

Memory Diagrams

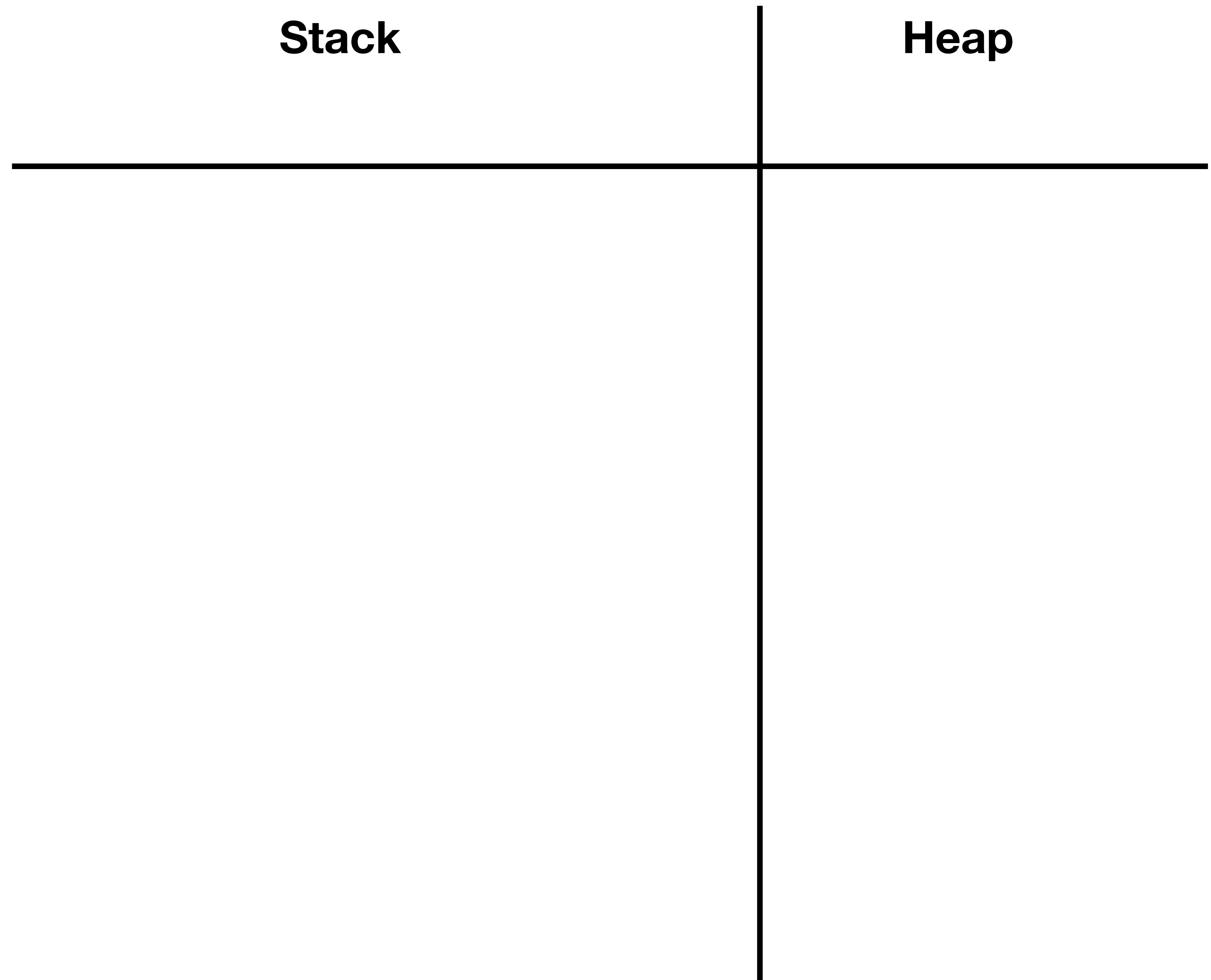
More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Draw a memory diagram for this program

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
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  z  
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def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- Start by setting up the diagram
- Separate columns for stack and heap memory

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
    val x: Int = 20
    if (y < 0) {
      val x: Int = 1
      z += x
    } else {
      val x: Int = 1
      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```

[illegible]

- Separate the stack into name and value

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
    val x: Int = 20
    if (y < 0) {
      val x: Int = 1
      z += x
    } else {
      val x: Int = 1
      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```

Stack		Heap
Name	Value	
		<u>in/out</u>

- Add a section wherever you have room for inputs and outputs
- This is where you what what's printed to the screen

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



Stack		Heap
Name	Value	
x	5	
y	2	
		<u>in/out</u>

- Start tracing the program from main
- First 2 lines add variables to the stack

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



Stack		Heap
Name	Value	
x	5	
y	2	
z		
		<u>in/out</u>

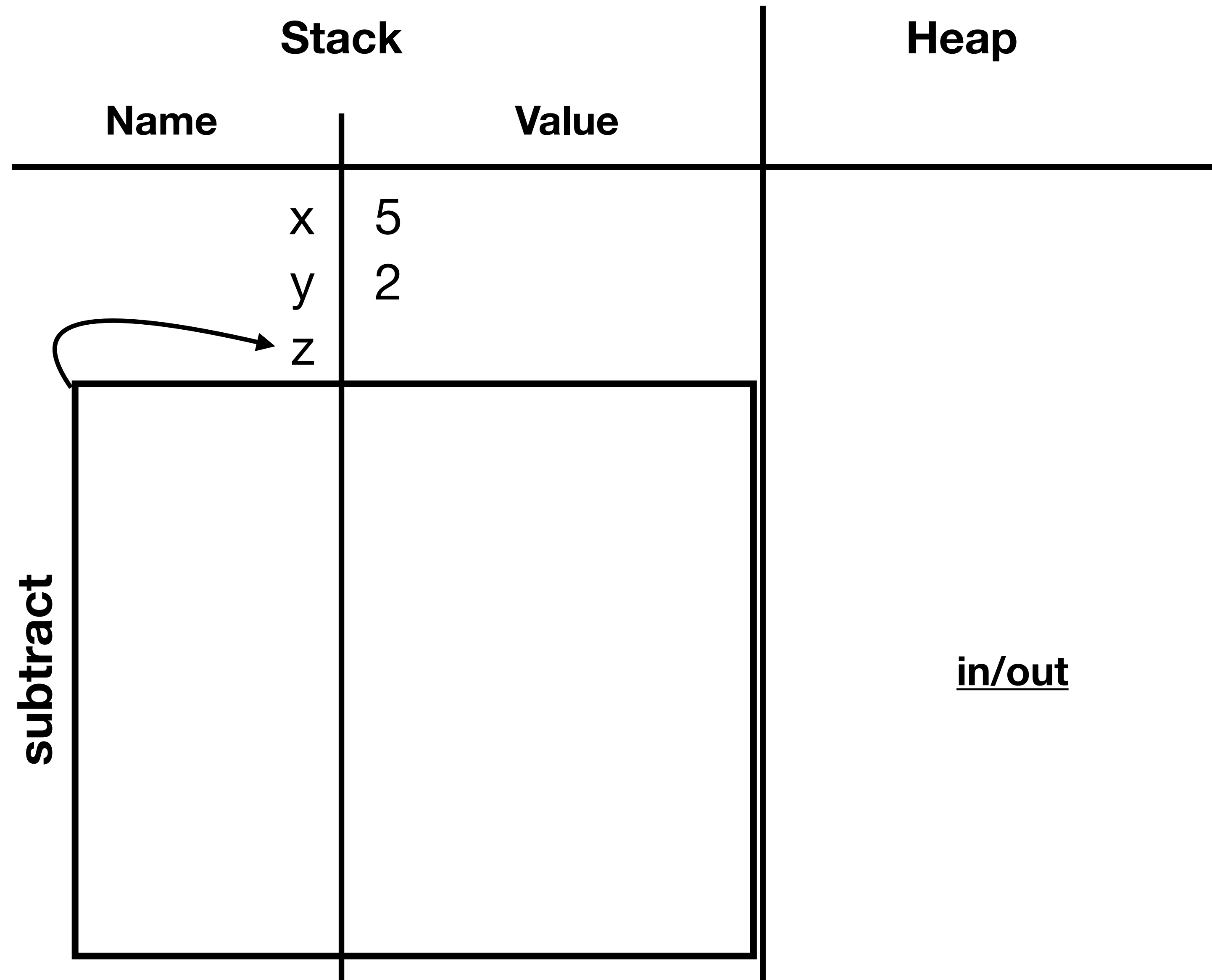
- We call a method named subtract
- Add the return variable to the stack

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
    val x: Int = 20
    if (y < 0) {
      val x: Int = 1
      z += x
    } else {
      val x: Int = 1
      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```

- Draw a solid box for the **Stack Frame**
- Arrow to the return variable and name of method being called

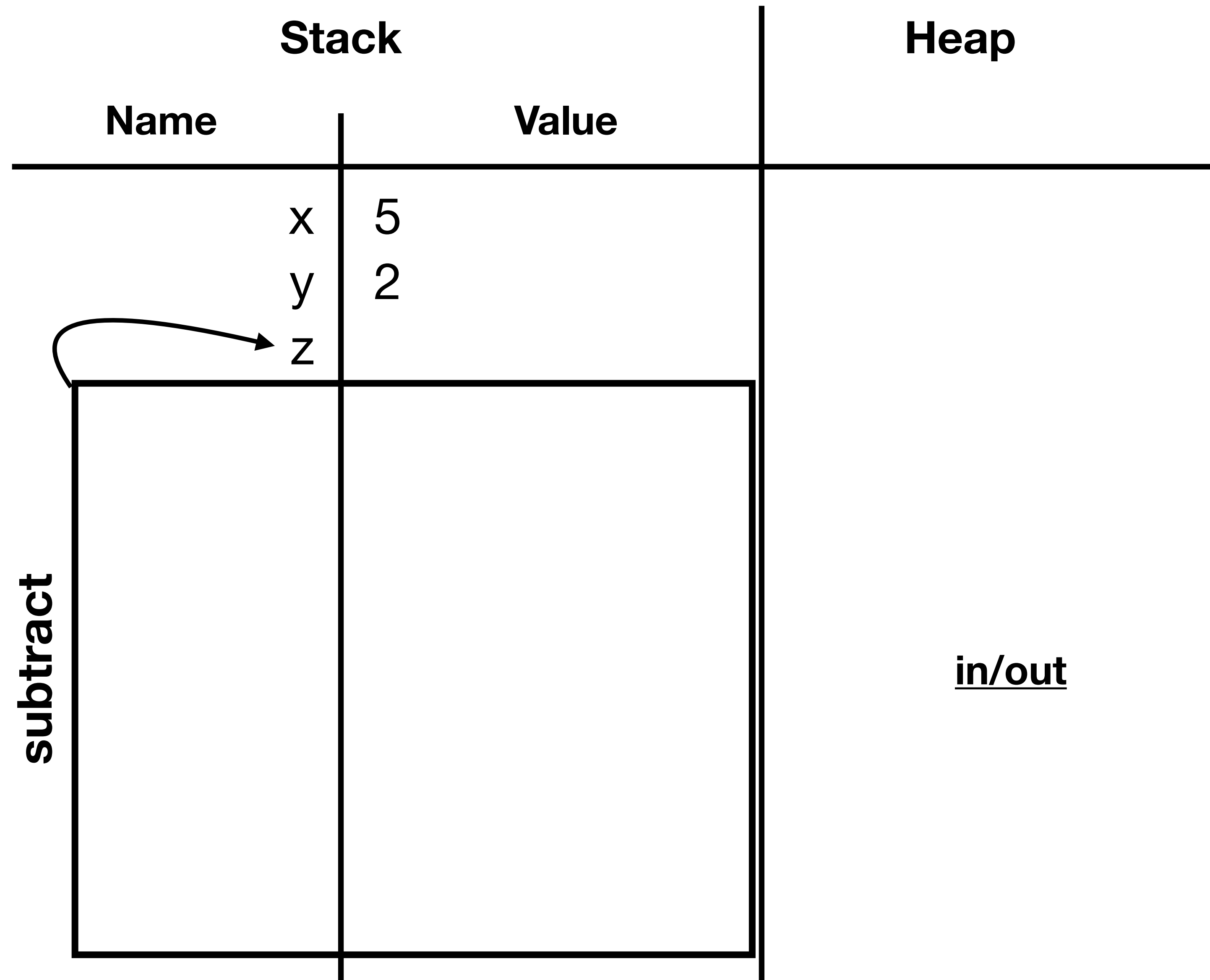


More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
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  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- The stack frame cannot be crossed
- Can't access variables across the solid box

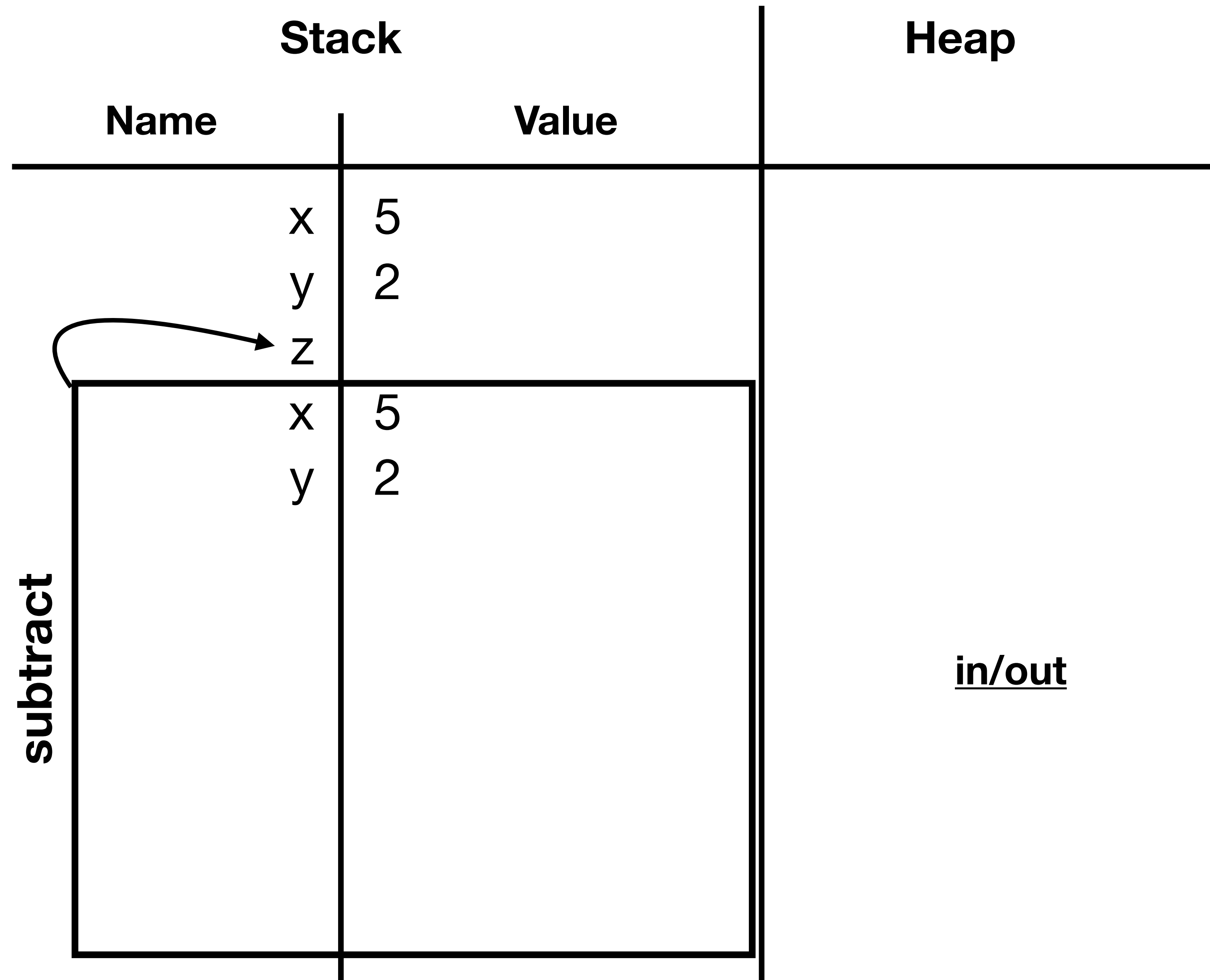


More Memory Examples



```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
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  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Add the names of the parameters with the values of the arguments inside the stack frame

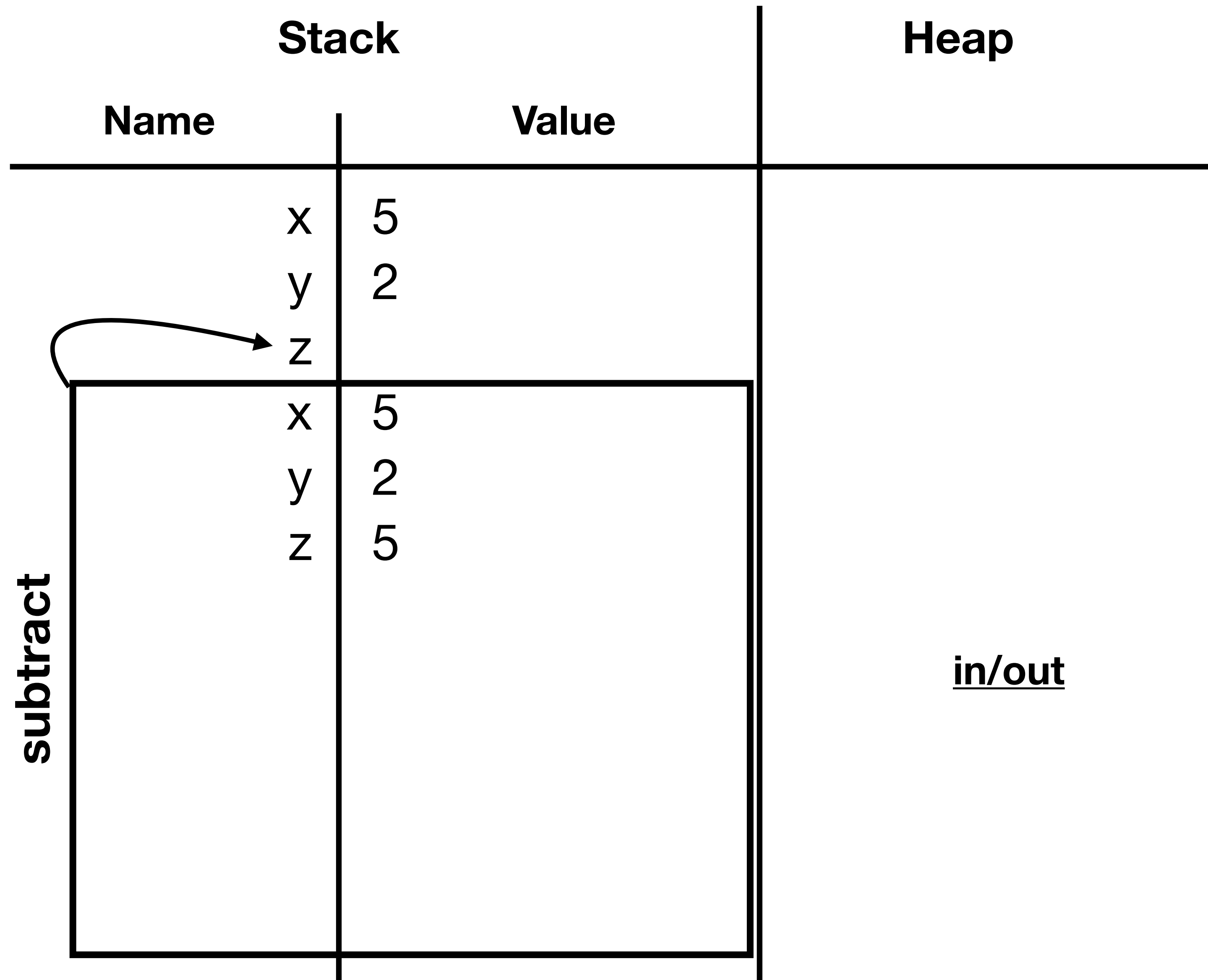


More Memory Examples



```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Add z equal to the value of x
- Two x's on the stack
- Only 1 inside this stack frame!

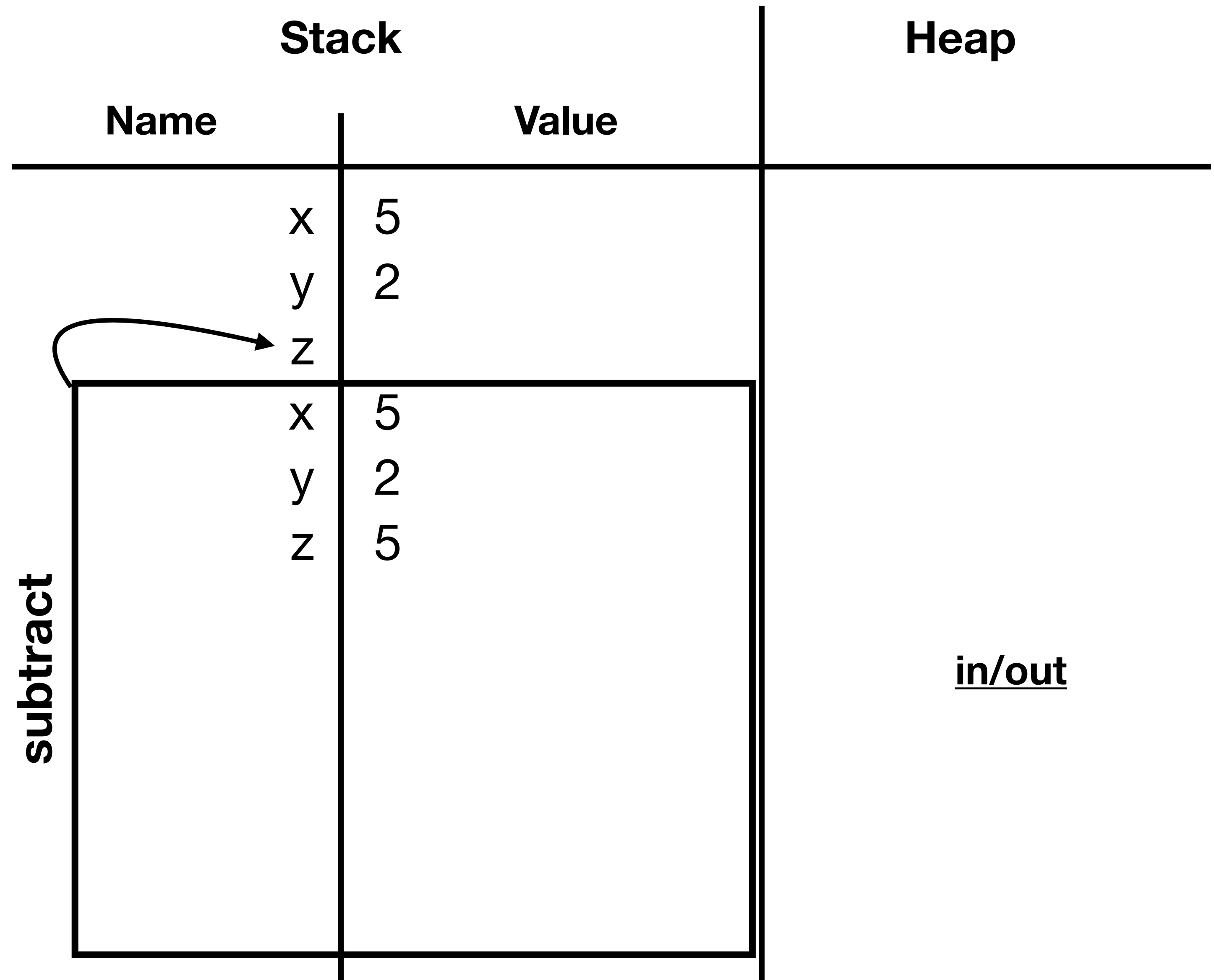


More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
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def main(args: Array[String]): Unit = {  
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  val y: Int = 2  
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  println(z)  
}
```

- Can reuse variable names in different stack frames

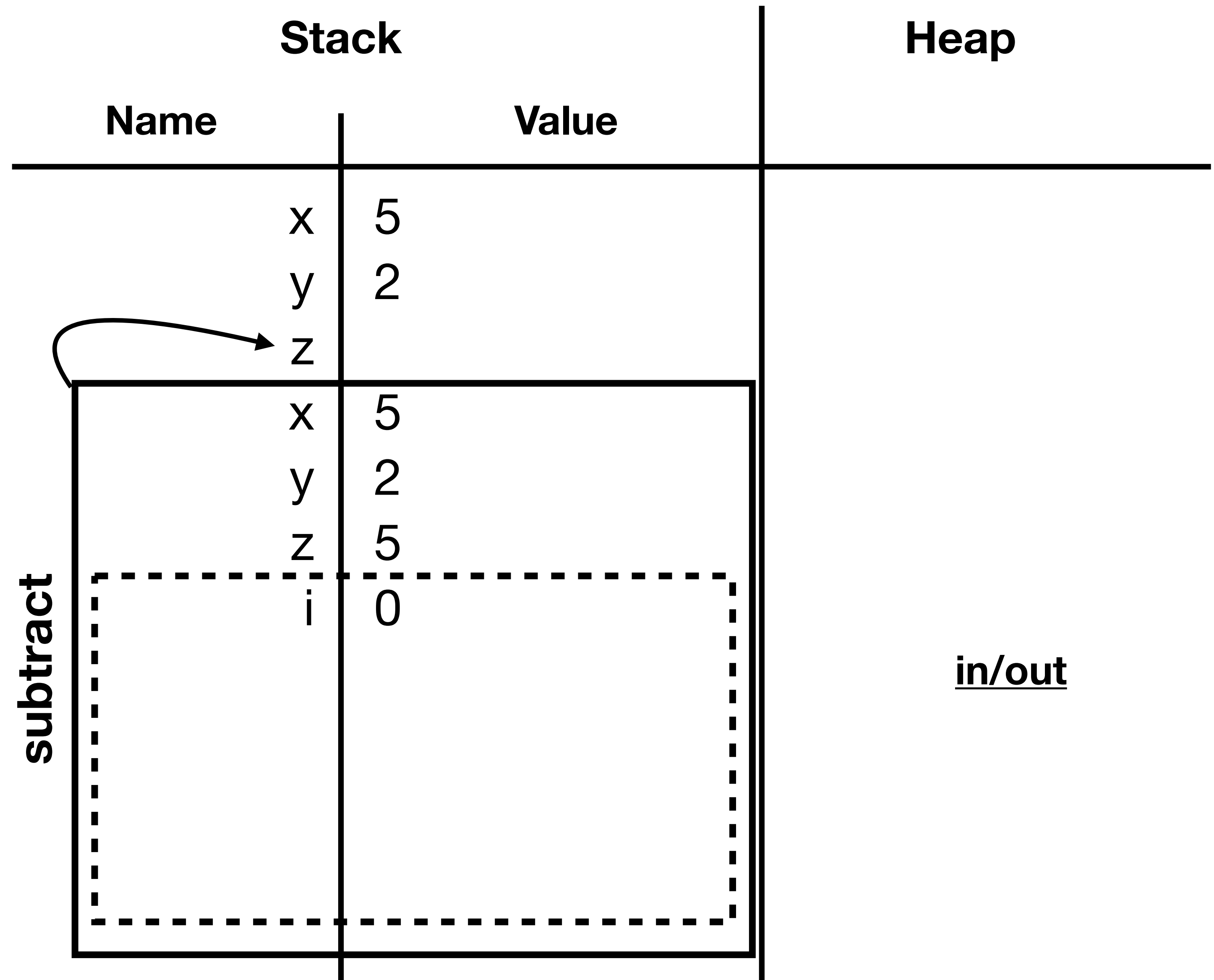


More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
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    if (y < 0) {  
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      z += x  
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      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Start of a code block for a loop
- New code block whenever there are { } that do not define a method

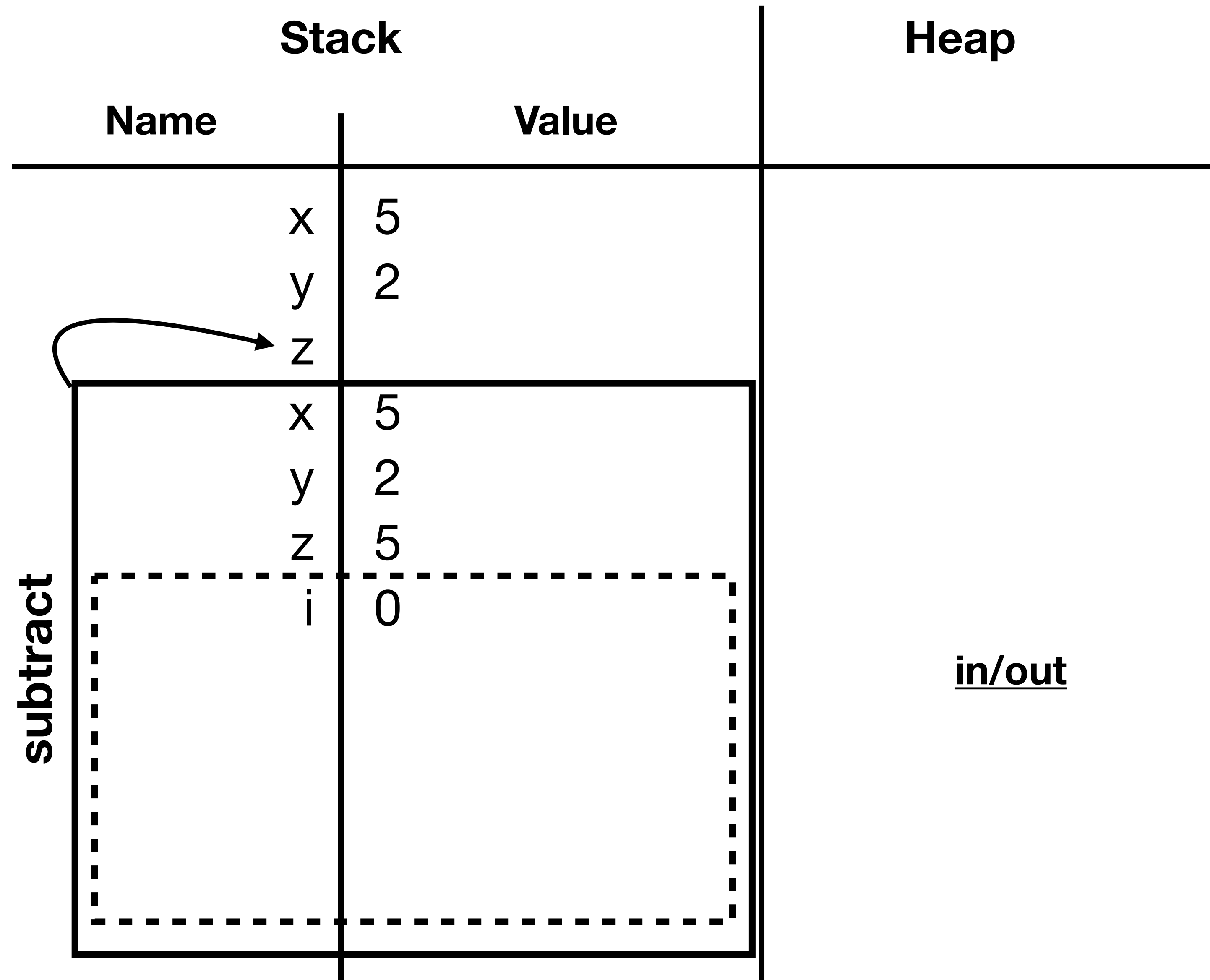


More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Draw a dotted box for code blocks
- Dotted lines can *sometimes* be crossed

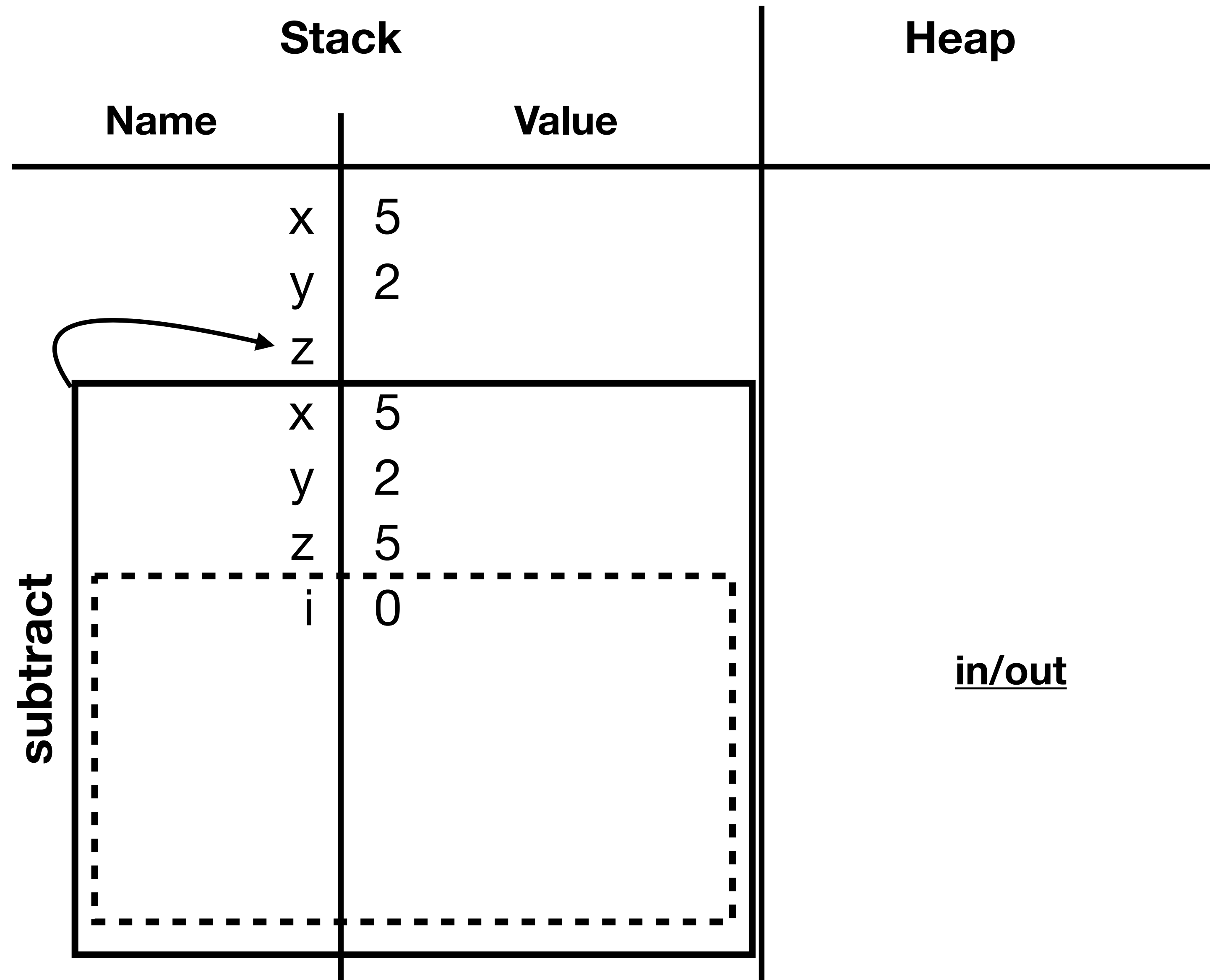


More Memory Examples



```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
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def main(args: Array[String]): Unit = {  
  val x: Int = 5  
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  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Code blocks affect **Variable Scope**
- Variable scope determines which variables can be accessed



More Memory Examples




- Variables in another stack frame are always **out of scope**
- Cannot access variables across stack frames

Stack		Heap
Name	Value	
x	5	
y	2	
z		
x	5	
y	2	
z	5	
i	0	

subtract

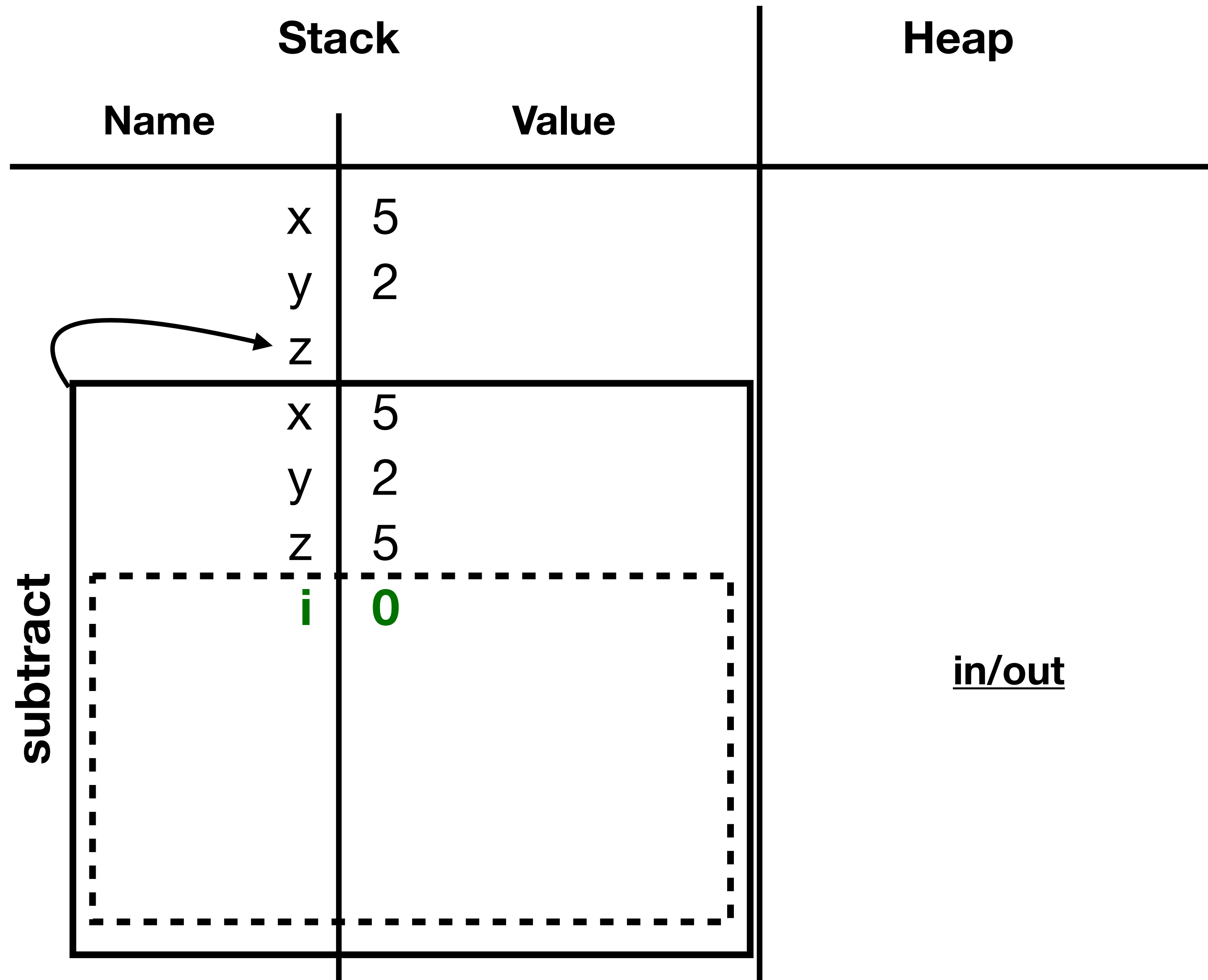
in/out

More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
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def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Variables in the current code block are always **in scope**
- Can always be accessed

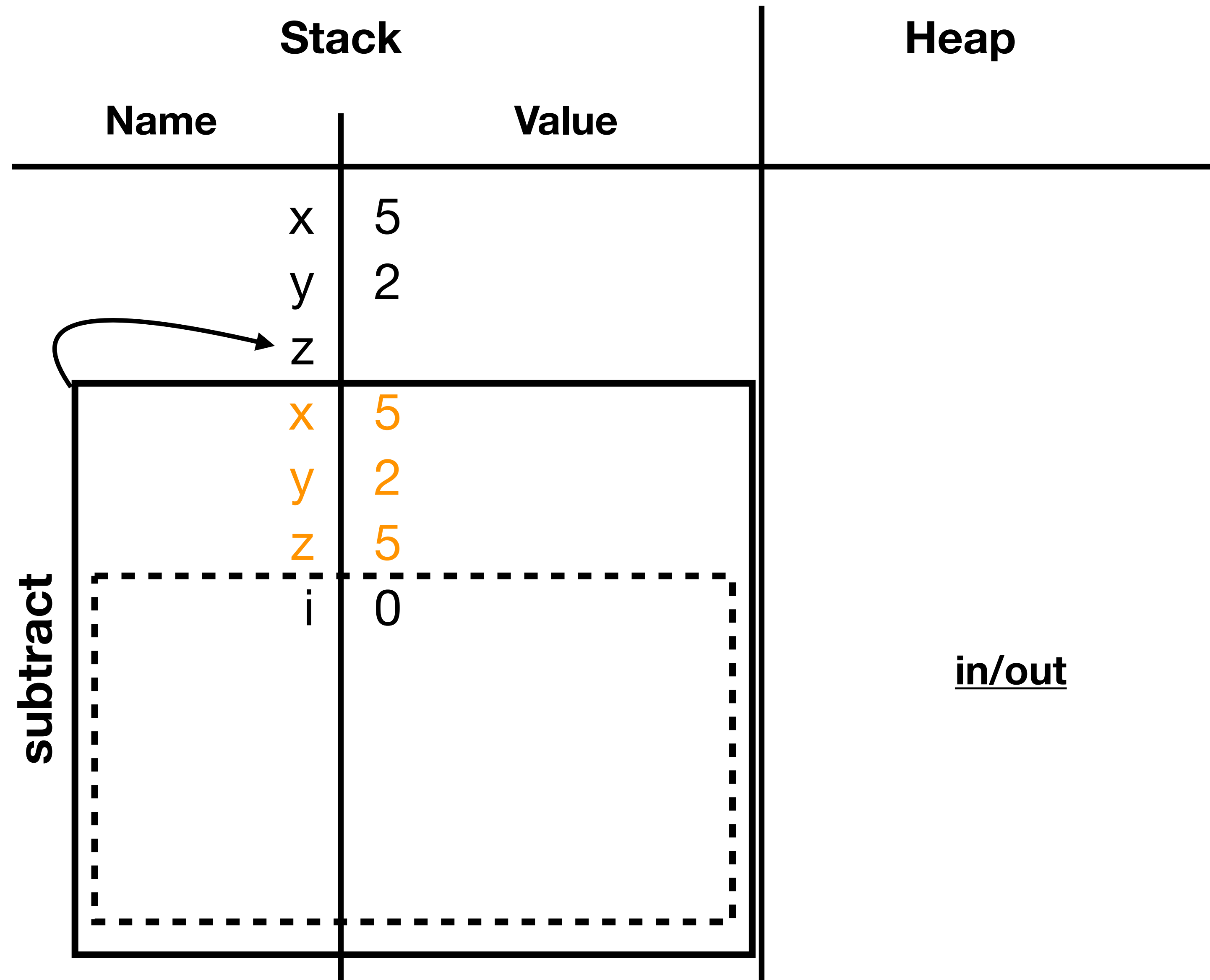


More Memory Examples




```
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  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
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def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Variable in the current stack frame, but not in the current code block, are *usually in scope*
- Except when another variable with the same name is in scope

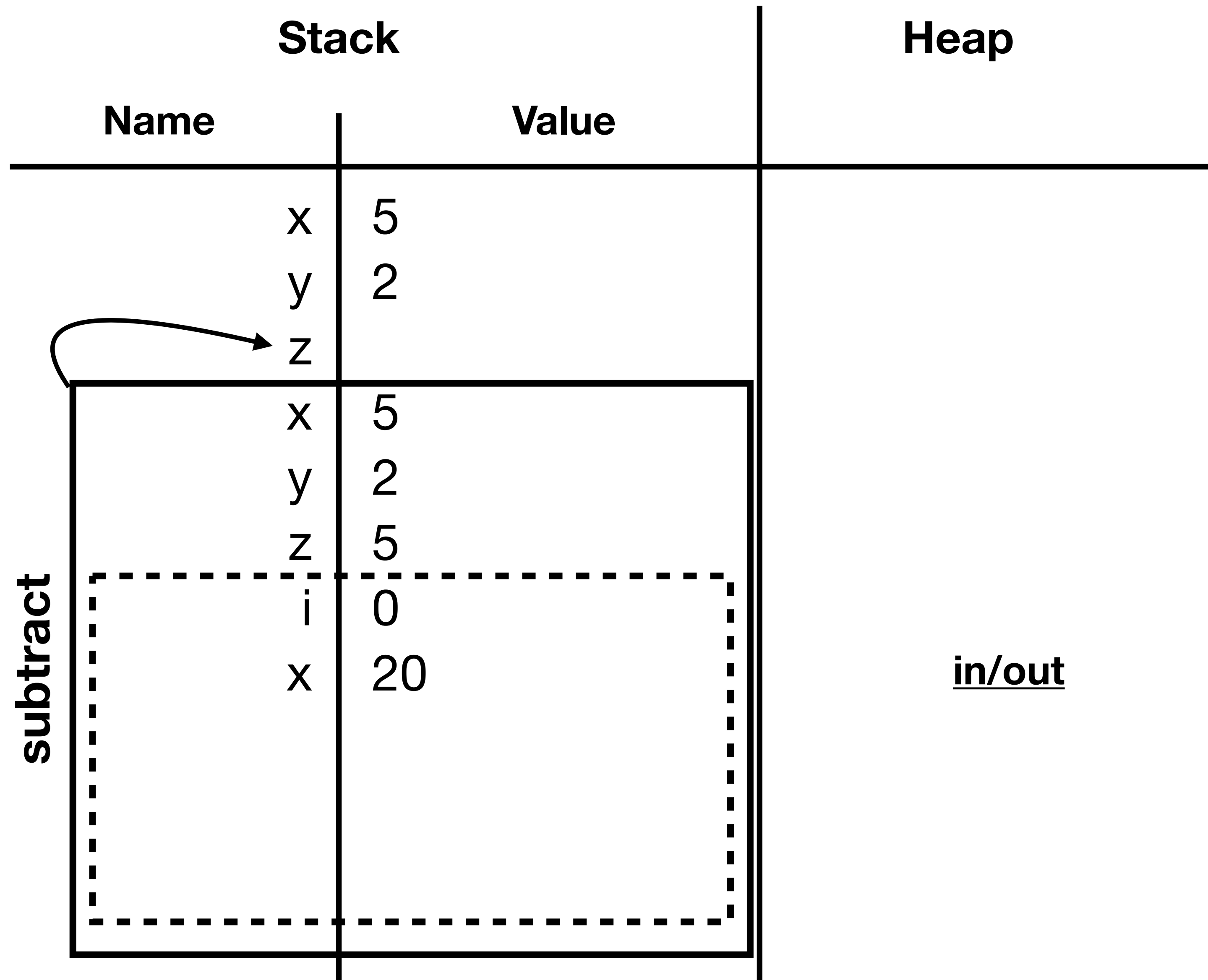


More Memory Examples




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  var z: Int = x  
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  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Whenever val or var are used, a new variable is being added to the stack
- We can have multiple variables with the same name in the same stack frame!

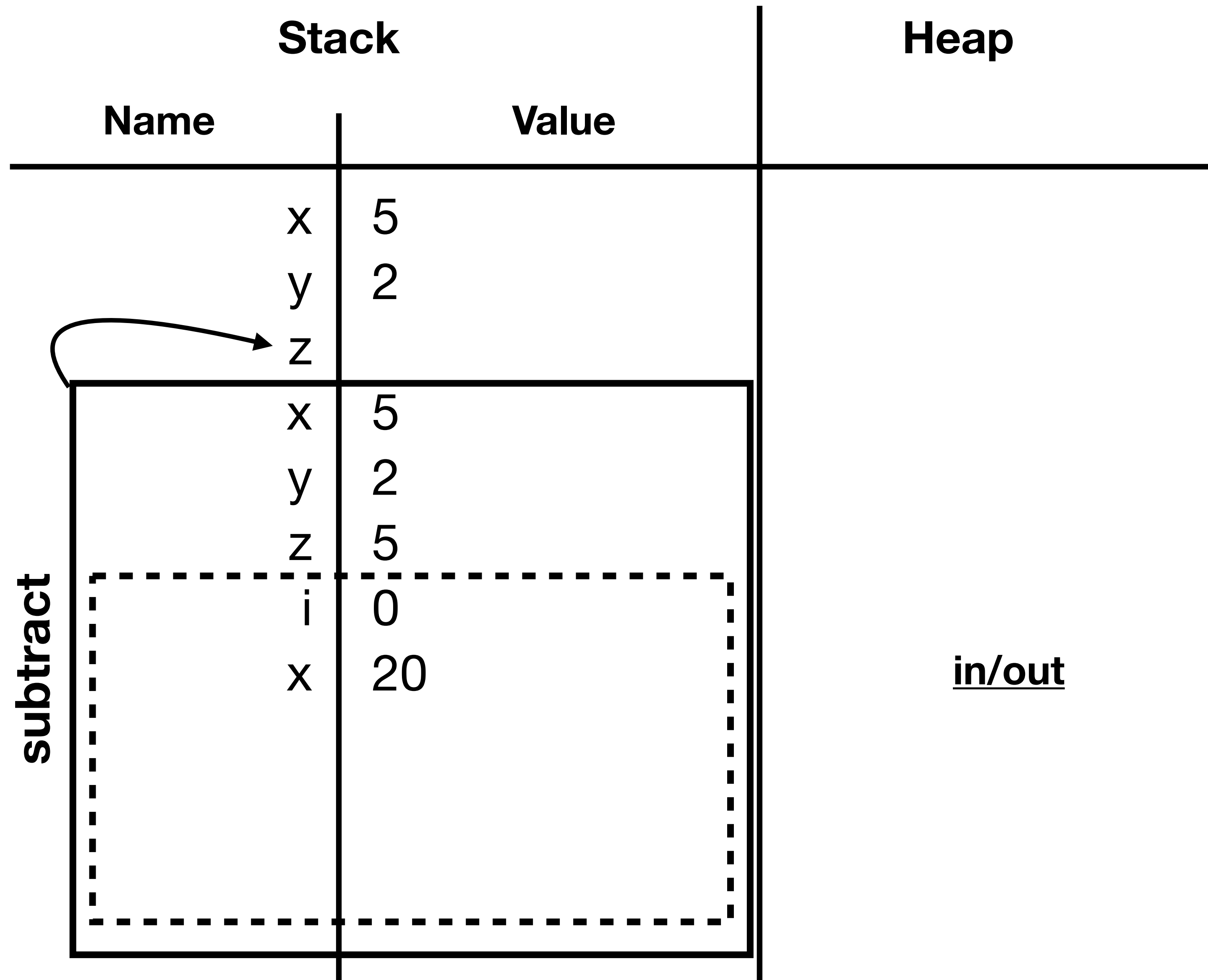


More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
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    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- We can have multiple variables with the same name in the same **stack frame**!
- As long as they are not in the same **code block**

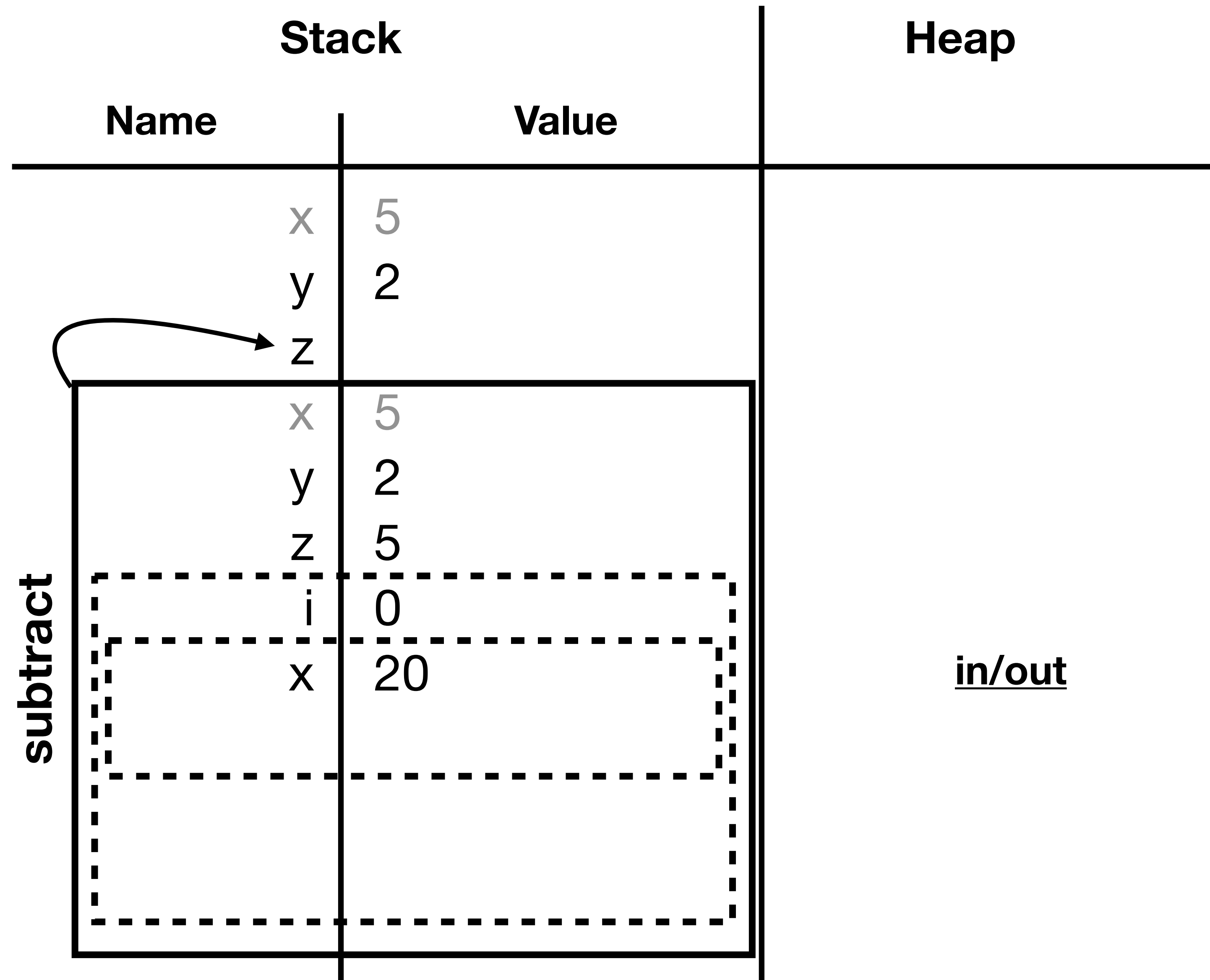


More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
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def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- For each iteration of the loop, draw a new dotted box
- Each iteration is a separate block with separate variables

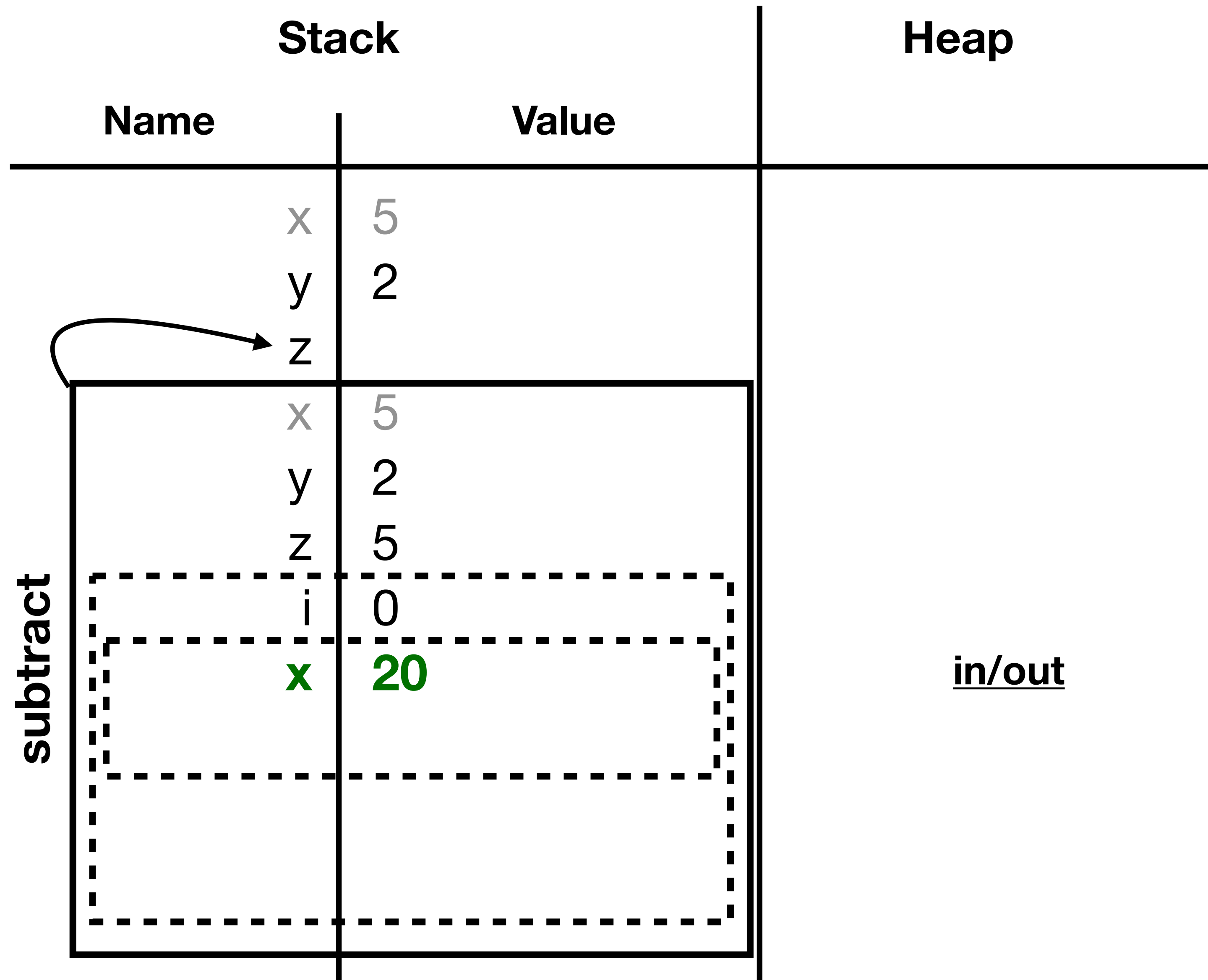


More Memory Examples




```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
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    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Since variables in the current code block are always in scope, the x with 20 will be accessed if x is used
- The other 2 x's cannot be accessed



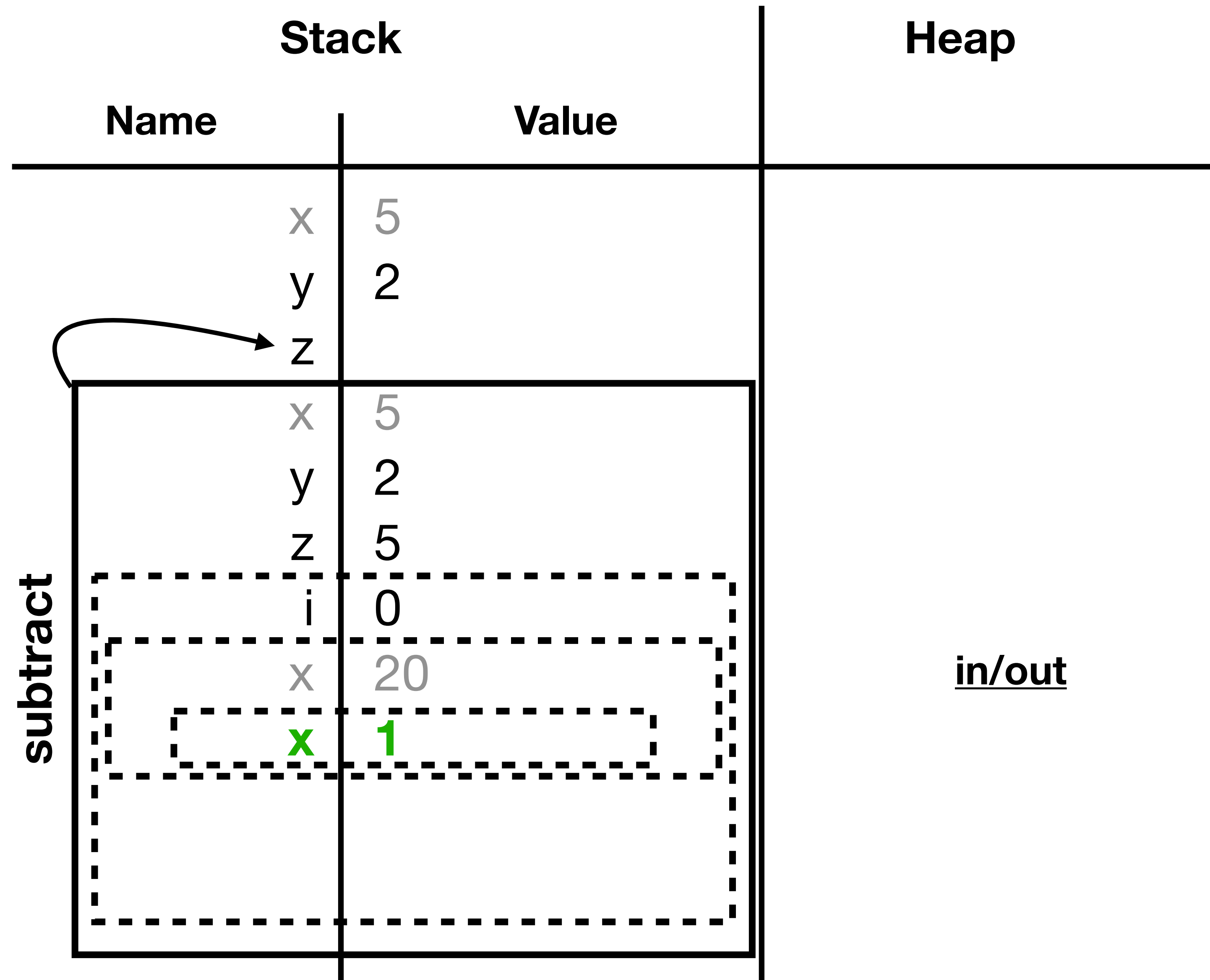
More Memory Examples




```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
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      z += x
    } else {
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      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```

- Add another x to the stack in a new code block
- Now this is the only x in scope

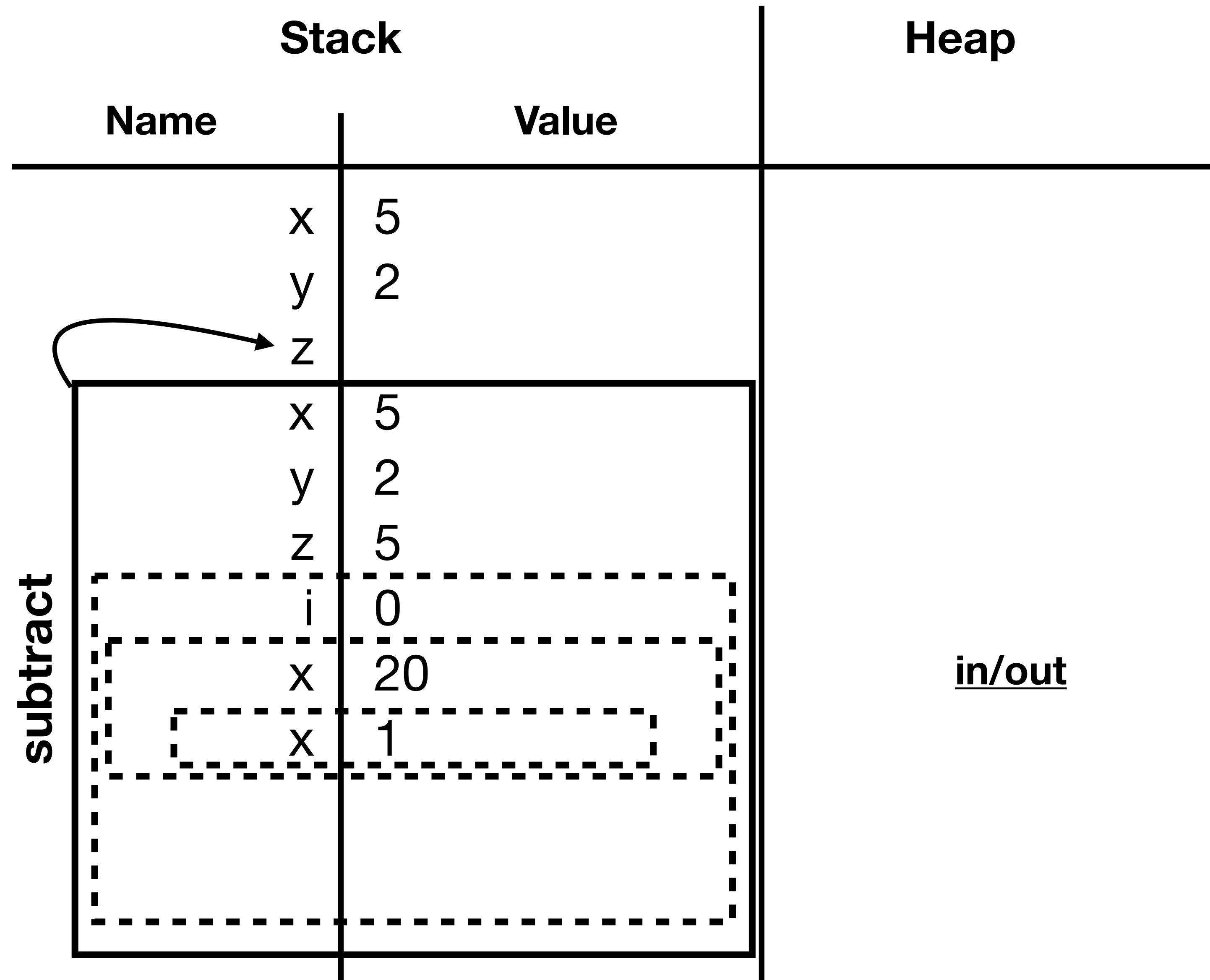


More Memory Examples



```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
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    if (y < 0) {  
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      z += x  
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      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- `z -= x`
- But we have 4 x's on the stack!
- Which one is used??

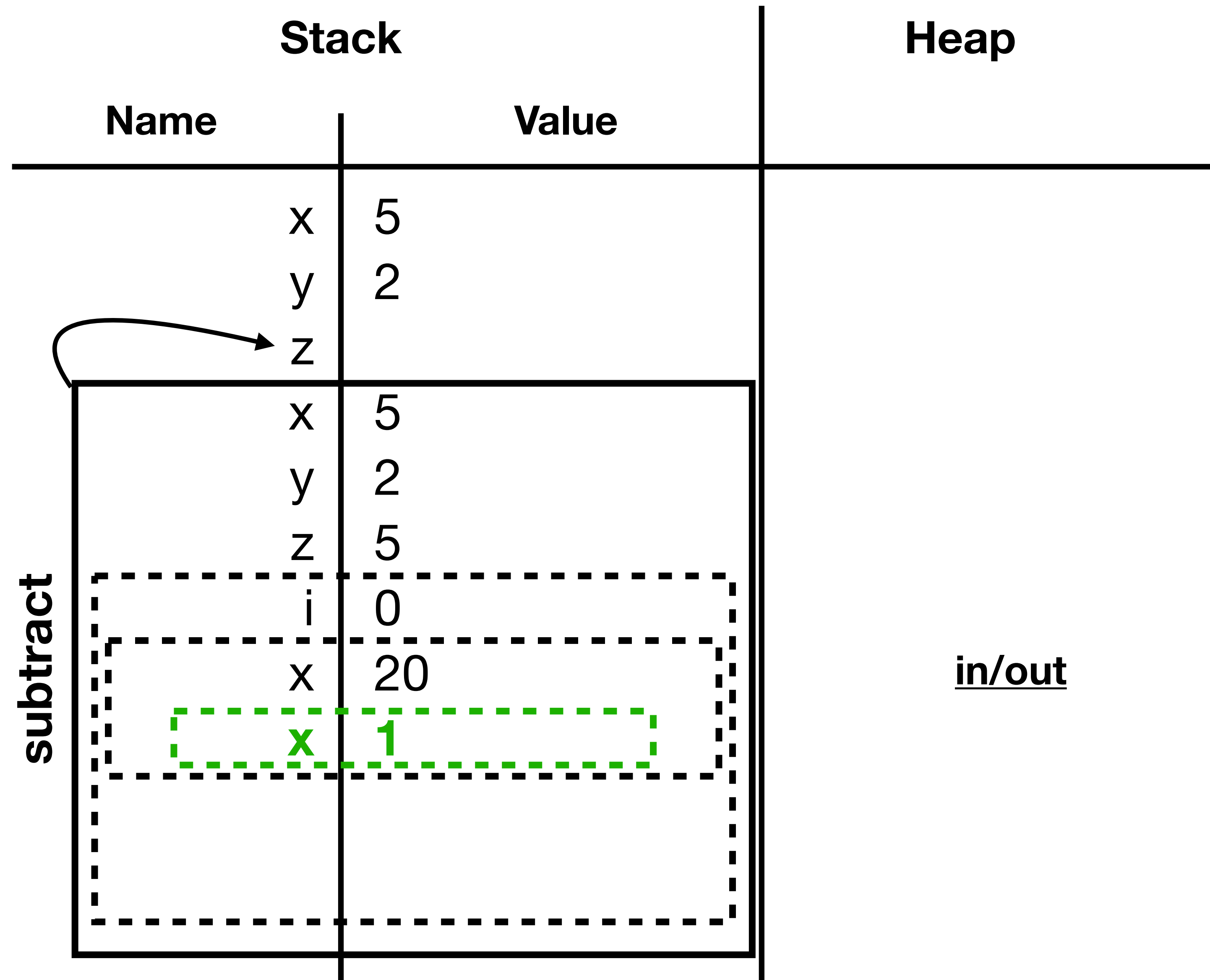


More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
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      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- Use the one in the inner-most code block
- The current code block has an x, use that one

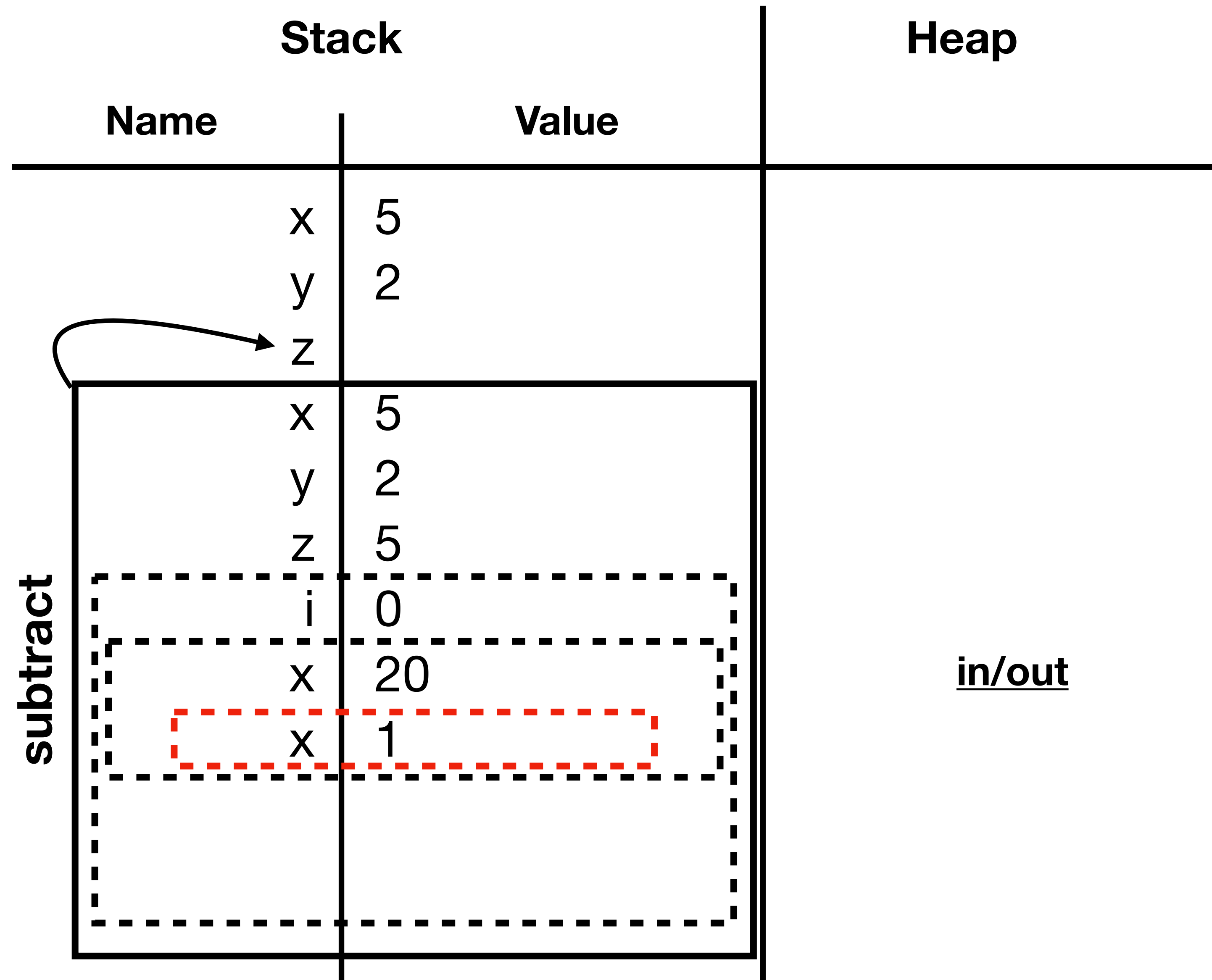


More Memory Examples

```
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  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
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    }  
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  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- We're also accessing z
- Current code block does not contain a z



More Memory Examples

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  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- Continue searching in the next code block
- Still no z...

Stack		Heap
Name	Value	
x	5	
y	2	
z		
subtract	x	5
	y	2
	z	5
	i	0
	x	20
	x	1

in/out

More Memory Examples


```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
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def main(args: Array[String]): Unit = {  
  val x: Int = 5  
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Stack		Heap
Name	Value	
x	5	
y	2	
z		
<div><div>subtract</div><div><div><div>x</div><div>5</div></div><div><div>y</div><div>2</div></div><div><div>z</div><div>5</div></div><div><div>i</div><div>0</div></div><div><div>x</div><div>20</div></div><div><div>x</div><div>1</div></div></div></div>		
		<u>in/out</u>

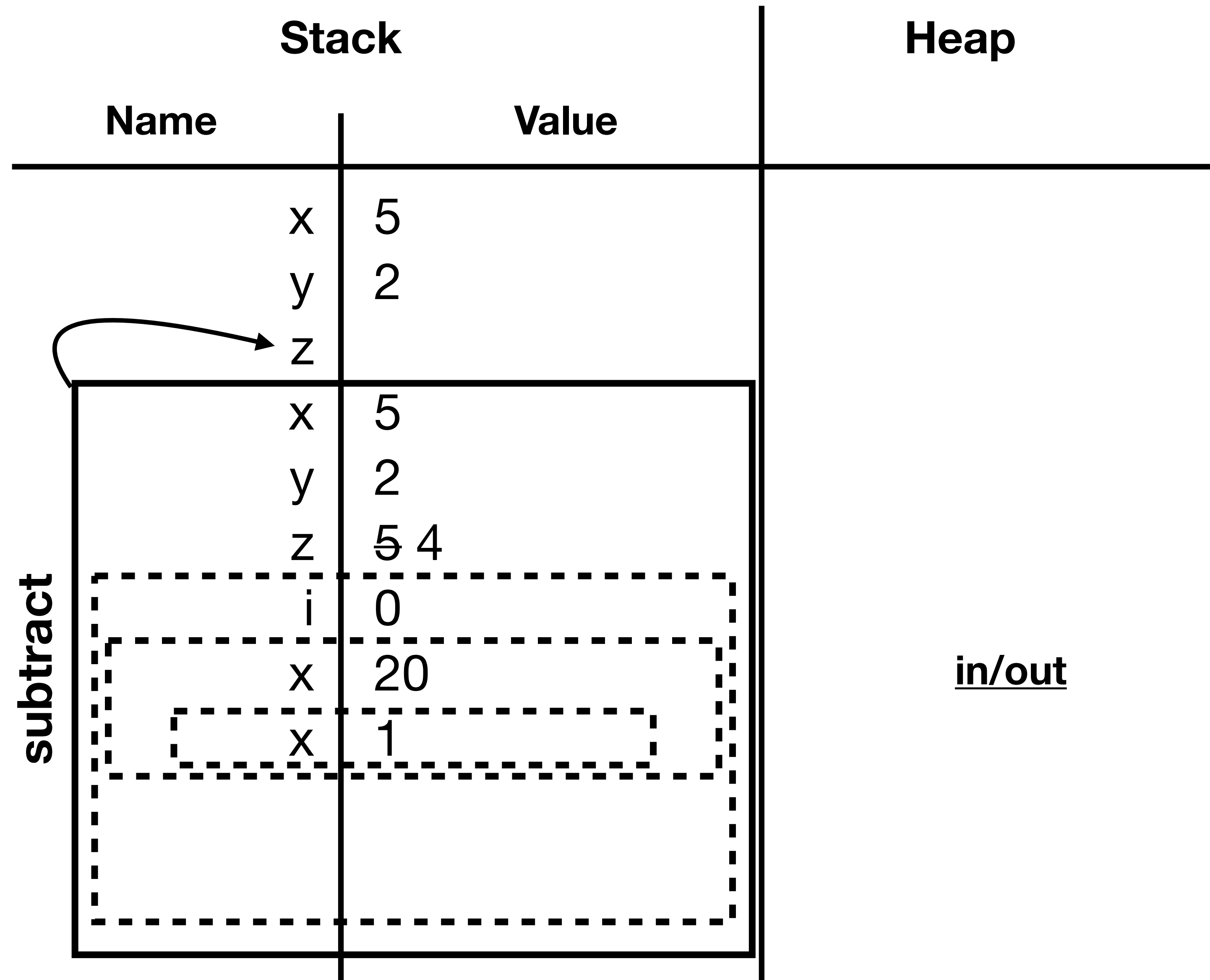
- Keep searching code blocks until we reach the stack frame
- Found a z! Use it.

More Memory Examples



```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
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def main(args: Array[String]): Unit = {  
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  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Subtract 1 from z

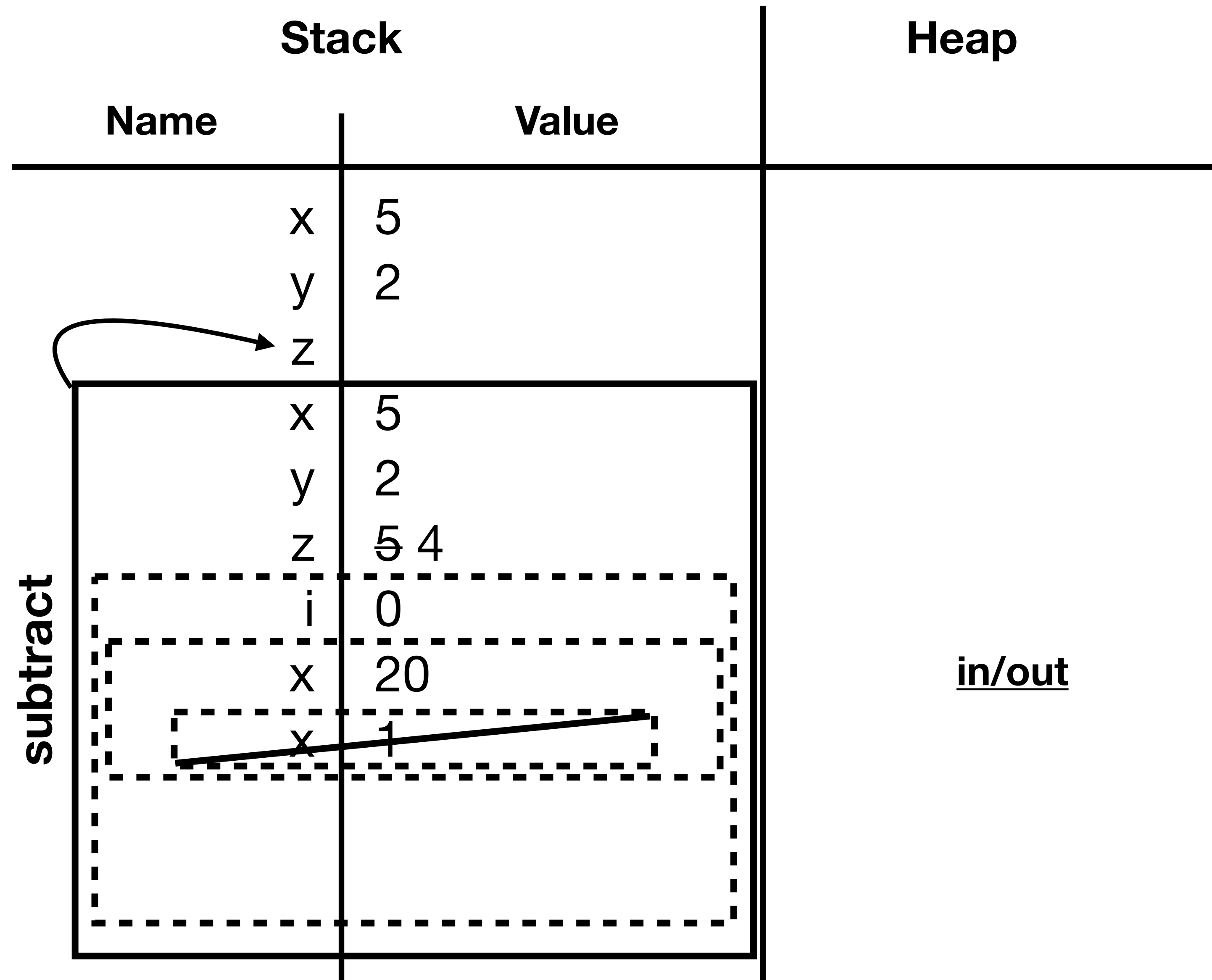


More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

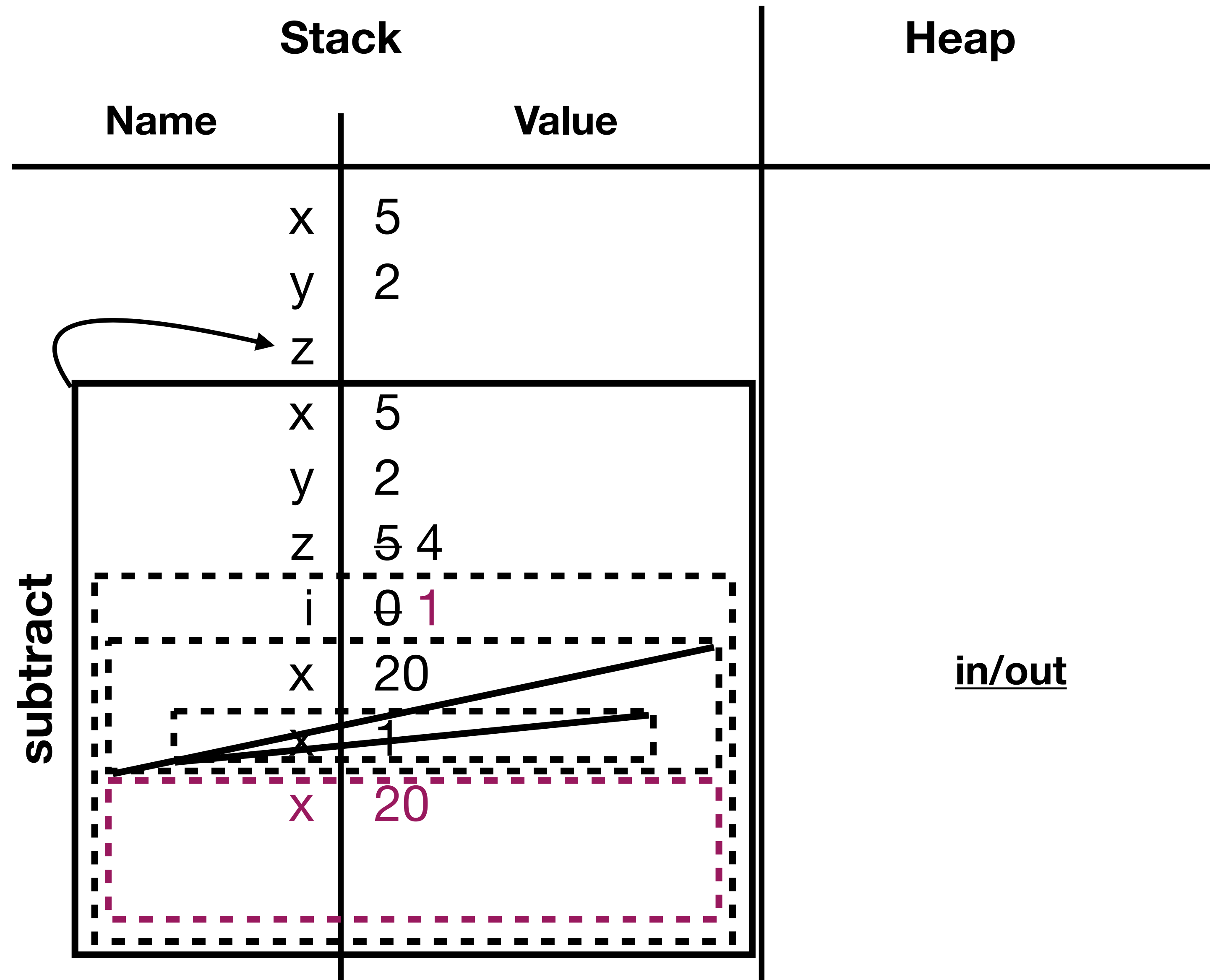


- End of the if/else code block
- Cross it out
- The x with value 1 is no longer on the stack and the x with 20 is back in scope



More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

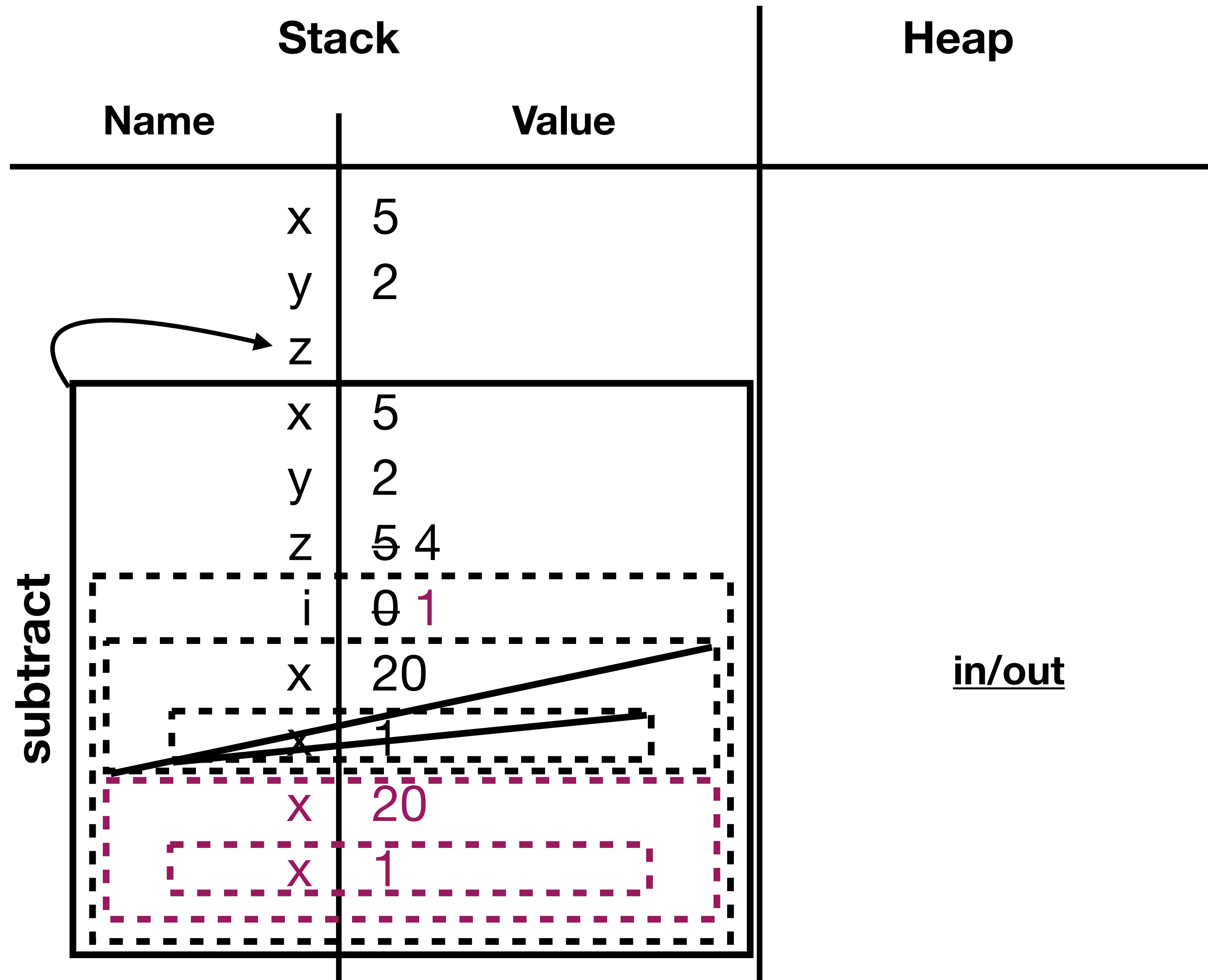


- This iteration of the loop ends
- Cross out the block and create a new block for the next one

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```

- Do the same thing for the next iteration

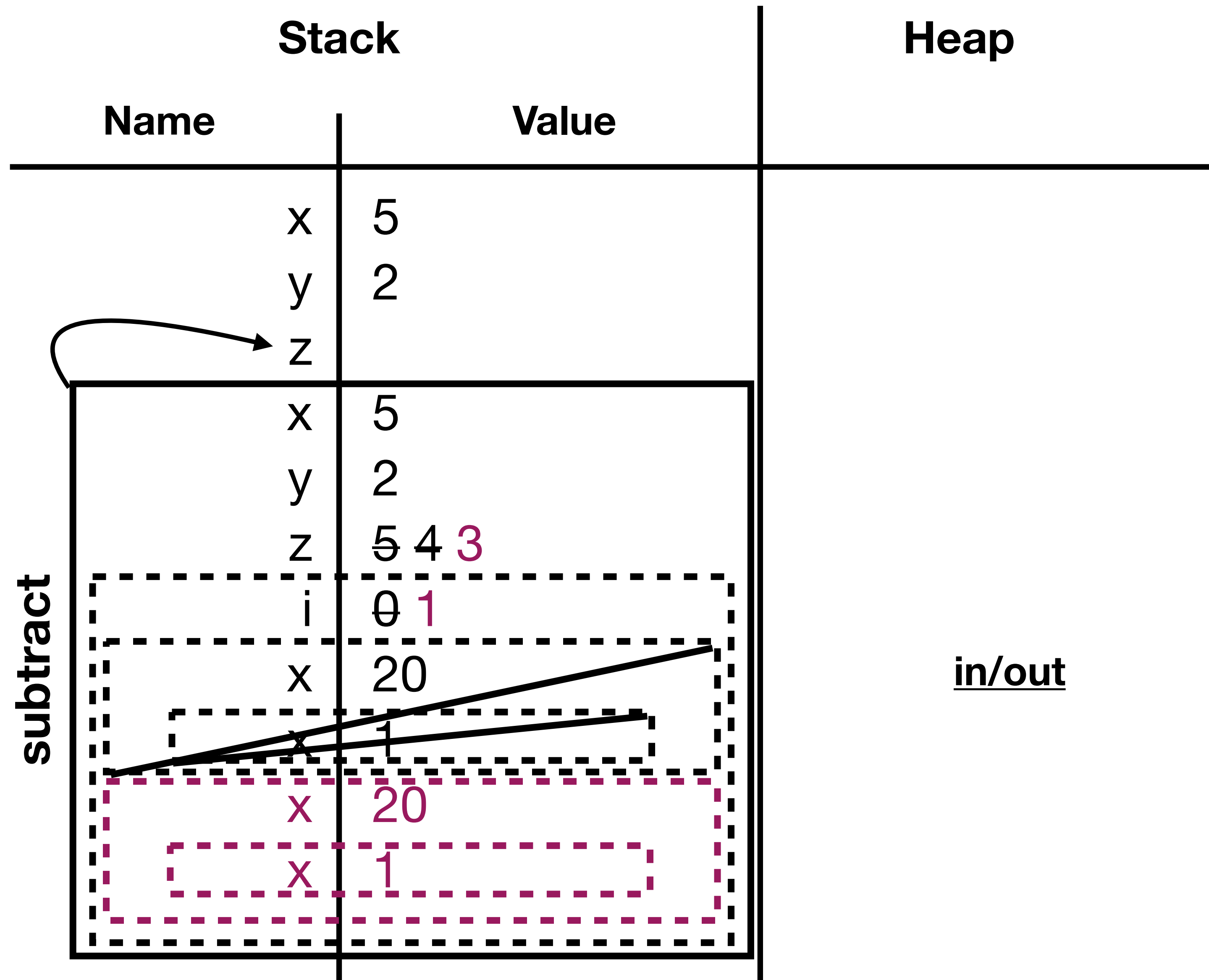


More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- Update z
- Found an x with value 1 in the inner-most block



More Memory Examples

```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
    val x: Int = 20
    if (y < 0) {
      val x: Int = 1
      z += x
    } else {
      val x: Int = 1
      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```

- End of the if/else block
- End of this iteration of the loop

Stack		Heap
Name	Value	
x	5	
y	2	
z		
x	5	
y	2	
z	5 4 3	
i	0 1	
x	20	
x	1	
x	20	
x	1	

Diagram illustrating memory layout and stack operations:

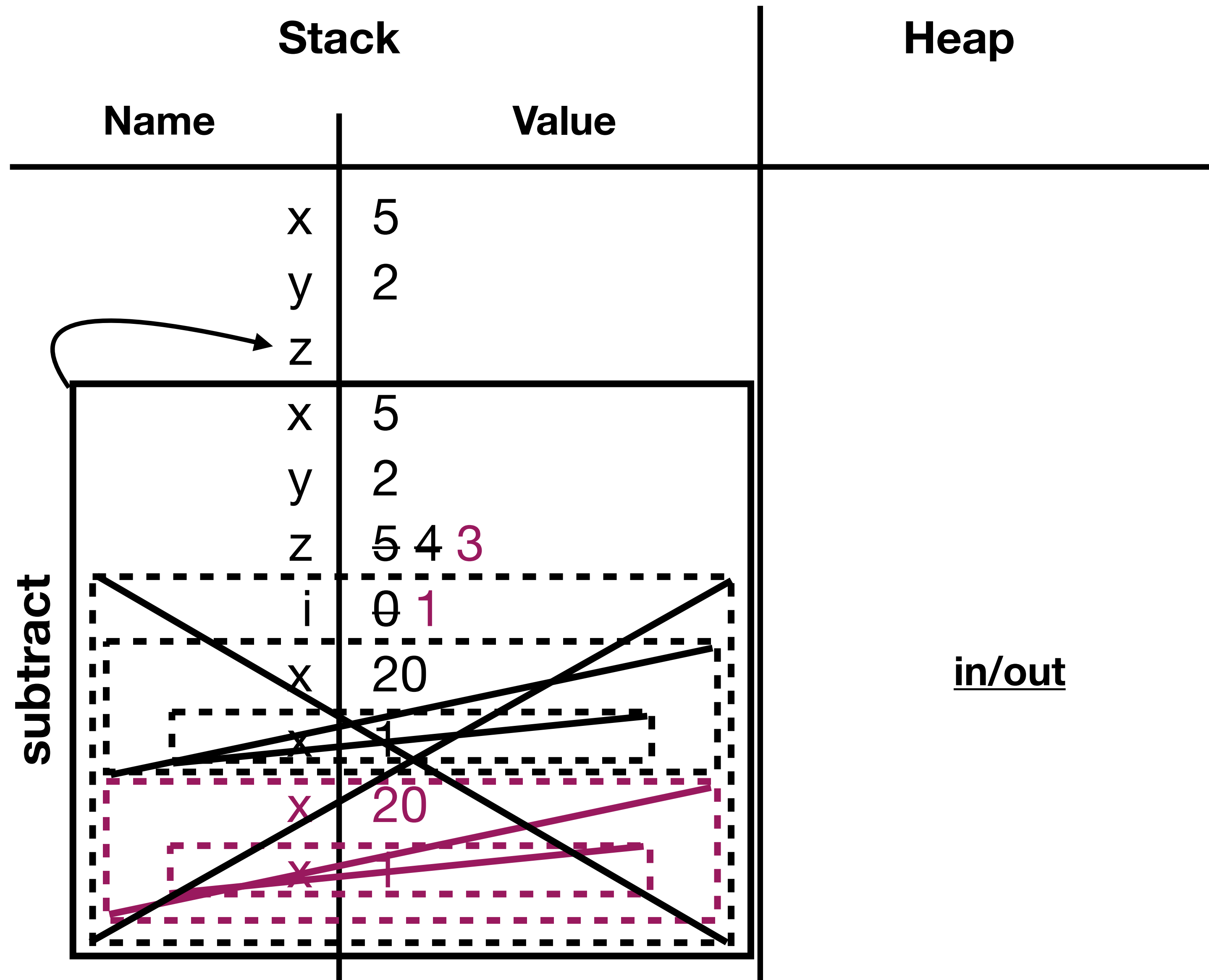
- Stack:** A vertical structure containing variables x, y, z, and their values (5, 2, 5 4 3). Below these are nested frames for variables i, x, and x, with values 0 1, 20, and 1 respectively. The stack is labeled "subtract" on the left.
- Heap:** A vertical structure containing the label "in/out" on the left.
- Annotations:**
 - A curved arrow points from the top of the stack to the variable z.
 - A solid black line connects the top of the stack to the variable x in the first nested frame.
 - A solid black line connects the top of the stack to the variable x in the second nested frame.
 - A solid magenta line connects the top of the stack to the variable x in the third nested frame.
 - A solid magenta line connects the top of the stack to the variable x in the fourth nested frame.

More Memory Examples

```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
    val x: Int = 20
    if (y < 0) {
      val x: Int = 1
      z += x
    } else {
      val x: Int = 1
      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```

- End of the entire loop
 - i is no longer on the stack
 - x with value 5 is back in scope



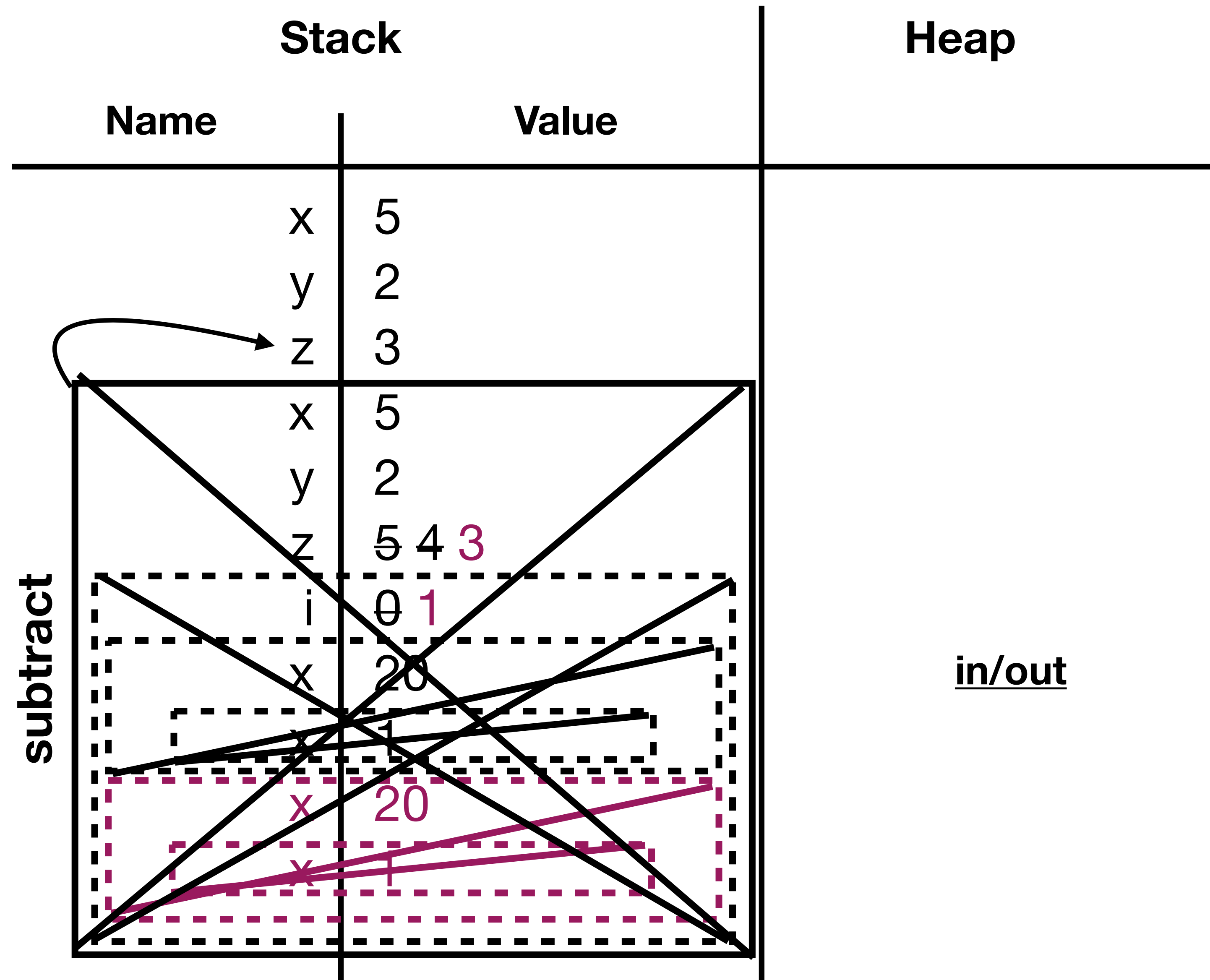
More Memory Examples

```
def subtract(x: Int, y: Int): Int = {
  var z: Int = x
  for (i <- 0 until Math.abs(y)) {
    val x: Int = 20
    if (y < 0) {
      val x: Int = 1
      z += x
    } else {
      val x: Int = 1
      z -= x
    }
  }
  z
}

def main(args: Array[String]): Unit = {
  val x: Int = 5
  val y: Int = 2
  val z: Int = subtract(x, y)
  println(z)
}
```



- Return the value of z to the variable z in the main stack frame
- Cross out the entire stack frame



More Memory Examples

```
def subtract(x: Int, y: Int): Int = {  
  var z: Int = x  
  for (i <- 0 until Math.abs(y)) {  
    val x: Int = 20  
    if (y < 0) {  
      val x: Int = 1  
      z += x  
    } else {  
      val x: Int = 1  
      z -= x  
    }  
  }  
  z  
}  
  
def main(args: Array[String]): Unit = {  
  val x: Int = 5  
  val y: Int = 2  
  val z: Int = subtract(x, y)  
  println(z)  
}
```



- Print 3 to the screen
- End of program

