

# Magnetic Forces

$$\vec{F} = q \vec{v} \times \vec{B}$$

$$\vec{F} = I \vec{\ell} \times \vec{B}$$



later on



circular path. What radius?  
 given:  $m$   $q$   $v$   $B$ .

$$\Sigma \vec{F} = m \vec{a}$$

$$qvB = ma_c$$

$$qvB = m \frac{v^2}{r}$$

$$a_c = \frac{v^2}{r}$$

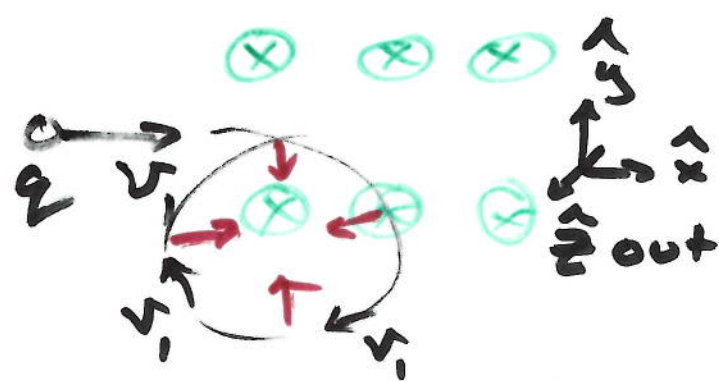
$$r = \frac{mv}{qB} = \frac{m}{q} \frac{v}{B}$$

W

②  
Charged  
Particle  
From  
the  
Sun.



$$\vec{F} = q \vec{v} \times \vec{B}$$



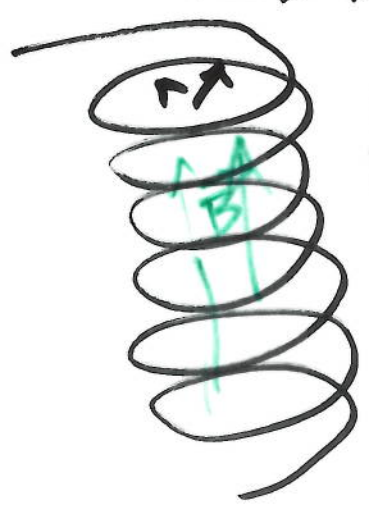
$$\vec{v} = v_1 \hat{x} + v_2 \hat{z}$$

↑  
small?

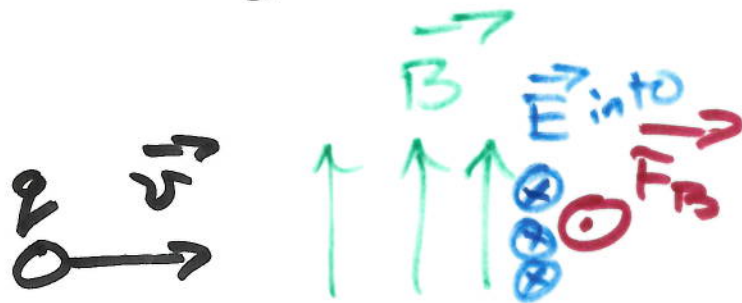
↑  
z

→ x, y

↓  $v_2 = \text{const.}$



Velocity selector:



$$\vec{F} = q \vec{v} \times \vec{B}$$

$$\vec{F} = q \vec{E}$$

given:  $q \vec{v} \vec{B}$  + picture

where should  $\vec{E}$  go so that *into page*

$$\sum \vec{F} = 0 \text{ on this } q?$$

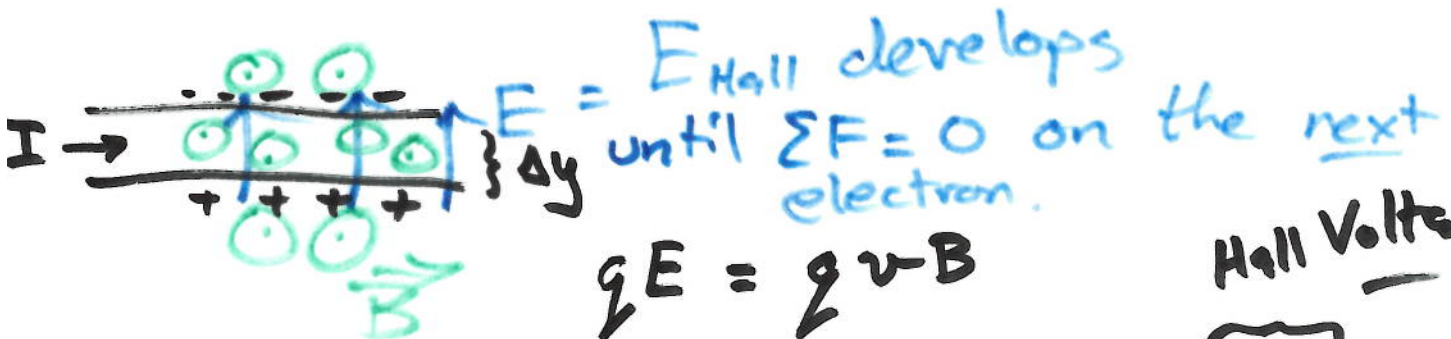
What is  $E$  in terms of:  $q v B, m$

$$\cancel{q} E = \cancel{q} v B$$

$$E = v B. \quad \text{or} \quad v = \frac{E}{B}$$

Hall Effect:  
how to measure  $\vec{B}$ ?

the right velocity to go straight.



$$q E = q v B$$

Hall Voltage

$$\text{and } E = -\frac{\partial V}{\partial y} \hat{y} \text{ so } \Delta \tilde{V} = \underbrace{\Delta y}_{\text{width}} E.$$

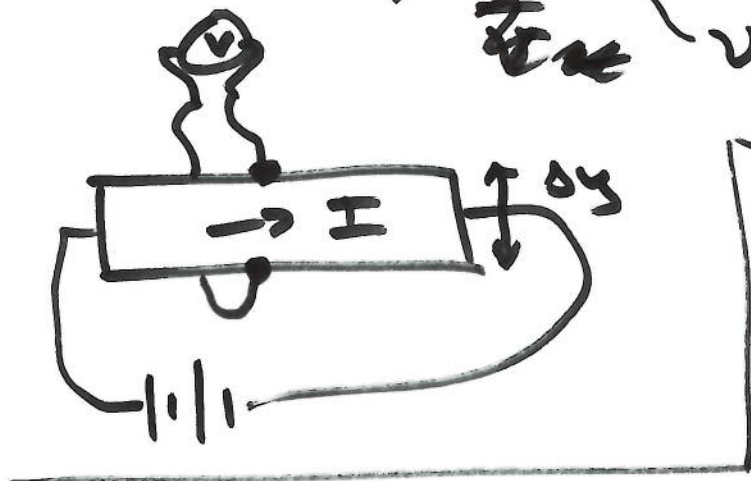


$$B = \frac{E}{v} \text{ and } E = \frac{\Delta V}{\Delta y}$$

$$B = \frac{\Delta V}{\Delta y} v$$

$$B = \frac{\Delta V}{\Delta y \cdot v}$$

$v \propto I$  (the current)

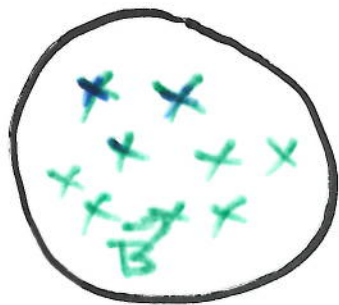


Faraday's Law of Induction

$$V = - \frac{d}{dt} \int \vec{B} \cdot d\vec{a}$$

↑  
sometimes  
called EMF or  $\mathcal{E}$

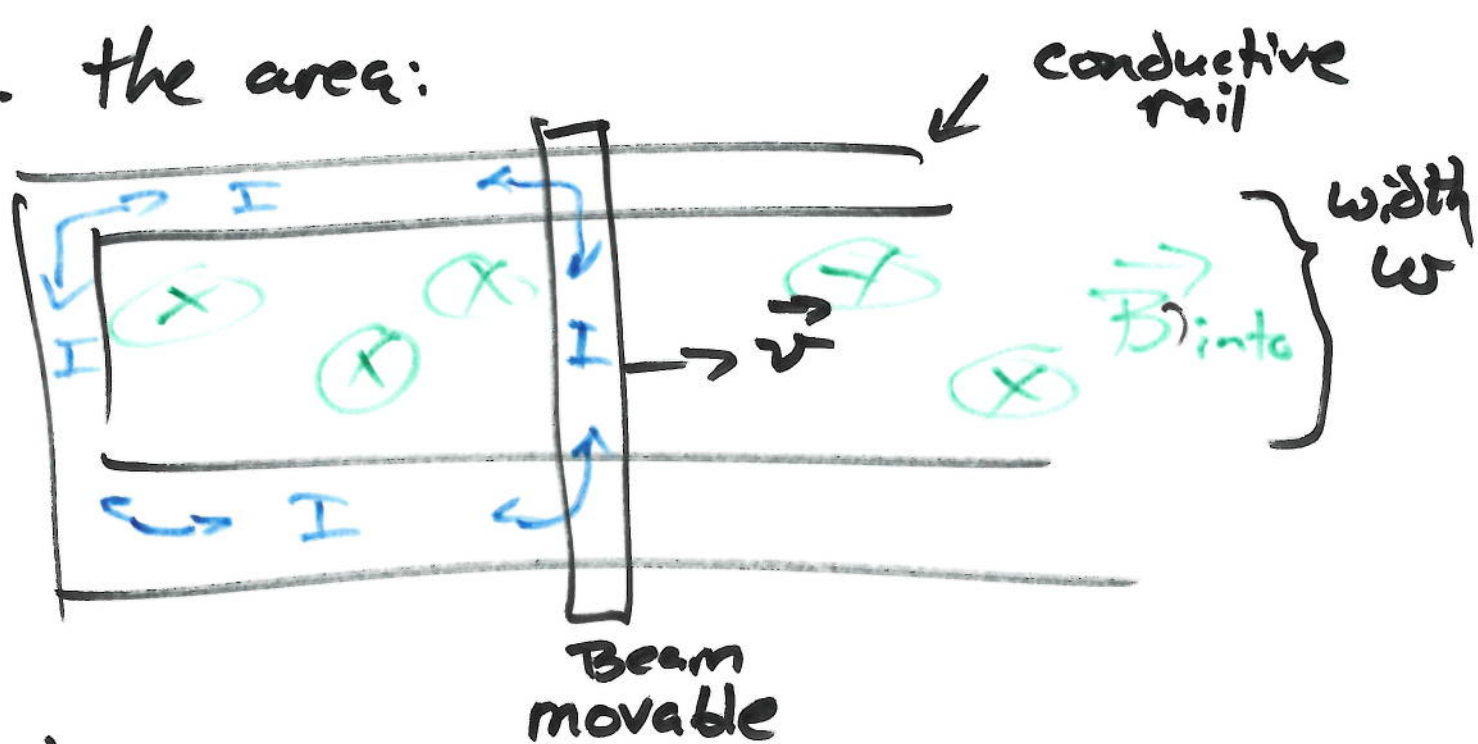
magnetic flux or  $\Phi_B$



3 options to change  
the Flux:

1. make  $B$  bigger or smaller.
2. Make area bigger or smaller
3. change  $\theta$  between  $\vec{B}$ ,  $d\vec{a}$

2. the area:



Need:

$B, v, w$  + picture.

The direction of current  $I$  given by Lenz's Law.

$$V = -\frac{d}{dt} \int \vec{B} \cdot d\vec{a} = \frac{d}{dt} \int B da$$

$B$  constant in space and time.

$$V = B \frac{d}{dt} \underbrace{\int da}_{\text{area}} = B \frac{d}{dt} \underbrace{L(t) \cdot w}_{L(t) \cdot w}$$

$$= B \frac{d}{dt} L(t) \cdot \underbrace{w}_{\text{width constant}}$$

$$= B w \frac{dL}{dt} = B w v$$

Lenz's Law:

The current will produce its own  $B$  which will counter the change in flux in loop.

This goes counter-clockwise

