## Υπολογισμός βασικών ολοκληρωμάτων

$$\int_{a}^{\beta} c dx = [cx]_{a}^{\beta} = c(\beta - a)$$

$$\int_{a}^{\beta} x dx = \left[ \frac{x^{2}}{2} \right]_{a}^{\beta} = \frac{\beta^{2}}{2} - \frac{a^{2}}{2}$$

$$\int_{a}^{\beta} x^{\nu} dx = \left[ \frac{x^{\nu+1}}{\nu+1} \right]_{a}^{\beta} = \frac{\beta^{\nu+1}}{\nu+1} - \frac{a^{\nu+1}}{\nu+1}$$

$$\int_{a}^{\beta} \frac{1}{2\sqrt{x}} dx = \left[\sqrt{x}\right]_{a}^{\beta} = \sqrt{\beta} - \sqrt{a}$$

$$\int_{a}^{\beta} \sqrt[\nu]{x^{\nu}} dx = \left[ \frac{x^{\frac{\mu}{\nu} + 1}}{\frac{\mu}{\nu} + 1} \right]_{a}^{\beta} = \frac{\beta^{\frac{\mu}{\nu} + 1}}{\frac{\mu}{\nu} + 1} - \frac{a^{\frac{\mu}{\nu} + 1}}{\frac{\mu}{\nu} + 1}$$

$$\int_{a}^{\beta} \frac{1}{x^2} \mathrm{d}x = \left[ -\frac{1}{x} \right]_{a}^{\beta} = -\frac{1}{\beta} + \frac{1}{a}$$

$$\int_{a}^{\beta} \eta \mu x dx = [-\sigma v x]_{a}^{\beta} = -\sigma v \beta + \sigma v a$$

$$\int_{a}^{\beta} \operatorname{dv} x dx = [\eta \mu x]_{a}^{\beta} = \eta \mu \beta - \eta \mu a$$

$$\int_{a}^{\beta} \frac{1}{\operatorname{duv}^{2} x} \mathrm{d}x = \left[ \varepsilon \varphi x \right]_{a}^{\beta} = \varepsilon \varphi \beta - \varepsilon \varphi a$$

$$\int_{a}^{\beta} \frac{1}{\eta \mu^{2} x} dx = \left[ -\sigma \varphi x \right]_{a}^{\beta} = -\sigma \varphi \beta + \sigma \varphi a$$

$$\int_a^\beta e^x \mathrm{d}x = [e^x]_a^\beta = e^\beta - e^a$$

$$\int_{a}^{\beta} \mu^{x} dx = \left[ \frac{\mu^{x}}{\ln a} \right]_{a}^{\beta} = \frac{\mu^{\beta}}{\ln \mu} - \frac{\mu^{a}}{\ln \mu}$$

$$\int_{a}^{\beta} \frac{1}{x} dx = [\ln |x|]_{a}^{\beta} = \ln |\beta| - \ln |a|$$