

# Operator Precedence Parser

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\* Two Restriction for Grammar

① no null production ( $\epsilon$ ).

eg  $\rightarrow A \rightarrow \epsilon$

② no two adjacent non-terminal in its RHS of production.

eg  $\rightarrow A \rightarrow ACB$

\* If any grammar/production is not in operator precedence grammar then convert into operator grammar.

Question - Check a grammar/production are in operator precedence Grammar or not.

①  $T \rightarrow T * T / T + T / id$

so, there is no  $\epsilon$  production and no two adjacent non-terminal in RHS of production

②  $S \rightarrow SAS / a$

$A \rightarrow bSb / a$

In  $S \rightarrow SAS$  is not a operator grammar  
so, convert it. operator grammar

①

$$S \rightarrow S b S b S / a / S a S$$

Now,  $A \rightarrow b S b / a$

All grammar are if follow the operator precedence grammar rules.

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Now, for parse a string we need a parsing construction Table.

So, we construct a parsing table.

Here, Build a Relation Table for OPP.

There are some rules follow  
check precedence but if same then left associativity.

①  $O_1 > O_2$  ; then  $O_1 \succ O_2$

②  $O_1 < O_2$  ; then  $O_1 \prec O_2$

③  $O_1 = O_1$  ; then  $O_1 \succ O_1$

$O_2 = O_2$  ; then  $O_2 \succ O_2$

$O_1 = O_2$  ; then  $O_1 \succ O_2$

(Left Associativity).

\*  $O_1, O_2$  are mathematical operator as it can be a terminal. And

②

\* For checking the string (w) is accepted or not.

There are two operations perform.

- ① If  $[stack < \cdot \text{Input Buffer}]$  then push(item) into stack and increase pointer.
- ② If  $[stack > \text{Input Buffer}]$  then pop(item) from stack.

L \ R	id	+	*	\$
id	—	$\cdot >$	$\cdot >$	$\cdot >$
+	$< \cdot$	$\cdot >$	$< \cdot$	$\cdot >$
*	$< \cdot$	$\cdot >$	$\cdot >$	$\cdot >$
\$	$< \cdot$	$< \cdot$	$< \cdot$	Accept

operator Relation Table for OP parser.

In, Table all terminals are in row and col ; And \$ is also append.

Question  $\rightarrow$  Construction parsing table of relation given grammar and check string  $w = (id + id * id)$  is accepted or not

$$T \rightarrow T * T / T + T / id.$$

The relation table is given above.

Now, check  $w = id + id * id$

\* append \$ input buffer and \$ is initially add in stack



id + id \* id \$  
~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~

Input Buffer

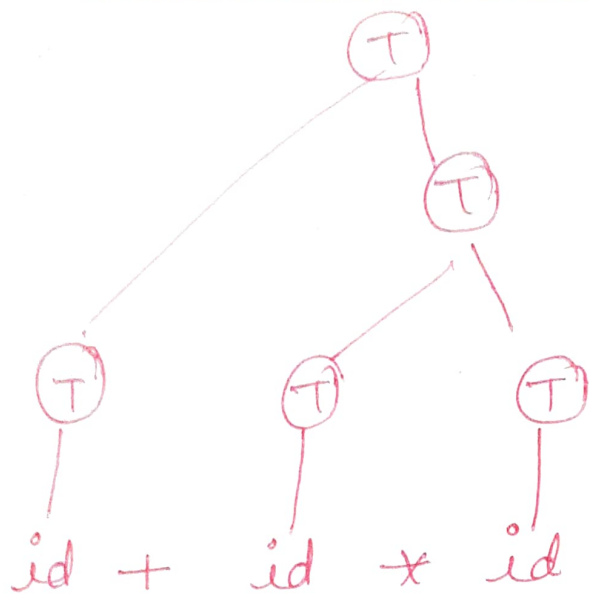
\$ id + id \* id

Stack

Operations by using O/P relation table.

- ①  $\$ \prec id$  push
- ②  $id \succ +$  pop ( $T \rightarrow id$ )
- ③  $\$ \prec +$  push
- ④  $+ \prec id$  push
- ⑤  $id \succ *$  pop ( $T \rightarrow id$ )
- ⑥  $+ \prec *$  push
- ⑦ ~~id~~  $* \prec id$  push
- ⑧  $id \succ \$$  pop ( $T \rightarrow id$ )
- ⑨  $* \succ \$$  pop ( $T \rightarrow T * T$ )
- ⑩  $+ \succ \$$  pop ( $T \rightarrow T + T$ )
- ⑪  $\$ - \$$  Accepted

Now, make parse tree.



Parse Tree

Now, Relation table size is  $4 \times 4 = 16$ .  
 if there is  $n$  terminal, then size  
 is  $(n \times n) = (n)^2$ . Complexity is  
 $O(n^2)$ .

SO, we need to reduce the size of table  
 The concept come of function

~~XX~~ we apply  
 on above  
 question

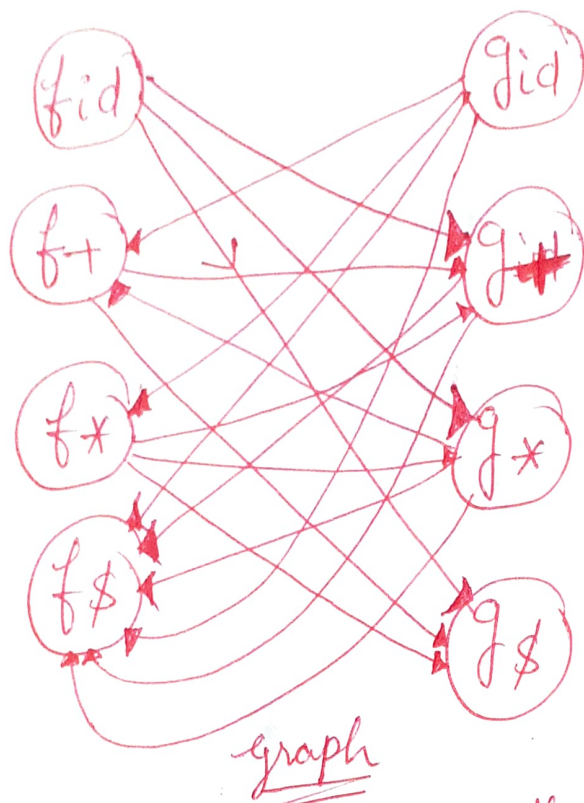
		g			
f		id	+	*	\$
	id	<del>id</del>	?	?	?
	+	?	?	?	?
	*	?	?	<del>*</del>	?
	\$	?	?	?	-

$(2 \times n)$  size  
 $O(2n)$  complexity,

Make a graph using relation table.

f Domain

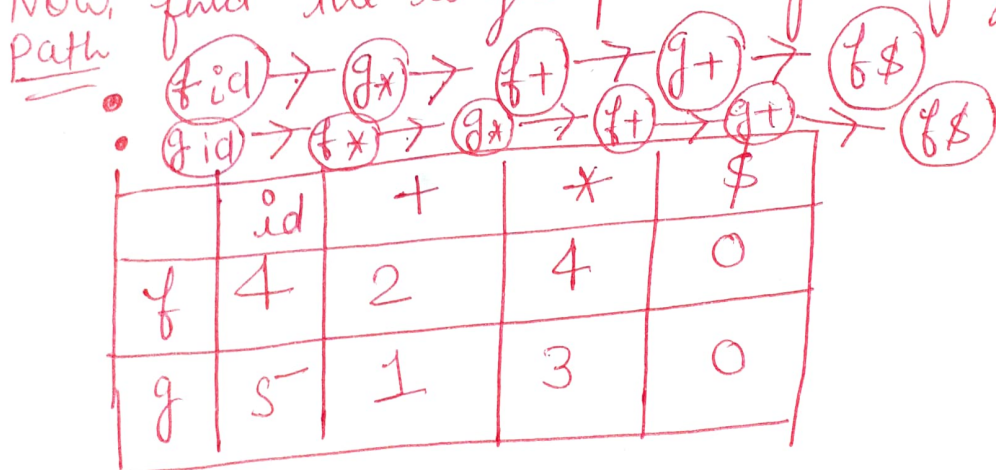
g Domain



Insure no cycle form

OP Relation Graph

Now, find the longest path by using graph



O.P. Function relation table

$w = id + id * id$  is accepted by function table or not.

So, Grammar is already above solved.

Operations by using OP relation function table.



input Buffer  
 $id \quad + \quad id \quad * \quad id \quad \$$   
 $\uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$

Stack  
 $\$ \quad id \quad + \quad id \quad * \quad id$

①  $\$ \quad id$  push

$tf \leftarrow gid$   
 $0 \quad 5$

②  $id \quad +$  ~~pop~~  
 $tf \rightarrow gt$  pop  
 $4 \quad 1$   $(T \rightarrow id)$

③  $\$ \leftarrow +$  push  
 $tf \leftarrow gt$   
 $0 \quad 1$

④  $+ \leftarrow id$  push  
 $tf \leftarrow gid$   
 $2 \quad 5$

⑤ ~~id  $\rightarrow +$  pop~~  
 $id \rightarrow +$  pop  
 $tf \leftarrow gt$   $(T \rightarrow id)$   
 $4 \quad 3$

⑥  $+ \leftarrow *$  push  
 $tf \leftarrow gt$   
 $2 \quad 3$

⑦  $* \leftarrow id$  push  
 $tf \leftarrow gid$   
 $4 \quad 5$

⑧  $id \rightarrow \$$  pop  
 $tf \leftarrow gt$   $(T \rightarrow id)$   
 $4 \quad 0$

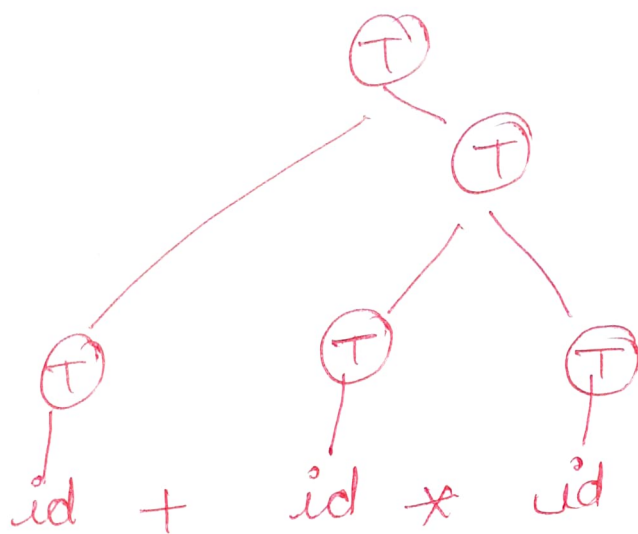
⑨  $* \rightarrow \$$  pop  
 $tf \leftarrow gt$   $(T \rightarrow T * T)$   
 $4 \quad 0$

⑩



10.  $+$   $\rightarrow$   $\$$  pop  
 $\downarrow +$   $\downarrow \$$   $(T \rightarrow T+T)$   
 2 0

(11)  $\$$   $\$$   
 $\downarrow \$$   $\downarrow \$$  Accepted  
 0 0



parse tree

The end

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