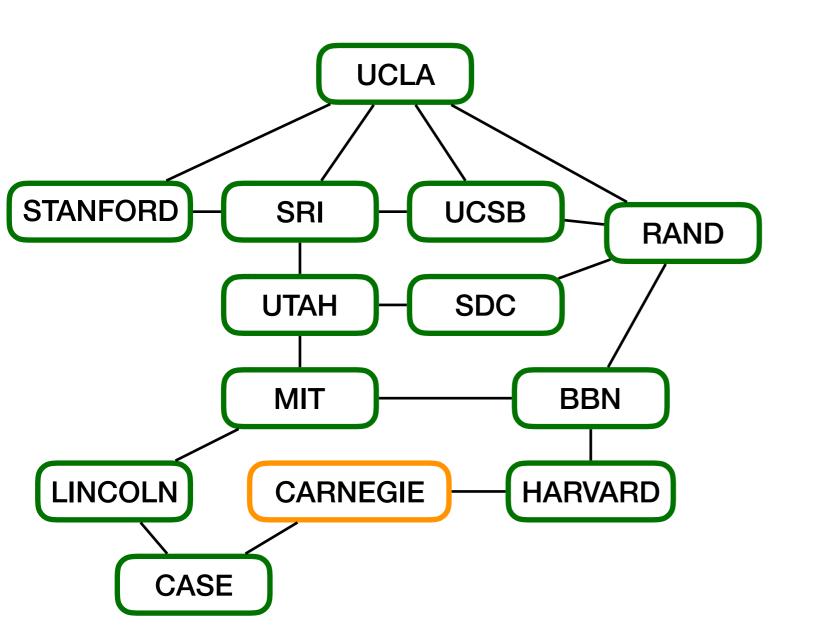
And it has levels!



- Number the level starting with 0
- The level number == the distance from the starting node to any node in that level

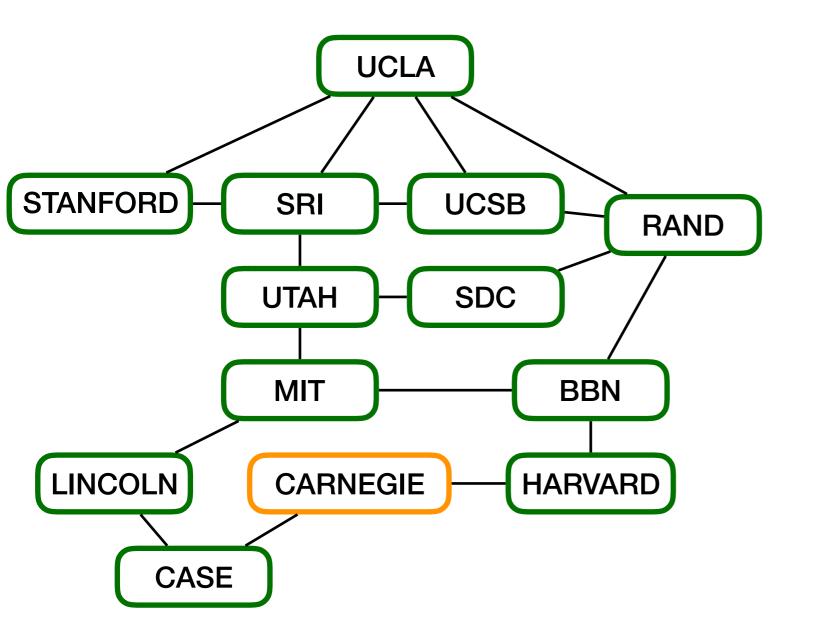


- But how do we track the levels?
- Track levels in a data structure



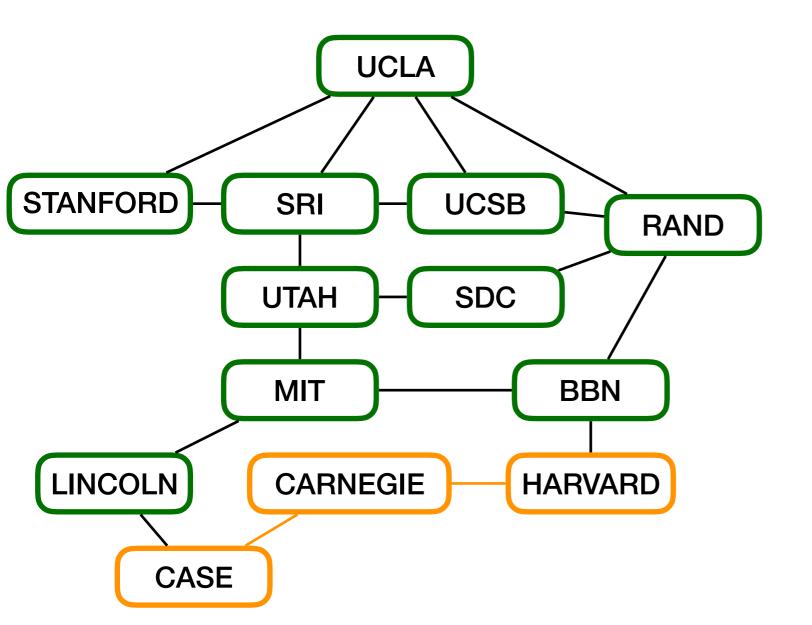
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SRI	00
UCSB	$\infty$
RAND	00
UTAH	$\infty$
SDC	00
MIT	$\infty$
BBN	00
LINCOLN	$\infty$
CARNEGIE	0
HARVARD	$\infty$
CASE	$\infty$

**CARNEGIE** 



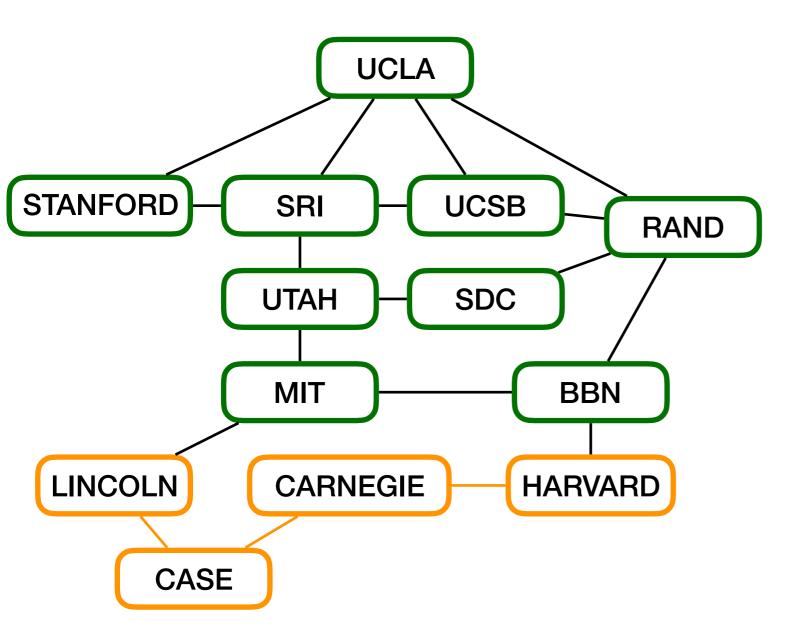
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HARVARD	00
CASE	00

CASE HARVARD



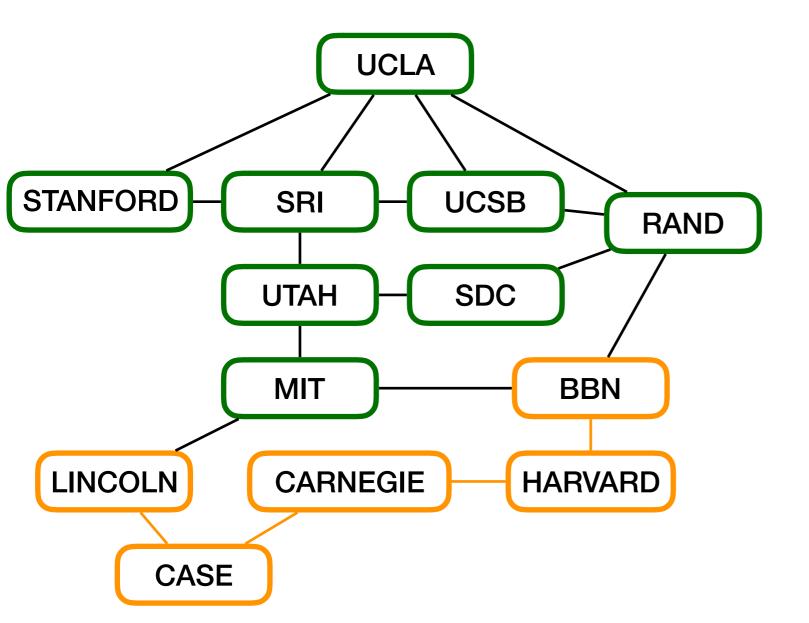
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MIT ∞	
BBN ∞	
LINCOLN ∞	
CARNEGIE 0	
HARVARD 1	
CASE 1	

HARVARD LINCOLN



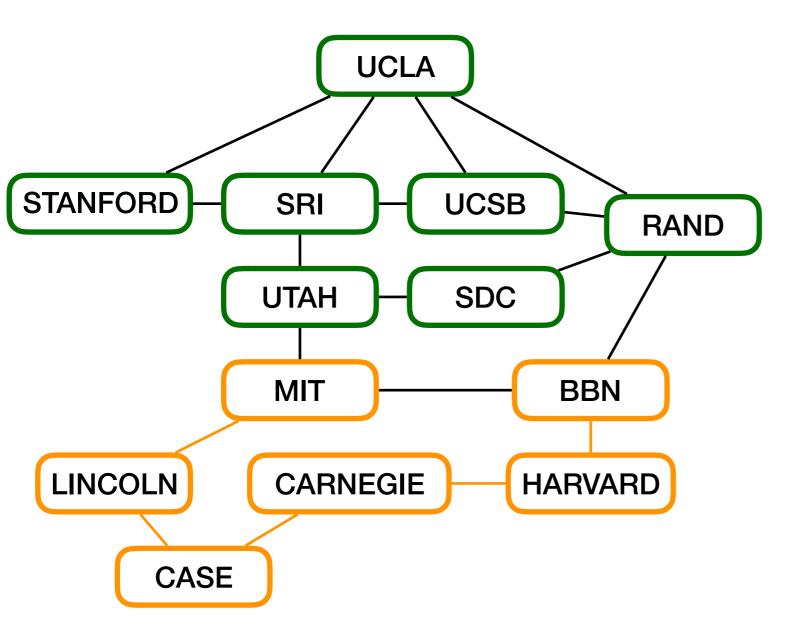
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CARNEGIE	0
HARVARD	1
CASE	1
	1

LINCOLN BBN



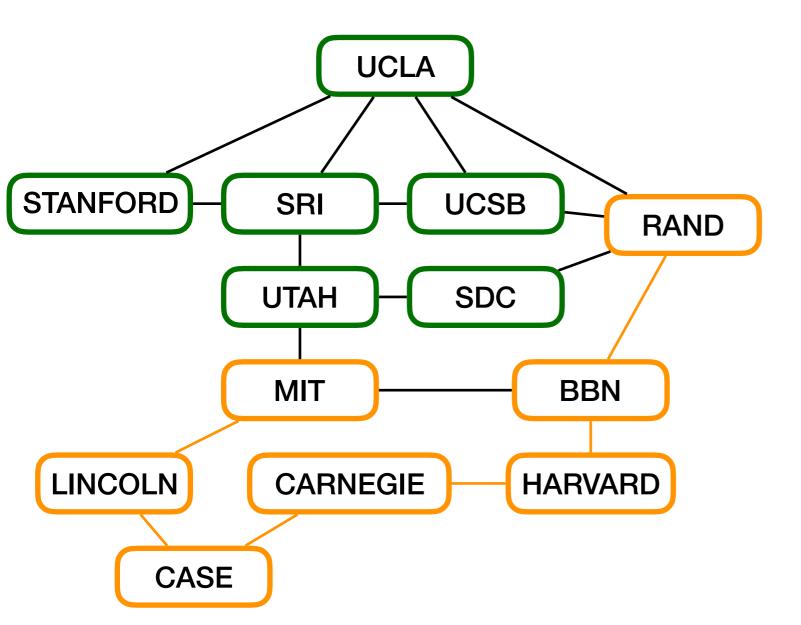
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MIT	00
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LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1

BBN MIT



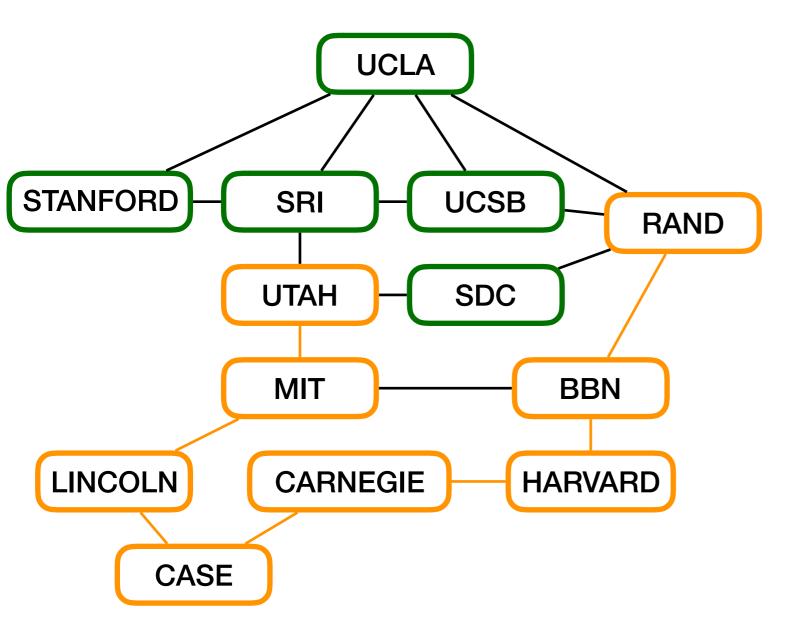
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SDC	00
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LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1

MIT RAND



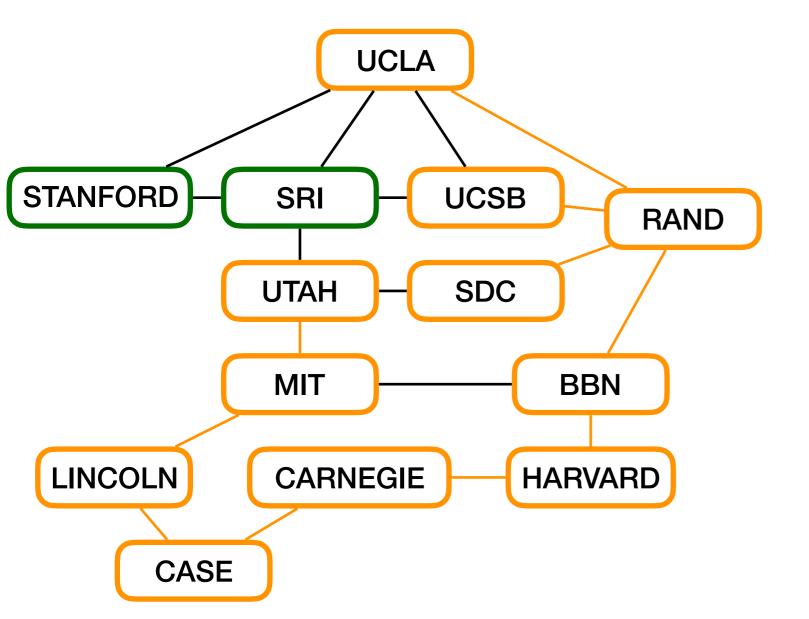
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LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1

RAND UTAH



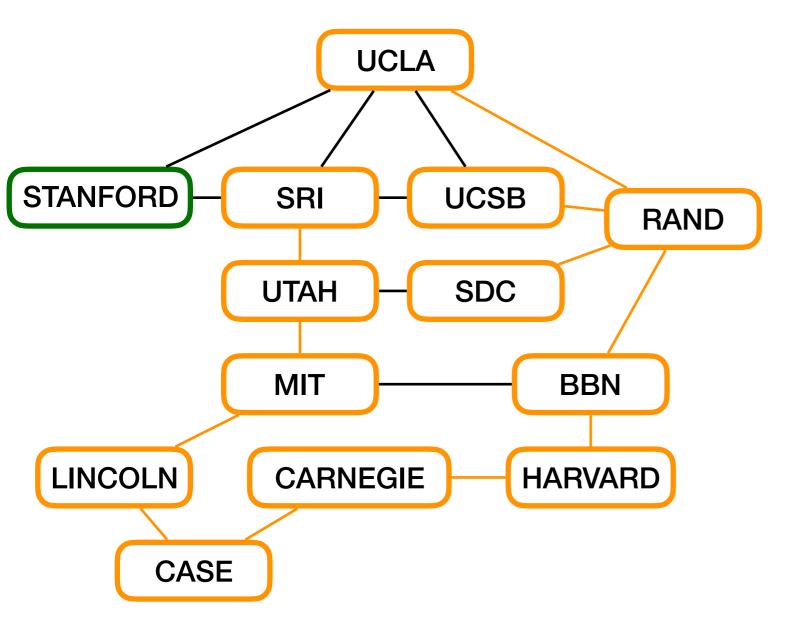
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LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1

UTAH UCLA UCSB SDC



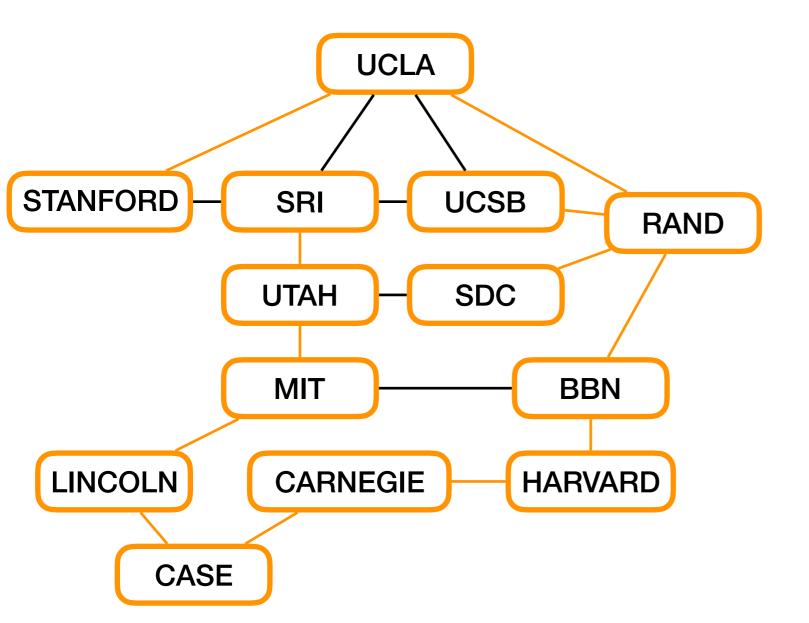
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BBN	2
LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1





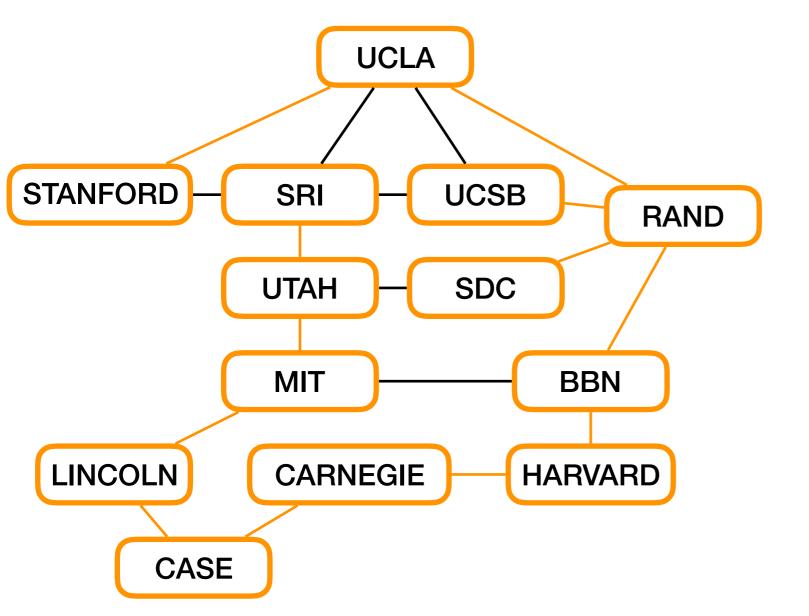
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CARNEGIE	0
HARVARD	1
CASE	1

UCSB SDC SRI STANFORD



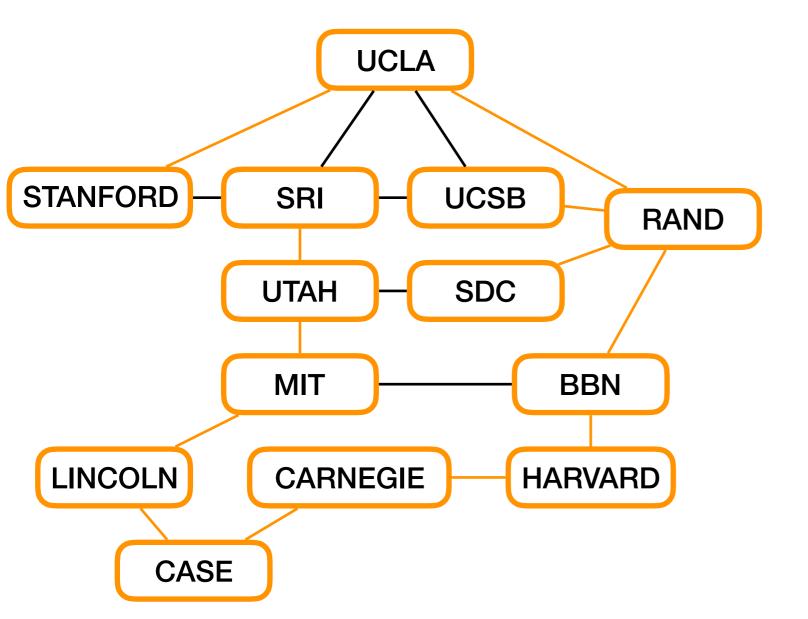
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HARVARD	1
CASE	1

SDC SRI STANFORD



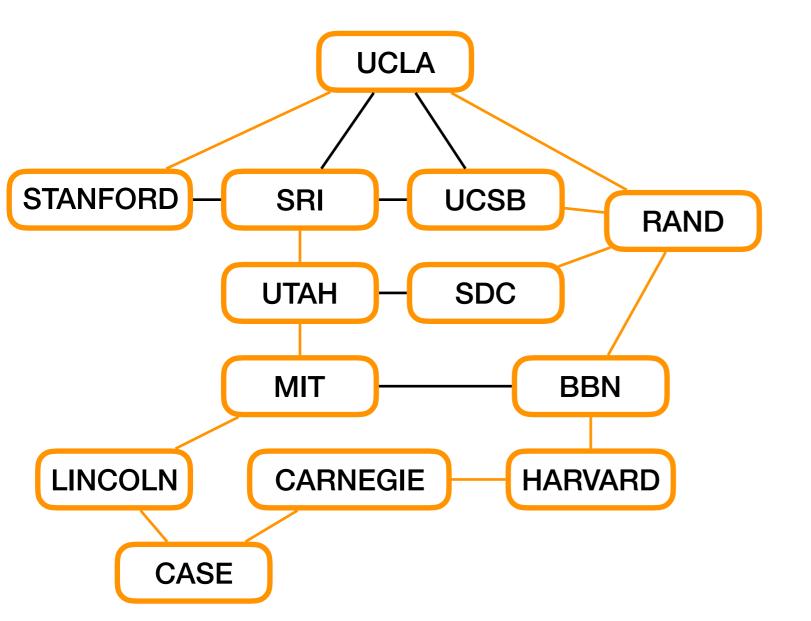
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HARVARD	1
CASE	1

SRI STANFORD

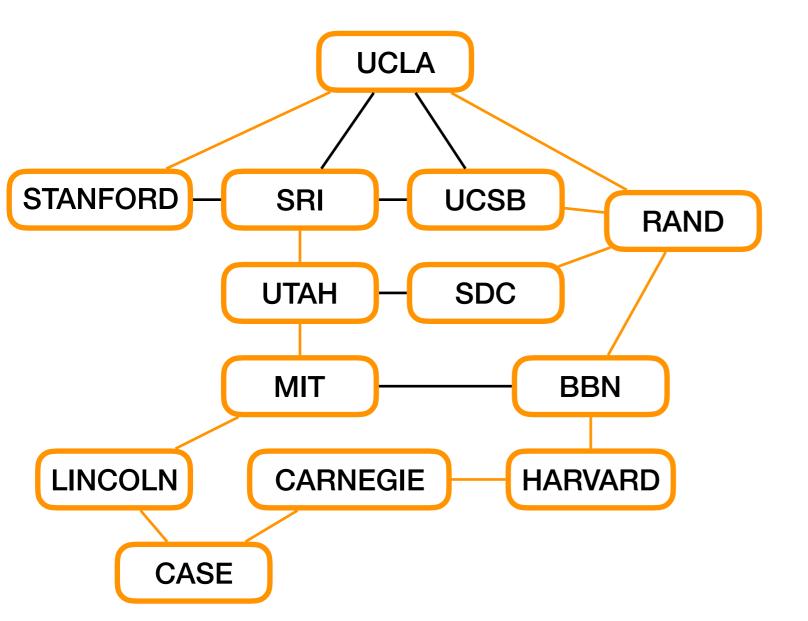


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UTAH	4
SDC	4
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BBN	2
LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1

STANFORD

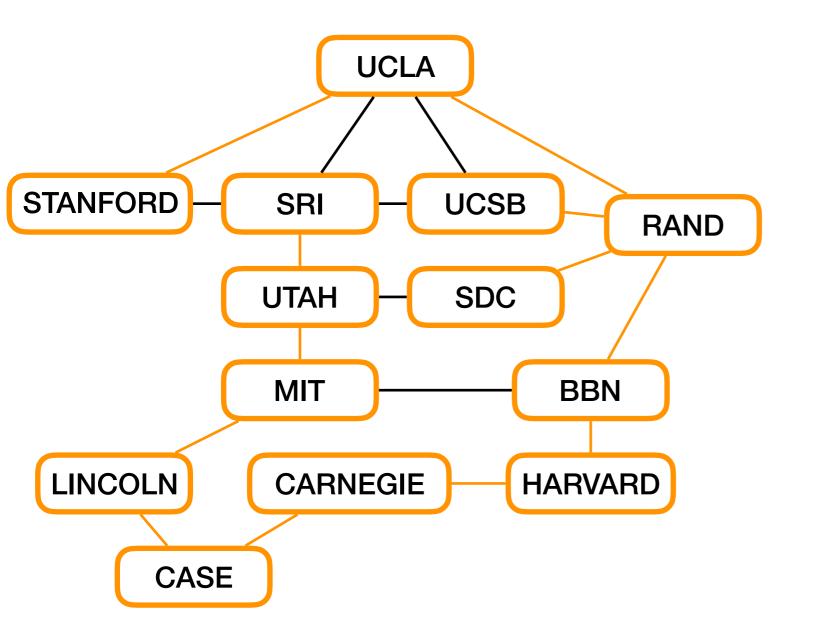


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HARVARD	1
CASE	1



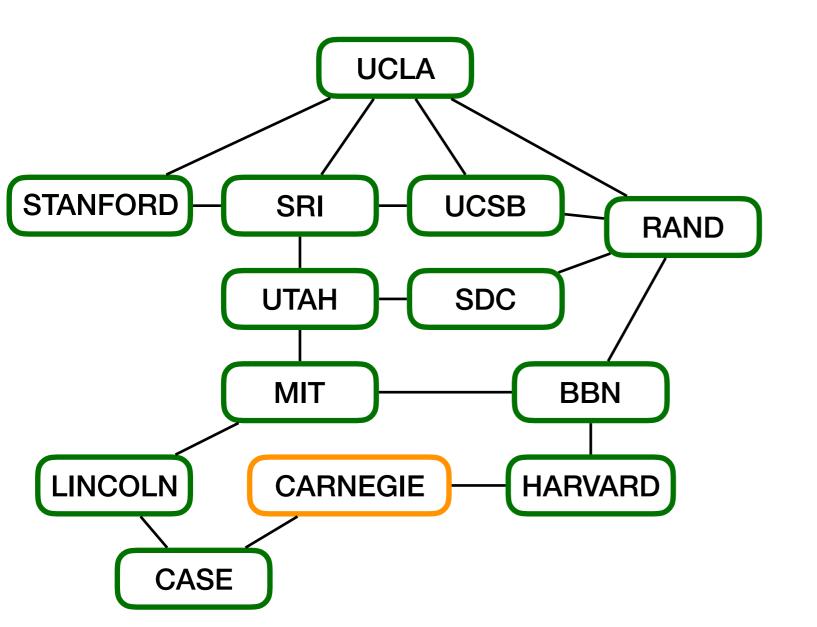
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UCSB	4
RAND	3
UTAH	4
SDC	4
MIT	3
BBN	2
LINCOLN	2
CARNEGIE	0
HARVARD	1
CASE	1

 And we have the distance from the start node to all other nodes in the graph



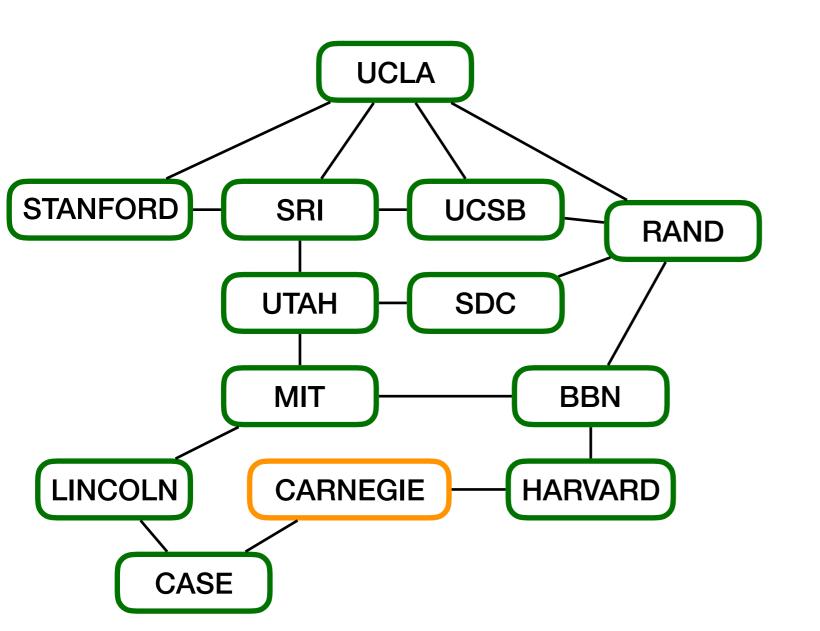
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UCSB 4  RAND 3  UTAH 4  SDC 4  MIT 3  BBN 2  LINCOLN 2  CARNEGIE 0	STANFORD	5
RAND       3         UTAH       4         SDC       4         MIT       3         BBN       2         LINCOLN       2         CARNEGIE       0	SRI	5
UTAH         4           SDC         4           MIT         3           BBN         2           LINCOLN         2           CARNEGIE         0	UCSB	4
SDC 4  MIT 3  BBN 2  LINCOLN 2  CARNEGIE 0	RAND	3
MIT 3 BBN 2 LINCOLN 2 CARNEGIE 0	UTAH	4
BBN 2 LINCOLN 2 CARNEGIE 0	SDC	4
LINCOLN 2  CARNEGIE 0	MIT	3
CARNEGIE 0	BBN	2
O7 II II TEGIE	LINCOLN	2
HARVARD 1	CARNEGIE	0
	HARVARD	1
CASE 1	CASE	1

- But don't we want to find the shorts path fir Towers 2?
  - Not just the length of the shortest path



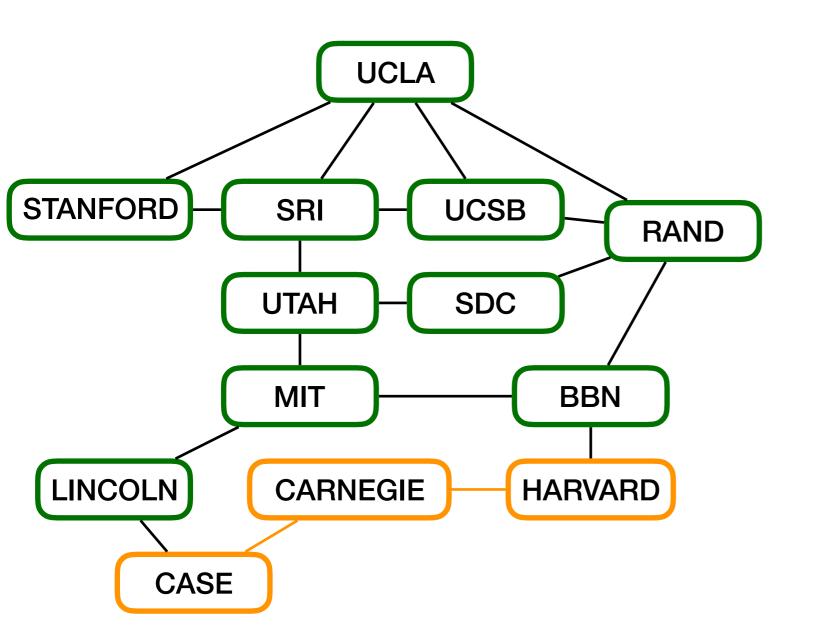
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STANFORD	<b>∞</b>
SRI	00
UCSB	00
RAND	00
UTAH	00
SDC	00
MIT	00
BBN	00
LINCOLN	00
CARNEGIE	0
HARVARD	00
CASE	00

 Instead of tracking the distance, track the node that discovered each node



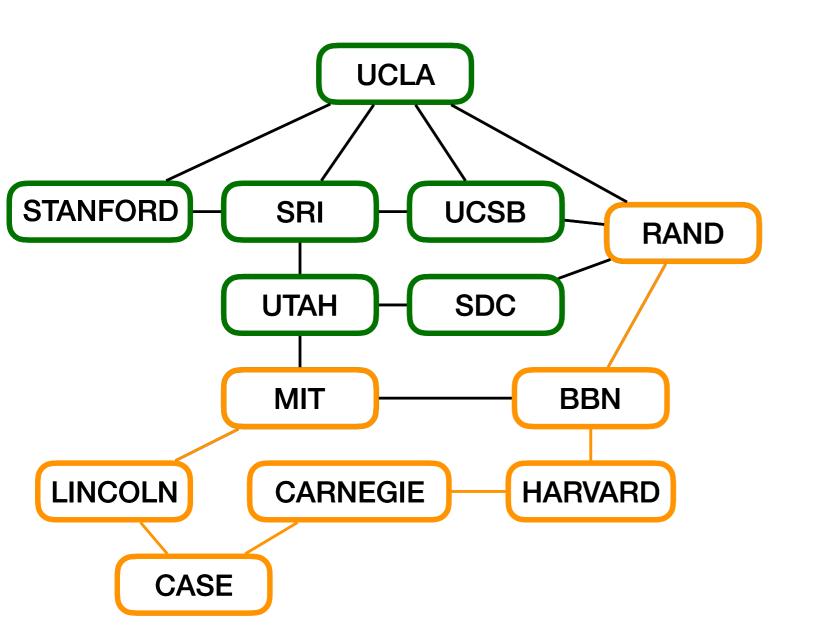
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SDC	unexplored
MIT	unexplored
BBN	unexplored
LINCOLN	unexplored
CARNEGIE	<start></start>
HARVARD	unexplored
CASE	unexplored

Now each node remembers how it was reached



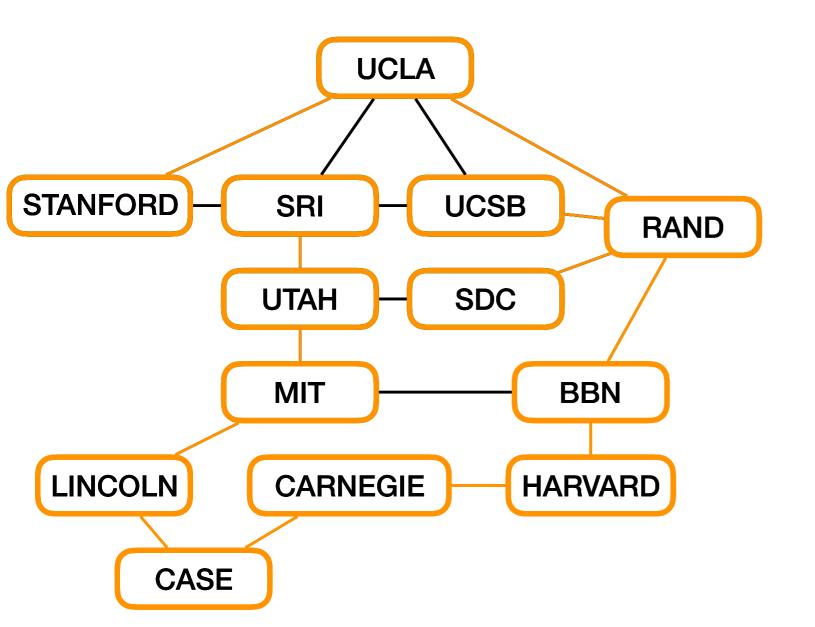
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SDC	unexplored
MIT	unexplored
BBN	unexplored
LINCOLN	unexplored
CARNEGIE	<start></start>
HARVARD	CARNEGIE
CASE	CARNEGIE

Repeat at each step



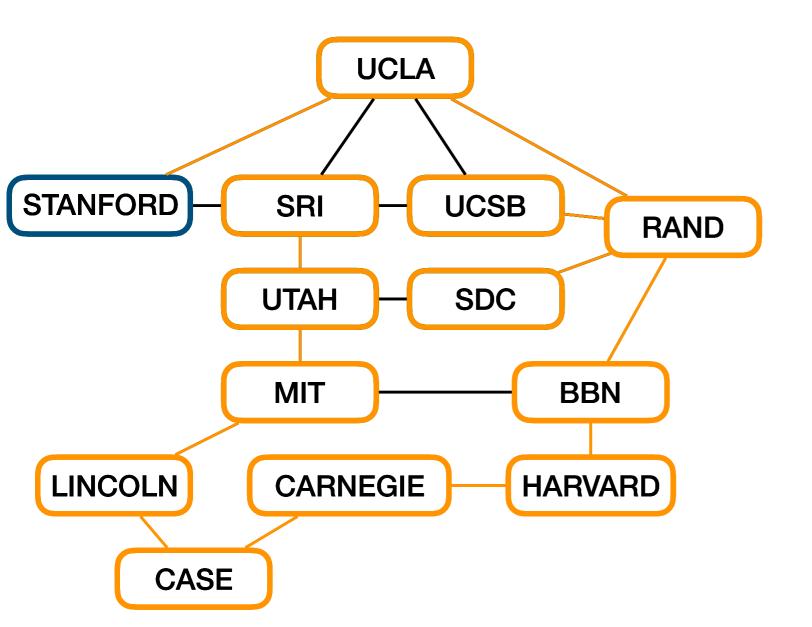
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SDC	unexplored
MIT	LINCOLN
BBN	HARVARD
LINCOLN	CASE
CARNEGIE	<start></start>
HARVARD	CARNEGIE
CASE	CARNEGIE

 At the end of the algorithm you'll know how each node was discovered



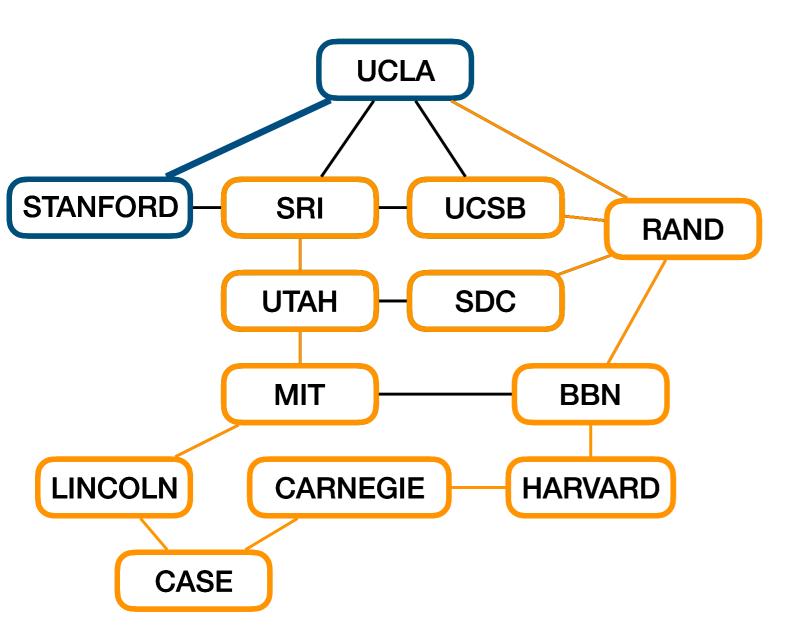
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UTAH	MIT
SDC	RAND
MIT	LINCOLN
BBN	HARVARD
LINCOLN	CASE
CARNEGIE	<start></start>
HARVARD	CARNEGIE
CASE	CARNEGIE

- Work backwards to build the shortest path
- Find path from CARNEGIE to STANFORD



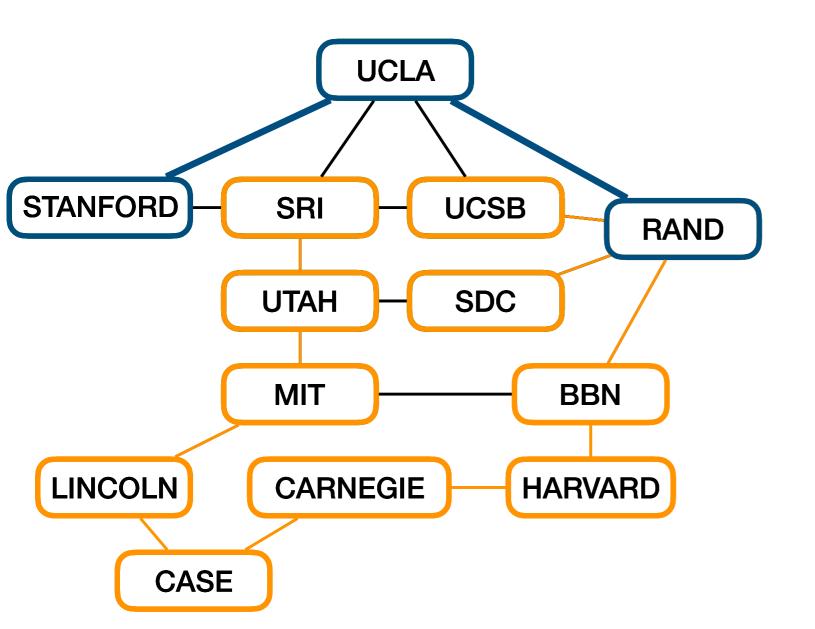
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CASE	CARNEGIE





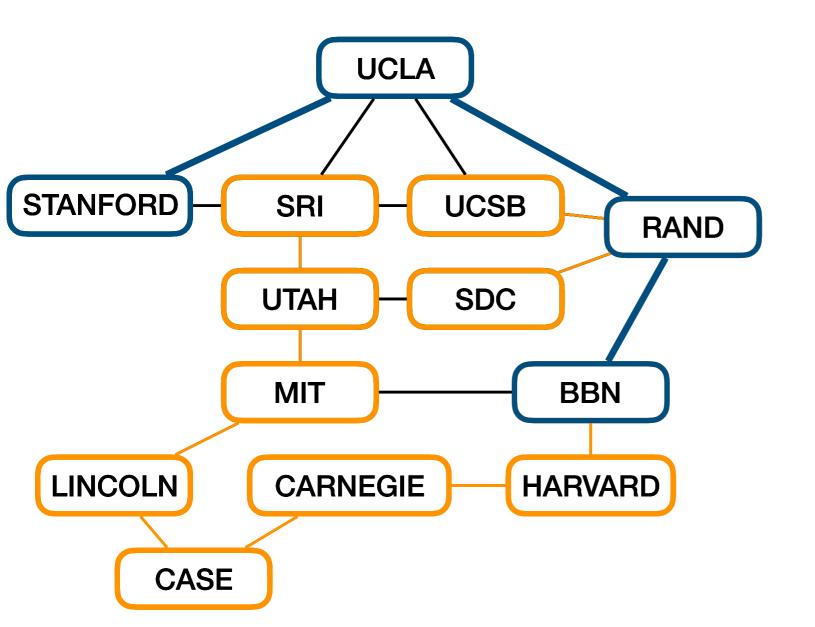
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CASE	CARNEGIE





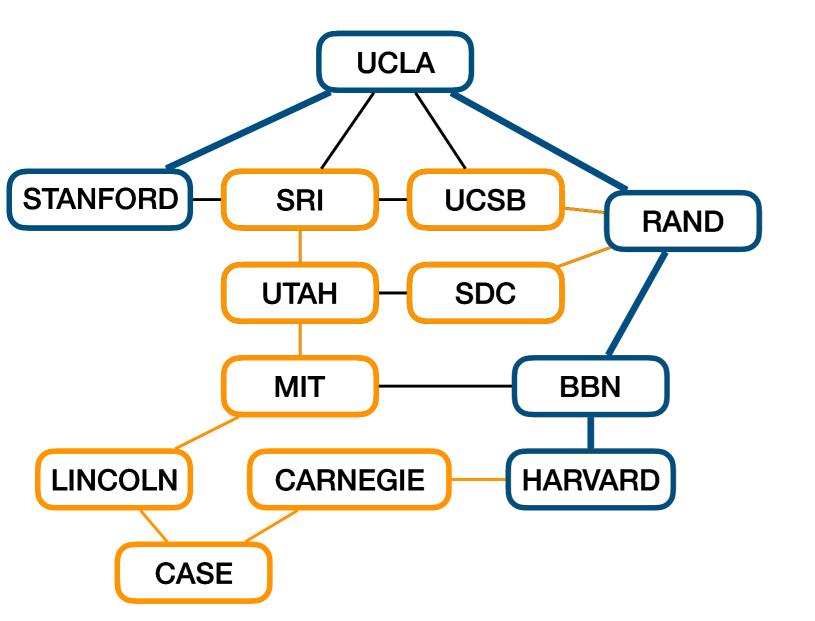
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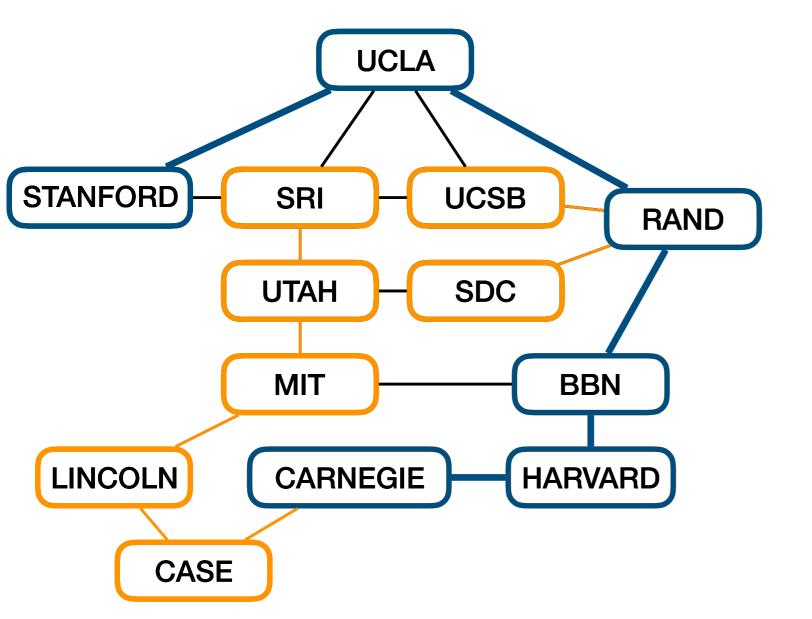
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LINCOLN	CASE
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CASE	CARNEGIE





UCLA	RAND
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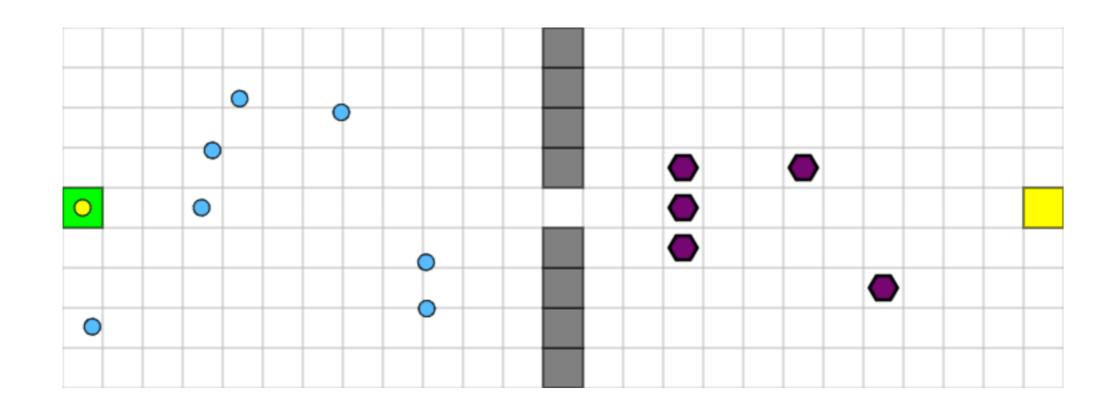




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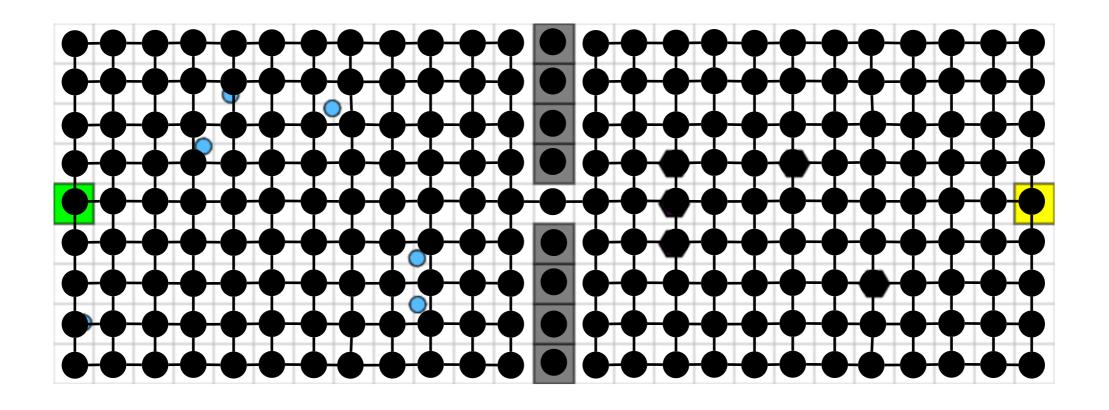
# But we have to find paths on a game board

How do graphs help with this?

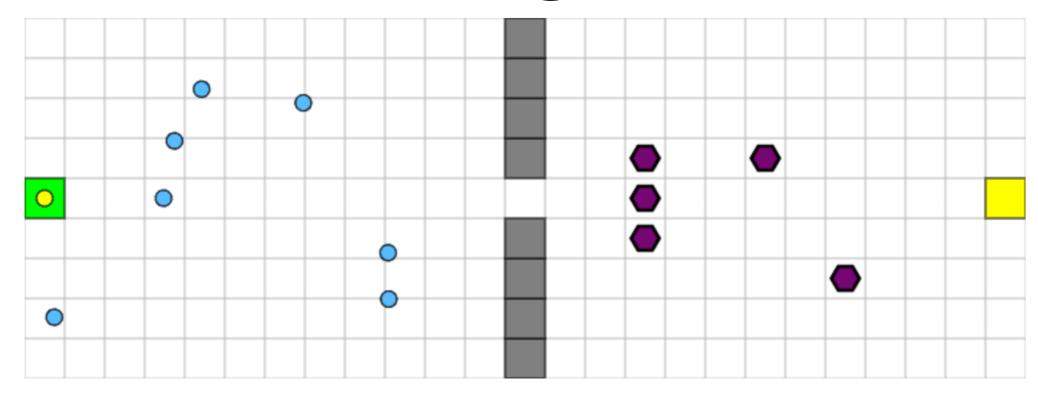


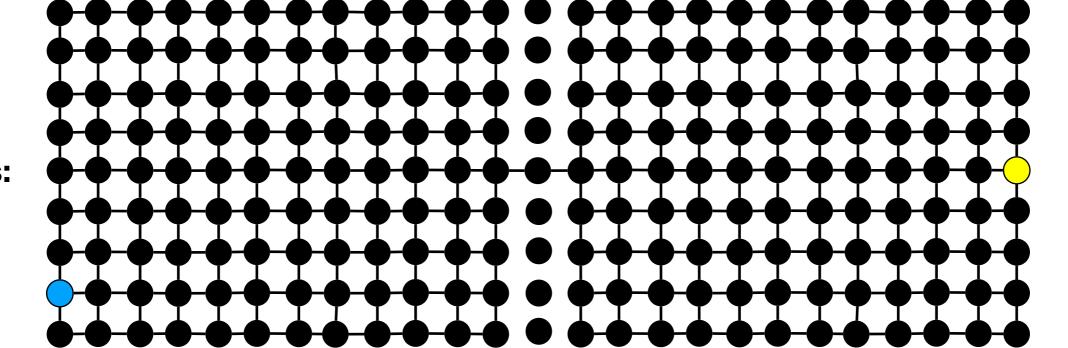
## Pathfinding on a Grid

- Convert the map to a graph
- Start at the node containing the Al Player location
- Run BFS until the enemy base is reached
- Backtrack to build the path for the AI to travel



## Pathfinding on a Grid





Al sees:

We see:

#### Lecture Question

## Task: Find the distance between two nodes in a graph

- In the Graph class
  - Write a method named distance that takes two node indices (Ints) and returns the distance between the two nodes
  - You may assume the two input nodes are connected