

STATISTICAL LEARNING & ASSOCIATION RULES MINING

ADVANCED DATA SCIENCE TRAINING I

“Data science does not replace statistical modeling and data analysis; it augments them.”

(P. Boily)

“Data is not information, information is not knowledge,
knowledge is not understanding, understanding is not wisdom.”

(attributed to Cliff Stoll in Keeler's *Nothing to Hide: Privacy in the 21st Century*, 2006)

LEARNING OBJECTIVES

Become familiar with the various statistical learning approaches (supervised, unsupervised, and so forth).

Become familiar with the fundamental concepts of association rules, and their application to data.

STATISTICAL LEARNING

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

“We learn from failure, not from success!”

(Bram Stoker, *Dracula*)

WHAT IS DATA SCIENCE? (REPRISE)

Data Science (DS) is the collection of processes by which we extract useful and **actionable insights** from data.

(paraphrased from T. Kwartler)

DS is the **working intersection** of statistics, engineering, computer science, domain expertise, and “hacking.” It involves two main thrusts: **analytics** (counting things) and **inventing new techniques** to draw insights from data.

(paraphrased from H. Mason)

THE MINING ANALOGY

What are we mining? data (**earth**)

What are we using to mine? data mining techniques (**digging tools**)

What are we mining for? looking for patterns/knowledge (**raw minerals**)

What do we do with the raw material? describe patterns/relationships (**refine minerals into something useful**)

What is the output, or product? models (**Ge, Ga, Si to build transistors**)

What do we do with the product? apply models to evidence-based decision support (**use transistor in electrical systems**)

LEARNING IN GENERAL

Beyond “just taking a quick look,” humans learn through:

- answering questions
- testing hypotheses
- creating concepts
- making predictions
- creating categories and classifying objects
- grouping objects

The central Data Science/Machine Learning problem is:

can we design algorithms that can learn?

TYPES OF LEARNING

Supervised Learning (learning with a teacher)

- classification, regression, rankings, recommendations
- uses **labeled training data** (student gives an answer to each test question based on what they learned from worked-out examples)
- performance is evaluated using **testing data** (teacher provides the correct answers)

Unsupervised Learning (grouping similar exercises together as a study aid)

- clustering, association rules discovery, link profiling, anomaly detection
- uses **unlabeled** observations (**teacher is not involved**)
- accuracy **cannot** be evaluated (**students might not end up with the same groupings**)

TYPES OF LEARNING

Semi-Supervised Learning (teacher providing worked-out examples **and** a list of unsolved problems)

Reinforcement Learning (embarking on a Ph.D. with an advisor)

In **supervised learning**, there's a target against which to train the model. In **unsupervised learning**, we don't know what the target is, or even if there is one.

The distinction is **crucial**. Make sure you understand it.

EXERCISES

What are some examples of supervised and unsupervised learning tasks in the business world? In a public policy/government setting?

EXERCISES

Assuming that data mining techniques are used in the following cases, identify whether the required task falls under **supervised (S)** or **unsupervised (U)** learning.

- Deciding whether to issue a loan to an applicant based on demographic and financial data (with reference to a database of similar data on prior customers)
- In an online bookstore, making recommendations to customers concerning additional items to buy based on the buying pattern in prior transactions.
- Identifying a network data packet as dangerous (virus, hacker attack) based on comparison to other packets with a known threat status.
- Identifying segments of similar customers.
- Predicting whether a company will go bankrupt based on comparing its financial data to those of similar bankrupt and non-bankrupt firms.

EXERCISES

Assuming that data mining techniques are used in the following cases, identify whether the required task falls under **supervised (S)** or **unsupervised (U)** learning.

- Estimating the repair time required for an aircraft based on a trouble ticket.
- Automated sorting of mail by zip code scanning.
- It is more difficult and expensive to win new customers than it is to retain existing customers. Scoring each customer on their likelihood to quit can help an organization design effective interventions, such as discounts or free services, to retain profitable customers in a cost-effective manner.
- Some medical practitioners conduct unnecessary tests and/or overbill their government or insurance companies. Using audit data, it may be possible to identify such providers and take appropriate action.

EXERCISES

Assuming that data mining techniques are used in the following cases, identify whether the required task falls under **supervised (S)** or **unsupervised (U)** learning.

- A market basket analysis can help develop predictive models to determine which products often sell together. This knowledge of affinities between products can help retailers create promotional bundles to push non-selling items along a set of products that sell well.
- Diagnosing the cause of a medical condition is the crucial first step in medical engagement. In addition to the current condition, other factors can be considered, including the patient's health history, medication history, family's history, and other environmental factors. A predictive model can absorb all of the information available to date (for this patient and others) and make probabilistic diagnoses, in the form of a decision tree, taking away most of the guess work involved.

EXERCISES

Assuming that data mining techniques are used in the following cases, identify whether the required task falls under **supervised (S)** or **unsupervised (U)** learning.

- Schools can develop models to identify students who are at risk of not returning to school. Such students can be flagged to be on the receiving end of potential corrective measures.
- In addition to customer data, telecom companies also store call detail records (CDR), which precisely describe the calling behaviour of each customer. The unique data can be used to profile customers, who may be marketed to based on the similarity of their CDR to other customers'.
- Statistically, all equipment is likely to break down at some point in time. Predicting which machine is likely to shut down is a complex process. Decision models to forecast machinery failure could be constructed using past data, which can lead to savings provided by preventative maintenance.

CASE STUDY: DANISH MEDICAL STUDY

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

Temporal disease trajectories condensed from population-wide registry data covering 6.2 million patients

(Jensen, A.B., Moseley, P.L., Oprea, T.I., Ellesøe, S.G., Eriksson, R., Schmock, H.,
Jensen, P.B., Jensen, L.J., Brunak, S. [2014], *Nature Communications*).

CONTEXT

The *Danish National Patient Registry* contains **68 million** health observations on **6.2 million** patients over a 15 year time span (Jan '96 – Nov '10).

Objectives:

- finding connections between different diagnoses
- determining how a diagnosis at some point in time might allow for the prediction of another diagnosis at a later point in time

METHODOLOGY

1. Compute **strength of correlation** for pairs of diagnoses over a 5 year interval on a representative subset of the data
2. Test diagnoses pairs for **directionality** (one diagnosis repeatedly occurring before the other)
3. Determine reasonable diagnosis trajectories (**thoroughfares**) by combining smaller frequent trajectories with overlapping diagnoses
4. Validate the trajectories by comparison with **non-Danish** data
5. Cluster the thoroughfares to identify central medical conditions (**key diagnoses**) around which disease progression is organized

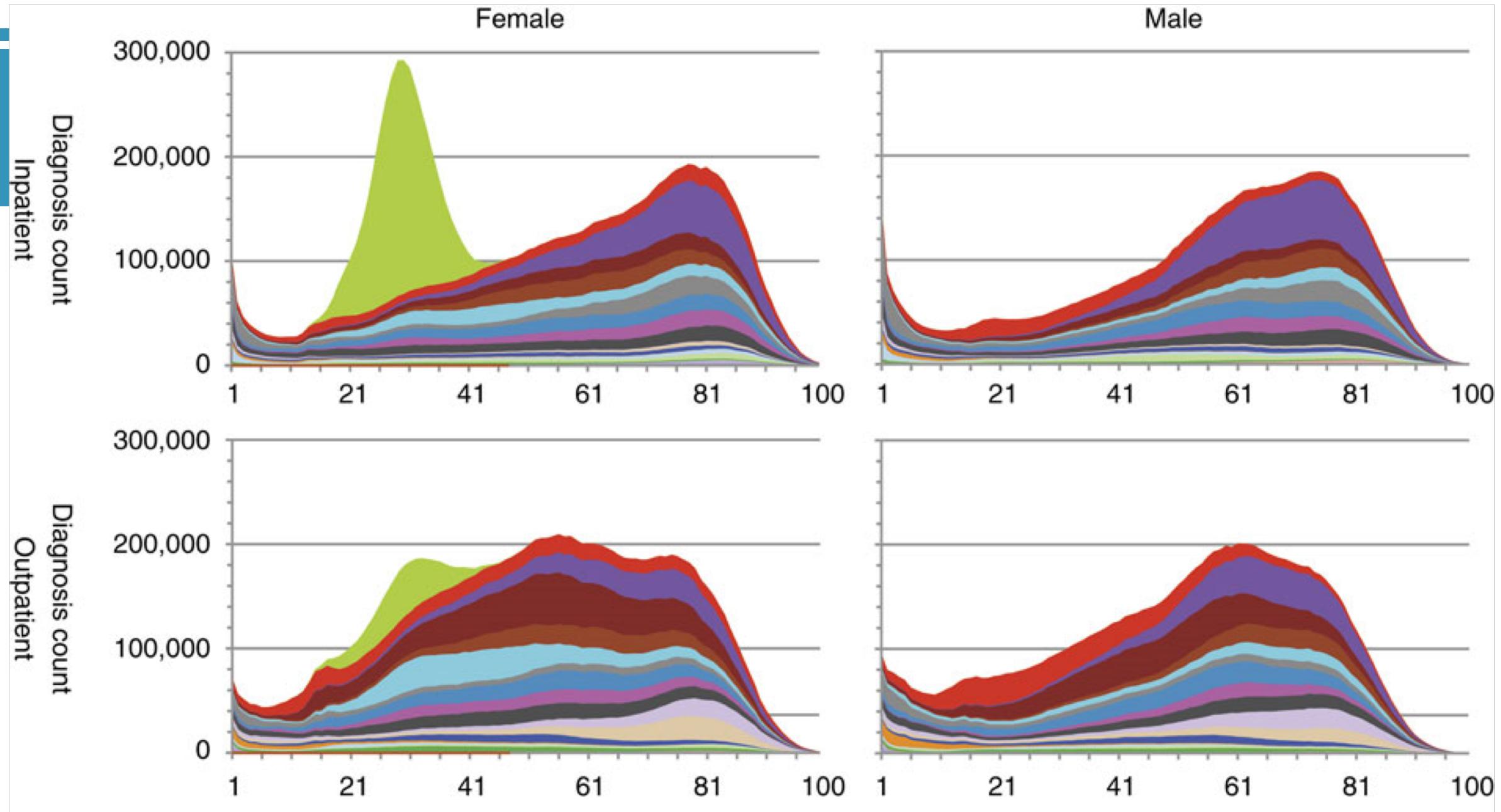
RESULTS

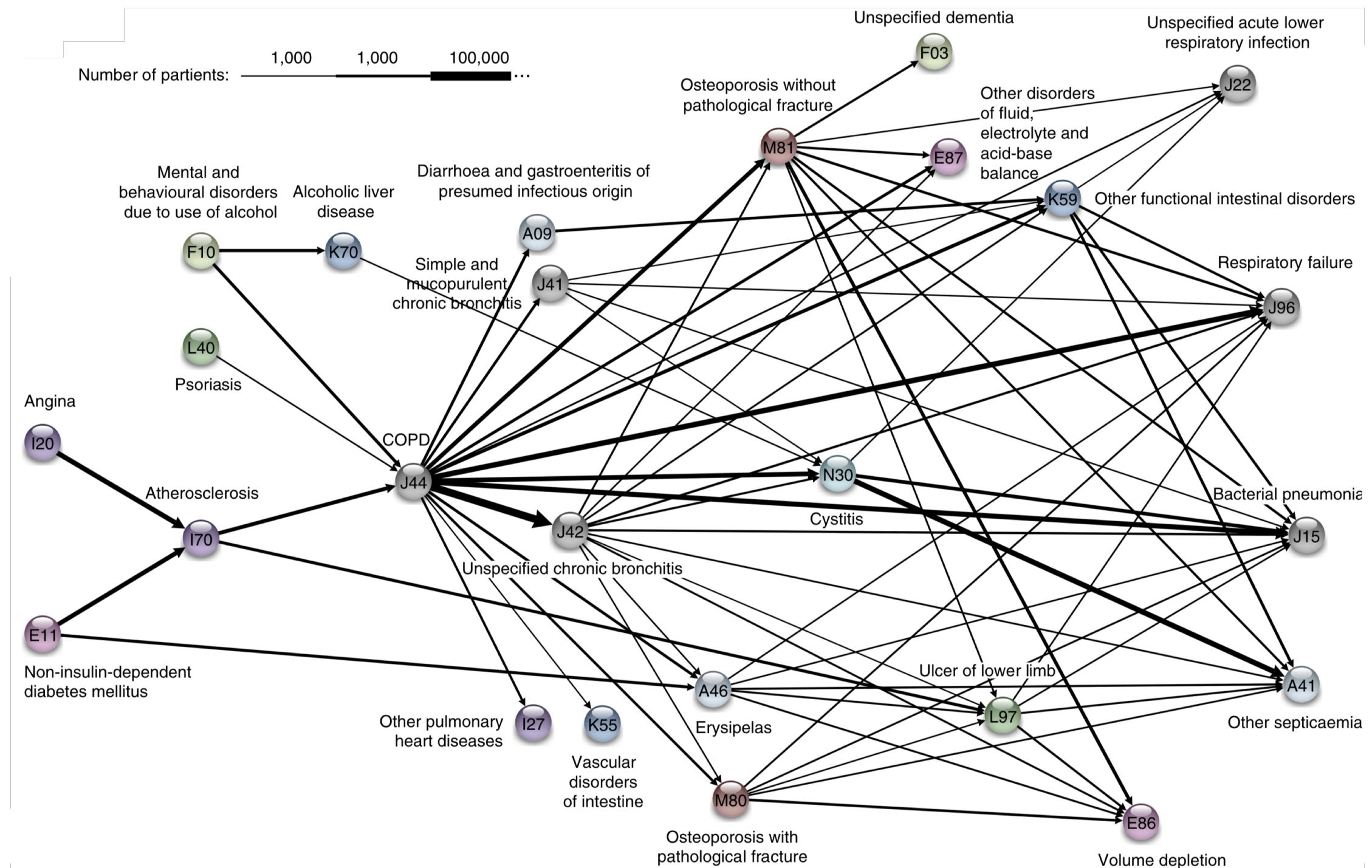
Data was reduced to 1,171 thoroughfares on the course of

- diabetes
- chronic obstructive pulmonary disease (COPD)
- cancer
- arthritis
- cardiovascular disease.

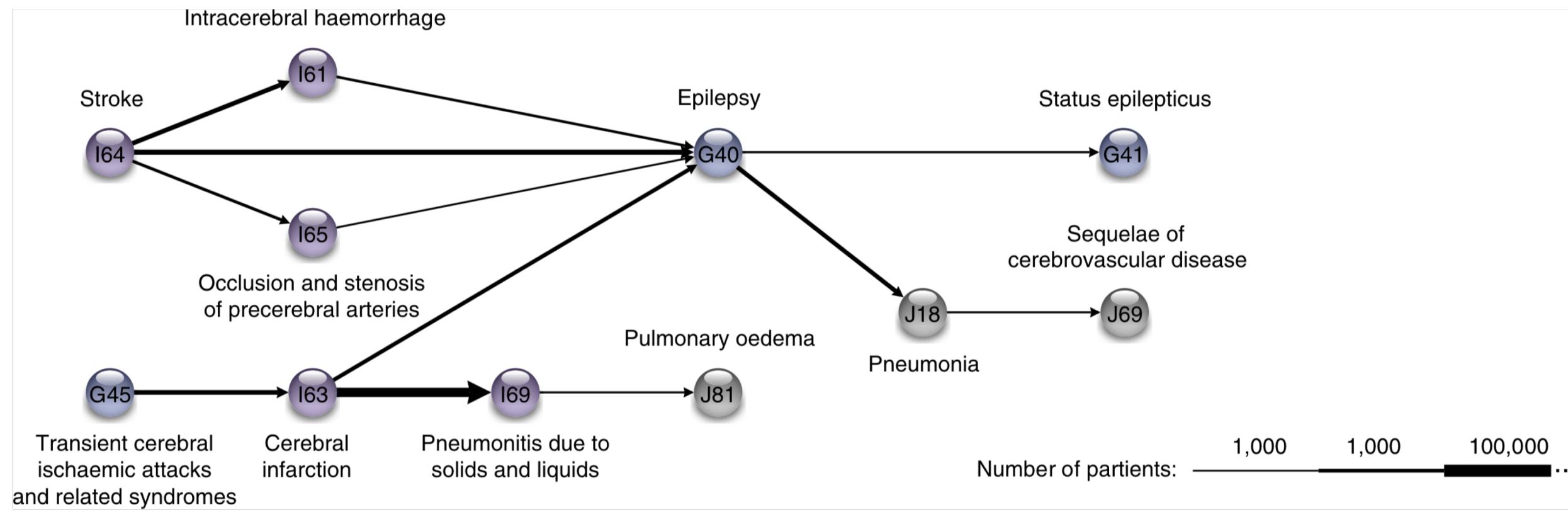
The data analysis showed, for example:

- diagnoses of anemia followed later by the discovery of colon cancer
- gout was identified as a step toward cardiovascular disease.
- COPD is **under-diagnosed** and **under-treated**.





RESULTS



TAKE-AWAYS

Data makes it possible to **view diseases in a larger context**.

The research could yield **tangible health benefits** as we move beyond one-size-fits-all medicine.

The sooner a health risk pattern is identified, the better we can **prevent and treat critical diseases**.

Instead of looking at each disease in isolation, you can talk about a complex system with many different interacting factors.

The order in which different diseases appear can help find **patterns and complex correlations** outlining the direction for each individual person.

DISCUSSION

Is this research applicable to the Canadian context? To the Chinese context?

What do you think some of the technical challenges were?

ASSOCIATION RULES BASICS

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

“Correlation isn’t causation. But it’s a big hint.”

(E. Tufte)

ASSOCIATION RULES BASICS

Association Rule Discovery is a type of unsupervised learning that finds connections among attributes (and combinations of attributes).

Example: we might analyze a dataset on the physical activities and purchasing habits of North Americans and discover that

- *runners who are also triathletes* (the **premise**) tend to *drive Subarus, drink microbrews, and use smartphones* (the **conclusion**), or
- individuals who have purchased home gym equipment are unlikely to be using it 1 year later (to name some fictitious possibilities)

ORIGINAL APPLICATION

Supermarkets record the contents of shopping carts at check-outs to determine items which are frequently purchased together.

Examples:

- bread and milk are often purchased together, but that's not so interesting given how often they are purchased individually
- hot dogs and mustard are also often purchased as a pair, but more rarely purchased individually

A supermarket could then have a sale on hot dogs while raising the price on condiments.

OTHER APPLICATIONS

Related Concepts

- looking for pairs (triplets, etc) of words that represent a joint concept
- {Ottawa, Senators}, {Michelle, Obama}, {veni, vidi, vici}, etc.

Plagiarism

- looking for sentences that appear in various documents
- looking for documents that share sentences

Biomarkers

- diseases that are frequently associated with a set of biomarkers

OTHER USES

Making predictions and decisions based on these rules

Alter circumstances or environment to take advantage of these correlations

Use the connections to modify the likelihood of certain outcomes

Imputing missing data

Text autofill and autocorrect

DISCUSSION

What are some public policy/government applications of association rules?

CAUSATION AND CORRELATION

Association rules can automate hypothesis discovery, but one must remain **correlation-savvy** (which is less prevalent among data scientists than one would hope...).

If attributes A and B are shown to be correlated, there are (at least) 5 possibilities:

- A and B are correlated **entirely by chance** in this particular dataset
- A is a relabeling of B
- A causes B
- B causes A
- combinations of other attributes C_1, \dots, C_n (known or not) cause A & B

CAUSATION AND CORRELATION

Insight	Organization
Pop-Tarts before a hurricane	Walmart
Higher crime, more Uber rides	Uber
Typing with proper capitalization indicates creditworthiness	A financial services startup company
Users of the Chrome and Firefox browsers make better employees	A human resources professional services firm, over employee data from Xerox and other firms
Men who skip breakfast get more coronary heart disease	Harvard University medical researchers
More engaged employees have fewer accidents	Shell
Smart people like curly fries	Researchers at the University of Cambridge and Microsoft Research
Female-named hurricanes are more deadly	University researchers
Higher status, less polite	Researchers examining Wikipedia behavior

DEFINITIONS



A rule $X \rightarrow Y$ is a statement of the form “if X then Y ” built from any logical combinations of a dataset attributes.

A rule **need not be true for all observations** in the dataset (i.e. rules are not necessarily 100% accurate).

In fact, sometimes the “best” rules could be those which are only accurate 10% of the time, as opposed to rules for which the accuracy is only 5% of the time, say.

As always, **it depends on the context**.

DEFINITIONS

To determine a rule's strength, we compute rule metrics:

- **Support** (coverage) measures the frequency at which a rule occurs in a dataset. A low coverage value indicates that the rule rarely occurs (whether it is true or not).
- **Confidence** (accuracy) measures the reliability of the rule: how often does the conclusion occur in the data given that the premises have occurred. Rules with high confidence are “truer”.
- **Interest** measures the difference between its confidence and the relative frequency of its conclusion. Rules with high absolute interest are... well, more interesting.
- **Lift** measures the increase in the frequency of the conclusion due to the premises. In a rule with a high lift (> 1), the conclusion occurs more frequently than it would if it was independent of the premises.

FORMULAS

If N is the number of observations in the dataset:

- $\text{Support}(X \rightarrow Y) = \frac{\text{Freq}(X \cap Y)}{N} \in [0,1]$ Proportion of instances where the premise and the conclusion occur together
- $\text{Confidence}(X \rightarrow Y) = P(Y|X) = \frac{\text{Freq}(X \cap Y)}{\text{Freq}(X)} \in [0,1]$ Proportion of instances where the conclusion occurs when the premise occurs
- $\text{Interest}(X \rightarrow Y) = \text{Confidence}(X \rightarrow Y) - \frac{\text{Freq}(Y)}{N} \in [-1,1]$
- $\text{Lift}(X \rightarrow Y) = \frac{N^2 \cdot \text{Support}(X \rightarrow Y)}{\text{Freq}(X) \cdot \text{Freq}(Y)} \in (0, N^2]$... ?!?

A SIMPLE EXAMPLE

Hypothetical music dataset containing data for $N = 15,356$ music lovers

Candidate Rule (RM): “If an individual is born before 1976 (X), then they own a copy of at least one Beatles album, in some format (Y)”.

Let's assume that

- $\text{Freq}(X) = 3888$ individuals were born before 1976
- $\text{Freq}(Y) = 9092$ individuals have a copy of at least one Beatles album
- $\text{Freq}(X \cap Y) = 2720$ individuals were born before 1976 and have a copy of at least one Beatles album

$$1.2 \approx \frac{0.70}{0.56}$$

A SIMPLE EXAMPLE

The 4 metrics are:

- $\text{Support}(RM) = \frac{2720}{15,356} \approx 18\% \text{ (RM occurs in 18\% of the observations)}$
- $\text{Confidence}(RM) = \frac{2720}{3888} \approx 70\% \text{ (RM is true in 70\% when born prior to 1976)}$
- $\text{Interest}(RM) = \frac{2720}{3888} - \frac{9092}{15356} \approx 0.11 \text{ (RM is not very interesting)}$
- $\text{Lift}(RM) = \frac{15,356^2 \cdot 0.18}{3888 \cdot 9092} \approx 1.2 \text{ (weak correlation between being born prior to 1976 and owning a copy of a Beatles' album)}$

Interpretation of the Lift: 70% of those born before 1986 own a copy, whereas 56% of those born after 1986 own a copy.

EXERCISE

Evaluate the following candidate rules:

- if an individual owns a classical music album (W), they also own a hip-hop album (Z), given that
 $\text{Freq}(W) = 2010, \text{Freq}(Z) = 6855, \text{Freq}(W \cap Z) = 132$
- if an individual owns both a Beatles and a classical music album, they were born before 1976,
given that $\text{Freq}(Y \cap W) = 1852, \text{Freq}(Y \cap W \cap X) = 1778$

Out of the 3 rules that have been established ($X \rightarrow Y, W \rightarrow Z, Y \& W \rightarrow X$), which do you think is more useful? Which is more surprising?

BRUTE FORCE ALGORITHM

1. Generate item sets (of size 1, 2, 3, 4, etc.)
 - e.g. {purchasing = Typical, membership = False, coupon = Yes}
2. Create rules from each item set
 - e.g. **IF** (purchasing = Typical AND membership = False) **THEN** coupon = Yes
3. Calculate the support, confidence, interest, lift for each rule
4. Retain only the rules with “high enough” coverage, accuracy, interest, and/or lift (or other metrics)
5. These rules are considered to be **true** for the dataset – they are **new knowledge derived from the data**

GENERATING RULES

An **item set** (or instances) is a list of attributes and values.

A set of **rules** can be created by adding '**IF ... THEN**' to each of the instances. As an example, from the instance set

{membership = True, age = Youth, purchasing = Typical}

we can create the rules

- **IF** (membership = True AND age = Youth) **THEN** purchasing = Typical
- **IF** membership = True **THEN** (age = Youth AND purchasing = Typical)
- **IF** \emptyset **THEN** (membership = True AND age = Youth AND purchasing = Typical)
- etc.

EXERCISE

A store that sells accessories for cellular phones runs a promotion on faceplates.

Customers who purchase multiple faceplates from a choice of 6 different colours get a discount. The store managers, who would like to know what colours of faceplates are likely to be purchased together, collected past transactions in `Transactions.csv`.

Consider the following rules:

- $\{\text{red}, \text{white}\} \Rightarrow \{\text{green}\}$
- $\{\text{green}\} \Rightarrow \{\text{white}\}$
- $\{\text{red}, \text{green}\} \Rightarrow \{\text{white}\}$
- $\{\text{green}\} \Rightarrow \{\text{red}\}$
- $\{\text{orange}\} \Rightarrow \{\text{red}\}$
- $\{\text{white}, \text{black}\} \Rightarrow \{\text{yellow}\}$
- $\{\text{black}\} \Rightarrow \{\text{green}\}$

EXERCISE

For each rule, compute the **support**, **confidence**, **interest**, and **lift**.

Amongst the rules for which the support is positive (> 0), which one has the highest lift? Confidence? Interest?

Build an additional 5-10 candidate rules, and evaluate them. Which of the 12-17 candidate rules do you think would be most useful for the store managers?

How would one determine reasonable threshold values for the support, coverage, interest, and lift of rules derived from a given dataset?

NOTES AND VALIDATION

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

“Remember that all models are wrong; the practical question is how wrong do they have to be before they are not useful anymore.”

(Box, G.E.P., and Draper, N. R., *Empirical Model Building and Response Surfaces*)

NUMBER OF RULES

Consider an item set C with n members.

In a rule derived from C , each of the n members shows up either in the **premise** or in the **conclusion**, so there are 2^n such rules.

The rule where each member is part of the premise (and the conclusion is empty) is not allowed, thus $2^n - 1$ rules can be derived from C .

The # of rules increases exponentially when the # of features increases linearly.

That's not good.

VALIDATION

The brute force algorithm works relatively well for **small datasets** (small number of features).

For **Big(ger) Data**, it can be costly to generate rules in that fashion (especially when the number of attributes increases). How do we generate **promising** candidate rules, in general?

How **reliable** are association rules? What is the likelihood that they occur by **chance**? How **relevant** are they? Can they be generalized **outside** the dataset, or to **new** data?

NOTES

Since frequent rules correspond to instances that occur repeatedly in the dataset, algorithms that generate item sets often try to **maximize coverage**.

When **rare events** are more meaningful (such as detection of a rare disease), we need algorithms that can generate rare item sets. **This is not a trivial problem.**

A reminder, in spite of Tufte's rejoinder: **correlation is not causation.**

OTHER ALGORITHMS

Continuous vs. Categorical: continuous data has to be binned into categorical data in order for association rules to be meaningful. There's more than one way to do that.

Item sets are sometimes called **market baskets**.

Other algorithms:

AIS, SETM, Apriori, AprioriTid, AprioriHybrid, Eclat, PCY, Multistage, Multihash, etc.

THE A PRIORI ALGORITHM

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

MR. SNIFF: What are you looking for?

MR. SNOOP: A five-dollar bill.

MR. SNIFF: Are you sure you lost it on this street?

MR. SNOOP: Oh no! I lost it in the next block, but I'm lookin' up here because the light is better.

(Boys' Life Magazine, 1932)

APRIORI ALGORITHM

Developed initially for transaction data

- every reasonable dataset can be transformed into a transaction dataset using dummy variables

Finds **frequent item sets** from which to build candidate rules

- instead of building rules from all possible item sets

Starts by identifying frequent individual items in the database and extends them to larger and larger item sets, assuming these are still found **frequently enough** in the dataset

- **bottom-up** approach, uses the downward closure property of support

APRIORI ALGORITHM

Prunes candidates which have **infrequent sub-patterns**

- requires a support threshold
- that threshold has to be set sufficiently high to minimize the number of frequent item sets

If a 1-item set is not frequent, any 2-item set containing it is also infrequent, for instance.

The algorithm terminates when no further successful extensions are found.

STRENGTHS AND LIMITATIONS

Easy to implement, easily parallelized.

Apriori is **slow** and it requires frequent data set scans.

- possible solutions: **sampling** and **partitioning**

Not ideal at finding rules for **infrequent** or **rare** item sets.

Other algorithms have since displaced it (historical value):

- **Max-Miner** tries to identify frequent item sets without enumerating them; performs jumps in space instead of using bottom-up approach
- **Eclat** is faster and uses depth-first search, but requires extensive memory storage

EXAMPLE:TITANIC

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

“Oh they built the ship Titanic to sail the ocean blue;
And they thought they had a ship that the water wouldn’t go through;
But Fate’s almighty hand knew the ship would never stand.
It was sad when that great ship went down.”

(*The Titanic Disaster*, Traditional Folk Song)

TITANIC DATASET

Compiled by Robert Dawson in 1995; it consists of 4 categorical attributes for each of the 2201 people aboard the Titanic when it sank in 1912.

Attributes are:

- **class** (first class, second class, third class, crewmember)
- **age** (adult, child)
- **sex** (male, female)
- **survival** (yes, no)

TITANIC DATASET

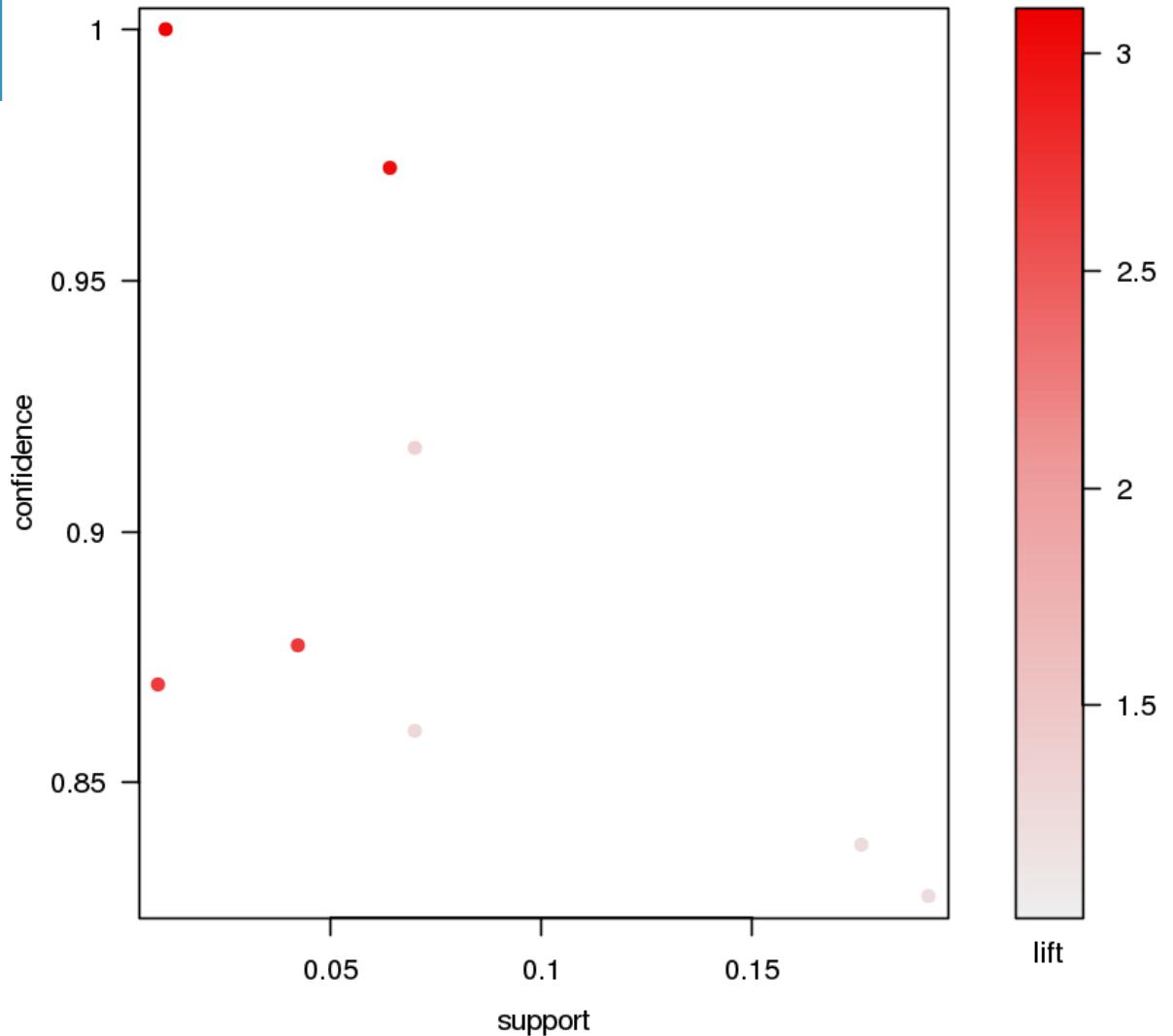
The natural question of interest for this dataset is how survival relates to the other attributes.

We use the `arules` implementation of *apriori* in R to generate and prune candidate rules, eventually leading to **8 rules**.

Is this a supervised or an unsupervised task?

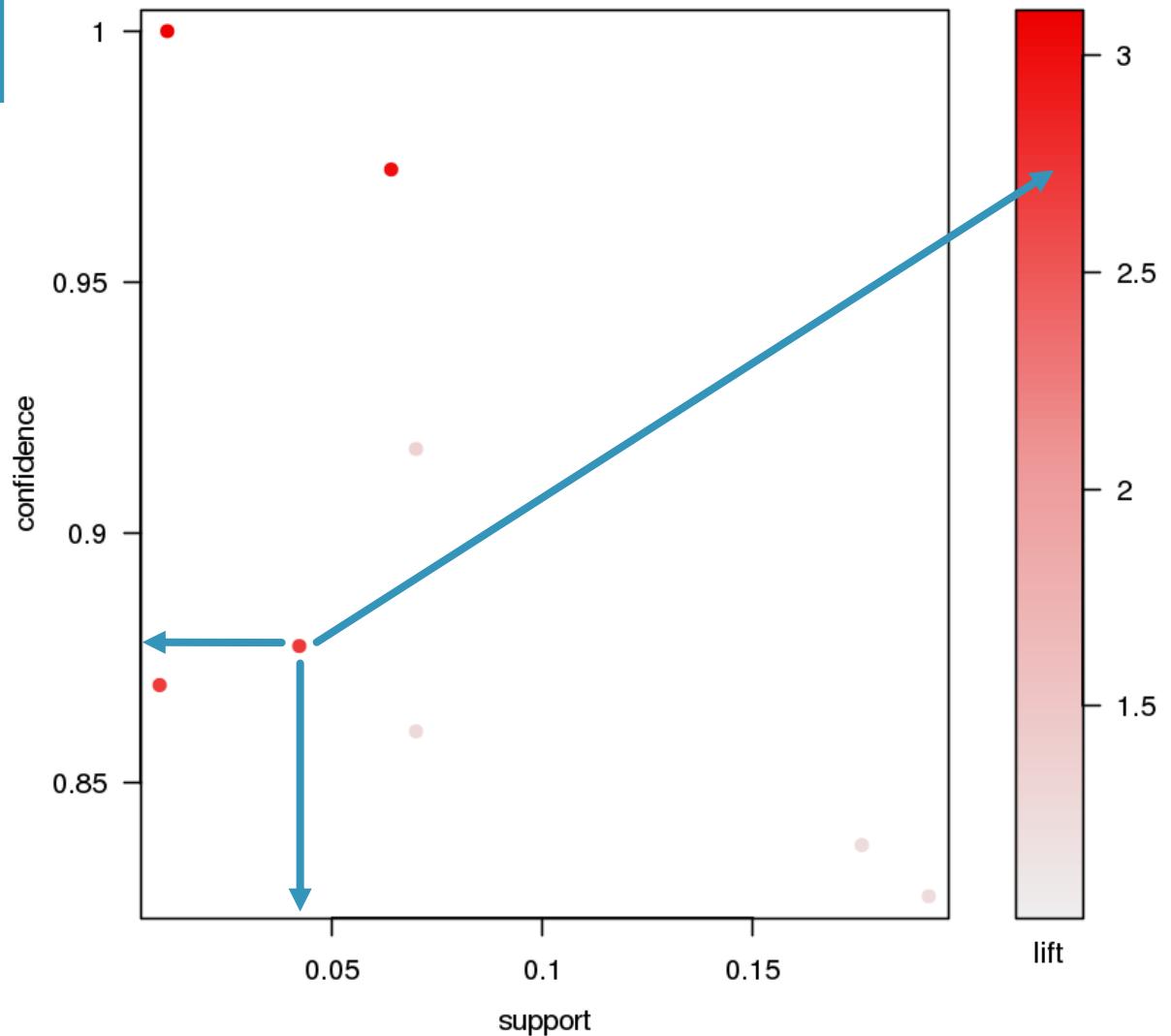
TITANIC DATASET

Rule	Supp	Conf	Lift
IF class = 2nd AND age = Child THEN survived = Yes	0.01	1	3.10
IF class = 1st AND sex = Female THEN survived = Yes	0.06	0.97	3.01
IF class = 2nd AND sex = Female THEN survived = Yes	0.04	0.88	2.72
IF class = Crew AND sex = Female THEN survived = Yes	0.00	0.87	2.70
IF class = 2nd AND sex = Male AND age = Adult THEN survived = No	0.07	0.92	1.35
IF class = 2nd AND sex = Male THEN survived = No	0.07	0.86	1.27
IF class = 3rd AND sex = Male AND age = Adult THEN survived = No	0.18	0.84	1.24
IF class = 3rd AND sex = Male THEN survived = No	0.19	0.83	1.22

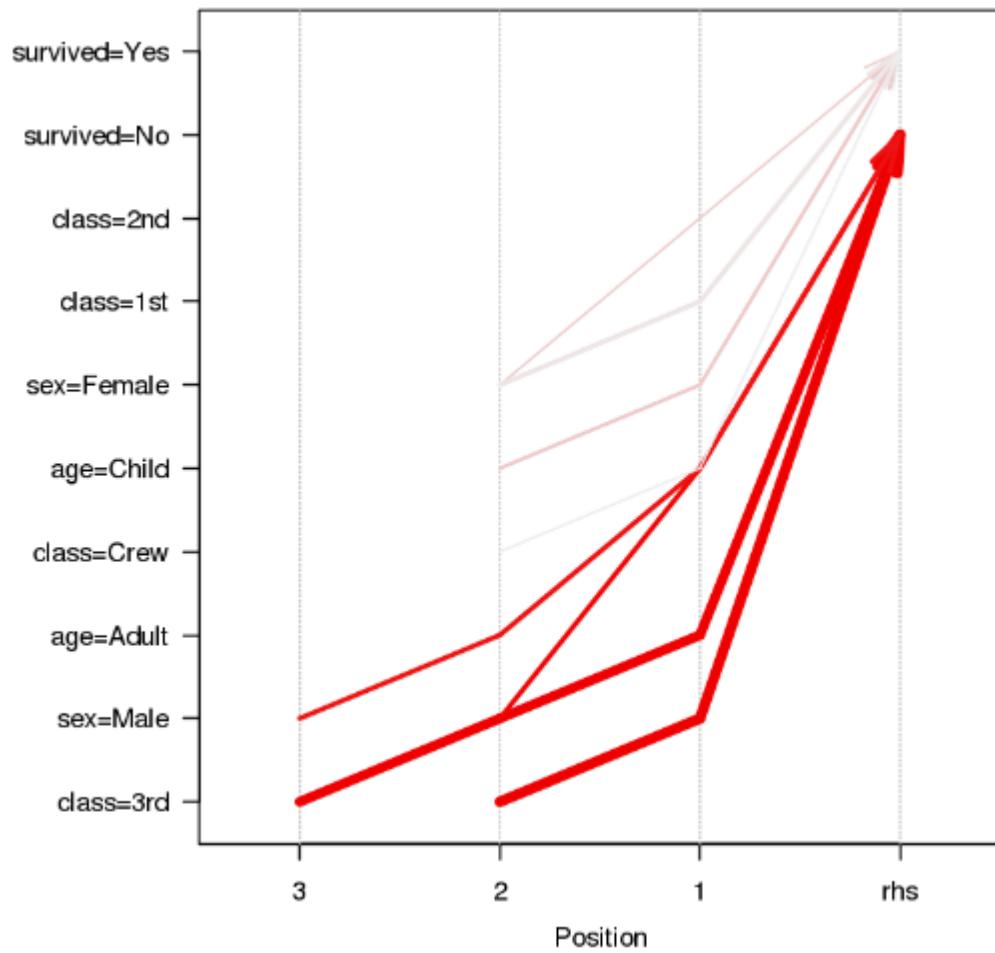
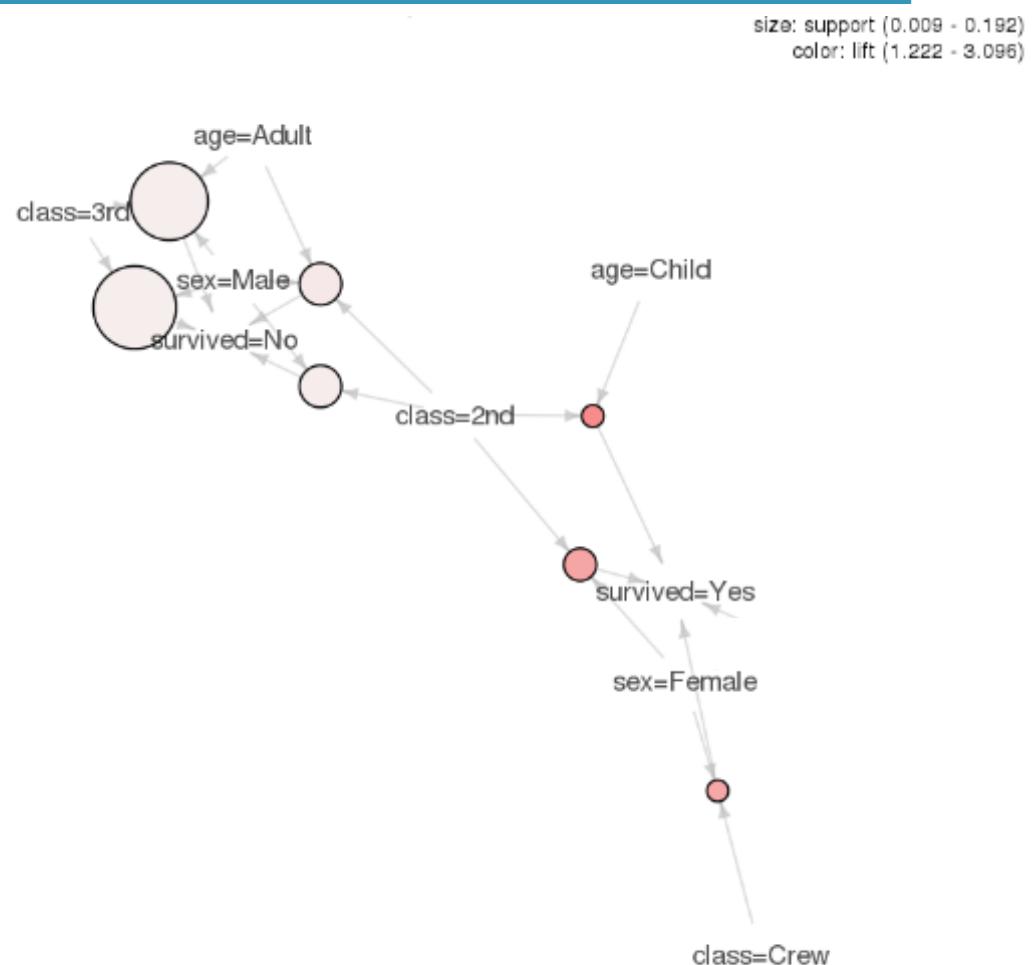


TITANIC DATASET

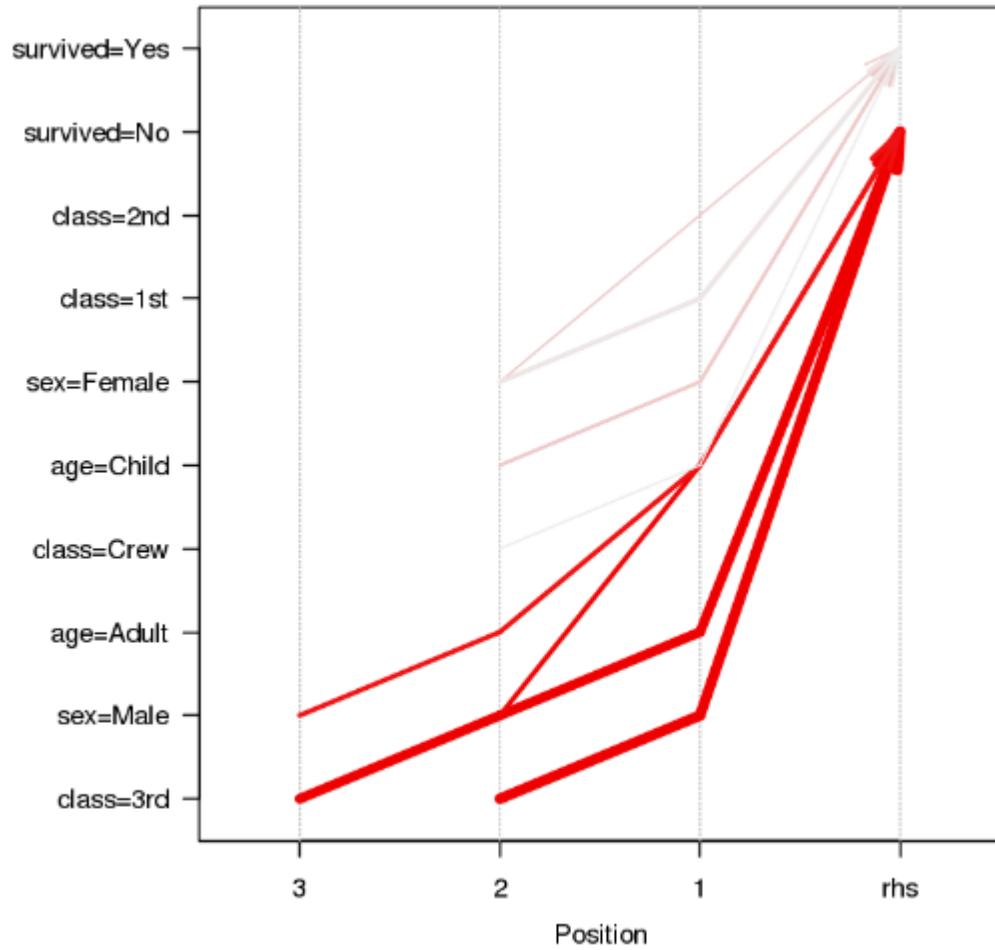
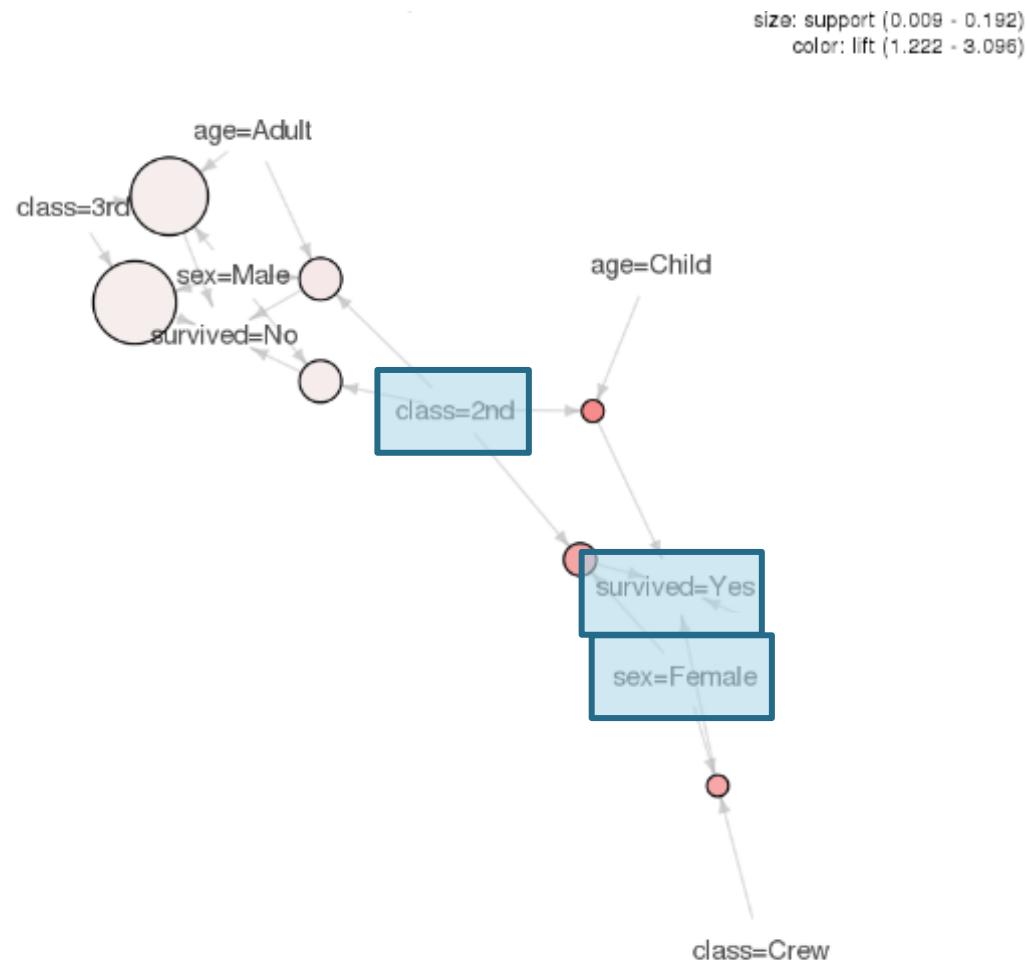
Rule	Supp	Conf	Lift
IF class = 2nd AND age = Child THEN survived = Yes	0.01	1	3.10
IF class = 1st AND sex = Female THEN survived = Yes	0.06	0.97	3.01
IF class = 2nd AND sex = Female THEN survived = Yes	0.04	0.88	2.72
IF class = Crew AND sex = Female THEN survived = Yes	0.00	0.87	2.70
IF class = 2nd AND sex = Male AND age = Adult THEN survived = No	0.07	0.92	1.35
IF class = 2nd AND sex = Male THEN survived = No	0.07	0.86	1.27
IF class = 3rd AND sex = Male AND age = Adult THEN survived = No	0.18	0.84	1.24
IF class = 3rd AND sex = Male THEN survived = No	0.19	0.83	1.22



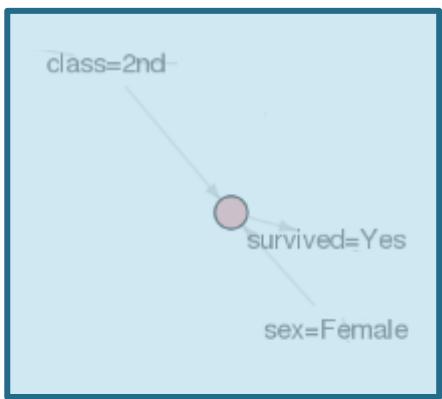
TITANIC DATASET



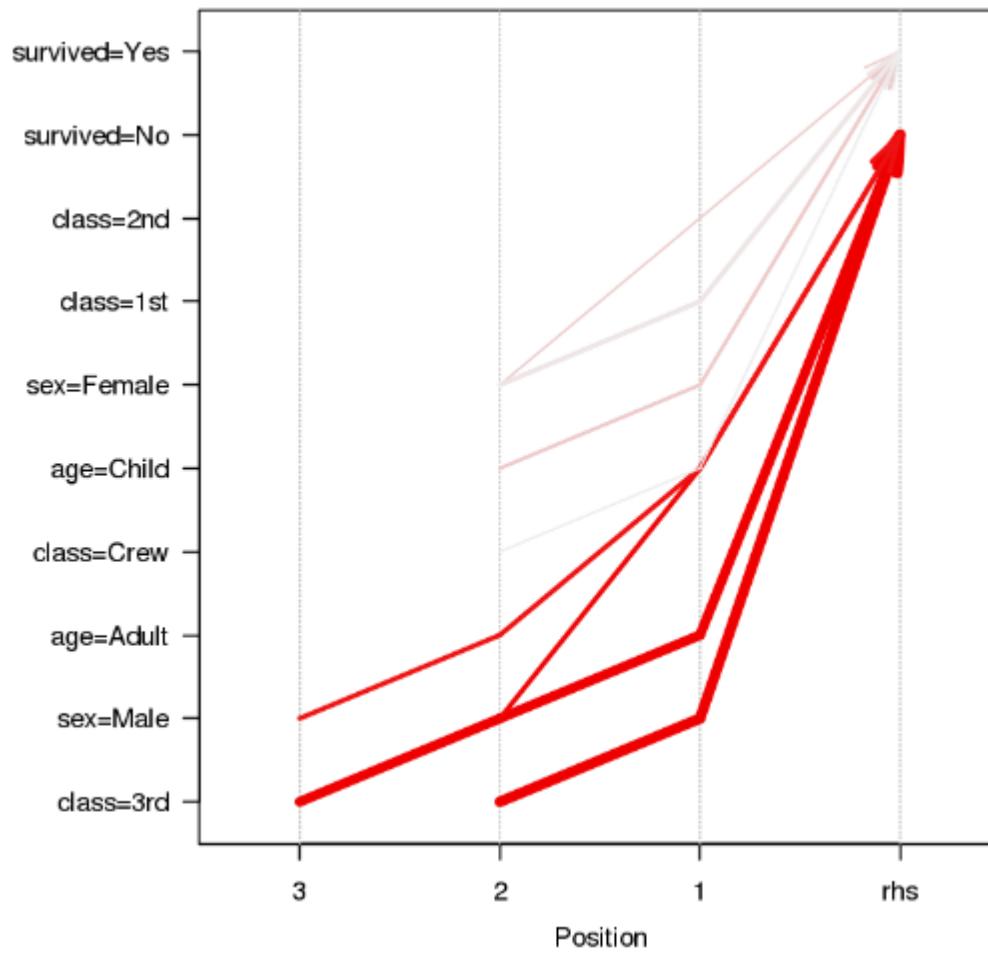
TITANIC DATASET



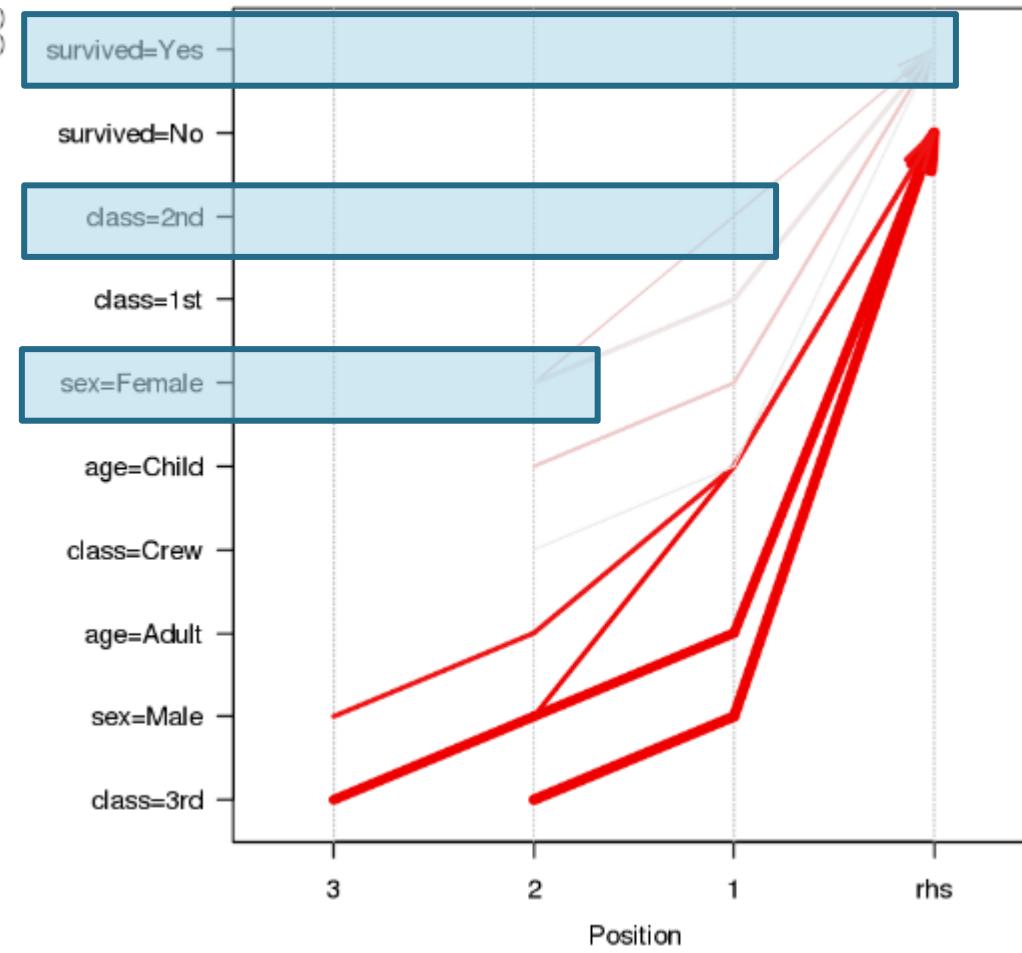
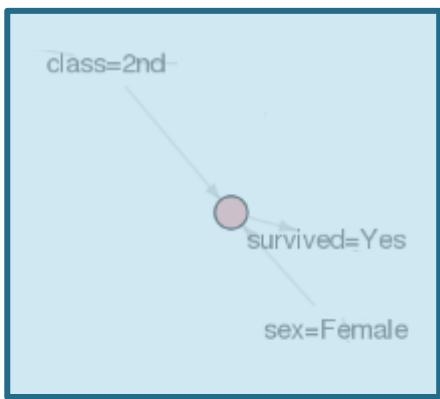
TITANIC DATASET



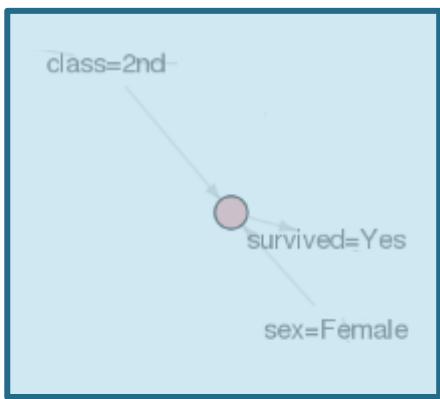
size: support (0.009 - 0.192)
color: lift (1.222 - 3.096)



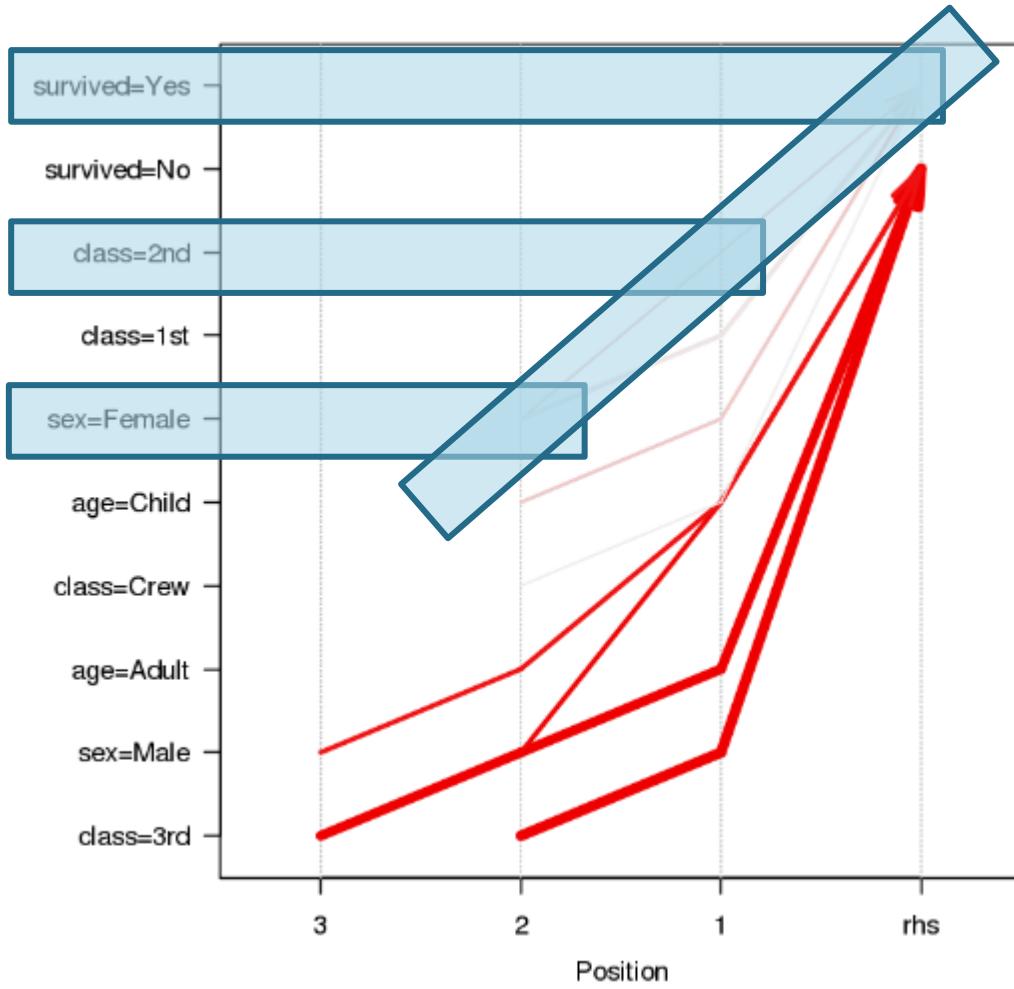
TITANIC DATASET



TITANIC DATASET



size: support (0.009 - 0.192)
color: lift (1.222 - 3.096)



EXERCISE

Conduct a similar analysis to obtain association rules related to the *Life in L.A.* and *Transactions* datasets.

REFERENCES

STATISTICAL LEARNING AND ASSOCIATION RULES MINING

REFERENCES

Brossette, S.E., Sprague, A.P., Hardin, J.M., Waites, K.B., Jones, W.T., Moser, S.A. (1998), Association Rules and Data Mining in Hospital Infection Control and Public Health Surveillance, Journal of American Medical Informatics Association, Vol.5, No.4, pp.373-381

Garcia, E., Romero, C., Ventura, S., Calders, T. (2007), Drawbacks and solutions of applying association rule mining in learning management systems, Proceedings of the International Workshop on Applying Data Mining in e-Learning 2007.

Boily, P., Schellinck, J., Hagiwara, S. [2019], *Introduction to Quantitative Consulting*, Data Action Lab.

Aggarwal, C.C., [2015], *Data Mining: The Textbook*, Springer.

Aggarwal, C.C., Han, J. (eds.) [2014], *Frequent Pattern Mining*, Springer.

REFERENCES

<http://www.rdatamining.com/examples/association-rules>

<https://cran.r-project.org/web/packages/arules/vignettes/arules.pdf>

<https://cran.r-project.org/web/packages/arulesViz/vignettes/arulesViz.pdf>

<https://www.lynda.com/R-tutorials/Up-Running-R/120612-2.html>

http://michael.hahsler.net/research/arules_RUG_2015/demo/