Examination Scheduling

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Outline

Problem

Modeling The Problem

Next Steps

PROBLEM

Problem

Find a good examination schedule for the exam period of the TUM.

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- Rooms for an exam are minimized
- Time between exams is maximized

MODELING THE PROBLEM

Variables

$$x_{i,k,l} := \begin{cases} 1, & \text{if exam } i \text{ is written in period } l \text{ in room } k \\ 0, & \text{otherwise} \end{cases}$$

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(1)
$$\sum_{\text{rooms } k} x_{i,k,l} \leq y_{i,l} \cdot M \quad \forall \text{ exams } i, \forall \text{ periods } l$$

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$$\sum_{\text{rooms } k} x_{i,k,l} \leq y_{i,l} \cdot M \quad \forall \text{ exams } i, \forall \text{ periods } l$$

(2)
$$\sum_{\text{rooms } k} x_{i,k,l} \geq y_{i,l} \qquad \forall \text{ exams } i, \forall \text{ periods } l$$

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(3)
$$\sum_{\text{periods } l} y_{i,l} = 1 \quad \forall \text{ exams } i$$

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(c.f. 2)
$$\sum_{\text{rooms } k} x_{i,k,l} \geq y_{i,l} \quad \forall \text{ exams } i, \forall \text{ periods } l$$

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• There are enough seats for the students in the exam rooms:

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$$(4) \qquad \sum_{\substack{\text{periods } I, \\ \text{rooms } k}} c_k \cdot x_{i,k,l} \qquad \geq s_i \qquad \forall \text{ exams } i$$

 $s_i := \#$ students taking exam i $c_k := \#$ seats in room k

• In every room there is at most one exam at a given time:

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(5)
$$\sum_{i,k,l} x_{i,k,l} \leq 1 \quad \forall \text{ rooms } k, \forall \text{ periods } l$$

• There are no conflicts for students taking multiple exams:

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(6)
$$\sum_{\substack{\text{exams } j, \\ j \text{ conflicts with } i}} y_{j,l} \leq (1 - y_{i,l}) \cdot M \quad \forall \text{exams } i, \forall \text{periods } l$$

• Minimize the total number of rooms:

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(a)
$$\min \sum_{\substack{\text{exams } i, \\ \text{rooms } k, \\ \text{periods } I}} x_{i,k,l}$$

• Maximize the time between two exams:

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(b)
$$\max \sum_{\text{exams } i \text{ conflicts with } i} \min_{d_{i,j}} d_{i,j}$$

 $d_{i,j} :=$ distance between exams i and j

• Combine the previous two objective functions using a weighting factor $\gamma > 0$:

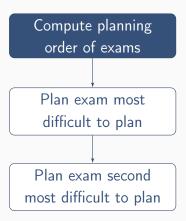
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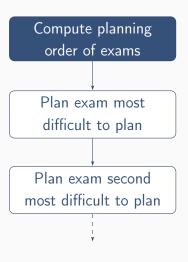
(a,b)
$$\min \sum_{\substack{\text{exams } i, \\ \text{rooms } k, \\ \text{periods } l}} x_{i,k,l} - \gamma \cdot \sum_{\substack{\text{exams } i \\ \text{exams } i \text{ conflicts with } i}} d_{i,j}$$

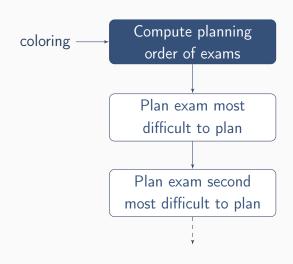
NEXT STEPS

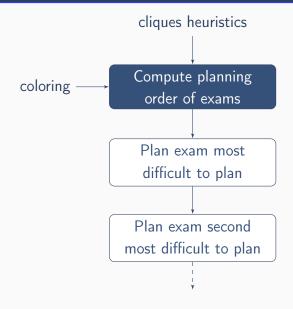
Compute planning order of exams

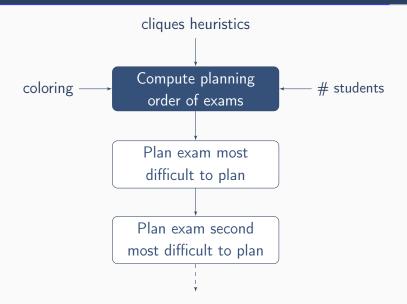












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- Remove absolute value in the objective function.
- Improve running time using heuristics, pre-solving, etc.
- Use a path-based model and column generation.

Data acquisition



Figure 1: Server, hopefully somewhere in Germany