

P201

Notes to be posted Day 22  
Thermal Physics : More Optics in Lab

## Temperature:

- How hot something is.
- Glow into visible when hot  
"red" hot  $\rightarrow$  yellow  $\rightarrow$  white  $\rightarrow$  blue

$$\overline{E_K} \propto T$$

$\uparrow$  translational  $E_K$  of gas:  $\frac{1}{2} m \overline{v^2}$

$$\overline{E_K} = \frac{3}{2} k_B T$$

$\uparrow$  Boltzmann's Constant

$$k_B = 1.38 \times 10^{-23} \frac{\text{J}}{\text{K}}$$

$\leftarrow$  Joules of Energy  
 $\leftarrow$  Kelvin, unit of T.

Common units of T:

Fahrenheit ( $^{\circ}\text{F}$ )

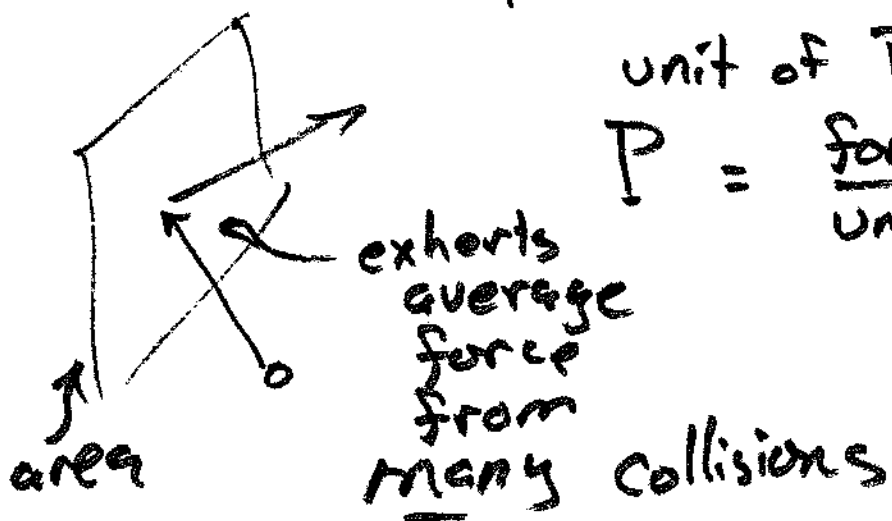
Celsius ( $^{\circ}\text{C}$ )

Kelvin (K)

$$T(^{\circ}\text{C}) = T(\text{K}) - 273.15^{\circ}\text{C}$$

$$T(^{\circ}\text{C}) = \frac{5}{9} T(^{\circ}\text{F}) - 32^{\circ}\text{C}$$

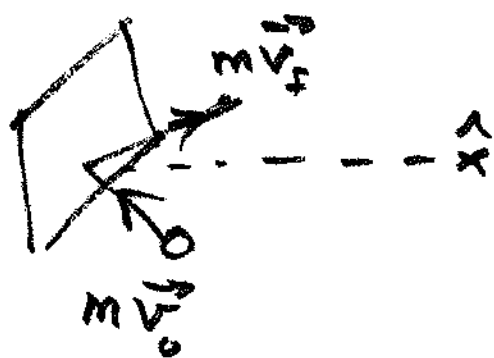
Ideal Gas Law:  
What is Pressure?



unit of Pressure:  $\frac{\text{Newton}}{\text{meter}^2} = \text{Pa}$   
 $P = \frac{\text{force}}{\text{unit area}}$   
 Pascal

1 atm of pressure =  $1.013 \times 10^5 \text{ Pa}$   
 many other units of Pressure:  
 torr, bar, mmHg, PSI =  $\frac{\text{pound}}{\text{inch}^2}$ ,

Collisions, on average can produce force:



in  $\hat{x}$  dir:

$$m v_{o_x} \rightarrow m v_{f_x}$$

elastic: (ideal gas)

$v_{o_x} = -v_{f_x}$  didn't lose energy.

$$F = ma$$

$$F = \frac{\Delta \vec{p}}{\Delta t} = \frac{2m v_x}{\Delta t}$$

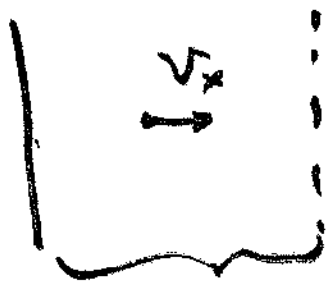
Δ momentum

Consider container,  $L \times L \times L = \text{Volume } V$

full of  $N$  particles, <sup>length</sup> each mass  $m$  and temperature  $T$ .  <sup>$\Delta P$  force</sup>

$$P = \frac{F}{\text{area}} = \frac{F}{L^2} = \frac{N \cdot 2m v_x / \Delta t}{L^2}$$

↑  
one wall



$$\frac{2L}{\Delta t} = v_x$$

$$\Delta t = \frac{2L}{v_x}$$

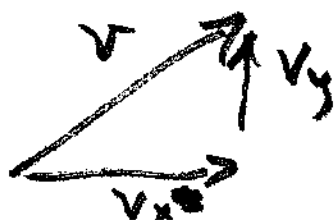
what is  $\Delta t$   
between strikes  
on left wall?

$$P = \frac{N \cdot m v_x \cdot \frac{v_x}{2L}}{L^2}$$

$\leftarrow L^3 = \text{the Volume}$

$$\bar{E}_K = \frac{3}{2} k_B T = \frac{1}{2} m \bar{v}^2$$

$$3 k_B T = m \bar{v}^2 = m (\bar{v}_x^2 + \bar{v}_y^2 + \bar{v}_z^2)$$



$$m \bar{v}_x^2 = k_B T$$

$$P = \frac{N k_B T}{V} \rightarrow PV = N k_B T$$

$$PV = nRT$$

$n = \# \text{ mols}$

$R = \text{the gas constant}$

$$n = \frac{N}{N_A}$$

$N_A \leftarrow \text{Avogadro's Number}$

$$R = k_B \cdot N_A$$

$$8.315 \frac{\text{J}}{\text{K}} = 1.38 \times 10^{-23} \frac{\text{J}}{\text{K}} \cdot 6.022 \times 10^{23}$$

$$\frac{3}{2} k_B T = \overline{E_K}$$

$\updownarrow$  3-D motion  $\Rightarrow \frac{3}{2} k_B T$

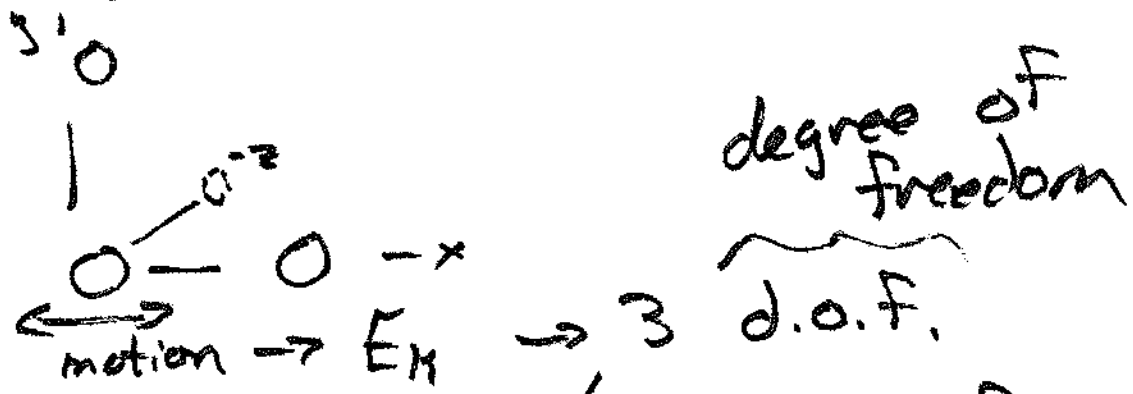
3 from "equipartition" of energy theorem  
each "available" place you can put energy

↑  
governed  
by  
quantum  
mechanics

degree of freedom

gets  $\frac{1}{2} k_B T$  of energy, on average

Solids at (near) room T:



the 'trivial' d.o.f.  
almost always have them  
and usually available.

and potential energy:

3 more d.o.f.

6 total:  $\bar{U} = \frac{6}{2} k_B T = 3 k_B T$

and this linked to "specific heat" =  $c$

$$C = \frac{d\bar{U}}{dT} = 3 k_B \text{ per molecule}$$

$$C = 3R \text{ per mole of material}$$

↳ a law... Dulong & Petit

d.o.f. linked to specific heat

easy to measure

specific heat of liquid water

$$1 \frac{\text{cal}}{\text{g} \cdot ^\circ\text{C}} = 4.184 \frac{\text{J}}{\text{g} \cdot ^\circ\text{C}}$$

also  
half if  
you freeze  
it.

about  $\frac{1}{2}$  in steam (vapor)

Thermal Expansion:

$$L(T) = L_0 (1 + \alpha \Delta T)$$

↑                      ↑                      ↑  
final                  init                      change in T  
length                  length

coefficient of  
thermal expansion

$\alpha$  generally  $> 0$

$\alpha < 0$  for water

( $0 \rightarrow 4.2^\circ\text{C}$ )

unusual.