Evaluating the Suitability of Lithic Illustrations in Morphometric Analyses

Christian Steven Hoggard, Thomas Birch, Cory Marie Stade, Katrien Janin and Felix Riede

Abstract

Illustrations of lithic artefacts are an abundant source of morphological and technological information for those interested in our human past. As a typical part of archaeological reports and publications, lithic drawings are - or have to be - trusted as faithful reproductions of the selected artefacts. Despite the considerable epistemic work lithic illustrations (and illustrators) are expected to do, usually little information is available regarding the illustrator's technical skill; thus, it remains unknown whether drawings produced by illustrators of differing technical skill are comparable or produce images of equal analytical potential to other media, e.g. photographs. The issue of lithic illustration accuracy is brought to the fore by the recent emergence of geometric morphometric approaches as innovative and powerful ways of describing and analysing complex shapes, as lithic illustrations provide one of the key sources for such analyses. Motivated by these issues, we present an experiment investigating the degree of error observed in illustrations of differing technical illustrative skill. Analyses suggest that lithic illustrations produced by individuals with a variety of experience in drawing lithics create, in the majority of instances, equally faithful representations (in outline shape) of chipped stone artefacts. With error observed in a small number of instances, archaeologists are still urged to be critical of an illustration's source prior to lineal and geometric morphometric methodologies. Despite this, archaeologists can be confident in their exactitude and we remain strong advocates in favour of lithic illustrations as a readily available legacy resource for morphometric analyses.

Introduction

This is a R Markdown documented associated with the article Evaluating the Suitability of Lithic Illustrations in Morphometric Analyses, original research for The Journal of the Lithic Studies Society (http://www.lithics.org/). This Markdown document details the analytical procedure used throughout the article, from data importing and the packages used, to the univariate and multivariate framework underpinning the article's findings.

Data files

For this markdown, a number of different files are necessary:

- 1. The three raw landmark files (for handaxe, tanged point and elongated artefacts), these are: **elongated.tps**, **handaxe.tps** and **tanged.tps**
- 2. The three data frames for the respective landmark files: elongated.csv, handaxe.csv and tanged.csv
- 3. The raw measurement length and width data for all artefacts: measurement_data.csv
- 4) The files necessary to investigate landmark digitisation error: **digitisation_error.tps** and **digitisation error.csv**
- 5) The file necessary to investigate measurement error: measurement_error.csv
- 6) The table of links for all landmark configurations: **curveslide.csv**

A copy of all files can also be found on GitHub and the Open Science Framework (OSF). GitHub: https://github.com/CSHoggard/-Lithic_Illustrations

OSF: https://osf.io/xtghn/

Stage 1: Package installation and data extraction

For this article, ten packages are required:

- 1. psych v.1.8.12 https://cran.r-project.org/web/packages/psych/index.html
- 2. **geomorph v.3.1.2** https://cran.r-project.org/web/packages/geomorph/index.html
- 3. tidyverse v.1.2.1 https://cran.r-project.org/web/packages/tidyverse/index.html
- 4. **vegan v.2.5-4** https://cran.r-project.org/web/packages/vegan/index.html
- 5. MASS v.7.3-51.4 https://cran.r-project.org/web/packages/MASS/index.html
- 6. **cowplot v.0.9.3** https://cran.r-project.org/web/packages/cowplot/index.html
- 7. $\mathbf{ggpubr}\ \mathbf{v.0.9.3}\ \mathrm{https://cran.r-project.org/web/packages/ggpubr/index.html}$
- 8. rio v.0.5.16 https://cran.r-project.org/web/packages/rio/index.html
- 9. LaMBDA v.0.1.0.9000 https://rdrr.io/github/akiopteryx/lambda/
- 10. devtools v.2.3.1 https://cran.r-project.org/web/packages/devtools/index.html

The latest versions of each package can be installed and sourced through the following code:

```
if(!require("psych")) install.packages('psych', repos='http://cran.us.r-project.org')
if(!require("geomorph")) install.packages('geomorph', repos='http://cran.us.r-project.org')
if(!require("tidyverse")) install.packages('tidyverse', repos='http://cran.us.r-project.org')
if(!require("vegan")) install.packages('vegan', repos='http://cran.us.r-project.org')
if(!require("MASS")) install.packages('MASS', repos='http://cran.us.r-project.org')
if(!require("cowplot")) install.packages('cowplot', repos='http://cran.us.r-project.org')
if(!require("ggpubr")) install.packages('ggpubr', repos='http://cran.us.r-project.org')
if(!require("rio")) install.packages('rio', repos='http://cran.us.r-project.org')
```

The LaMBDA package (LandMark-Based Data Assessment) is not on CRAN and requires downloading from GitHub (via the devtools package):

```
install.packages("devtools")
devtools::install_github("akiopteryx/lambda")
```

Should specific functions become outdated then please refer to the package versions as cited above. Once downloaded, activate all packages:

```
library(psych) ### load the listed package
library(geomorph) ### load the listed package
library(tidyverse) ### load the listed package
library(vegan) ### load the listed package
library(MASS) ### load the listed package
library(cowplot) ### load the listed package
library(ggpubr) ### load the listed package
library(LaMBDA) ### load the listed package
library(rio) ### load the listed package
```

Stage 2: Bringing all files into the R Environment

Given the large number of files required for the individual analyses (shape analysis, metric analysis, digitisation error and measurement error), and to prevent issues of working directories, all files are brought into the R Environment as .rds objects; these are objects which were imported into R and stored on GitHub (and downloaded when required). Using the rio::import() function allows all objects to be brought into the workspace.

landmarks_elongated <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/landmarks_ landmarks_handaxe <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/landmarks_handmarks_tanged <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/landmarks_tanged data_elongated <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/shape_data_shape_data_tanged <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/shape_data_t</pre> shape_data_handaxe <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/shape_data_
metric_data <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/metric_data.rds")
digitisation_error_landmarks <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/d
digitisation_error_landmarks_data <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/dig
shape_data_sliders <- import("https://github.com/CSHoggard/-Lithic_Illustrations/raw/master/dig</pre>

Stage 3: Sources of Error and Investigating Landmark Count

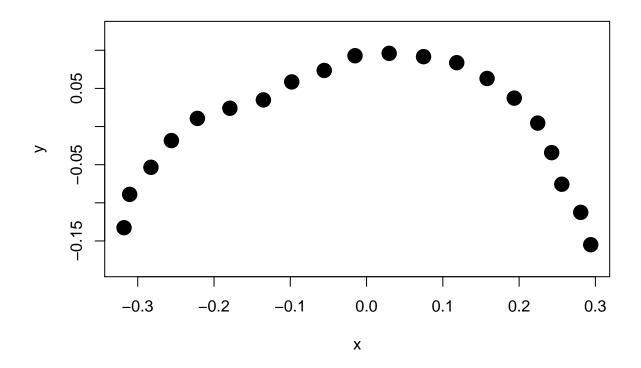
Stage 3A: Digitisation and Landmark Error

A Procrustes ANOVA (see in-text) was performed to calculate error associated with the digitisation of landmarks.

```
gpa_digi_error <- gpagen(digitisation_error_landmarks, Proj = TRUE, curves = shape_data_sliders, ProcD</pre>
gpa_digi_error ### calls the GPA landmark configuration
##
## Call:
## gpagen(A = digitisation_error_landmarks, curves = shape_data_sliders,
       surfaces = NULL, ProcD = TRUE, Proj = TRUE, print.progress = FALSE)
##
##
##
## Generalized Procrustes Analysis
## with Partial Procrustes Superimposition
##
## 2 fixed landmarks
## 18 semilandmarks (sliders)
## 2-dimensional landmarks
## 3 GPA iterations to converge
## Minimized squared Procrustes Distance used
##
## Consensus (mean) Configuration
##
##
## 1 -0.31796682 -0.132644965
## 2 -0.31060449 -0.088929377
## 3 -0.28269701 -0.053436920
     -0.25585407 -0.018405380
## 5 -0.22179239 0.010680904
## 6 -0.17917516 0.024001159
## 7 -0.13525110 0.034933759
## 8
     -0.09809871 0.058525436
## 9 -0.05547201 0.073540152
## 10 -0.01513393 0.092829862
## 11 0.02965721 0.095950162
## 12 0.07472658 0.091629691
## 13 0.11822149 0.083726851
## 14 0.15801543 0.063045388
## 15 0.19363531 0.037275511
## 16 0.22441752 0.004551561
## 17 0.24271449 -0.034206469
## 18 0.25597780 -0.075621222
```

```
## 19  0.28077551 -0.112520244
## 20  0.29390492 -0.154928393
```

plot(gpa_digi_error) ### visualisation of the landmark configuration



gpa_digi_error_df <- geomorph.data.frame(gpa_digi_error, attempt = digitisation_error_landmarks_data\$At
gpaprocD <- procD.lm(coords ~ attempt, data = gpa_digi_error_df, print.progress = FALSE) ### ANOVA (coo
summary(gpaprocD) ### summary</pre>

```
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
                        SS
##
             Df
                                   MS
                                        Rsq
                                                 F
                                                         Z Pr(>F)
              1 1.1246e-06 1.1246e-06 0.086 0.2823 -2.2192 0.9915
## Residuals 3 1.1952e-05 3.9841e-06 0.914
## Total
              4 1.3077e-05
## Call: procD.lm(f1 = coords ~ attempt, data = gpa_digi_error_df, print.progress = FALSE)
gpaprocD$aov.table$SS[1]/gpaprocD$aov.table$SS[3]*100 ### error expressed as a percentage (8.599812%)
## [1] 8.599812
```

Stage 3B: Measurement Error

To calculate error associated with lineal measurements fractional uncertainty (standard error divided by the mean) was calculated:

```
head(digitisation_error_metrics)
##
                    Attempt Scale_Factor Length_mm Width_mm
                                                        22.51
## T_Image_1_Copy_1
                           1
                                 0.026200
                                               82.15
## T_Image_1_Copy_2
                           2
                                 0.026390
                                               82.77
                                                        22.61
## T_Image_1_Copy_3
                           3
                                               81.80
                                                        22.29
                                 0.026080
## T_Image_1_Copy_4
                           4
                                 0.026140
                                               82.01
                                                        22.30
                           5
## T_Image_1_Copy_5
                                 0.026110
                                               81.98
                                                        22.35
## T_Image_1_Copy_6
                           6
                                 0.026316
                                               82.55
                                                        22.26
statsl <- describe(digitisation_error_metrics$Length_mm) ### descriptive statistics
statsw <- describe(digitisation_error_metrics\states \text{Width_mm}) ### descriptive statistics
statssf <- describe(digitisation_error_metrics$Scale_Factor) ### descriptive statistics</pre>
(statsl$se/statsl$mean)
                           * 100 ### fractional uncertainity (length)
## [1] 0.1188221
(statsw\se/statsw\mean)
                           * 100 ### fractional uncertainity (width)
## [1] 0.2275143
(statssf$se/statssf$mean) * 100 ### fractional uncertainity (scale factor: as calibrated through tpsDig
## [1] 0.1223673
```

Stage 3C: Investigating Landmark Count

The LaMBDA::LaSEC() function is used to assess the fidelity of morphological characterisation. This function helps the user to identify under- and over-sampling of landmarks, the robustness of the characterisation and determine how many landmarks can be removed without compromising the necessary shape information. A two-dimensional array of each landmark file was used, with 500 iterations, to determine if twenty landmarks were suitable. 500 iterations were used for the analysis, here 10 iterations are exemplified (for ease and speed):

```
lasec(two.d.array(landmarks_elongated), 2, iter = 10, show.progress = F) ### may take some time
```

```
## $fit
##
                          [,3]
                                     [,4]
                                                                    [,7]
         [,1] [,2]
                                               [,5]
                                                          [,6]
                                                                              [,8]
##
                NA 0.16353116 0.2532542 0.3203179 0.3921320 0.4496996 0.8641523
    \lceil 1. \rceil
    [2,]
                NA 0.52824807 0.6014112 0.6811728 0.7021068 0.7223433 0.8103473
##
           NA
##
    [3,]
           NA
                NA 0.33084838 0.4658694 0.6749621 0.7175439 0.7704487 0.8053725
   [4,]
##
           NA
                NA 0.10452644 0.4400741 0.6158463 0.6742656 0.7702470 0.7889963
##
    [5,]
           NA
                NA 0.08285789 0.2776336 0.6209322 0.6558858 0.7371672 0.7439683
##
    [6,]
                NA 0.14387346 0.5701167 0.6745579 0.6741968 0.7714671 0.8127097
           NA
                NA 0.38129853 0.5247893 0.6657151 0.7078289 0.8160774 0.8225324
##
    [7,]
           NA
    [8,]
                NA 0.25844652 0.3773386 0.6950926 0.8182842 0.8504605 0.8818444
##
           NA
##
   [9,]
           NA
                NA 0.13512499 0.1713878 0.2673203 0.4473745 0.6795436 0.7641056
##
   [10,]
                NA 0.41662444 0.6528608 0.6720454 0.7376002 0.8230296 0.8497633
               [,9]
##
                        [,10]
                                  [,11]
                                             [,12]
                                                       [,13]
                                                                  [,14]
                                                                            [,15]
##
   [1,] 0.8763064 0.8745613 0.9003915 0.9221413 0.9310493 0.9403371 0.9490036
   [2,] 0.8482248 0.8743404 0.8886915 0.9155578 0.9518321 0.9649648 0.9694788
##
    [3,] 0.8274601 0.9214266 0.9345165 0.9397551 0.9469293 0.9563559 0.9616411
```

```
[4,] 0.8821818 0.8987399 0.9112453 0.9193910 0.9313445 0.9406548 0.9486728
   [5,] 0.8589064 0.8688101 0.8740344 0.8844424 0.8879074 0.9196396 0.9376273
##
   [6,] 0.8288089 0.8527485 0.8966499 0.9036842 0.9114113 0.9155344 0.9373540
   [7,] 0.8626579 0.8757108 0.8871334 0.9145820 0.9273358 0.9342071 0.9385756
   [8,] 0.8918670 0.9013592 0.9225814 0.9433432 0.9557917 0.9663552 0.9718803
  [9,] 0.7730955 0.7750793 0.7866916 0.7896447 0.8028147 0.8012668 0.8124653
##
## [10.] 0.8624582 0.9100098 0.9217635 0.9275385 0.9462556 0.9567803 0.9615444
##
             [,16]
                      [,17]
                                [,18]
                                          [,19] [,20]
##
   [1,] 0.9745360 0.9865534 0.9910919 0.9951146
##
   [2,] 0.9757659 0.9824092 0.9885669 0.9939606
   [3,] 0.9661377 0.9836512 0.9885583 0.9939523
   [4,] 0.9525787 0.9808720 0.9832653 0.9890343
##
   [5,] 0.9498876 0.9594395 0.9647885 0.9928333
  [6,] 0.9572932 0.9695654 0.9775017 0.9939523
  [7,] 0.9454061 0.9512646 0.9837778 0.9939523
   [8,] 0.9770720 0.9841295 0.9886862 0.9963338
   [9,] 0.9666450 0.9772675 0.9892422 0.9950913
                                                    1
  [10,] 0.9677554 0.9820975 0.9876514 0.9939523
##
## $median.fit
##
   Г1]
              NA
                        NA 0.2109888 0.4529717 0.6688803 0.6881862 0.7703478
   [8] 0.8115285 0.8606823 0.8751360 0.8985207 0.9174744 0.9311969 0.9404959
## [15] 0.9488382 0.9663914 0.9814848 0.9881049 0.9939523 1.0000000
## $maxfit.landmark
## 
##
## $minfit.landmark
## 
##
## $fit.cs
##
  [1]
                        NA 0.9990298 0.9994840 0.9994428 0.9994783 0.9996251
              NA
  [8] 0.9997835 0.9998566 0.9998498 0.9998973 0.9999261 0.9999295 0.9999589
## [15] 0.9999697 0.9999791 0.9999839 0.9999936 0.9999967 1.0000000
lasec(two.d.array(landmarks_tanged), 2, iter = 10, show.progress = F) ### may take some time
## $fit
                        [,3]
                                  [,4]
                                           [,5]
                                                     [,6]
##
        [,1] [,2]
                                                               [,7]
               NA 0.3637104 0.4970388 0.5437679 0.6313296 0.6665750 0.6941520
   [1,]
##
   [2,]
          NA
               NA 0.4702792 0.7561133 0.8677004 0.8637114 0.8670633 0.9310894
##
   [3,]
         NA
              NA 0.2949477 0.5681083 0.7685849 0.7926670 0.7898533 0.7949672
         NA NA 0.5210015 0.7368207 0.8773437 0.8796057 0.8908005 0.9004354
##
  [4,]
##
   [5,]
         NA NA 0.3858198 0.4722266 0.5711067 0.6838602 0.7448244 0.9003974
##
   [6,]
               NA 0.4746495 0.6695535 0.7769632 0.9077250 0.9104285 0.9253586
   [7,]
               NA 0.1195304 0.3216357 0.5695952 0.5737160 0.8653222 0.8863542
##
          NA
##
   [8,]
               NA 0.3083874 0.4017041 0.7292814 0.7406238 0.7159066 0.7578050
   [9,]
               NA 0.3605516 0.4532269 0.8254409 0.8966036 0.9085586 0.8945971
##
          NA
##
  [10,]
               NA 0.5357263 0.6840842 0.8430015 0.8498234 0.8805263 0.8943378
##
              [,9]
                       [,10]
                                          [,12]
                                [,11]
                                                    [,13]
                                                              [,14]
                                                                        [,15]
   [1,] 0.9220333 0.9255628 0.9404104 0.9657278 0.9662211 0.9672965 0.9742326
   [2,] 0.9391179 0.9434230 0.9576137 0.9620358 0.9691823 0.9687496 0.9880111
##
   [3,] 0.9511377 0.9443155 0.9482071 0.9637054 0.9679705 0.9681118 0.9660157
  [4,] 0.8984567 0.9433475 0.9488213 0.9566490 0.9602328 0.9710564 0.9821300
## [5,] 0.9117537 0.9157032 0.9127381 0.9204037 0.9687928 0.9808239 0.9825749
```

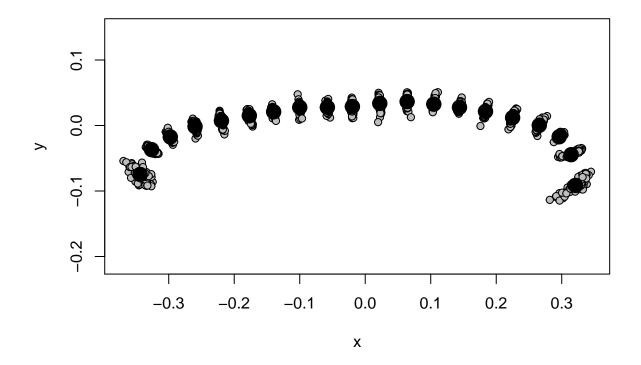
```
[6,] 0.9253685 0.9485701 0.9630692 0.9654016 0.9787967 0.9808377 0.9833579
   [7,] 0.9536132 0.9672120 0.9687005 0.9697125 0.9756404 0.9800621 0.9825824
##
    [8,] 0.7580566 0.8838261 0.8911148 0.8809086 0.9841480 0.9859973 0.9901149
   [9,] 0.9095510 0.9196096 0.9232251 0.9646382 0.9663521 0.9720790 0.9702083
##
  [10,] 0.9027873 0.9064047 0.9074050 0.9417934 0.9442489 0.9445892 0.9447509
                                           [,19] [,20]
##
             [,16]
                       [,17]
                                 [,18]
   [1.] 0.9761445 0.9745929 0.9891150 0.9928224
##
   [2,] 0.9896031 0.9910047 0.9939657 0.9976160
##
   [3,] 0.9759641 0.9741435 0.9780492 0.9985716
   [4,] 0.9880010 0.9935069 0.9961252 0.9984673
   [5,] 0.9892960 0.9906517 0.9920892 0.9940233
   [6,] 0.9838510 0.9850888 0.9936976 0.9983303
##
   [7,] 0.9838759 0.9852637 0.9966887 0.9984673
  [8,] 0.9922575 0.9925156 0.9972689 0.9990520
## [9,] 0.9773046 0.9808418 0.9961766 0.9972152
                                                    1
## [10,] 0.9478968 0.9721460 0.9932081 0.9952842
##
## $median.fit
                        NA 0.3747651 0.5325736 0.7727740 0.8212452 0.8661928
##
   [1]
              NA
    [8] 0.8944674 0.9168935 0.9344551 0.9443088 0.9628706 0.9683817 0.9715677
## [15] 0.9823524 0.9838634 0.9851763 0.9938316 0.9979732 1.0000000
##
## $maxfit.landmark
## 
##
## $minfit.landmark
## 
##
## $fit.cs
##
                        NA 0.9992925 0.9996987 0.9997926 0.9998255 0.9998709
   Г1]
              NA
## [8] 0.9999137 0.9999194 0.9999317 0.9999483 0.9999431 0.9999561 0.9999608
## [15] 0.9999665 0.9999642 0.9999812 0.9999915 0.9999978 1.0000000
lasec(two.d.array(landmarks_handaxe), 2, iter = 10, show.progress = F) ### may take some time
## $fit
                                  [,4]
##
         [,1] [,2]
                        [,3]
                                            [,5]
                                                      [,6]
               NA 0.6855587 0.7103135 0.8025947 0.8509098 0.8573438 0.8689123
##
    [1,]
   [2,]
               NA 0.2804016 0.8955476 0.9131987 0.9283516 0.9324729 0.9475356
##
               NA 0.6258260 0.7414667 0.7410309 0.7382395 0.7155373 0.7004799
   [3,]
##
   [4,]
          NA
               NA 0.7452771 0.8061092 0.7799164 0.7790021 0.9467000 0.9558506
##
   [5,]
          NA
              NA 0.8797704 0.8899131 0.9148558 0.9219254 0.9347888 0.9474790
##
   [6,]
               NA 0.8511077 0.8853058 0.8991234 0.9391811 0.9462415 0.9484214
##
   [7,]
          NA
               NA 0.6772855 0.7809577 0.7668213 0.8819412 0.8759503 0.8559443
##
    [8,]
               NA 0.2700441 0.7646333 0.7668143 0.8426508 0.8425407 0.9442350
   [9,]
               NA 0.5435225 0.8424814 0.8477936 0.8448803 0.8435495 0.9111778
##
          NA
##
  [10,]
               NA 0.8242519 0.8852478 0.9024199 0.9312038 0.9341052 0.9432530
##
              [,9]
                                 [,11]
                                           [,12]
                                                     [,13]
                                                               [,14]
                       [,10]
                                                                         [,15]
##
   [1,] 0.8839044 0.8994479 0.9253058 0.9623100 0.9763859 0.9816885 0.9818936
##
   [2,] 0.9501617 0.9534634 0.9634309 0.9688812 0.9755900 0.9783093 0.9796748
   [3,] 0.6906477 0.9723285 0.9793204 0.9845823 0.9856407 0.9910867 0.9920987
   [4,] 0.9738044 0.9811761 0.9848224 0.9861031 0.9889872 0.9895479 0.9921942
##
   [5,] 0.9568907 0.9707670 0.9728024 0.9740955 0.9773217 0.9806615 0.9819932
  [6,] 0.9620719 0.9668667 0.9700201 0.9749305 0.9774886 0.9833139 0.9861461
  [7,] 0.8559095 0.9487660 0.9682635 0.9713208 0.9755099 0.9761948 0.9899015
```

```
[8,] 0.9665686 0.9652620 0.9654490 0.9849790 0.9864889 0.9918007 0.9924210
   [9,] 0.9095742 0.9351353 0.9323753 0.9339304 0.9715195 0.9761736 0.9809275
## [10,] 0.9616632 0.9726396 0.9796293 0.9823730 0.9854570 0.9861743 0.9873440
##
            [,16]
                      [,17]
                                [,18]
                                          [,19] [,20]
##
   [1,] 0.9823700 0.9871082 0.9930286 0.9945479
  [2,] 0.9881773 0.9942921 0.9971337 0.9984116
##
## [3,] 0.9939808 0.9947631 0.9972426 0.9983804
## [4,] 0.9936505 0.9963348 0.9983437 0.9992688
   [5,] 0.9862378 0.9871127 0.9921415 0.9983021
  [6,] 0.9870036 0.9900438 0.9957442 0.9986945
  [7,] 0.9913917 0.9926340 0.9941598 0.9990658
## [8,] 0.9944044 0.9953030 0.9970115 0.9985557
                                                   1
## [9,] 0.9866891 0.9904447 0.9918592 0.9989569
                                                   1
## [10,] 0.9892900 0.9909397 0.9928622 0.9983804
##
## $median.fit
   [1]
                        NA 0.6814221 0.8242953 0.8251942 0.8664255 0.9042116
##
              NA
   [8] 0.9437440 0.9535262 0.9660643 0.9691418 0.9745130 0.9774051 0.9825012
## [15] 0.9867451 0.9887337 0.9917869 0.9949520 0.9984836 1.0000000
##
## $maxfit.landmark
## 
##
## $minfit.landmark
## 
## $fit.cs
                        NA 0.9987699 0.9987841 0.9991353 0.9994381 0.9994530
   [1]
              NA
## [8] 0.9995515 0.9996893 0.9997335 0.9997917 0.9998494 0.9998864 0.9998809
## [15] 0.9999144 0.9999383 0.9999785 0.9999666 0.9999938 1.0000000
```

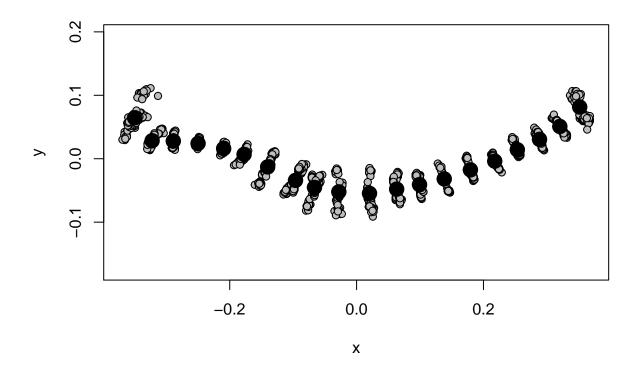
Stage 4: Generalised Procrustes Analysis (GPA)

With all errors calculated and deemed insignificant, we can now transform each artefact class through a GPA using the geomorph::gpagen() function as above:

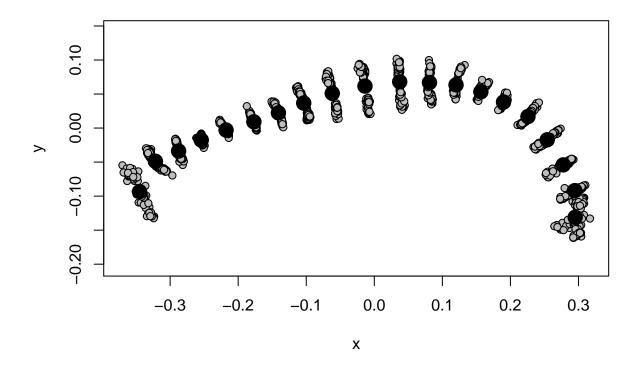
```
gpa_elongated <- gpagen(landmarks_elongated, Proj = TRUE, ProcD = TRUE, curves = shape_data_sliders, su
plot(gpa_elongated) ### plots the procrustes coordinates for all elongated artefacts
```



gpa_tanged <- gpagen(landmarks_tanged, Proj = TRUE, ProcD = TRUE, curves = shape_data_sliders, surfaces
plot(gpa_tanged) ### plots the procrustes coordinates for all tanged artefacts</pre>



gpa_handaxe <- gpagen(landmarks_handaxe, Proj = TRUE, ProcD = TRUE, curves = shape_data_sliders, surfac
plot(gpa_handaxe) ### plots the procrustes coordinates for all handaxe artefacts</pre>



Stage 5: Exploratory Analysis through Principal Component Analysis (PCA)

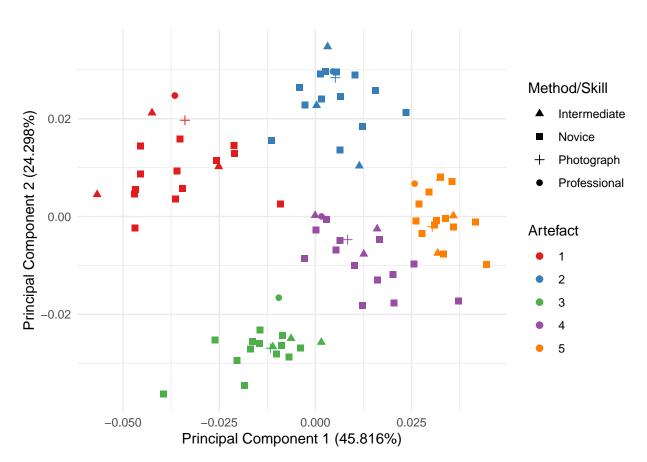
Individual PCAs for all artefact classes were created to visualise differences in illustration skill between and within the different artefacts. PCAs were made in geomorph, through the <code>geomorph:gm.prcomp()</code> function, before being exported and modified (for better visualisation) in the tidyverse Note: specific shape differences can be calculated through the created files. The visualisations can then be exported through the tidyverse: <code>ggsave()</code> function.

```
pca_elongated <- gm.prcomp(gpa_elongated$coords) ### pca (geomorph)</pre>
pca_elongated ### pca summary
##
## Ordination type: Principal Component Analysis
  Centering and projection: OLS
  Number of observations 90
  Number of vectors 40
##
##
##
   Importance of Components:
##
                                  Comp1
                                               Comp2
                                                            Comp3
                                                                          Comp4
                          0.0006240892 0.0003309824 0.0001584863 5.961311e-05
## Eigenvalues
## Proportion of Variance 0.4581554039 0.2429803127 0.1163477493 4.376308e-02
##
  Cumulative Proportion 0.4581554039 0.7011357166 0.8174834660 8.612466e-01
##
                                               Comp6
                                                            Comp7
## Eigenvalues
                          3.529451e-05 3.177163e-05 0.0000203628 1.880991e-05
## Proportion of Variance 2.591035e-02 2.332414e-02 0.0149487086 1.380870e-02
## Cumulative Proportion 8.871569e-01 9.104810e-01 0.9254297512 9.392385e-01
##
                                  Comp9
                                              Comp10
                                                           Comp11
                                                                         Comp12
```

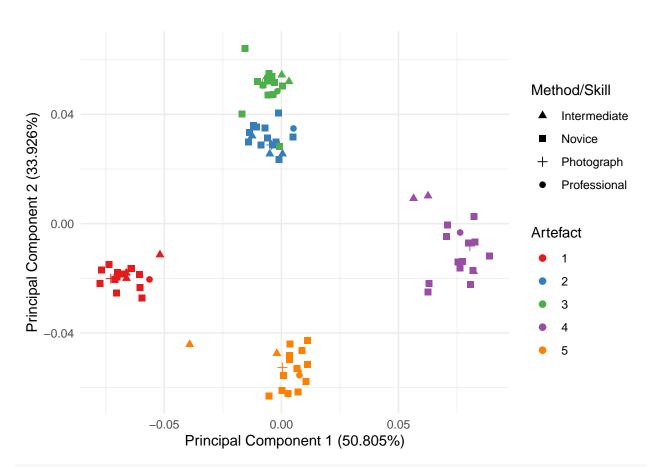
```
## Eigenvalues
                          1.340489e-05 1.198961e-05 1.008453e-05 8.642198e-06
## Proportion of Variance 9.840777e-03 8.801791e-03 7.403236e-03 6.344397e-03
  Cumulative Proportion 9.490792e-01 9.578810e-01 9.652843e-01 9.716287e-01
##
                                Comp13
                                             Comp14
                                                           Comp15
                                                                        Comp16
## Eigenvalues
                          6.693848e-06 5.406835e-06 4.978051e-06 4.684685e-06
## Proportion of Variance 4.914078e-03 3.969257e-03 3.654479e-03 3.439114e-03
  Cumulative Proportion 9.765427e-01 9.805120e-01 9.841665e-01 9.876056e-01
                                Comp17
                                             Comp18
                                                           Comp19
## Eigenvalues
                          3.897801e-06 3.361388e-06 2.190264e-06 1.677687e-06
## Proportion of Variance 2.861448e-03 2.467657e-03 1.607913e-03 1.231621e-03
  Cumulative Proportion 9.904670e-01 9.929347e-01 9.945426e-01 9.957742e-01
##
                                Comp21
                                             Comp22
                                                           Comp23
## Eigenvalues
                          1.463887e-06 8.279955e-07 7.209098e-07 5.838376e-07
## Proportion of Variance 1.074666e-03 6.078468e-04 5.292332e-04 4.286060e-04
## Cumulative Proportion 9.968489e-01 9.974567e-01 9.979860e-01 9.984146e-01
##
                                                           Comp27
                                Comp25
                                             Comp26
                                                                        Comp28
## Eigenvalues
                          3.725275e-07 3.456928e-07 2.633273e-07 2.420822e-07
## Proportion of Variance 2.734793e-04 2.537795e-04 1.933134e-04 1.777170e-04
  Cumulative Proportion 9.986881e-01 9.989418e-01 9.991351e-01 9.993129e-01
                                Comp29
                                             Comp30
                                                           Comp31
## Eigenvalues
                          2.363967e-07 1.846166e-07 1.492681e-07 1.177400e-07
## Proportion of Variance 1.735432e-04 1.355305e-04 1.095805e-04 8.643509e-05
## Cumulative Proportion 9.994864e-01 9.996219e-01 9.997315e-01 9.998180e-01
                                Comp33
                                             Comp34
                                                           Comp35
## Eigenvalues
                          8.787721e-08 7.107291e-08 4.752191e-08 2.573367e-08
## Proportion of Variance 6.451228e-05 5.217594e-05 3.488671e-05 1.889157e-05
## Cumulative Proportion 9.998825e-01 9.999346e-01 9.999695e-01 9.999884e-01
                                Comp37
                                             Comp38
                                                           Comp39
                                                                        Comp40
## Eigenvalues
                          1.454692e-08 1.228972e-09 1.832541e-22 5.967109e-34
## Proportion of Variance 1.067916e-05 9.022114e-07 1.345302e-19 4.380565e-31
## Cumulative Proportion 9.999991e-01 1.000000e+00 1.000000e+00 1.000000e+00
elongated_ds <- cbind(shape_data_elongated, pca_elongated$x) ### tidyverse compatible format
pca_tanged <- gm.prcomp(gpa_tanged$coords) ### pca (geomorph)</pre>
pca_tanged ### pca summary
##
## Ordination type: Principal Component Analysis
## Centering and projection: OLS
## Number of observations 90
## Number of vectors 40
##
## Importance of Components:
##
                                            Comp2
                                                          Comp3
                                                                      Comp4
                                Comp1
                          0.002108332 0.001407887 0.0002833669 0.000161115
## Eigenvalues
## Proportion of Variance 0.508049684 0.339261820 0.0682835983 0.038824262
  Cumulative Proportion 0.508049684 0.847311504 0.9155951019 0.954419364
                                 Comp5
                                              Comp6
                                                            Comp7
## Eigenvalues
                          4.604155e-05 2.857256e-05 1.833576e-05 1.477163e-05
## Proportion of Variance 1.109474e-02 6.885197e-03 4.418412e-03 3.559556e-03
## Cumulative Proportion 9.655141e-01 9.723993e-01 9.768177e-01 9.803773e-01
                                 Comp9
                                                           Comp11
                                                                        Comp12
                                             Comp10
## Eigenvalues
                          1.262627e-05 9.103601e-06 8.270341e-06 7.226064e-06
## Proportion of Variance 3.042582e-03 2.193716e-03 1.992924e-03 1.741282e-03
```

```
## Cumulative Proportion 9.834199e-01 9.856136e-01 9.876065e-01 9.893478e-01
##
                                             Comp14
                                                           Comp15
                                                                        Comp16
                                Comp13
## Eigenvalues
                          6.433424e-06 0.0000059361 4.986095e-06 4.260570e-06
## Proportion of Variance 1.550278e-03 0.0014304362 1.201511e-03 1.026680e-03
  Cumulative Proportion 9.908981e-01 0.9923284887 9.935300e-01 9.945567e-01
##
                                Comp17
                                             Comp18
                                                           Comp19
## Eigenvalues
                          3.425980e-06 2.990619e-06 2.843070e-06 2.461052e-06
## Proportion of Variance 8.255666e-04 7.206566e-04 6.851013e-04 5.930455e-04
  Cumulative Proportion 9.953822e-01 9.961029e-01 9.967880e-01 9.973810e-01
##
                                Comp21
                                             Comp22
                                                           Comp23
## Eigenvalues
                          2.244288e-06 1.821357e-06 1.559110e-06 1.216749e-06
## Proportion of Variance 5.408114e-04 4.388967e-04 3.757024e-04 2.932029e-04
## Cumulative Proportion 9.979219e-01 9.983608e-01 9.987365e-01 9.990297e-01
##
                                Comp25
                                             Comp26
                                                           Comp27
## Eigenvalues
                          7.597572e-07 5.893029e-07 5.709725e-07 4.840509e-07
## Proportion of Variance 1.830805e-04 1.420057e-04 1.375886e-04 1.166429e-04
## Cumulative Proportion 9.992127e-01 9.993547e-01 9.994923e-01 9.996090e-01
##
                                Comp29
                                             Comp30
                                                           Comp31
                          4.310409e-07 2.515842e-07 2.356631e-07 2.089888e-07
## Eigenvalues
## Proportion of Variance 1.038689e-04 6.062485e-05 5.678829e-05 5.036052e-05
  Cumulative Proportion 9.997128e-01 9.997735e-01 9.998303e-01 9.998806e-01
                                             Comp34
                                Comp33
                                                           Comp35
## Eigenvalues
                          1.713893e-07 1.193250e-07 1.144246e-07 5.925712e-08
## Proportion of Variance 4.130009e-05 2.875404e-05 2.757317e-05 1.427933e-05
  Cumulative Proportion 9.999219e-01 9.999507e-01 9.999783e-01 9.999925e-01
                                Comp37
                                             Comp38
                                                           Comp39
## Eigenvalues
                          2.710922e-08 3.891138e-09 8.741952e-23 1.53472e-33
## Proportion of Variance 6.532573e-06 9.376569e-07 2.106569e-20 3.69825e-31
## Cumulative Proportion 9.999991e-01 1.000000e+00 1.000000e+00 1.00000e+00
tanged_ds <- cbind(shape_data_tanged, pca_tanged$x) ### tidyverse compatible format
pca_handaxe <- gm.prcomp(gpa_handaxe$coords) ### pca (qeomorph)</pre>
pca_handaxe ### pca summary
## Ordination type: Principal Component Analysis
## Centering and projection: OLS
## Number of observations 90
  Number of vectors 40
##
  Importance of Components:
##
                                Comp1
                                             Comp2
                                                           Comp3
                                                                        Comp4
## Eigenvalues
                          0.004147443 0.0003415703 0.0001480715 5.776983e-05
## Proportion of Variance 0.848362755 0.0698684628 0.0302881402 1.181686e-02
  Cumulative Proportion 0.848362755 0.9182312181 0.9485193583 9.603362e-01
##
                                 Comp5
                                              Comp6
                                                            Comp7
## Eigenvalues
                          3.702773e-05 2.686763e-05 1.884701e-05 1.644421e-05
## Proportion of Variance 7.574051e-03 5.495794e-03 3.855170e-03 3.363675e-03
  Cumulative Proportion 9.679103e-01 9.734061e-01 9.772612e-01 9.806249e-01
                                 Comp9
                                             Comp10
                                                           Comp11
## Eigenvalues
                          1.401099e-05 1.294287e-05 1.019683e-05 8.733280e-06
## Proportion of Variance 2.865959e-03 2.647474e-03 2.085770e-03 1.786399e-03
## Cumulative Proportion 9.834909e-01 9.861383e-01 9.882241e-01 9.900105e-01
##
                                Comp13
                                             Comp14
                                                           Comp15
                                                                        Comp16
```

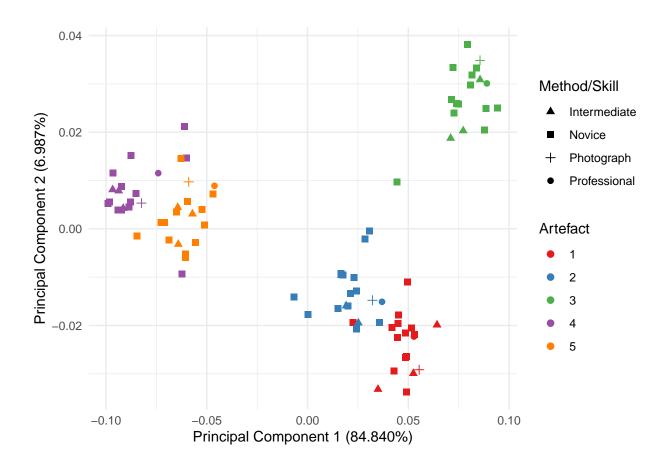
```
## Eigenvalues
                          7.370640e-06 6.467041e-06 4.826731e-06 4.408248e-06
## Proportion of Variance 1.507670e-03 1.322838e-03 9.873115e-04 9.017105e-04
## Cumulative Proportion 9.915182e-01 9.928410e-01 9.938283e-01 9.947300e-01
##
                                Comp17
                                             Comp18
                                                          Comp19
                                                                       Comp20
## Eigenvalues
                          3.801114e-06 3.306690e-06 3.009149e-06 2.486183e-06
## Proportion of Variance 7.775208e-04 6.763861e-04 6.155238e-04 5.085508e-04
## Cumulative Proportion 9.955076e-01 9.961840e-01 9.967995e-01 9.973080e-01
                                Comp21
                                             Comp22
                                                          Comp23
## Eigenvalues
                          2.276660e-06 1.958038e-06 1.744844e-06 1.488234e-06
## Proportion of Variance 4.656925e-04 4.005181e-04 3.569091e-04 3.044195e-04
## Cumulative Proportion 9.977737e-01 9.981742e-01 9.985311e-01 9.988356e-01
##
                                Comp25
                                             Comp26
                                                          Comp27
## Eigenvalues
                          1.367614e-06 8.485558e-07 8.095846e-07 7.015244e-07
## Proportion of Variance 2.797465e-04 1.735727e-04 1.656012e-04 1.434974e-04
## Cumulative Proportion 9.991153e-01 9.992889e-01 9.994545e-01 9.995980e-01
##
                                Comp29
                                             Comp30
                                                          Comp31
                                                                        Comp32
## Eigenvalues
                          5.635145e-07 3.907648e-07 2.811766e-07 2.106388e-07
## Proportion of Variance 1.152673e-04 7.993123e-05 5.751488e-05 4.308632e-05
## Cumulative Proportion 9.997133e-01 9.997932e-01 9.998507e-01 9.998938e-01
                                Comp33
                                             Comp34
                                                          Comp35
## Eigenvalues
                          1.589855e-07 1.475755e-07 1.146792e-07 7.430645e-08
## Proportion of Variance 3.252060e-05 3.018668e-05 2.345772e-05 1.519944e-05
## Cumulative Proportion 9.999263e-01 9.999565e-01 9.999799e-01 9.999951e-01
                                Comp37
                                             Comp38
                                                          Comp39
## Eigenvalues
                          1.945077e-08 4.274790e-09 2.907959e-21 9.892121e-34
## Proportion of Variance 3.978670e-06 8.744115e-07 5.948252e-19 2.023441e-31
## Cumulative Proportion 9.999991e-01 1.000000e+00 1.000000e+00 1.000000e+00
handaxe_ds <- cbind(shape_data_handaxe, pca_handaxe$x) ### tidyverse compatible format
ggplot(elongated_ds) +
 geom_point(aes(x = Comp1, y = Comp2, colour = Artefact, shape = Class), size = 2) +
 labs(x = "Principal Component 1 (45.816%)", y = "Principal Component 2 (24.298%)", shape = "Method/Sk
  scale_color_manual(values=c("#e41a1c","#377eb8","#4daf4a","#984ea3","#ff7f00")) +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() ### figure 5 creation
```



```
ggplot(tanged_ds) +
  geom_point(aes(x = Comp1, y = Comp2, colour = Artefact, shape = Class), size = 2) +
  labs(x = "Principal Component 1 (50.805%)", y = "Principal Component 2 (33.926%)", shape = "Method/Sk
  scale_color_manual(values=c("#e41a1c","#377eb8","#4daf4a","#984ea3","#ff7f00")) +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() ### figure 6 creation
```



```
ggplot(handaxe_ds) +
  geom_point(aes(x = Comp1, y = Comp2, colour = Artefact, shape = Class), size = 2) +
  labs(x = "Principal Component 1 (84.840%)", y = "Principal Component 2 (6.987%)", shape = "Method/Ski
  scale_color_manual(values=c("#e41a1c","#377eb8","#4daf4a","#984ea3","#ff7f00")) +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() ### figure 7 creation
```



Stage 6: Further analysis (MANOVA and Discriminant Analysis)

Each individual artefact (and the collections of drawings for each artefact) was then analysed to examine whether differences in illustrator skill were observed. This was first done through a Procrustes ANOVA, providing a statistical framework for detecting any such difference. Discriminant analyses were then conducted for each artefact to test for between-group variance. The code for each artefact follows this order:

- 1) The Procrustes coordinates from an artefact are extracted from the dataframe.
- 2) A geomorph-specific data-frame is created through the geomorph::geomorph.data.frame() function, with the Procrustes coordinates and the class factor.
- 3) A Procrustes ANOVA is then performed through the geomorph::procD.lm() function, with the results summarised through the base::summary() argument.
- 4) A new data frame is generated to produce the discriminant analysis (through the MASS::lda() function).
- 5) The subsequent data is visualised through the tidyverse package.
- 6) This is repeated for each artefact within each artefact class.

```
elongated1 <- gpa_elongated$coords[, , 1:18]
df_elongated1 <- geomorph.data.frame(shape = elongated1, class = shape_data_elongated$Class[1:18], arte
E1 <- procD.lm(shape ~ class, data = df_elongated1, print.progress = FALSE)
summary(E1)</pre>
```

```
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                        SS
                                   MS
                                          Rsq
                                                   F
                                                            Z Pr(>F)
              3 0.0016387 0.00054623 0.17824 1.0122 0.18333 0.398
## class
## Residuals 14 0.0075548 0.00053963 0.82176
             17 0.0091935
## Total
##
## Call: procD.lm(f1 = shape ~ class, data = df_elongated1, print.progress = FALSE)
elongated1pcs <- as.data.frame(pca_elongated$x[1:18, 1:10])
elongated1class <- shape_data_elongated$Class[1:18]</pre>
elongated1pcs <- cbind(elongated1pcs, elongated1class)</pre>
elongated1pcs <- rename(elongated1pcs, Class = elongated1class)</pre>
elongated1lda <- lda(Class ~ ., data = elongated1pcs)</pre>
elongated1ldapredict <- predict(elongated1lda)</pre>
elongated1ldaplot <- cbind(elongated1ldapredict$x[, 1:3], elongated1pcs)</pre>
elongated1ldaplotggplot <- ggplot(elongated1ldaplot, aes(LD1, LD2)) +
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale shape manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element blank(),
        axis.text.y = element_blank(),
        axis.title.x = element_text(size = 6),
        axis.title.y = element_text(size = 6),
        legend.position = "none")
elongated2 <- gpa_elongated$coords[, , 19:36]</pre>
df_elongated2 <- geomorph.data.frame(shape = elongated2, class = shape_data_elongated$Class[19:36], art
E2 <- procD.lm(shape ~ class, data = df_elongated2, print.progress = FALSE)
summary(E2)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                                          Rsq
                                                            Z Pr(>F)
              3 0.0007434 0.00024780 0.08883 0.4549 -1.8498 0.976
## Residuals 14 0.0076257 0.00054469 0.91117
## Total
             17 0.0083691
##
## Call: procD.lm(f1 = shape ~ class, data = df_elongated2, print.progress = FALSE)
elongated2pcs <- as.data.frame(pca_elongated$x[19:36, 1:10])
elongated2class <- shape_data_elongated$Class[19:36]</pre>
```

```
elongated2pcs <- cbind(elongated2pcs, elongated2class)</pre>
elongated2pcs <- rename(elongated2pcs, Class = elongated2class)</pre>
elongated2lda <- lda(Class ~ ., elongated2pcs)</pre>
elongated2ldapredict <- predict(elongated2lda)</pre>
elongated2ldaplot <- cbind(elongated2ldapredict$x[, 1:3], elongated2pcs)</pre>
elongated2ldaplotggplot <- ggplot(elongated2ldaplot, aes(LD1, LD2)) +</pre>
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
elongated3 <- gpa_elongated$coords[, , 37:54]</pre>
df_elongated3 <- geomorph.data.frame(shape = elongated3, class = shape_data_elongated$Class[37:54], art
E3 <- procD.lm(shape ~ class, data = df_elongated3, print.progress = FALSE)
summary(E3)
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             \mathsf{Df}
                                                              Z Pr(>F)
                        SS
                                   MS
                                           Rsq
                                                    F
              3 0.0007131 0.00023771 0.14157 0.7696 -0.28451
## Residuals 14 0.0043243 0.00030888 0.85843
             17 0.0050375
## Total
##
## Call: procD.lm(f1 = shape ~ class, data = df_elongated3, print.progress = FALSE)
elongated3pcs <- as.data.frame(pca_elongated$x[37:54, 1:10])
elongated3class <- shape_data_elongated$Class[37:54]</pre>
elongated3pcs <- cbind(elongated3pcs, elongated3class)</pre>
elongated3pcs <- rename(elongated3pcs, Class = elongated3class)</pre>
elongated3lda <- lda(Class ~ ., elongated3pcs)
elongated3ldapredict <- predict(elongated3lda)</pre>
elongated3ldaplot <- cbind(elongated3ldapredict$x[, 1:3], elongated3pcs)</pre>
elongated3ldaplotggplot <- ggplot(elongated3ldaplot, aes(LD1, LD2)) +</pre>
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
```

```
elongated4 <- gpa_elongated$coords[, , 55:72]</pre>
df_elongated4 <- geomorph.data.frame(shape = elongated4, class = shape_data_elongated$Class[55:72], art</pre>
E4 <- procD.lm(shape ~ class, data = df_elongated4, print.progress = FALSE)
summary(E4)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                                          Rsq
                                                    F
                                                            Z Pr(>F)
              3 0.0007477 0.00024923 0.10896 0.5707 -0.7742 0.793
## class
## Residuals 14 0.0061144 0.00043675 0.89104
## Total
             17 0.0068621
##
## Call: procD.lm(f1 = shape ~ class, data = df_elongated4, print.progress = FALSE)
elongated4pcs <- as.data.frame(pca_elongated$x[55:72, 1:10])
elongated4class <- shape_data_elongated$Class[55:72]</pre>
elongated4pcs <- cbind(elongated4pcs, elongated4class)</pre>
elongated4pcs <- rename(elongated4pcs, Class = elongated4class)</pre>
elongated4lda <- lda(Class ~ ., elongated4pcs)
elongated4ldapredict <- predict(elongated4lda)</pre>
elongated4ldaplot <- cbind(elongated4ldapredict$x[, 1:3], elongated4pcs)</pre>
elongated4ldaplotggplot <- ggplot(elongated4ldaplot, aes(LD1, LD2)) +</pre>
  geom point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
elongated5 <- gpa_elongated$coords[, , 73:90]</pre>
df_elongated5 <- geomorph.data.frame(shape = elongated5, class = shape_data_elongated$Class[73:90], art
E5 <- procD.lm(shape ~ class, data = df_elongated5, print.progress = FALSE)
summary(E5)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                                                           Z Pr(>F)
                        SS
                                   MS
                                         Rsq
              3 0.0005381 0.00017936 0.0878 0.4492 -1.2749 0.905
## Residuals 14 0.0055901 0.00039929 0.9122
```

```
## Total
             17 0.0061282
##
## Call: procD.lm(f1 = shape ~ class, data = df_elongated5, print.progress = FALSE)
elongated5pcs <- as.data.frame(pca_elongated$x[73:90, 1:10])
elongated5class <- shape_data_elongated$Class[73:90]</pre>
elongated5pcs <- cbind(elongated5pcs, elongated5class)</pre>
elongated5pcs <- rename(elongated5pcs, Class = elongated5class)</pre>
elongated5lda <- lda(Class ~ ., elongated5pcs)</pre>
elongated5ldapredict <- predict(elongated5lda)</pre>
elongated5ldaplot <- cbind(elongated5ldapredict$x[, 1:3], elongated5pcs)</pre>
elongated5ldaplotggplot <- ggplot(elongated5ldaplot, aes(LD1, LD2)) +</pre>
  geom point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
tanged1 <- gpa_tanged$coords[, , 1:18]</pre>
df_tanged1 <- geomorph.data.frame(shape = tanged1, class = shape_data_tanged$Class[1:18], artefact = sh
T1 <- procD.lm(shape ~ class, data = df_tanged1, print.progress = FALSE)
summary(T1)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             \mathsf{Df}
                        SS
                                                             Z Pr(>F)
                                    MS
                                          Rsq
                                                   F
              3 0.0006374 0.00021247 0.1445 0.7882 -0.41375 0.659
## class
## Residuals 14 0.0037737 0.00026955 0.8555
## Total
             17 0.0044111
##
## Call: procD.lm(f1 = shape ~ class, data = df_tanged1, print.progress = FALSE)
tanged1pcs <- as.data.frame(pca_tanged$x[1:18, 1:10])</pre>
tanged1class <- shape_data_tanged$Class[1:18]</pre>
tanged1pcs <- cbind(tanged1pcs, tanged1class)</pre>
tanged1pcs <- rename(tanged1pcs, Class = tanged1class)</pre>
tanged1lda <- lda(Class ~ ., tanged1pcs)</pre>
tanged1ldapredict <- predict(tanged1lda)</pre>
tanged1ldaplot <- cbind(tanged1ldapredict$x[, 1:3], tanged1pcs)
tanged1ldaplotggplot <- ggplot(tanged1ldaplot, aes(LD1, LD2)) +</pre>
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() +
  theme(axis.text.x = element_blank(),
```

```
axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
tanged2 <- gpa_tanged$coords[, , 19:36]</pre>
df_tanged2 <- geomorph.data.frame(shape = tanged2, class = shape_data_tanged$Class[19:36], artefact = si
T2 <- procD.lm(shape ~ class, data = df tanged2, print.progress = FALSE)
summary(T2)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
             Df
                       SS
##
                                                    F
                                                            Z Pr(>F)
                                   MS
                                          Rsq
              3 0.0005912 0.00019707 0.17446 0.9862 0.12861 0.418
## class
## Residuals 14 0.0027976 0.00019983 0.82554
## Total 17 0.0033888
##
## Call: procD.lm(f1 = shape ~ class, data = df_tanged2, print.progress = FALSE)
tanged2pcs <- as.data.frame(pca_tanged$x[19:36, 1:10])</pre>
tanged2class <- shape_data_tanged$Class[19:36]</pre>
tanged2pcs <- cbind(tanged2pcs, tanged2class)</pre>
tanged2pcs <- rename(tanged2pcs, Class = tanged2class)</pre>
tanged2lda <- lda(Class ~ ., tanged2pcs)</pre>
tanged2ldapredict <- predict(tanged2lda)</pre>
tanged2ldaplot <- cbind(tanged2ldapredict$x[, 1:3], tanged2pcs)</pre>
tanged2ldaplotggplot <- ggplot(tanged2ldaplot, aes(LD1, LD2)) +</pre>
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
tanged3 <- gpa_tanged$coords[, , 37:54]</pre>
df_tanged3 <- geomorph.data.frame(shape = tanged3, class = shape_data_tanged$Class[37:54], artefact = si
T3 <- procD.lm(shape ~ class, data = df_tanged3, print.progress = FALSE)
summary(T3)
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
```

Sums of Squares and Cross-products: Type I

```
## Effect sizes (Z) based on F distributions
##
##
             Df
                        SS
              3 0.0004659 0.00015530 0.13042 0.6999 -0.47251 0.649
## class
## Residuals 14 0.0031064 0.00022189 0.86958
## Total
             17 0.0035724
##
## Call: procD.lm(f1 = shape ~ class, data = df_tanged3, print.progress = FALSE)
tanged3pcs <- as.data.frame(pca_tanged$x[37:54, 1:10])</pre>
tanged3class <- shape_data_tanged$Class[37:54]</pre>
tanged3pcs <- cbind(tanged3pcs, tanged3class)</pre>
tanged3pcs <- rename(tanged3pcs, Class = tanged3class)</pre>
tanged3lda <- lda(Class ~ ., tanged3pcs)</pre>
tanged3ldapredict <- predict(tanged3lda)</pre>
tanged3ldaplot <- cbind(tanged3ldapredict$x[, 1:3], tanged3pcs)</pre>
tanged3ldaplotggplot <- ggplot(tanged3ldaplot, aes(LD1, LD2)) +</pre>
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element text(size = 6))
tanged4 <- gpa_tanged$coords[, , 55:72]</pre>
df_tanged4 <- geomorph.data.frame(shape = tanged4, class = shape_data_tanged$Class[55:72], artefact = si
T4 <- procD.lm(shape ~ class, data = df_tanged4, print.progress = FALSE)
summary(T4)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                        SS
                                    MS
                                           Rsq
                                                     F
                                                             7. Pr(>F)
              3 0.0020486 0.00068286 0.21029 1.2427 0.64326 0.242
## class
## Residuals 14 0.0076931 0.00054951 0.78971
## Total
             17 0.0097417
##
## Call: procD.lm(f1 = shape ~ class, data = df_tanged4, print.progress = FALSE)
tanged4pcs <- as.data.frame(pca_tanged$x[55:72, 1:10])</pre>
tanged4class <- shape data tanged$Class[55:72]</pre>
tanged4pcs <- cbind(tanged4pcs, tanged4class)</pre>
tanged4pcs <- rename(tanged4pcs, Class = tanged4class)</pre>
tanged4lda <- lda(Class ~ ., tanged4pcs)</pre>
tanged4ldapredict <- predict(tanged4lda)</pre>
tanged4ldaplot <- cbind(tanged4ldapredict$x[, 1:3], tanged4pcs)</pre>
tanged4ldaplotggplot <- ggplot(tanged4ldaplot, aes(LD1, LD2)) +</pre>
```

```
geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element text(size = 6),
        axis.title.x = element text(size = 6))
tanged5 <- gpa_tanged$coords[, , 73:90]</pre>
df_tanged5 <- geomorph.data.frame(shape = tanged5, class = shape_data_tanged$Class[73:90], artefact = si
T5 <- procD.lm(shape ~ class, data = df_tanged5, print.progress = FALSE)
summary(T5)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
                                                            Z Pr(>F)
                                          Rsq
                                                   F
              3 0.0014793 0.00049310 0.19693 1.1444 0.44278 0.237
## class
## Residuals 14 0.0060323 0.00043088 0.80307
## Total
             17 0.0075116
##
## Call: procD.lm(f1 = shape ~ class, data = df_tanged5, print.progress = FALSE)
tanged5pcs <- as.data.frame(pca_tanged$x[73:90, 1:10])</pre>
tanged5class <- shape_data_tanged$Class[73:90]</pre>
tanged5pcs <- cbind(tanged5pcs, tanged5class)</pre>
tanged5pcs <- rename(tanged5pcs, Class = tanged5class)</pre>
tanged5lda <- lda(Class ~ ., tanged5pcs)</pre>
tanged5ldapredict <- predict(tanged5lda)</pre>
tanged5ldaplot <- cbind(tanged5ldapredict$x[, 1:3], tanged5pcs)</pre>
tanged5ldaplotggplot <- ggplot(tanged5ldaplot, aes(LD1, LD2)) +</pre>
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element text(size = 6),
        axis.title.x = element_text(size = 6))
handaxe1 <- gpa_handaxe$coords[, , 1:18]
df_handaxe1 <- geomorph.data.frame(shape = handaxe1, class = shape_data_handaxe$Class[1:18], artefact =
H1 <- procD.lm(shape ~ class, data = df_handaxe1, print.progress = FALSE)
summary(H1)
```

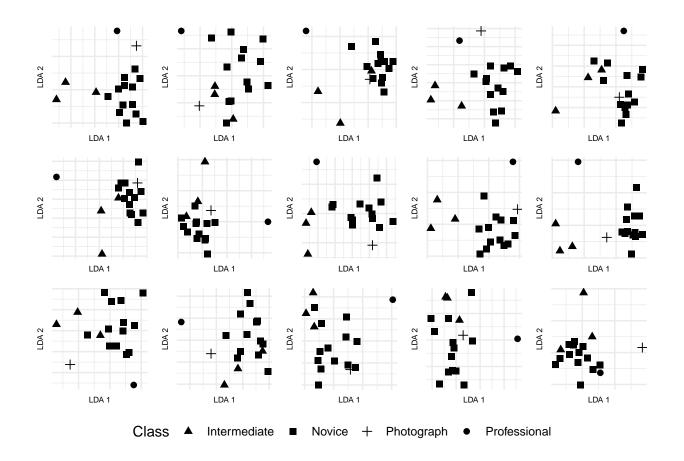
##

```
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                                          Rsq
                                                  F
                                                            7. Pr(>F)
## class
              3 0.0012319 0.00041064 0.14025 0.7613 -0.42438 0.604
## Residuals 14 0.0075520 0.00053943 0.85975
            17 0.0087839
## Call: procD.lm(f1 = shape ~ class, data = df_handaxe1, print.progress = FALSE)
handaxe1pcs <- as.data.frame(pca_handaxe$x[1:18, 1:10])
handaxe1class <- shape_data_handaxe$Class[1:18]
handaxe1pcs <- cbind(handaxe1pcs, handaxe1class)</pre>
handaxe1pcs <- rename(handaxe1pcs, Class = handaxe1class)</pre>
handaxe1lda <- lda(Class ~ ., handaxe1pcs)</pre>
handaxe1ldapredict <- predict(handaxe1lda)</pre>
handaxe1ldaplot <- cbind(handaxe1ldapredict$x[, 1:3], handaxe1pcs)
handaxe1ldaplotggplot <- ggplot(handaxe1ldaplot, aes(LD1, LD2)) +
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
handaxe2 <- gpa_handaxe$coords[, , 19:36]
df_handaxe2 <- geomorph.data.frame(shape = handaxe2, class = shape_data_handaxe$Class[19:36], artefact
H2 <- procD.lm(shape ~ class, data = df_handaxe2, print.progress = FALSE)
summary(H2)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                       SS
                                  MS
                                          Rsq
                                                   F
                                                           Z Pr(>F)
## class
              3 0.0007207 0.00024023 0.11133 0.5846 -1.0482 0.843
## Residuals 14 0.0057525 0.00041090 0.88867
## Total
             17 0.0064732
##
## Call: procD.lm(f1 = shape ~ class, data = df_handaxe2, print.progress = FALSE)
handaxe2pcs <- as.data.frame(pca_handaxe$x[19:36, 1:10])
handaxe2class <- shape_data_handaxe$Class[19:36]
handaxe2pcs <- cbind(handaxe2pcs, handaxe2class)</pre>
```

```
handaxe2pcs <- rename(handaxe2pcs, Class = handaxe2class)</pre>
handaxe2lda <- lda(Class ~ ., handaxe2pcs)</pre>
handaxe2ldapredict <- predict(handaxe2lda)
handaxe2ldaplot <- cbind(handaxe2ldapredict$x[, 1:3], handaxe2pcs)
handaxe2ldaplotggplot <- ggplot(handaxe2ldaplot, aes(LD1, LD2)) +
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
handaxe3 <- gpa_handaxe$coords[, , 37:54]</pre>
df_handaxe3 <- geomorph.data.frame(shape = handaxe3, class = shape_data_handaxe$Class[37:54], artefact
H3 <- procD.lm(shape ~ class, data = df_handaxe3, print.progress = FALSE)
summary(H3)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             Df
                                          Rsq
                                                            Z Pr(>F)
              3 0.0010882 0.00036274 0.11811 0.625 -0.64478 0.73
## class
## Residuals 14 0.0081253 0.00058038 0.88189
            17 0.0092135
## Total
## Call: procD.lm(f1 = shape ~ class, data = df_handaxe3, print.progress = FALSE)
handaxe3pcs <- as.data.frame(pca_handaxe$x[37:54, 1:10])
handaxe3class <- shape_data_handaxe$Class[37:54]
handaxe3pcs <- cbind(handaxe3pcs, handaxe3class)</pre>
handaxe3pcs <- rename(handaxe3pcs, Class = handaxe3class)</pre>
handaxe3lda <- lda(Class ~ ., handaxe3pcs)</pre>
handaxe3ldapredict <- predict(handaxe3lda)</pre>
handaxe3ldaplot <- cbind(handaxe3ldapredict$x[, 1:3], handaxe3pcs)
handaxe3ldaplotggplot <- ggplot(handaxe3ldaplot, aes(LD1, LD2)) +
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
handaxe4 <- gpa_handaxe$coords[, , 55:72]</pre>
```

```
df_handaxe4 <- geomorph.data.frame(shape = handaxe4, class = shape_data_handaxe$Class[55:72], artefact
H4 <- procD.lm(shape ~ class, data = df_handaxe4, print.progress = FALSE)
summary(H4)
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
##
             \mathsf{Df}
                                  MS
                                          Rsq
                                                   F
                                                           7. Pr(>F)
              3 0.0006189 0.00020630 0.08025 0.4072 -1.4387 0.938
## Residuals 14 0.0070934 0.00050667 0.91975
## Total
           17 0.0077123
##
## Call: procD.lm(f1 = shape ~ class, data = df_handaxe4, print.progress = FALSE)
handaxe4pcs <- as.data.frame(pca_handaxe$x[55:72, 1:10])
handaxe4class <- shape_data_handaxe$Class[55:72]</pre>
handaxe4pcs <- cbind(handaxe4pcs, handaxe4class)</pre>
handaxe4pcs <- rename(handaxe4pcs, Class = handaxe4class)
handaxe4lda <- lda(Class ~ ., handaxe4pcs)</pre>
handaxe4ldapredict <- predict(handaxe4lda)</pre>
handaxe4ldaplot <- cbind(handaxe4ldapredict$x[, 1:3], handaxe4pcs)
handaxe4ldaplotggplot <- ggplot(handaxe4ldaplot, aes(LD1, LD2)) +
  geom_point(aes(shape = Class), size = 2) +
 labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
handaxe5 <- gpa_handaxe$coords[, , 73:90]</pre>
df_handaxe5 <- geomorph.data.frame(shape = handaxe5, class = shape_data_handaxe$Class[73:90], artefact
H5 <- procD.lm(shape ~ class, data = df_handaxe5, print.progress = FALSE)
summary(H5)
##
## Analysis of Variance, using Residual Randomization
## Permutation procedure: Randomization of null model residuals
## Number of permutations: 1000
## Estimation method: Ordinary Least Squares
## Sums of Squares and Cross-products: Type I
## Effect sizes (Z) based on F distributions
##
                                  MS
                                          Rsq
                                                  F
                                                           Z Pr(>F)
## class
              3 0.0007086 0.00023620 0.11527 0.608 -0.93807 0.822
## Residuals 14 0.0054387 0.00038848 0.88473
            17 0.0061473
## Total
```

```
##
## Call: procD.lm(f1 = shape ~ class, data = df_handaxe5, print.progress = FALSE)
handaxe5pcs <- as.data.frame(pca_handaxe$x[73:90, 1:10])
handaxe5class <- shape_data_handaxe$Class[73:90]</pre>
handaxe5pcs <- cbind(handaxe5pcs, handaxe5class)</pre>
handaxe5pcs <- rename(handaxe5pcs, Class = handaxe5class)</pre>
handaxe5lda <- lda(Class ~ ., handaxe5pcs)</pre>
handaxe5ldapredict <- predict(handaxe5lda)</pre>
handaxe5ldaplot <- cbind(handaxe5ldapredict$x[, 1:3], handaxe5pcs)
handaxe5ldaplotggplot <- ggplot(handaxe5ldaplot, aes(LD1, LD2)) +
  geom_point(aes(shape = Class), size = 2) +
  labs(x = "LDA 1", y = "LDA 2") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none",
        axis.title.y = element_text(size = 6),
        axis.title.x = element_text(size = 6))
lda.figure <- plot_grid(elongated1ldaplotggplot,</pre>
                          elongated2ldaplotggplot,
                          elongated3ldaplotggplot,
                          elongated4ldaplotggplot,
                          elongated5ldaplotggplot,
                          tanged1ldaplotggplot,
                          tanged2ldaplotggplot,
                          tanged3ldaplotggplot,
                          tanged4ldaplotggplot,
                          tanged5ldaplotggplot,
                          handaxe1ldaplotggplot,
                          handaxe2ldaplotggplot,
                          handaxe3ldaplotggplot,
                          handaxe4ldaplotggplot,
                          handaxe5ldaplotggplot,
                          ncol = 5, align = 'v')
lda.figure.legend <- get_legend(elongated1ldaplotggplot +</pre>
                                   guides(color = guide_legend(nrow = 1)) +
                                   theme(legend.position = "bottom"))
plot_grid(lda.figure, lda.figure.legend, ncol = 1, rel_heights = c(1, .1))
```



Stage 7: Measurement Data (Exploratory Framework)

To first examine the metric data, bivariate plots for all three artefact groups were generated in ggplot:

```
metric_data_elongated <- metric_data[which(metric_data$Type=="Elongated"),]</pre>
                     <- metric_data[which(metric_data$Type=="Handaxe"),]</pre>
metric data handaxe
                      <- metric_data[which(metric_data$Type=="Tanged"),]</pre>
metric_data_tanged
figure_7a <- ggplot(metric_data_elongated, aes(Length_mm, Width_mm, colour = Artefact, shape = Class))</pre>
  geom_point() +
  facet grid(cols = vars(Artefact), scales = "free", labeller=label both) +
  labs(x = "Length (mm)", y = "Width (mm)") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme_minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
        legend.position = "none")
figure_7b <- ggplot(metric_data_tanged, aes(Length_mm, Width_mm, colour = Artefact, shape = Class)) +
  geom_point() +
  facet_grid(cols = vars(Artefact), scales = "free", labeller=label_both) +
  labs(x = "Length (mm)", y = "Width (mm)") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
        axis.text.y = element_blank(),
```

```
legend.position = "none")
figure_7c <- ggplot(metric_data_handaxe, aes(Length_mm, Width_mm, colour = Artefact, shape = Class)) +
  geom_point() +
  facet_grid(cols = vars(Artefact), scales = "free", labeller=label_both) +
  labs(x = "Length (mm)", y = "Width (mm)") +
  scale_shape_manual(values=c(17,15,3,16)) +
  theme minimal() +
  theme(axis.text.x = element_blank(),
         axis.text.y = element_blank(),
        legend.position = "none")
figure_7 <- plot_grid(figure_7a,
                        figure_7b,
                        figure_7c,
                        labels= "AUTO",
                        ncol = 1,
                        align = 'v')
plot_grid(figure_7, lda.figure.legend, ncol = 1, rel_heights = c(1, .1))
 Α
         Artefact: 1
                            Artefact: 2
                                               Artefact: 3
                                                                  Artefact: 4
                                                                                     Artefact: 5
 Width (mm)
                                             Length (mm)
Width (mm) B
         Artefact: 1
                            Artefact: 2
                                               Artefact: 3
                                                                  Artefact: 4
                                                                                     Artefact: 5
                                             Length (mm)
Width (mm)
         Artefact: 1
                            Artefact: 2
                                               Artefact: 3
                                                                  Artefact: 4
                                                                                     Artefact: 5
                                             Length (mm)
                Class
                            Intermediate
                                             Novice + Photograph ● Professional
```

Stage 8: Measurement Data (Analytical Framework)

```
metric_data_elongated <- arrange(metric_data_elongated, Artefact, Class)</pre>
```

```
metric_data_elongated[1:18,] %>%
  group_by(Class) %>%
  summarise(count = n(),
            mean = mean(Length_mm, na.rm = TRUE),
            sd = sd(Length_mm, na.rm = TRUE),
            min = min(Length_mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length mm, na.rm = TRUE)/mean(Length mm, na.rm = TRUE)*100) %>%
  dplyr::mutate if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                  count mean
                                 sd
                                          min
                                                 max
     <chr>>
                  <chr> <chr>
                                 <chr>
                                          <chr> <chr> <chr>
## 1 Intermediate 3 110.6033 1.516652 108.99 112.00 1.371253
## 2 Novice
                 13
                       110.8454 1.739443 106.87 113.60 1.569251
## 3 Photograph
                                          115.47 115.47 NA
                  1
                        115.4700 NA
## 4 Professional 1
                        115.1400 NA
                                          115.14 115.14 NA
metric_data_elongated[1:18,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
     count
## 1
       17 1.725882
metric_data_elongated[19:36,] %>%
  group_by(Class) %>%
  summarise(count = n(), mean = mean(Length_mm, na.rm = TRUE),
            sd = sd(Length_mm, na.rm = TRUE),
            min = min(Length mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length mm, na.rm = TRUE)/mean(Length mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                  count mean
                                 sd
                                          min
                                                 max
     <chr>
                  <chr> <chr>
                                 <chr>
                                          <chr> <chr>
                                                        <chr>
                        126.6633 1.915446 124.67 128.49 1.512234
## 1 Intermediate 3
                        128.3285 2.477559 123.27 132.80 1.930639
## 2 Novice
                  13
## 3 Photograph
                        131.8400 NA
                                          131.84 131.84 NA
## 4 Professional 1
                        131.3500 NA
                                          131.35 131.35 NA
metric_data_elongated[19:36,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
     count
       17 1.932418
## 1
```

```
metric_data_elongated[37:54,] %>%
  group_by(Class) %>%
  summarise(count = n(),
            mean = mean(Length_mm, na.rm = TRUE),
            sd = sd(Length_mm, na.rm = TRUE),
            min = min(Length_mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length mm, na.rm = TRUE)/mean(Length mm, na.rm = TRUE)*100) %>%
  dplyr::mutate if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                  count mean
                                 sd
                                          min
                                                 max
     <chr>>
                  <chr> <chr>
                                 <chr>
                                          <chr> <chr> <chr>
## 1 Intermediate 3
                       123.8233 1.464559 122.43 125.35 1.182781
## 2 Novice
                  13
                        123.6092 1.578076 121.67 127.20 1.276665
                                          129.68 129.68 NA
## 3 Photograph
                  1
                        129.6800 NA
## 4 Professional 1
                        128.4700 NA
                                          128.47 128.47 NA
metric_data_elongated[37:54,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
     count
## 1
        17 1.511663
metric_data_elongated[55:72,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
            sd = sd(Length mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
           max = max(Length mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
     Class
                  count mean
                                 sd
                                          min
                                                max
     <chr>
                  <chr> <chr>
##
                                 <chr>>
                                          <chr> <chr> <chr>
                        95.60333 1.429452 94.37 97.17 1.495191
## 1 Intermediate 3
                        96.54923 1.292810 94.31 99.33 1.339016
## 2 Novice
                  13
## 3 Photograph 1
                        97.38000 NA
                                          97.38 97.38 NA
## 4 Professional 1
                        98.30000 NA
                                          98.30 98.30 NA
metric_data_elongated[55:72,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate if(is.numeric, format, 1)
##
     count
## 1
       17 1.41499
```

```
metric_data_elongated[73:90,] %>%
 group_by(Class) %>%
 summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
           max = max(Length_mm, na.rm = TRUE),
           cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %%
 dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                 count mean
                              sd
                                       min
                                              max
##
    <chr>
                <chr> <chr> <chr>
                                       <chr> <chr> <chr>
## 1 Intermediate 3 181.76 1.408226 180.17 182.85 0.7747721
## 2 Novice 13 183.56 1.501927 181.08 186.11 0.8182210
## 3 Photograph 1
                                    191.97 191.97 NA
                       191.97 NA
## 4 Professional 1
                       189.22 NA
                                       189.22 189.22 NA
metric_data_elongated[73:90,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
 summarise(count = n(),
           cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
    count
## 1
       17 1.161859
shapiro.test(metric_data_elongated$Length_mm[2:4])
##
  Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[2:4]
## W = 0.994, p-value = 0.8519
shapiro.test(metric_data_elongated$Width_mm[2:4])
##
##
  Shapiro-Wilk normality test
##
## data: metric data elongated$Width mm[2:4]
## W = 0.8097, p-value = 0.1379
shapiro.test(metric_data_elongated$Length_mm[5:17])
##
##
  Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[5:17]
## W = 0.93829, p-value = 0.4352
shapiro.test(metric_data_elongated$Width_mm[5:17])
##
   Shapiro-Wilk normality test
##
```

```
## data: metric_data_elongated$Width_mm[5:17]
## W = 0.95188, p-value = 0.6271
shapiro.test(metric_data_elongated$Length_mm[20:22])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[20:22]
## W = 0.86266, p-value = 0.2749
shapiro.test(metric_data_elongated$Width_mm[20:22])
##
##
   Shapiro-Wilk normality test
## data: metric_data_elongated$Width_mm[20:22]
## W = 0.99576, p-value = 0.8755
shapiro.test(metric_data_elongated$Length_mm[23:35])
##
##
   Shapiro-Wilk normality test
## data: metric_data_elongated$Length_mm[23:35]
## W = 0.9602, p-value = 0.7568
shapiro.test(metric_data_elongated$Width_mm[23:35])
##
##
   Shapiro-Wilk normality test
## data: metric_data_elongated$Width_mm[23:35]
## W = 0.88869, p-value = 0.0936
shapiro.test(metric_data_elongated$Length_mm[38:40])
##
##
   Shapiro-Wilk normality test
## data: metric_data_elongated$Length_mm[38:40]
## W = 0.87597, p-value = 0.3127
shapiro.test(metric_data_elongated$Width_mm[38:40])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Width_mm[38:40]
## W = 0.93589, p-value = 0.5111
shapiro.test(metric_data_elongated$Length_mm[41:53])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[41:53]
## W = 0.86234, p-value = 0.04136
```

```
shapiro.test(metric_data_elongated$Width_mm[41:53])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Width_mm[41:53]
## W = 0.92754, p-value = 0.3164
shapiro.test(metric_data_elongated$Length_mm[56:58])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[56:58]
## W = 0.91854, p-value = 0.4472
shapiro.test(metric_data_elongated$Width_mm[56:58])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Width_mm[56:58]
## W = 0.90007, p-value = 0.3857
shapiro.test(metric_data_elongated$Length_mm[59:71])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[59:71]
## W = 0.97937, p-value = 0.9763
shapiro.test(metric_data_elongated$Width_mm[59:71])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_elongated$Width_mm[59:71]
## W = 0.98079, p-value = 0.9831
shapiro.test(metric_data_elongated$Length_mm[74:76])
##
##
   Shapiro-Wilk normality test
## data: metric_data_elongated$Length_mm[74:76]
## W = 0.80888, p-value = 0.1359
shapiro.test(metric_data_elongated$Width_mm[74:76])
##
   Shapiro-Wilk normality test
##
##
## data: metric_data_elongated$Width_mm[74:76]
## W = 0.93099, p-value = 0.4923
shapiro.test(metric_data_elongated$Length_mm[77:89])
```

##

```
## Shapiro-Wilk normality test
##
## data: metric_data_elongated$Length_mm[77:89]
## W = 0.83103, p-value = 0.01632
shapiro.test(metric_data_elongated$Width_mm[77:89])
##
##
  Shapiro-Wilk normality test
##
## data: metric data elongated$Width mm[77:89]
## W = 0.95961, p-value = 0.7476
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_elongated[1:18,]))
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.7104 2.5707
                                   6
                                         28 0.04128 *
## Residuals 14
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary.aov(manova(cbind(Length mm, Width mm) ~ Class,
                  data = metric_data_elongated[1:18,]))
## Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
              3 36.277 12.092 4.1384 0.02699 *
## Residuals
             14 40.908
                         2.922
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Response Width_mm :
              Df Sum Sq Mean Sq F value Pr(>F)
##
              3 30.542 10.1808 3.4272 0.04676 *
## Class
## Residuals
             14 41.588 2.9706
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_elongated[19:36,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.59119
                       1.9583
                                    6
                                          28 0.106
## Residuals 14
summary.aov(manova(cbind(Length mm, Width mm) ~ Class,
                  data = metric_data_elongated[19:36,]))
## Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 29.647 9.8824 1.7081 0.211
## Residuals
             14 80.997 5.7855
##
## Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
              3 74.511 24.8370 5.0069 0.01451 *
## Residuals 14 69.448 4.9606
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_elongated[37:54,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.78278 3.0011
                                    6
                                          28 0.02159 *
## Residuals 14
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary.aov(manova(cbind(Length mm, Width mm) ~ Class,
                  data = metric_data_elongated[37:54,]))
## Response Length_mm :
##
              Df Sum Sq Mean Sq F value
                                        Pr(>F)
## Class
               3 53.177 17.726 7.2617 0.003573 **
## Residuals
             14 34.174
                        2.441
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 11.829 3.9430 3.2225 0.05519 .
## Residuals
              14 17.130 1.2236
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_elongated[55:72,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.37886 1.0906
                                    6
                                          28 0.3922
## Residuals 14
summary.aov(manova(cbind(Length mm, Width mm) ~ Class,
                  data = metric_data_elongated[55:72,]))
## Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
              3 6.4359 2.1453
                                  1.244 0.3312
             14 24.1430 1.7245
## Residuals
##
##
   Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 10.653 3.5511 0.9591 0.4392
             14 51.837 3.7026
## Residuals
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_elongated[73:90,]))
##
            Df Pillai approx F num Df den Df
                                               Pr(>F)
## Class
             3 0.96814
                       4.3785
                                          28 0.003066 **
                                    6
## Residuals 14
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_elongated[73:90,]))
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value
                                            Pr(>F)
## Class
               3 108.308 36.103 16.286 7.665e-05 ***
## Residuals
             14 31.036
                           2.217
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  Response Width_mm :
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 74.424 24.8082
                                   2.875 0.07372 .
## Residuals
              14 120.803 8.6288
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
metric_data_handaxe <- arrange(metric_data_handaxe, Artefact, Class)</pre>
metric_data_handaxe[1:18,] %>%
 group_by(Class) %>%
 summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
           max = max(Length_mm, na.rm = TRUE),
           cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %%
 dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
           count mean
                                sd
                                         min
                                                max
                                                       CV
    <chr>
                 <chr> <chr>
                                         <chr> <chr> <chr>
                                <chr>>
                       115.6233 5.201167 110.63 121.01 4.498371
## 1 Intermediate 3
## 2 Novice 13
                       117.6562 2.969151 113.84 123.76 2.523583
## 3 Photograph 1
                       122.2600 NA
                                        122.26 122.26 NA
## 4 Professional 1
                       123.4300 NA
                                         123.43 123.43 NA
metric_data_handaxe[1:18,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
 summarise(count = n(),
           cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
## count
       17 3.047414
## 1
metric_data_handaxe[19:36,] %>%
 group_by(Class) %>%
 summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length mm, na.rm = TRUE),
           max = max(Length_mm, na.rm = TRUE),
           cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
```

```
dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                 count mean
                                 Sd
                                          min
                                                 max
                                                        CV
     <chr>>
                  <chr> <chr>
                                 <chr>>
                                          <chr> <chr> <chr>
## 1 Intermediate 3
                        102.0900 0.080000 102.01 102.17 0.07836223
## 2 Novice
                13
                        101.1138 1.780503 98.74 104.27 1.76088978
## 3 Photograph 1
                        105.3500 NA
                                          105.35 105.35 NA
## 4 Professional 1
                                          105.56 105.56 NA
                        105.5600 NA
metric data handaxe[19:36,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %%
  dplyr::mutate_if(is.numeric, format, 1)
##
   count
## 1
       17 1.866549
metric_data_handaxe[37:54,] %>%
  group_by(Class) %>%
  summarise(count = n(), mean = mean(Length_mm, na.rm = TRUE), sd = sd(Length_mm, na.rm = TRUE), min = recommendation
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
    Class
                  count mean
                                 sd
                                          min
                                                 max
##
     <chr>>
                  <chr> <chr>
                                 <chr>
                                          <chr> <chr> <chr>
                       102.9600 1.015923 101.92 103.95 0.9867164
## 1 Intermediate 3
## 2 Novice
                        103.3415 2.663196 97.45 108.02 2.5770820
                13
## 3 Photograph 1
                        102.4300 NA
                                          102.43 102.43 NA
                                          102.44 102.44 NA
## 4 Professional 1
                        102.4400 NA
metric data handaxe[37:54,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(), cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
##
     count
## 1
       17 2.274329
metric_data_handaxe[55:72,] %>%
  group_by(Class) %>%
  summarise(count = n(),
            mean = mean(Length_mm, na.rm = TRUE),
            sd = sd(Length_mm, na.rm = TRUE),
            min = min(Length_mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
    Class
                  count mean
                                 sd
                                          min
                                                 max
                                                        CV
```

```
<chr> <chr>
                                <chr>
                                         <chr> <chr> <chr>
                       188.9167 7.650054 181.25 196.55 4.049433
## 1 Intermediate 3
                       187.2654 3.720118 177.76 192.04 1.986549
## 2 Novice 13
                       192.6300 NA
                                         192.63 192.63 NA
## 3 Photograph
                 1
## 4 Professional 1
                       192.8800 NA
                                         192.88 192.88 NA
metric data handaxe[55:72,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %%
  dplyr::mutate_if(is.numeric, format, 1)
##
     count
## 1
       17 2.366245
metric_data_handaxe[73:90,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length mm, na.rm = TRUE),
            sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
           max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                 count mean
                                sd
                                         min
                                                max
     <chr>
                 <chr> <chr>
                                <chr>
                                         <chr> <chr> <chr>
## 1 Intermediate 3 180.1900 1.185411 178.91 181.25 0.6578674
## 2 Novice
                       180.1177 2.722349 172.88 183.23 1.5114281
                13
## 3 Photograph 1
                       186.7500 NA
                                         186.75 186.75 NA
## 4 Professional 1
                       186.3700 NA
                                         186.37 186.37 NA
metric_data_handaxe[73:90,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %%
 dplyr::mutate_if(is.numeric, format, 1)
##
   count
## 1
       17 1.569395
shapiro.test(metric_data_handaxe$Length_mm[2:4])
##
## Shapiro-Wilk normality test
## data: metric_data_handaxe$Length_mm[2:4]
## W = 0.85647, p-value = 0.2579
shapiro.test(metric_data_handaxe$Width_mm[2:4])
##
## Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[2:4]
```

```
## W = 0.97381, p-value = 0.6896
shapiro.test(metric_data_handaxe$Length_mm[5:17])
##
##
   Shapiro-Wilk normality test
## data: metric_data_handaxe$Length_mm[5:17]
## W = 0.85528, p-value = 0.0334
shapiro.test(metric_data_handaxe$Width_mm[5:17])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[5:17]
## W = 0.94153, p-value = 0.4771
shapiro.test(metric_data_handaxe$Length_mm[20:22])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Length_mm[20:22]
## W = 0.80959, p-value = 0.1376
shapiro.test(metric_data_handaxe$Width_mm[20:22])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[20:22]
## W = 0.75, p-value < 2.2e-16
shapiro.test(metric_data_handaxe$Length_mm[23:35])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Length_mm[23:35]
## W = 0.92891, p-value = 0.3298
shapiro.test(metric_data_handaxe$Width_mm[23:35])
##
   Shapiro-Wilk normality test
## data: metric_data_handaxe$Width_mm[23:35]
## W = 0.95638, p-value = 0.6972
shapiro.test(metric_data_handaxe$Length_mm[38:40])
##
##
  Shapiro-Wilk normality test
## data: metric_data_handaxe$Length_mm[38:40]
## W = 0.99997, p-value = 0.9892
```

```
shapiro.test(metric_data_handaxe$Width_mm[38:40])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[38:40]
## W = 0.98821, p-value = 0.7922
shapiro.test(metric_data_handaxe$Length_mm[41:53])
##
   Shapiro-Wilk normality test
## data: metric_data_handaxe$Length_mm[41:53]
## W = 0.94426, p-value = 0.5144
shapiro.test(metric_data_handaxe$Width_mm[41:53])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[41:53]
## W = 0.64516, p-value = 0.0001654
shapiro.test(metric_data_handaxe$Length_mm[56:58])
##
##
   Shapiro-Wilk normality test
## data: metric_data_handaxe$Length_mm[56:58]
## W = 0.99874, p-value = 0.9323
shapiro.test(metric_data_handaxe$Width_mm[56:58])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[56:58]
## W = 0.83824, p-value = 0.2095
shapiro.test(metric_data_handaxe$Length_mm[59:71])
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Length_mm[59:71]
## W = 0.923, p-value = 0.2753
shapiro.test(metric_data_handaxe$Width_mm[59:71])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Width_mm[59:71]
## W = 0.87222, p-value = 0.05601
shapiro.test(metric_data_handaxe$Length_mm[74:76])
```

##

```
## Shapiro-Wilk normality test
##
## data: metric_data_handaxe$Length_mm[74:76]
## W = 0.92031, p-value = 0.4534
shapiro.test(metric_data_handaxe$Width_mm[74:76])
##
##
   Shapiro-Wilk normality test
##
## data: metric data handaxe$Width mm[74:76]
## W = 0.80075, p-value = 0.1163
shapiro.test(metric_data_handaxe$Length_mm[77:89])
##
##
   Shapiro-Wilk normality test
## data: metric_data_handaxe$Length_mm[77:89]
## W = 0.94055, p-value = 0.464
shapiro.test(metric_data_handaxe$Width_mm[77:89])
##
##
   Shapiro-Wilk normality test
## data: metric_data_handaxe$Width_mm[77:89]
## W = 0.98557, p-value = 0.9964
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_handaxe[1:18,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.54763
                        1.7596
                                     6
                                           28 0.1441
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_handaxe[1:18,]))
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 65.912 21.971 1.9237 0.1722
## Class
## Residuals
             14 159.895 11.421
##
## Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 76.939 25.6464 2.8436 0.07571 .
## Residuals
             14 126.264 9.0189
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_handaxe[19:36,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.59356
                        1.9695
                                     6
                                           28 0.1042
## Residuals 14
```

```
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_handaxe[19:36,]))
   Response Length_mm :
##
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 33.082 11.0275 4.0569 0.02869 *
## Residuals
              14 38.055 2.7182
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 45.094 15.0313 3.6851 0.03813 *
              14 57.105 4.0789
## Residuals
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
adonis(cbind(Length mm, Width mm) ~ Class,
      data = metric_data_handaxe[37:54,])
##
## Call:
## adonis(formula = cbind(Length_mm, Width_mm) ~ Class, data = metric_data_handaxe[37:54,
                                                                                               ])
## Permutation: free
## Number of permutations: 999
## Terms added sequentially (first to last)
##
            Df SumsOfSqs
##
                            MeanSqs F.Model
                                                 R2 Pr(>F)
## Class
              3 0.0003423 0.00011411 0.49079 0.09516 0.592
## Residuals 14 0.0032550 0.00023250
                                            0.90484
## Total
            17 0.0035973
                                             1.00000
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_handaxe[55:72,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
              3 0.27216 0.73507
                                           28 0.6256
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_handaxe[55:72,]))
##
   Response Length_mm :
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 54.38 18.127 0.8963 0.4674
## Residuals
              14 283.12 20.223
##
##
   Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 84.734 28.245 1.5192 0.2531
              14 260.287 18.592
## Residuals
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_handaxe[73:90,]))
```

```
Df Pillai approx F num Df den Df Pr(>F)
## Class
                                           28 0.1218
             3 0.57182 1.8685
                                     6
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                   data = metric_data_handaxe[73:90,]))
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 73.558 24.5195 3.7416 0.0365 *
## Class
## Residuals 14 91.745 6.5532
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
              3 135.10 45.034 3.9909 0.03015 *
## Residuals 14 157.98 11.284
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
metric_data_tanged <- arrange(metric_data_tanged, Artefact, Class)</pre>
metric_data_tanged[1:18,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
           max = max(Length_mm, na.rm = TRUE),
           cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                 count mean
                                sd
                                          min
                                              max
##
     <chr>>
                 <chr> <chr>
                                          <chr> <chr> <chr>
                                <chr>
## 1 Intermediate 3 84.07333 0.4119871 83.76 84.54 0.490033
## 2 Novice
                 13
                       84.19154 1.4370679 81.38 85.84 1.706903
## 3 Photograph
                1
                       87.12000 NA
                                          87.12 87.12 NA
## 4 Professional 1
                                          87.41 87.41 NA
                       87.41000 NA
metric_data_tanged[1:18,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
##
     count
## 1
       17 1.754211
metric_data_tanged[19:36,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
```

```
min = min(Length_mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
    Class
                 count mean
                                sd
                                          min
                                                 max
##
                 <chr> <chr>
     <chr>
                                <chr>
                                          <chr> <chr> <chr>
                       105.6333 0.5614564 105.27 106.28 0.5315145
## 1 Intermediate 3
## 2 Novice 13
                       105.8038 2.0141356 101.13 108.62 1.9036507
## 3 Photograph 1
                       107.9200 NA
                                          107.92 107.92 NA
                                          108.20 108.20 NA
## 4 Professional 1
                       108.2000 NA
metric_data_tanged[19:36,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(), cv = sd(Length mm, na.rm = TRUE)/mean(Length mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
##
   count
## 1
       17 1.749417
metric_data_tanged[37:54,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
    Class
                 count mean
                                sd
                                          min
                                                max
##
     <chr>
                 <chr> <chr>
                                <chr>
                                           <chr> <chr> <chr>
## 1 Intermediate 3
                       87.53000 0.8166395 86.66 88.28 0.9329824
## 2 Novice
                       88.27692 1.5441901 84.78 90.49 1.7492568
                13
## 3 Photograph 1
                       88.83000 NA
                                        88.83 88.83 NA
## 4 Professional 1
                       89.23000 NA
                                          89.23 89.23 NA
metric_data_tanged[37:54,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
##
     count
## 1
       17 1.614196
metric_data_tanged[55:72,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
            sd = sd(Length_mm, na.rm = TRUE),
```

```
min = min(Length_mm, na.rm = TRUE),
            max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
    Class
                 count mean
                                sd
                                         min
                                               max
     <chr>
                 <chr> <chr>
##
                                <chr>
                                          <chr> <chr> <chr>
                       54.83000 1.783003 53.64 56.88 3.251875
## 1 Intermediate 3
## 2 Novice
                       54.95231 1.324425 53.20 57.82 2.410136
            13
## 3 Photograph 1
                       57.01000 NA
                                         57.01 57.01 NA
                                         57.80 57.80 NA
## 4 Professional 1
                       57.80000 NA
metric_data_tanged[55:72,] %>%
  filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
##
     count
                 CV
## 1
       17 2.691978
metric_data_tanged[73:90,] %>%
  group_by(Class) %>%
  summarise(count = n(),
           mean = mean(Length_mm, na.rm = TRUE),
           sd = sd(Length_mm, na.rm = TRUE),
           min = min(Length_mm, na.rm = TRUE),
           max = max(Length_mm, na.rm = TRUE),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %%
  dplyr::mutate_if(is.numeric, format, 1)
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 4 x 7
##
    Class
                 count mean
                                sd
                                          min max
     <chr>
                                <chr>
                                          <chr> <chr> <chr>
                 <chr> <chr>
## 1 Intermediate 3
                       60.11000 0.7754354 59.58 61.00 1.290027
## 2 Novice 13
                       59.83846 1.2881631 58.06 62.62 2.152734
                                          62.81 62.81 NA
## 3 Photograph 1
                       62.81000 NA
## 4 Professional 1
                       62.22000 NA
                                          62.22 62.22 NA
metric_data_tanged[73:90,] %>%
 filter(Class=="Novice" | Class == "Intermediate" | Class == "Professional") %>%
  summarise(count = n(),
            cv = sd(Length_mm, na.rm = TRUE)/mean(Length_mm, na.rm = TRUE)*100) %>%
 dplyr::mutate_if(is.numeric, format, 1)
##
   count
## 1
       17 2.140211
shapiro.test(metric_data_tanged$Length_mm[2:4])
##
##
   Shapiro-Wilk normality test
##
```

```
## data: metric_data_tanged$Length_mm[2:4]
## W = 0.95243, p-value = 0.5801
shapiro.test(metric_data_tanged$Width_mm[2:4])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Width_mm[2:4]
## W = 0.99986, p-value = 0.9773
shapiro.test(metric_data_tanged$Length_mm[5:17])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Length_mm[5:17]
## W = 0.96154, p-value = 0.7772
shapiro.test(metric_data_tanged$Width_mm[5:17])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Width_mm[5:17]
## W = 0.94549, p-value = 0.5318
shapiro.test(metric_data_tanged$Length_mm[20:22])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Length_mm[20:22]
## W = 0.99957, p-value = 0.9604
shapiro.test(metric_data_tanged$Width_mm[20:22])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Width_mm[20:22]
## W = 0.85465, p-value = 0.253
shapiro.test(metric_data_tanged$Length_mm[23:35])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Length_mm[23:35]
## W = 0.93546, p-value = 0.4009
shapiro.test(metric_data_tanged$Width_mm[23:35])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Width_mm[23:35]
## W = 0.95349, p-value = 0.652
```

```
shapiro.test(metric_data_tanged$Length_mm[38:40])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Length_mm[38:40]
## W = 0.93746, p-value = 0.5173
shapiro.test(metric_data_tanged$Width_mm[38:40])
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Width_mm[38:40]
## W = 0.99882, p-value = 0.9344
shapiro.test(metric_data_tanged$Length_mm[41:53])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Length_mm[41:53]
## W = 0.946, p-value = 0.5391
shapiro.test(metric_data_tanged$Width_mm[41:53])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Width_mm[41:53]
## W = 0.91872, p-value = 0.2411
shapiro.test(metric_data_tanged$Length_mm[56:58])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Length_mm[56:58]
## W = 0.99389, p-value = 0.8506
shapiro.test(metric_data_tanged$Width_mm[56:58])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Width_mm[56:58]
## W = 0.83275, p-value = 0.1953
shapiro.test(metric_data_tanged$Length_mm[59:71])
##
   Shapiro-Wilk normality test
##
##
## data: metric_data_tanged$Length_mm[59:71]
## W = 0.93757, p-value = 0.4262
shapiro.test(metric_data_tanged$Width_mm[59:71])
```

##

```
## Shapiro-Wilk normality test
##
## data: metric_data_tanged$Width_mm[59:71]
## W = 0.94463, p-value = 0.5195
shapiro.test(metric_data_tanged$Length_mm[74:76])
##
##
   Shapiro-Wilk normality test
##
## data: metric data tanged$Length mm[74:76]
## W = 0.99856, p-value = 0.9275
shapiro.test(metric_data_tanged$Width_mm[74:76])
##
##
   Shapiro-Wilk normality test
##
## data: metric_data_tanged$Width_mm[74:76]
## W = 0.98702, p-value = 0.7819
shapiro.test(metric_data_tanged$Length_mm[77:89])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Length_mm[77:89]
## W = 0.92621, p-value = 0.3038
shapiro.test(metric_data_tanged$Width_mm[77:89])
##
##
   Shapiro-Wilk normality test
## data: metric_data_tanged$Width_mm[77:89]
## W = 0.9138, p-value = 0.2066
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_tanged[1:18,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
             3 0.56874 1.8544
## Class
                                     6
                                            28 0.1245
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_tanged[1:18,]))
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 17.112 5.7041 3.1789 0.0572 .
## Class
             14 25.121 1.7944
## Residuals
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
              3 2.5154 0.83848 0.4928 0.693
## Class
## Residuals
             14 23.8228 1.70163
```

```
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_tanged[19:36,]))
            Df Pillai approx F num Df den Df Pr(>F)
##
## Class
              3 0.48288
                         1.4853
                                      6
                                            28 0.2193
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_tanged[19:36,]))
  Response Length_mm :
              Df Sum Sq Mean Sq F value Pr(>F)
##
## Class
               3 9.418 3.1392 0.8913 0.4698
             14 49.311 3.5222
## Residuals
##
##
  Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
               3 8.0821 2.69404 3.1918 0.05659 .
## Residuals
             14 11.8169 0.84406
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_tanged[37:54,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
              3 0.23153 0.61096
## Class
                                     6
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_tanged[37:54,]))
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 2.858 0.95265 0.4453 0.7244
## Class
              14 29.948 2.13915
## Residuals
##
##
  Response Width mm:
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 3.4126 1.1376 0.9378 0.4486
## Class
## Residuals
              14 16.9828 1.2131
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_tanged[55:72,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.52873 1.6771
                                           28 0.1636
                                     6
## Residuals 14
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                   data = metric_data_tanged[55:72,]))
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
## Class
              3 11.244 3.7480 1.9145 0.1736
## Residuals 14 27.407 1.9577
```

```
Response Width_mm :
##
##
              Df Sum Sq Mean Sq F value Pr(>F)
                         2.5617 2.8893 0.07283 .
## Class
               3 7.6851
              14 12.4124
                          0.8866
## Residuals
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(manova(cbind(Length_mm, Width_mm) ~ Class,
              data = metric_data_tanged[73:90,]))
##
            Df Pillai approx F num Df den Df Pr(>F)
## Class
             3 0.66976
                         2.3496
                                     6
                                           28 0.05791 .
## Residuals 14
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary.aov(manova(cbind(Length_mm, Width_mm) ~ Class,
                  data = metric_data_tanged[73:90,]))
##
   Response Length_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 12.610
                         4.2032 2.7869 0.07947 .
## Class
## Residuals
              14 21.115
                         1.5082
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   Response Width_mm :
##
              Df Sum Sq Mean Sq F value Pr(>F)
               3 2.8109 0.93696 1.3714 0.2922
## Class
## Residuals
              14 9.5652 0.68323
```

Concluding Remarks

For any queries, or for more information on any aspect of this markdown, please contact C.S.Hoggard@soton.ac.uk.

Acknowledgements

We thank Moesgaard Museum for loaning the artefacts used throughout this study. We would also like to thank all illustrators for their time during this experiment. CSH and FR thank the Independent Research Fund Denmark for grant #610700059B and FR also gratefully acknowledges funding the European Research Council (grant agreement 817564 under the Horizon 2020 research and innovation programme). We also thank John McNabb for comments on earlier drafts of this paper.