

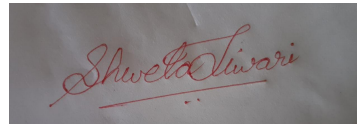
CD: COMPILER DESIGN
CD: UNIT-2 09/2022

SEPTEMBER 2022 / IT-3rd year, Vth semester
FALL SEMESTER, YEAR (Vth, 3rd)
FALL SESSION (2022-23)
(CD)
MS. SHWETA TIWARI
Published: SEPTEMBER, 2022

PREPARED FOR
Engineering Students
All Engineering College

CD: COMPILER DESIGN

INSTRUCTOR: Ms. SHWETA TIWARI
shwetatiwari08@recabn.ac.in
shwetatiwari08aug@gmail.com



September 2022

TOPIC On: QUESTION And ANSWER ON-

Left Recursion, Left Factoring, FIRST() AND FOLLOW()

1. QUESTION And ANSWER ON- Eliminate Left Recursion

-
1. Consider the following grammar and eliminate left recursion-

$$A \rightarrow ABd / Aa / a$$

$$B \rightarrow Be / b$$

Answer-1. The grammar after eliminating left recursion is-

$$A \rightarrow aA'$$

$$A' \rightarrow BdA' / aA' / \in$$

$$B \rightarrow bB'$$

$$B' \rightarrow eB' / \in$$

2. Consider the following grammar and eliminate left recursion-

$$E \rightarrow E + E / E \times E / a$$

Answer-2. The grammar after eliminating left recursion is-

$$E \rightarrow aA$$

$$A \rightarrow +EA / \times EA / \in$$

3. Consider the following grammar and eliminate left recursion-

$$E \rightarrow E + T / T$$

$$T \rightarrow T \times F / F$$

$$F \rightarrow id$$

Answer-3. The grammar after eliminating left recursion is-

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \in$$

$$T \rightarrow FT'$$

$$T' \rightarrow \times FT' / \in$$

$$F \rightarrow id$$

-
4. Consider the following grammar and eliminate left recursion-

$$S \rightarrow (L) / a$$

$$L \rightarrow L, S / S$$

Answer-4. The grammar after eliminating left recursion is-

$$S \rightarrow (L) / a$$

$$L \rightarrow SL'$$

$$L' \rightarrow ,SL' / \in$$

5. Consider the following grammar and eliminate left recursion-

$$S \rightarrow SoS1S / o1$$

Answer-5. The grammar after eliminating left recursion is-

$$S \rightarrow o1A$$

$$A \rightarrow oS1SA / \in$$

6. Consider the following grammar and eliminate left recursion-

$$S \rightarrow A$$

$$A \rightarrow Ad / Ae / aB / ac$$

$$B \rightarrow bBc / f$$

Answer-6. The grammar after eliminating left recursion is-

$$S \rightarrow A$$

$$A \rightarrow aBA' / acA'$$

$$A' \rightarrow dA' / eA' / \in$$

$$B \rightarrow bBc / f$$

7. Consider the following grammar and eliminate left recursion-

$$A \rightarrow AA\alpha / \beta$$

Answer-7. The grammar after eliminating left recursion is-

$$A \rightarrow \beta A'$$

$$A' \rightarrow A\alpha A' / \epsilon$$

8. Consider the following grammar and eliminate left recursion-

$$A \rightarrow Ba / Aa / c$$

$$B \rightarrow Bb / Ab / d$$

Answer-8. The grammar after eliminating left recursion is-

This is a case of indirect left recursion.

Step-01:

First let us eliminate left recursion from $A \rightarrow Ba / Aa / c$

Eliminating left recursion from here, we get-

$$A \rightarrow BaA' / cA'$$

$$A' \rightarrow aA' / \epsilon$$

Now, given grammar becomes-

$$A \rightarrow BaA' / cA'$$

$$A' \rightarrow aA' / \epsilon$$

$$B \rightarrow Bb / Ab / d$$

Step-02:

Substituting the productions of A in $B \rightarrow Ab$, we get the following grammar-

$$A \rightarrow BaA' / cA'$$

$$A' \rightarrow aA' / \epsilon$$

$$B \rightarrow Bb / BaA'b / cA'b / d$$

Step-03:

Now, eliminating left recursion from the productions of B, we get the following grammar-

$$A \rightarrow BaA' / cA'$$

$$A' \rightarrow aA' / \epsilon$$

$$B \rightarrow cA'bB' / dB'$$

$$B' \rightarrow bB' / aA'bB' / \epsilon$$

This is the final grammar after eliminating left recursion.

9. Consider the following grammar and eliminate left recursion-

$$X \rightarrow XSb / Sa / b$$

$$S \rightarrow Sb / Xa / a$$

Answer-9. The grammar after eliminating left recursion is-

This is a case of indirect left recursion.

Step-01:

First let us eliminate left recursion from $X \rightarrow XSb / Sa / b$

Eliminating left recursion from here, we get-

$$X \rightarrow SaX' / bX'$$

$$X' \rightarrow SbX' / \epsilon$$

Now, given grammar becomes-

$$X \rightarrow SaX' / bX'$$

$$X' \rightarrow SbX' / \epsilon$$

$$S \rightarrow Sb / Xa / a$$

Step-02:

Substituting the productions of X in $S \rightarrow Xa$, we get the following grammar-

$$X \rightarrow SaX' / bX'$$

$$X' \rightarrow SbX' / \epsilon$$

$$S \rightarrow Sb / SaX'a / bX'a / a$$

Step-03:

Now, eliminating left recursion from the productions of S, we get the following grammar-

$$X \rightarrow SaX' / bX'$$

$$X' \rightarrow SbX' / \epsilon$$

$$S \rightarrow bX'aS' / aS'$$

$$S' \rightarrow bS' / aX'aS' / \epsilon$$

This is the final grammar after eliminating left recursion.

10. Consider the following grammar and eliminate left recursion-

$$S \rightarrow Aa / b$$

$$A \rightarrow Ac / Sd / \epsilon$$

Answer-10. The grammar after eliminating left recursion is-

This is a case of indirect left recursion.

Step-01:

First let us eliminate left recursion from $S \rightarrow Aa / b$

This is already free from left recursion.

Step-02:

Substituting the productions of S in $A \rightarrow Sd$, we get the following grammar-

$$S \rightarrow Aa / b$$

$$A \rightarrow Ac / Aad / bd / \in$$

Step-03:

Now, eliminating left recursion from the productions of A, we get the following grammar-

$$S \rightarrow Aa / b$$

$$A \rightarrow bdA' / A'$$

$$A' \rightarrow cA' / adA' / \in$$

This is the final grammar after eliminating left recursion.

2. QUESTION And ANSWER ON- Eliminate Left Factoring

1. Do left factoring in the following grammar-

$$S \rightarrow iEtS / iEtSeS / a$$

$$E \rightarrow b$$

Answer-1. The grammar after eliminating left factoring is-

$$S \rightarrow iEtSS' / a$$

$$S' \rightarrow eS / \epsilon$$

$$E \rightarrow b$$

2. Do left factoring in the following grammar-

$$A \rightarrow aAB / aBc / aAc$$

Answer-2. The grammar after eliminating left factoring is-

Step-01:

$$A \rightarrow aA'$$

$$A' \rightarrow AB / Bc / Ac$$

Again, this is a grammar with common prefixes.

Step-02:

$$A \rightarrow aA'$$

$$A' \rightarrow AD / Bc$$

$$D \rightarrow B / c$$

This is left factored grammar.

3. Do left factoring in the following grammar-

$$S \rightarrow bSSaaS / bSSaSb / bSb / a$$

Answer-3. The grammar after eliminating left factoring is-

Step-01:

$$S \rightarrow bSS' / a$$

$$S' \rightarrow SaaS / SaSb / b$$

Again, this is a grammar with common prefixes.

Step-02:

$$S \rightarrow bSS' / a$$

$$S' \rightarrow SaA / b$$

$$A \rightarrow aS / Sb$$

This is left -factored grammar.

4. Do left factoring in the following grammar-

$$S \rightarrow aSSbS / aSaSb / abb / b$$

Answer-4. The grammar after eliminating left factoring is-

Step-01:

$$S \rightarrow aS' / b$$

$$S' \rightarrow SSbS / SaSb / bb$$

Again, this is a grammar with common prefixes.

Step-02:

$$S \rightarrow aS' / b$$

$$S' \rightarrow SA / bb$$

$$A \rightarrow SbS / aSb$$

This is left -factored grammar.

5. Do left factoring in the following grammar-

$$S \rightarrow a / ab / abc / abcd$$

Answer-5. The grammar after eliminating left factoring is-

Step-01:

$$S \rightarrow aS'$$

$$S' \rightarrow b / bc / bcd / \epsilon$$

Again, this is a grammar with common prefixes.

Step-02:

$$S \rightarrow aS'$$

$$S' \rightarrow bA / \epsilon$$

$$A \rightarrow c / cd / \epsilon$$

Again, this is a grammar with common prefixes.

Step-03:

$$S \rightarrow aS'$$

$$S' \rightarrow bA / \in$$

$$A \rightarrow cB / \in$$

$$B \rightarrow d / \in$$

This is left factored grammar.

6. Do left factoring in the following grammar-

$$S \rightarrow aAd / aB$$

$$A \rightarrow a / ab$$

$$B \rightarrow ccd / ddc$$

Answer-6. The grammar after eliminating left factoring is-

$$S \rightarrow aS'$$

$$S' \rightarrow Ad / B$$

$$A \rightarrow aA'$$

$$A' \rightarrow b / \in$$

$$B \rightarrow ccd / ddc$$

This is left factored grammar.

3. QUESTION And ANSWER ON-*Find FIRST()* *And FOLLOW()*

1. Calculate the first and follow functions for the given grammar-

$S \rightarrow aBDh$

$B \rightarrow cC$

$C \rightarrow bC / \in$

$D \rightarrow EF$

$E \rightarrow g / \in$

$F \rightarrow f / \in$

Answer-1. The first and follow functions are as follows-

First Functions-

- $\text{First}(S) = \{ a \}$
- $\text{First}(B) = \{ c \}$
- $\text{First}(C) = \{ b, \in \}$
- $\text{First}(D) = \{ \text{First}(E) - \in \} \cup \text{First}(F) = \{ g, f, \in \}$
- $\text{First}(E) = \{ g, \in \}$
- $\text{First}(F) = \{ f, \in \}$

Follow Functions-

- $\text{Follow}(S) = \{ \$ \}$
- $\text{Follow}(B) = \{ \text{First}(D) - \in \} \cup \text{First}(h) = \{ g, f, h \}$
- $\text{Follow}(C) = \text{Follow}(B) = \{ g, f, h \}$
- $\text{Follow}(D) = \text{First}(h) = \{ h \}$
- $\text{Follow}(E) = \{ \text{First}(F) - \in \} \cup \text{Follow}(D) = \{ f, h \}$
- $\text{Follow}(F) = \text{Follow}(D) = \{ h \}$

<u>Grammar/Production</u>	<u>FIRST()</u>	<u>FOLLOW()</u>
$S \rightarrow aBDh$	$\{ a \}$	$\{ \$ \}$
$B \rightarrow cC$	$\{ c \}$	$\{ g, f, h \}$

$C \rightarrow bC / \epsilon$	$\{b, \epsilon\}$	$\{g, f, h\}$
$D \rightarrow EF$	$\{g, f, \epsilon\}$	$\{h\}$
$E \rightarrow g / \epsilon$	$\{g, \epsilon\}$	$\{f, h\}$
$F \rightarrow f / \epsilon$	$\{f, \epsilon\}$	$\{h\}$

2. Calculate the first and follow functions for the given grammar-

$$S \rightarrow A$$

$$A \rightarrow aB / Ad$$

$$B \rightarrow b$$

$$C \rightarrow g$$

Answer-2. The first and follow functions are as follows-

We have-

- The given grammar is left recursive.
- So, we first remove left recursion from the given grammar.

After eliminating left recursion, we get the following grammar-

$$S \rightarrow A$$

$$A \rightarrow aBA'$$

$$A' \rightarrow dA' / \epsilon$$

$$B \rightarrow b$$

$$C \rightarrow g$$

Now, the first and follow functions are as follows-

First Functions-

- $\text{First}(S) = \text{First}(A) = \{ a \}$
- $\text{First}(A) = \{ a \}$
- $\text{First}(A') = \{ d, \epsilon \}$
- $\text{First}(B) = \{ b \}$
- $\text{First}(C) = \{ g \}$

Follow Functions-

- $\text{Follow}(S) = \{ \$ \}$
- $\text{Follow}(A) = \text{Follow}(S) = \{ \$ \}$
- $\text{Follow}(A') = \text{Follow}(A) = \{ \$ \}$
- $\text{Follow}(B) = \{ \text{First}(A') - \epsilon \} \cup \text{Follow}(A) = \{ d, \$ \}$
- $\text{Follow}(C) = \text{NA}$

<u>Grammar/Production</u>	<u>FIRST()</u>	<u>FOLLOW()</u>
$S \rightarrow A$	$\{a\}$	$\{ \$ \}$
$A \rightarrow aBA'$	$\{a\}$	$\{ \$ \}$
$A' \rightarrow dA' / \epsilon$	$\{d, \epsilon\}$	$\{ \$ \}$
$B \rightarrow b$	$\{b\}$	$\{d, \$ \}$
$C \rightarrow g$	$\{g\}$	NA

3. Calculate the first and follow functions for the given grammar-

$$S \rightarrow (L) / a$$

$$L \rightarrow SL'$$

$$L' \rightarrow ,SL' / \in$$

Answer-3. The first and follow functions are as follows-

First Functions-

- $\text{First}(S) = \{ (, a \}$
- $\text{First}(L) = \text{First}(S) = \{ (, a \}$
- $\text{First}(L') = \{ , , \in \}$

Follow Functions-

- $\text{Follow}(S) = \{ \$ \} \cup \{ \text{First}(L') - \in \} \cup \text{Follow}(L) \cup \text{Follow}(L') = \{ \$, , ,) \}$
- $\text{Follow}(L) = \{) \}$
- $\text{Follow}(L') = \text{Follow}(L) = \{) \}$

<u>Grammar/Production</u>	<u>FIRST()</u>	<u>FOLLOW()</u>
$S \rightarrow (L) / a$	$\{(, a\}$	$\{\$, , , \in\}$
$L \rightarrow SL'$	$\{(, a\}$	$\{)\}$
$L' \rightarrow ,SL' / \in$	$\{, , \in\}$	$\{)\}$

4. Calculate the first and follow functions for the given grammar-

$$S \rightarrow AaAb / BbBa$$

$$A \rightarrow \in$$

$$B \rightarrow \in$$

Answer-4. The first and follow functions are as follows-

First Functions-

- $\text{First}(S) = \{ \text{First}(A) - \epsilon \} \cup \text{First}(a) \cup \{ \text{First}(B) - \epsilon \} \cup \text{First}(b) = \{ a, b \}$
- $\text{First}(A) = \{ \epsilon \}$
- $\text{First}(B) = \{ \epsilon \}$

Follow Functions-

- $\text{Follow}(S) = \{ \$ \}$
- $\text{Follow}(A) = \text{First}(a) \cup \text{First}(b) = \{ a, b \}$
- $\text{Follow}(B) = \text{First}(b) \cup \text{First}(a) = \{ a, b \}$

<u>Grammar/Production</u>	<u>FIRST()</u>	<u>FOLLOW()</u>
$S \rightarrow AaAb / BbBa$	$\{a,b\}$	$\{\$ \}$
$A \rightarrow \epsilon$	$\{\epsilon\}$	$\{a,b\}$
$B \rightarrow \epsilon$	$\{\epsilon\}$	$\{a,b\}$

5. Calculate the first and follow functions for the given grammar-

$$E \rightarrow E + T / T$$

$$T \rightarrow T \times F / F$$

$$F \rightarrow (E) / \text{id}$$

Answer-5. The first and follow functions are as follows-

We have-

- The given grammar is left recursive.
- So, we first remove left recursion from the given grammar.

After eliminating left recursion, we get the following grammar-

$$E \rightarrow TE'$$

$$E' \rightarrow + TE' / \in$$

$$T \rightarrow FT'$$

$$T' \rightarrow x FT' / \in$$

$$F \rightarrow (E) / id$$

Now, the first and follow functions are as follows-

First Functions-

- $\text{First}(E) = \text{First}(T) = \text{First}(F) = \{ (, id \}$
- $\text{First}(E') = \{ +, \in \}$
- $\text{First}(T) = \text{First}(F) = \{ (, id \}$
- $\text{First}(T') = \{ x, \in \}$
- $\text{First}(F) = \{ (, id \}$

Follow Functions-

- $\text{Follow}(E) = \{ \$,) \}$
- $\text{Follow}(E') = \text{Follow}(E) = \{ \$,) \}$
- $\text{Follow}(T) = \{ \text{First}(E') - \in \} \cup \text{Follow}(E) \cup \text{Follow}(E') = \{ +, \$,) \}$
- $\text{Follow}(T') = \text{Follow}(T) = \{ +, \$,) \}$
- $\text{Follow}(F) = \{ \text{First}(T') - \in \} \cup \text{Follow}(T) \cup \text{Follow}(T') = \{ x, +, \$,) \}$

<u>Grammar/Production</u>	<u>FIRST()</u>	<u>FOLLOW()</u>
$E \rightarrow TE'$	{(,id}	{\$,)}
$E' \rightarrow + TE' / \in$	{+, \in }	{\$,)}
$T \rightarrow FT'$	{(,id}	{+,\$,)}
$T' \rightarrow x FT' / \in$	{x, \in }	{+,\$,)}
$F \rightarrow (E) / id$	{(,id}	{x,+, \$,)}

6. Calculate the first and follow functions for the given grammar-

$$S \rightarrow ACB / CbB / Ba$$

$$A \rightarrow da / BC$$

$$B \rightarrow g / \in$$

$$C \rightarrow h / \in$$

Answer-6. The first and follow functions are as follows-

First Functions-

- $\text{First}(S) = \{ \text{First}(A) - \in \} \cup \{ \text{First}(C) - \in \} \cup \text{First}(B) \cup \text{First}(b) \cup \{ \text{First}(B) - \in \} \cup \text{First}(a) = \{ d, g, h, \in, b, a \}$
- $\text{First}(A) = \text{First}(d) \cup \{ \text{First}(B) - \in \} \cup \text{First}(C) = \{ d, g, h, \in \}$
- $\text{First}(B) = \{ g, \in \}$
- $\text{First}(C) = \{ h, \in \}$

Follow Functions-

- $\text{Follow}(S) = \{ \$ \}$
- $\text{Follow}(A) = \{ \text{First}(C) - \in \} \cup \{ \text{First}(B) - \in \} \cup \text{Follow}(S) = \{ h, g, \$ \}$
- $\text{Follow}(B) = \text{Follow}(S) \cup \text{First}(a) \cup \{ \text{First}(C) - \in \} \cup \text{Follow}(A) = \{ \$, a, h, g \}$

-
- $\text{Follow}(C) = \{ \text{First}(B) - \epsilon \} \cup \text{Follow}(S) \cup \text{First}(b) \cup \text{Follow}(A) = \{ g, \$, b, h \}$

<u>Grammar/Production</u>	<u>FIRST()</u>	<u>FOLLOW()</u>
$S \rightarrow ACB / CbB / Ba$	$\{a,b,d,g,h,\epsilon\}$	$\{\$\}$
$A \rightarrow da / BC$	$\{d,g,h,\epsilon\}$	$\{h,g,\$\}$
$B \rightarrow g / \epsilon$	$\{g,\epsilon\}$	$\{\$,h,g,a\}$
$C \rightarrow h / \epsilon$	$\{h,\epsilon\}$	$\{b,g,\$,h\}$
