

KEY POINTS

Hash Maps :

Used to store **key value pairs** which can be accessed in **$O(1)$ time**.

Achieved by **hashing** a value to compute the **address** e.g.

$$\text{addr} = \text{key} \bmod \text{size}$$

One can also use the **folding method** to calculate the address.

Collisions can be avoided by using open or closed addr.

$$\text{load factor} = \frac{\text{items stored}}{\text{size of list}}$$

When the l.f. reaches a threshold we can resize the list.

open \Rightarrow find next slot

closed \Rightarrow linked list for each key.

NAME/DATE/SUBJECT

Hash Tables

NOTES

ADT

- Stores **key-value** pairs in an array. Look ups take place in **mostly constant time**.
- This happens by **calculating the index** to store the KVP in, allowing for random searches.

$$\text{memory location} = \text{key value} \bmod n$$

Hashing algorithm: a function $f: \text{key} \rightarrow \text{addr}$.

The **folding method** is another way to **divide the key** into **equal parts** and then **add the parts together**.

e.g. phone # 014528345654

$$\Rightarrow 01 + 45 + 28 + 34 + 56 + 54 = 218$$

You may **divide by some constant** and take the remainder, depending on the size of the table.

SUMMARY

Collisions - Open Addressing

NOTES

Collisions occur when **two keys take the same index** (from the hashing function).

Open addressing: placing an item **elsewhere than it should be**.

Linear probing - placing it in the **next available spot**.

This will use a **linear search** to **keep searching for the next spot**. If there is no space by the time you reach the end, then you wrap to the beginning of the list.

↳ This applies for **locating clashed objects!** You start at the index and keep searching.

Another way to **reduce the number of clashes** is to **allocate more memory than required**.

$$\text{Load factor} = \frac{\text{number of items stored}}{\text{size of array}} \quad \text{e.g. LF} = 70\%$$

You could use a **threshold** to decide when the hash table should be **resized**.

L.P may lead to **clustering** - all the information gets **stuck in one part of the map**.

Open Addressing

NOTES

Plus 3 Rehash : We look at every **third place along** when looking for **free slots**.

Quadratic probing : look at **$(\text{failed attempts})^2$** along each time,

Double hashing : the **result of the second hash** will describe the **number of positions to shift** when looking.

HASH FUNCTION GOALS :

- All elements have a **unique position**.
- The elements use **all the space available**.



these are perfect conditions

Realistic goals :

- **Minimise collisions**
- **Uniform distributions**
- The HF will be **easy to calculate**, and provides **good collis. resolution**.

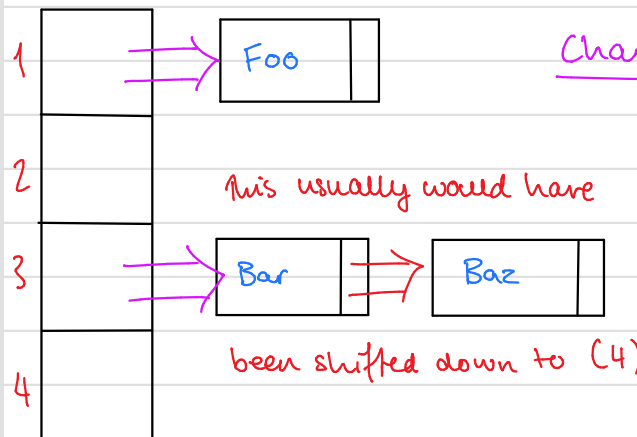
KEY POINTS

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Collisions - closed addressing

NOTES

Closed Addressing: when each key in the map is a pointer to the head of a linked list.



Chaining: You will need to calculate the index, then traverse the linked list in order to locate the value.

Chaining is typically better than worst case array traversal; however, if the load factor is small then linear probing may be faster.

SUMMARY