#### Lexical Analysis and Lexical Analyzer Generators

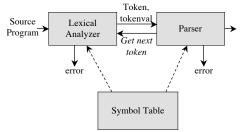
Chapter 3

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The Reason Why Lexical Analysis is a Separate Phase

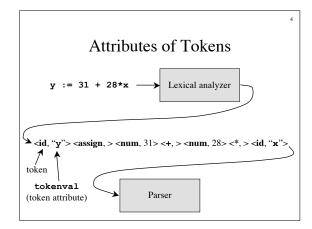
- Simplifies the design of the compiler
  - LL(1) or LR(1) parsing with 1 token lookahead would not be possible (multiple characters/tokens to match)
- Provides efficient implementation
  - Systematic techniques to implement lexical analyzers by hand or automatically from specifications
  - Stream buffering methods to scan input
- · Improves portability
  - Non-standard symbols and alternate character encodings can be normalized (e.g. trigraphs)

Interaction of the Lexical Analyzer with the Parser



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exical



Tokens, Patterns, and Lexemes

- A token is a classification of lexical units
  - For example: id and num
- Lexemes are the specific character strings that make up a token
  - For example: abc and 123
- *Patterns* are rules describing the set of lexemes belonging to a token
  - For example: "letter followed by letters and digits" and "non-empty sequence of digits"

Specification of Patterns for Tokens: *Definitions* 

- An *alphabet* Σ is a finite set of symbols (characters)
- A *string* s is a finite sequence of symbols from  $\Sigma$ 
  - |s| denotes the length of string s
  - $\epsilon$  denotes the empty string, thus  $\left| \, \epsilon \, \right| \, = 0$
- A language is a specific set of strings over some fixed alphabet  $\Sigma$

#### Specification of Patterns for Tokens: String Operations

- The *concatenation* of two strings x and y is denoted by xy
- The *exponentation* of a string s is defined by

$$s^0 = \varepsilon$$
  
 
$$s^i = s^{i-1}s \quad \text{for } i > 0$$

note that  $s\varepsilon = \varepsilon s = s$ 

#### Specification of Patterns for Tokens: Language Operations

• Union
$$L \cup M = \{s \mid s \in L \text{ or } s \in M\}$$
• Concatenation

• Concatenation

$$LM = \{xy \mid x \in L \text{ and } y \in M\}$$

• Exponentiation

$$L^{0} = \{ \epsilon \}; L^{i} = L^{i-1}L$$

• Kleene closure

$$L^* = \bigcup_{i=0,\dots,\infty} L^i$$

• Positive closure

 $L^+ = \bigcup_{i=1,...,\infty} L^i$ 

#### Specification of Patterns for Tokens: Regular Expressions

- Basis symbols:
  - $\varepsilon$  is a regular expression denoting language  $\{\varepsilon\}$
  - $a \in \Sigma$  is a regular expression denoting  $\{a\}$
- If r and s are regular expressions denoting languages L(r) and M(s) respectively, then
  - $-r \mid s$  is a regular expression denoting  $L(r) \cup M(s)$
  - rs is a regular expression denoting L(r)M(s)
  - $-r^*$  is a regular expression denoting  $L(r)^*$
  - -(r) is a regular expression denoting L(r)
- · A language defined by a regular expression is called a regular set

Specification of Patterns for Tokens: Regular Definitions

•	Regular	definitions	introduce a	a naming	convention:

$$d_1 \rightarrow r_1$$

$$d_2 \rightarrow r_2$$
...
$$d_1 \rightarrow r$$

where each  $r_i$  is a regular expression over  $\Sigma \cup \{d_1, d_2, ..., d_{i\text{-}1}\,\}$ 

• Any  $d_i$  in  $r_i$  can be textually substituted in  $r_i$  to obtain an equivalent set of definitions

Specification of Patterns for Tokens: Regular Definitions

• Example:

$$\begin{array}{c} letter \rightarrow A \, \big| \, B \, \big| \, \dots \, \big| \, Z \, \big| \, a \, \big| \, b \, \big| \, \dots \, \big| \, z \\ digit \rightarrow 0 \, \big| \, 1 \, \big| \, \dots \, \big| \, 9 \\ id \rightarrow letter \, ( \, letter \, \big| \, digit \, )^* \end{array}$$

• Regular definitions are not recursive:

digits → digit digits | digit wrong!

Specification of Patterns for Tokens: Notational Shorthand

• The following shorthands are often used:

$$r^+ = rr^*$$
 $r? = r \mid \varepsilon$ 
 $[\mathbf{a} - \mathbf{z}] = \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \dots \mid \mathbf{z}$ 

• Examples:  $\mathbf{digit} \rightarrow [0-9]$ num  $\rightarrow$  digit<sup>+</sup> (. digit<sup>+</sup>)? ( E (+ | -)? digit<sup>+</sup> )?

## Regular Definitions and Grammars

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```
Grammar

stmt \rightarrow if expr then stmt

| if expr then stmt else stmt
| \epsilon

expr \rightarrow term relop term

| term \rightarrow id

| if \rightarrow if

| num

| then \rightarrow then

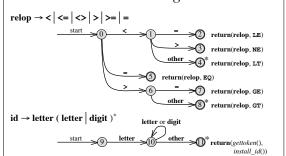
| else \rightarrow else

| relop \rightarrow < | <= | <> | > | >= |

| id \rightarrow letter (letter | digit)^*

| num \rightarrow digit^+ (. digit^+)? (E (+ | -)? digit^+)?
```

#### Coding Regular Definitions in Transition Diagrams



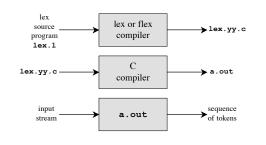
# Coding Regular Definitions in Transition Diagrams: Code

```
token nexttoken()
{
    white (1) {
        switch (state) {
            case 0: c = nextchar();
            if (comblank || comblank || c
```

#### The Lex and Flex Scanner Generators

- Lex and its newer cousin flex are scanner generators
- Systematically translate regular definitions into C source code for efficient scanning
- Generated code is easy to integrate in C applications

#### Creating a Lexical Analyzer with Lex and Flex



#### Lex Specification

• A lex specification consists of three parts: regular definitions, C declarations in %{ %}

translation rules

user-defined auxiliary procedures

• The translation rules are of the form:

 $\{ action_1 \}$ { action<sub>2</sub> }  $p_2$ 

 $\{ action_n \}$ 

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```
Regular Expressions in Lex

x match the character x
\lambda. match the character .

"string" match contents of string of characters

match any character except newline

and the end of a line

[xyz] match one character x, y, or z (use \ to escape -)

[az] match one of a to z

r closure (match zero or more occurrences)

r+ positive closure (match one or more occurrences)

r2 positive closure (match one or more occurrences)

r3 positive closure (match one or more occurrences)

r4 positive closure (concatenation)

r5 proprio match r1 then r5 (concatenation)

r1 proprio match r1 when followed by r5

{d} match the regular expression defined by d
```

```
Example Lex Specification 1

Contains the matching lexeme state of the matching lexeme state of the matching lexeme state of the lexical state of the lexica
```

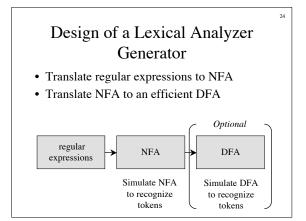
```
Example Lex Specification 3

*{
    #include <stdio.h> Regular
    definitions
    digit [0-9]
    letter [A-Za-z]
    id {letter}({letter}|{digit})*

    {
        (digit)+ { printf("number: %s\n", yytext); }
        (d) { printf("ident: %s\n", yytext); }
        (printf("other: %s\n", yytext); }

        main()
        (yylex();
}
```

# Example Lex Specification 4 \[ \begin{align\*} \( \begin{align\*} \text{definitions of manifest constants \*/} \\ \text{define LT (256)} \\ \text{delin} \\ \text{delin} \\ \text{delin} \\ \text{letter (256)} \\ \text{delin} \\ \text{letter (164ter) ((digit)) \* token to number (digit) \* ((digit) \*) ? (E[\*\-1?(digit) \*) ? parser \\ \text{delin} \\ \text{del (seturn IEF;) } \\ \text{delin} \\ \text{delin}



#### Nondeterministic Finite Automata

• An NFA is a 5-tuple  $(S, \Sigma, \delta, s_0, F)$  where

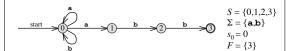
S is a finite set of *states*  $\Sigma$  is a finite set of symbols, the *alphabet*  $\delta$  is a *mapping* from  $S \times \Sigma$  to a set of states  $s_0 \in S$  is the *start state*  $F \subseteq S$  is the set of *accepting* (or *final*) *states* 

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#### Transition Graph

• An NFA can be diagrammatically represented by a labeled directed graph called a *transition graph* 



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#### **Transition Table**

• The mapping δ of an NFA can be represented in a *transition table* 

The Language Defined by an NFA

- An NFA *accepts* an input string *x* if and only if there is some path with edges labeled with symbols from *x* in sequence from the start state to some accepting state in the transition graph
- A state transition from one state to another on the path is called a *move*
- The language defined by an NFA is the set of input strings it accepts, such as (a | b)\*abb for the example NFA

Design of a Lexical Analyzer Generator: RE to NFA to DFA

Lex specification with regular expressions

 $p_2$ 

lar expressions 
$$\{ action_1 \}$$
  $\{ action_2 \}$ 



Subset construction

DFA

NFA

From Regular Expression to NFA (Thompson's Construction)

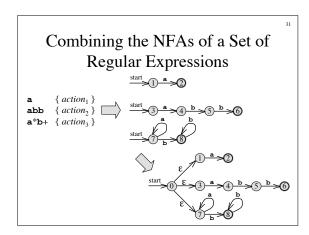
$$\varepsilon \xrightarrow{\text{start}} i \xrightarrow{\varepsilon} \emptyset$$

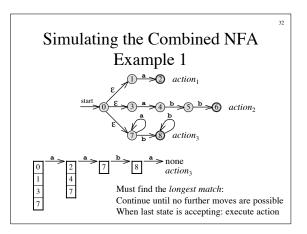
$$r_1 \mid r_2$$
  $\underbrace{\epsilon \quad N(r_1) \quad \epsilon}_{\epsilon \quad N(r_2) \quad \epsilon}$ 

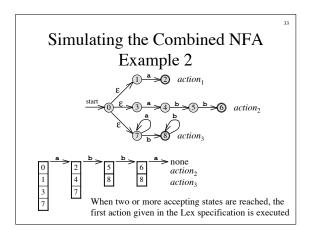
$$r_1r_2$$
  $\xrightarrow{\text{start}}$   $(i) N(r_1) (N(r_2)) (f)$ 

$$r^*$$
  $\frac{\epsilon}{\epsilon}$ 

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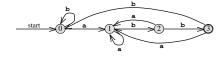
#### Deterministic Finite Automata

- A deterministic finite automaton is a special case of an NFA
  - No state has an ε-transition
  - For each state s and input symbol a there is at most one edge labeled a leaving s
- Each entry in the transition table is a single state
  - At most one path exists to accept a string
  - Simulation algorithm is simple

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#### Example DFA

A DFA that accepts (a | b)\*abb



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### Conversion of an NFA into a DFA

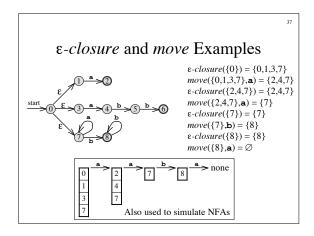
• The *subset construction algorithm* converts an NFA into a DFA using:

 $\varepsilon$ -closure(s) = {s}  $\cup$  {t | s  $\rightarrow_{\varepsilon} ... \rightarrow_{\varepsilon} t$ }  $\varepsilon$ -closure(T) =  $\cup_{s \leftarrow \tau} \varepsilon$ -closure(s)

 $\varepsilon$ -closure(T) =  $\bigcup_{s \in T} \varepsilon$ -closure(s)  $move(T,a) = \{t \mid s \rightarrow_a t \text{ and } s \in T\}$ 

• The algorithm produces:

Dstates is the set of states of the new DFA consisting of sets of states of the NFA Dtran is the transition table of the new DFA



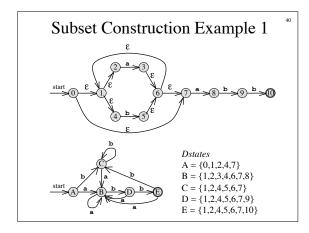
## Simulating an NFA using $\varepsilon$ -closure and move

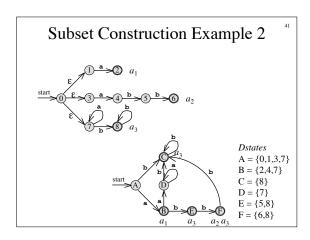
 $S := \varepsilon \text{-} closure(\{s_0\})$   $S_{prev} := \emptyset$  a := nextchar()while  $S \neq \emptyset$  do  $S_{prev} := S$   $S := \varepsilon \text{-} closure(move(S,a))$  a := nextchar()end do
if  $S_{prev} \cap F \neq \emptyset$  then
execute action in  $S_{prev}$ return "yes"
else return "no"

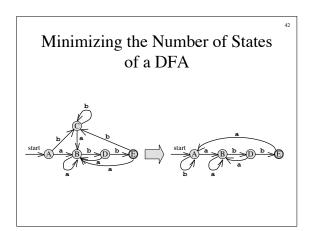
## The Subset Construction Algorithm

Initially,  $\varepsilon$ -closure( $s_0$ ) is the only state in Dstates and it is unmarked while there is an unmarked state T in Dstates  $\mathbf{do}$  mark T for each input symbol  $a \in \Sigma$   $\mathbf{do}$   $U := \varepsilon$ -closure(move(T,a)) if U is not in Dstates  $\mathbf{then}$  add U as an unmarked state to Dstates  $\mathbf{end}$  if Dtran[T,a] := U

end do







From Regular Expression to DFA Directly

- The "important states" of an NFA are those without an  $\epsilon$ -transition, that is if  $move(\{s\},a) \neq \emptyset$  for some a then s is an important state
- The subset construction algorithm uses only the important states when it determines  $\epsilon$ -closure(move(T,a))

From Regular Expression to DFA Directly (Algorithm)

- Augment the regular expression r with a special end symbol # to make accepting states important: the new expression is r#
- Construct a syntax tree for r#
- Traverse the tree to construct functions nullable, firstpos, lastpos, and followpos

From Regular Expression to DFA Directly: Syntax Tree of (alb)\*abb# closure position

number (for leafs ≠ε)

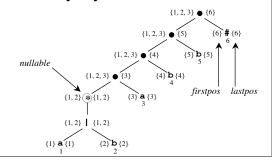
## From Regular Expression to DFA Directly: Annotating the Tree

- *nullable(n)*: the subtree at node *n* generates languages including the empty string
- *firstpos*(*n*): set of positions that can match the first symbol of a string generated by the subtree at node *n*
- lastpos(n): the set of positions that can match the last symbol of a string generated be the subtree at node n
- *followpos(i)*: the set of positions that can follow position *i* in the tree

## From Regular Expression to DFA Directly: Annotating the Tree

Node n	nullable(n)	firstpos(n)	lastpos(n)
Leaf ε	true	Ø	Ø
Leaf i	false	{ <i>i</i> }	{ <i>i</i> }
, \ c <sub>1</sub> c <sub>2</sub>	$nullable(c_1)$ or $nullable(c_2)$	$firstpos(c_1)$ $\cup$ $firstpos(c_2)$	$\begin{array}{c} lastpos(c_1) \\ \cup \\ lastpos(c_2) \end{array}$
· / \ c <sub>1</sub> · c <sub>2</sub>	$\begin{array}{c} \textit{nullable}(c_1) \\ \text{and} \\ \textit{nullable}(c_2) \end{array}$	if $nullable(c_1)$ then $firstpos(c_1) \cup$ $firstpos(c_2)$ else $firstpos(c_1)$	if $nullable(c_2)$ then $lastpos(c_1) \cup$ $lastpos(c_2)$ else $lastpos(c_2)$
*   c <sub>1</sub>	true	$firstpos(c_1)$	$lastpos(c_1)$

## From Regular Expression to DFA Directly: Syntax Tree of (alb)\*abb#



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## From Regular Expression to DFA Directly: *followpos*

for each node n in the tree do

if n is a cat-node with left child  $c_1$  and right child  $c_2$  then

for each i in  $lastpos(c_1)$  do  $followpos(i) := followpos(i) \cup firstpos(c_2)$ end do

else if n is a star-node

for each i in lastpos(n) do  $followpos(i) := followpos(i) \cup firstpos(n)$ end do

end if

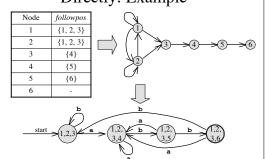
end do

# From Regular Expression to DFA Directly: Algorithm

 $s_0 := firstpos(root)$  where root is the root of the syntax tree  $Dstates := \{s_0\}$  and is unmarked while there is an unmarked state T in Dstates do mark T for each input symbol  $a \in \Sigma$  do let U be the set of positions that are in followpos(p) for some position p in T, such that the symbol at position p is a if U is not empty and not in Dstates then add U as an unmarked state to Dstates end if Dtran[T,a] := U end do

# From Regular Expression to DFA Directly: Example

end do



Time-Space Tradeoffs

Automaton	Space (worst case)	Time (worst case)				
NFA	O( r )	$O( r  \times  x )$				
DFA	$O(2^{ r })$	O( x )				