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MS. SHWETA TIWARI
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CD: COMPILER DESIGN

INSTRUCTOR: Ms. SHWETA TIWARI shwetatiwari08@recabn.ac.in shwetatiwari08aug@gmail.com



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TOPIC On: UNIT-2 OPERATOR PRECEDENCE PARSER

By SHWETA TIWARI

Under On: Basic Parsing Techniques

OPERATOR PRECEDENCE PARSER

Operator Precedence Grammar-

A grammar that satisfies the following 2 conditions is called as **Operator Precedence Grammar**—

- There exists no production rule which contains ε on its RHS.
- There exists no production rule which contains two non-terminals adjacent to each other on its RHS.
- It represents a small class of grammar.
- But it is an important class because of its widespread applications.

Examples-

$$E \rightarrow EAE \mid (E) \mid -E \mid id$$

$$A \rightarrow + \mid - \mid x \mid / \mid ^{\wedge}$$

Operator Precedence Grammar



 $\mathsf{E} \to \mathsf{E} + \mathsf{E} \mid \mathsf{E} - \mathsf{E} \mid \mathsf{E} \times \mathsf{E} \mid \mathsf{E} / \mathsf{E} \mid \mathsf{E} \wedge \mathsf{E} \mid (\mathsf{E}) \mid -\mathsf{E} \mid \mathsf{id}$

Operator Precedence Grammar



Operator Precedence Parser-

A parser that reads and understand an operator precedence grammar

is called an Operator Precedence Parser.

Designing Operator Precedence Parser-

In operator precedence parsing,

- Firstly, we define precedence relations between every pair of terminal symbols.
- Secondly, we construct an operator precedence table.

Defining Precedence Relations-

The precedence relations are defined using the following rules-

Rule-01:

- If precedence of b is higher than precedence of a, then we define a < b
- If precedence of b is same as precedence of a, then we define a = b
- If precedence of b is lower than precedence of a, then we define a > b

Rule-02:

- An identifier is always given the higher precedence than any other symbol.
- \$ symbol is always given the lowest precedence.

Rule-03:

• If two operators have the same precedence, then we go by checking their associativity.

Parsing A Given String-

The given input string is parsed using the following steps-

Step-01:

Insert the following-

- \$ symbol at the beginning and ending of the input string.
- Precedence operator between every two symbols of the string by referring to the operator precedence table.

Step-02:

- Start scanning the string from LHS in the forward direction until > symbol is encountered.
- Keep a pointer on that location.

Step-03:

- Start scanning the string from RHS in the backward direction until < symbol is encountered.
- Keep a pointer on that location.

Step-04:

- Everything that lies in the middle of < and > forms the handle.
- Replace the handle with the head of the respective production.

Step-05:

Keep repeating the cycle from Step-02 to Step-04 until the start symbol is reached.

Advantages-

The advantages of operator precedence parsing are-

- The implementation is very easy and simple.
- The parser is quite powerful for expressions in programming languages.

Disadvantages-

The disadvantages of operator precedence parsing are-

- The handling of tokens known to have two different precedence becomes difficult.
- Only small class of grammars can be parsed using this parser.

Important Note-

- In practice, operator precedence table is not stored by the operator precedence parsers.
- This is because it occupies the large space.
- Instead, operator precedence parsers are implemented in a very unique style.
- They are implemented using operator precedence functions.

Operator Precedence Functions-

Precedence functions perform the mapping of terminal symbols to the integers.

- To decide the precedence relation between symbols, a numerical comparison is performed.
- It reduces the space complexity to a large extent.

PRACTICE PROBLEMS BASED ON OPERATOR PRECEDENCE PARSING-

Problem-01:

Consider the following grammar-

$$E \rightarrow EAE \mid id$$

$$A \rightarrow + \mid x$$

Construct the operator precedence parser and parse the string $id + id \times id$.

Solution-

Step-01:

We convert the given grammar into operator precedence grammar.

The equivalent operator precedence grammar is-

$$E \rightarrow E + E \mid E \times E \mid id$$

Step-02:

The terminal symbols in the grammar are $\{id, +, x, \$\}$

We construct the operator precedence table as-

	id	+	×	\$
id		>	>	>
+	<	>	<	>
×	<	>	>	>
\$	<	<	<	

Operator Precedence Table

Parsing Given String-

Given string to be parsed is $id + id \times id$.

We follow the following steps to parse the given string-

Step-01:

We insert \$ symbol at both ends of the string as-

$$$ id + id x id $$$

We insert precedence operators between the string symbols as-

$$4 < id > + < id > x < id >$$

Step-02:

We scan and parse the string as-

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = \frac{1}{2} + \frac{1}{2} = \frac{1}{2} + \frac{1}{2} = \frac{1}$$

$$E + < id > x < id >$$

$$E + E \times < id >$$

$$E + E \times E$$

$$+ x$$
\$

\$\$

Problem-02:

Consider the following grammar-

$$S \rightarrow (L) \mid a$$

$$L \rightarrow L$$
, $S \mid S$

Construct the operator precedence parser and parse the string (a , (a , a)).

Solution-

The terminal symbols in the grammar are $\{\ (\ ,\)\ ,a\ ,\ ,\ \}$

We construct the operator precedence table as-

	a	()	,	\$
a		>	>	>	>
(<	>	>	>	>
)	<	>	>	>	>
,	<	<	>	>	>
\$	<	<	<	<	

Operator Precedence Table

Parsing Given String-

Given string to be parsed is (a, (a, a)).

We follow the following steps to parse the given string-

Step-01:

We insert \$ symbol at both ends of the string as-

We insert precedence operators between the string symbols as-

Step-02:

We scan and parse the string as-

$$\$ < (< a >, < (< a >, < a >) >) > \$$$

$$\$ < (S, < (S, \underline{< a >}) >) > \$$$

$$\$ < (S, < (L, S) >) > \$$$

$$\$ < (S, \underline{< (L) >}) > \$$$

$$\$ \leq (S,S) > \$$$

$$\frac{(L,S)}{}$$

$$\frac{(L)}{}$$

$$\frac{S}{S}$$

\$\$

Problem-03:

Consider the following grammar-

$$E \rightarrow E + E \mid E \times E \mid id$$

- 1. Construct Operator Precedence Parser.
- 2. Find the Operator Precedence Functions.

Solution-

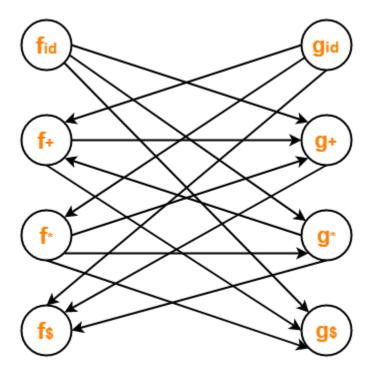
The terminal symbols in the grammar are $\{+, x, id, \$\}$

We construct the operator precedence table as-

g →					
		id	+	x	\$
	id		>	>	>
f↓	+	<	>	<	>
	х	<	>	>	>
	\$	<	<	<	

Operator Precedence Table

The graph representing the precedence functions is-



Graph Representing Precedence Functions

Here, the longest paths are-

$$\bullet \qquad f_{id} \to g_x \to f_+ \to g_+ \to f_g$$

$$\begin{array}{ll} \bullet & & f_{id} \! \to g_x \! \to f_+ \! \to g_+ \! \to f_\$ \\ \bullet & & g_{id} \! \to f_x \! \to g_x \! \to f_+ \! \to g_+ \! \to f_\$ \end{array}$$

The resulting precedence functions are-

	+	x	id	\$
f	2	4	4	0
g	1	3	5	0

To gain better understanding about Operator Precedence Parsing,