

Kyla Ma A18254929
Sathwika Peechara A18323107
Shreyansika Singh A17758951
Shivani Sridhar A18301752
Emma Wolfgram A17807337

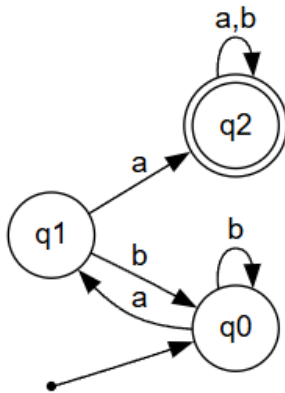
Section 1: Problem 1

Consider DFA $M = (Q = \{q_0, q_1, q_2\}, \Sigma = \{a, b\}, \delta, q_0 = q_0, F = \{q_2\})$ with transitions:

- $\delta(q_0, a) = q_1, \delta(q_0, b) = q_0$
- $\delta(q_1, a) = q_2, \delta(q_1, b) = q_0$
- $\delta(q_2, a) = q_2, \delta(q_2, b) = q_2$

Trace the computation on input $w = abba$.

List the sequence of states visited (including start state) and state whether the input w is accepted.



$w = abba$

Sequence: $q_0, q_1, q_0, q_0, q_1 \rightarrow$ we end at state q_1 , which is not an accept state so we reject w .

Kyla Ma A18254929

Sathwika Peechara A18323107

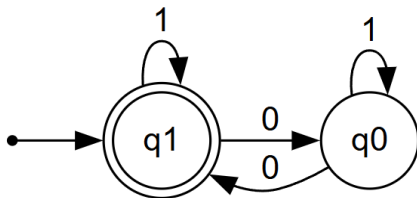
Shreyansika Singh A17758951

Shivani Sridhar A18301752

Emma Wolfgram A17807337

Section 2: Problem 5

Draw a DFA over the alphabet $\{0,1\}$ that accepts all strings containing an even number of 0's.



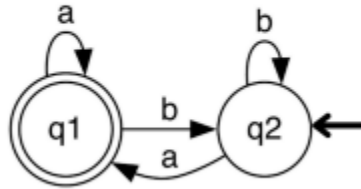
$M = (\{q_0, q_1\}, \{0, 1\}, \delta, q_1, \{q_1\})$

Input in $Q \times E$	Output in Q
$(q_1, 1)$	q_1
$(q_1, 0)$	q_0
$(q_0, 0)$	q_1
$(q_0, 1)$	q_0

Kyla Ma A18254929
Sathwika Peechara A18323107
Shreyansika Singh A17758951
Shivani Sridhar A18301752
Emma Wolfgram A17807337

Section 3: Problem 11

Consider the DFA over $\{a,b\}$ below. Explain what type of strings this DFA accepts?



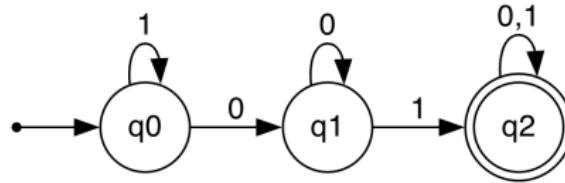
Hint: List down 5 strings this DFA accepts. Do you notice a pattern?

- 5 example strings: a / a,a,a,a,a,a / b,a / b,b,b,b,a / a,b,b,b,a
- The DFA only accepts strings that end in an 'a' because the accept state is q1. All the incoming transition arrows to q1 (the accepted state) are labeled 'a', meaning the last element in the sequence of any w must be 'a'.
- $\{w \mid w \text{ ends with } a\}$

Kyla Ma A18254929
Sathwika Peechara A18323107
Shreyansika Singh A17758951
Shivani Sridhar A18301752
Emma Wolfgram A17807337

Section 4: Problem 14

Given the DFA below, write its 5-tuple $(Q, \Sigma, \delta, q_0, F)$ explicitly. Use a table to define δ .



$M = (\{q_0, q_1, q_2\}, \{0, 1\}, \delta, q_0, \{q_2\})$

Input in $Q \times E$	Output in Q
$(q_0, 0)$	q_1
$(q_0, 1)$	q_0
$(q_1, 0)$	q_1
$(q_1, 1)$	q_2
$(q_2, 0)$	q_2
$(q_2, 1)$	q_2