

α. $\overrightarrow{AB} = (2 - 4, 5 - (-1)) = (-2, 6)$ και $\overrightarrow{AG} = (-3 - 4, 4 - (-1)) = (-7, 5)$. 'Αρα

$$\overrightarrow{AB} \cdot \overrightarrow{AG} = (-2, 6) \cdot (-7, 5) = (-2) \cdot (-7) + 6 \cdot 5 = 14 + 30 = 44$$

β. $\overrightarrow{BG} = (-3 - 2, 4 - 5) = (-5, -1)$ οπότε

$$\overrightarrow{AG} \cdot \overrightarrow{BG} = (-7, 5) \cdot (-5, -1) = (-7) \cdot (-5) + 5 \cdot (-1) = 35 - 5 = 30$$

Το M είναι μέσο του BG οπότε

$$x_M = \frac{x_B + x_G}{2} = \frac{2 - 3}{2} = -\frac{1}{2}$$

και

$$y_M = \frac{y_B + y_G}{2} = \frac{5 + 4}{2} = \frac{9}{2}$$

οπότε $M \left(-\frac{1}{2}, \frac{9}{2} \right)$.