Physics 201 Electromagnetic Wave Homework One

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The wave equation for the magnetic field in an electromagnetic wave is:  $\frac{d^2}{dx^2}\vec{B} = \frac{1}{c^2}\frac{d^2}{dt^2}\vec{B}$ . Note that there are no units here, the speed you get will have no real units, so it will not equal the true speed of light, c.

- 1. Verify that  $B(x,t) = 4\sin(5x 6t)$  works, in that it satisfies the equation. What is the wave speed?
- 2. Verify that  $B(x,t) = 5(6x 8t)^2$  works.
- 3. Verify the function  $B(x,t) = 6x^2 8t$  does not work.

In deriving the wave equation, we get equations like:  $\frac{d}{dx}E_y = -\frac{d}{dt}B_z$ . Here the subscripts indicate the vector components of E and B. (The y-component of E, and the z component of B).

- 4. If  $E_y = A\sin(kx \omega t)$ , find a suitable function for  $B_z$ . There are multiple answers. Just find one.
- 5. The units of electric field, E, are volt per meter or newton per coulomb. If x is in meters, and t in seconds, what are the units of k and  $\omega$ ? The unit of B is the tesla (T), and verify that the units of your answer in 4 above work. You will need to know what a tesla is in terms of something else. One source of such information is the course equation sheet.