Discrete and Algorithmic Geometry

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Sheet 0

Due on Thursday, November 7, 2019:

- (-7) Learn about the versioning software git, and practice until you become comfortable using it.
- (-6) git only supports versioning, but not issue tracking. However, since we will be writing code and talking about it, this is a desirable feature for us. Several solutions exist for this, and the UPC even has dedicated infrastructure for it. However, this infrastructure doesn't support teaching, so we have to use a commercial service. This year, we will try gitlab.com, so please sign up there. Be careful not to use the "Try Gitlab for Free" button (which makes you pay in a month's time), but the sign in link on the main page, which lets you use enough of the company's services for free. There, click on "register".
- (-5) Send your chosen username to julian.pfeifle@upc.edu so I can add you to the repository.
- (-4) Learn how to use ssh keys on gitlab, on your account's "settings" page.
- (-3) When I reply to your email, you can check out the repository of this course using

git clone git@gitlab.com:julian-upc/2019-dag-upc.

- (-2) Create a new branch your-name-cv in the repository, and edit the file participants.tex to include a short cv and some information about your mathematical interests. Then commmit and push your changes. When you feel your work is done, log in and create a merge request at the relevant issue page so that all the different stories may be merged.
- (-1) Organize into teams of 2-3 people to work on the exercises, and edit participants.tex to reflect this. As always, commit and push your changes, and create a merge request at the gitlab instance.

Due on Tuesday, November 12, 2019:

(0) Read up on **two** programming languages of your choice that your team will use in this course. One of these should be a scripting language for rapid iteration, the other a compiled language for efficiency. If you have never programmed before, a good choice for a scripted language is python/sage, and a good choice for a compiled language is julia. If you already know some languages, take the opportunity to learn a new one! Some suggestions are c++, perl/raku, rust, haskell, ocaml, ruby, lisp/scheme (I myself have not used all of these).

Put your results and observations into the wiki of the class.

To submit your solutions to the next two exercises,

- ▷ create and switch to a branch your-awesome-team-name-sheet-0,
- ▷ create a subdirectory exercises/sheet0/your-awesome-team-name/coding,
- ▶ and add all files you create to your commits, without encryption.
- ▶ Record your results in sheet0/results.tex, and create a merge request.

This will make it possible to have conversations about your code in your merge requests.

When developing your programs, bear in mind that since we all share the same repository, your code is likely to be read by the members of other teams who would like to compare the language they're using to yours. Therefore, please take the opportunity to document your code very well, so as to make it as easy for them as possible to understand what you're doing! In return, you'll be rewarded by awesomely documented code in languages you didn't have time to learn, but where you know exactly what problems it is solving.

Use the facilities that git offers to synchronize and collaborate on your code across devices and operating systems.

- (1) A collection \mathcal{B} of sets is the set of bases of a matroid if it satisfies the following axioms:
 - (i) $\mathscr{B} \neq \emptyset$
 - (ii) (Exchange axiom)

Given
$$B_1, B_2 \in \mathcal{B}$$
 and $x \in B_1 \setminus B_2$, there exists $y \in B_2 \setminus B_1$ such that $B_1 \setminus \{x\} \cup \{y\} \in \mathcal{B}$.

In the programming languages of your choice, write code that checks whether the sets of integers contained in various files in the directory exercises/sheet0/matroid-or-not satisfy the matroid basis axioms or not. Some of the files have the extension .txt and are there to help you validate your code. The files with the extension .bases contain as many bases as their name indicates, and some of them form bases of a matroid while others don't.

- (a) How many of these files can your code process?
- (b) What is the combinatorial complexity of your code?
- (c) Do you see a difference between the execution of the code in the scripting language and the compiled language your team chose?