



# Revisiting VAE for Unsupervised Time Series Anomaly Detection: A Frequency Perspective

Zexin Wang\*  
wangzexin@cnic.cn  
Computer Network Information  
Center, Chinese Academy of Sciences  
Beijing, China

Changhua Pei†  
chpei@cnic.cn  
Computer Network Information  
Center, Chinese Academy of Sciences  
Beijing, China

Minghua Ma  
minghuama@microsoft.com  
Microsoft  
Beijing, China

Xin Wang  
x.wang@stonybrook.edu  
Stony Brook University  
New York, United States

Zhihan Li  
lizhihan03@kuaishou.com  
Kuaishou Technology  
Beijing, China

Dan Pei  
peidan@tsinghua.edu.cn  
Tsinghua University  
Beijing, China

Saravan Rajmohan  
saravan.rajmohan@microsoft.com  
Microsoft  
Redmond, United States

Dongmei Zhang  
dongmeiz@microsoft.com  
Microsoft  
Beijing, China

Qingwei Lin  
qlin@microsoft.com  
Microsoft  
Beijing, China

Haiming Zhang  
hai@cnic.cn  
Computer Network Information  
Center, Chinese Academy of Sciences  
Beijing, China

Jianhui Li  
lijh@cnic.cn  
Computer Network Information  
Center, Chinese Academy of Sciences  
Beijing, China

Gaogang Xie  
xie@cnic.cn  
Computer Network Information  
Center, Chinese Academy of Sciences  
Beijing, China

## ABSTRACT

Time series Anomaly Detection (AD) plays a crucial role for web systems. Various web systems rely on time series data to monitor and identify anomalies in real time, as well as to initiate diagnosis and remediation procedures. Variational Autoencoders (VAEs) have gained popularity in recent decades due to their superior denoising capabilities, which are useful for anomaly detection. However, our study reveals that VAE-based methods face challenges in capturing long-periodic heterogeneous patterns and detailed short-periodic trends simultaneously. To address these challenges, we propose Frequency-enhanced Conditional Variational Autoencoder (FCVAE), a novel unsupervised AD method for univariate time series. To ensure an accurate AD, FCVAE exploits an innovative approach to concurrently integrate both the global and local frequency features into the condition of Conditional Variational Autoencoder (CVAE) to significantly increase the accuracy of reconstructing the normal data. Together with a carefully designed “target attention” mechanism, our approach allows the model to pick the most useful information from the frequency domain for better short-periodic trend construction. Our FCVAE has been evaluated

on public datasets and a large-scale cloud system, and the results demonstrate that it outperforms state-of-the-art methods. This confirms the practical applicability of our approach in addressing the limitations of current VAE-based anomaly detection models.

## CCS CONCEPTS

• **Mathematics of computing** → **Time series analysis**; • **Computing methodologies** → **Anomaly detection**.

## KEYWORDS

Univariate time series, Anomaly detection, Conditional variational autoencoder

### ACM Reference Format:

Zexin Wang, Changhua Pei, Minghua Ma, Xin Wang, Zhihan Li, Dan Pei, Saravan Rajmohan, Dongmei Zhang, Qingwei Lin, Haiming Zhang, Jianhui Li, and Gaogang Xie. 2024. Revisiting VAE for Unsupervised Time Series Anomaly Detection: A Frequency Perspective. In *Proceedings of the ACM Web Conference 2024 (WWW '24)*, May 13–17, 2024, Singapore, Singapore. ACM, New York, NY, USA, 10 pages. <https://doi.org/10.1145/3589334.3645710>

\* Also with University of Chinese Academy of Sciences.

† Corresponding author.



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WWW '24, May 13–17, 2024, Singapore, Singapore  
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ACM ISBN 979-8-4007-0171-9/24/05.  
<https://doi.org/10.1145/3589334.3645710>

## 1 INTRODUCTION

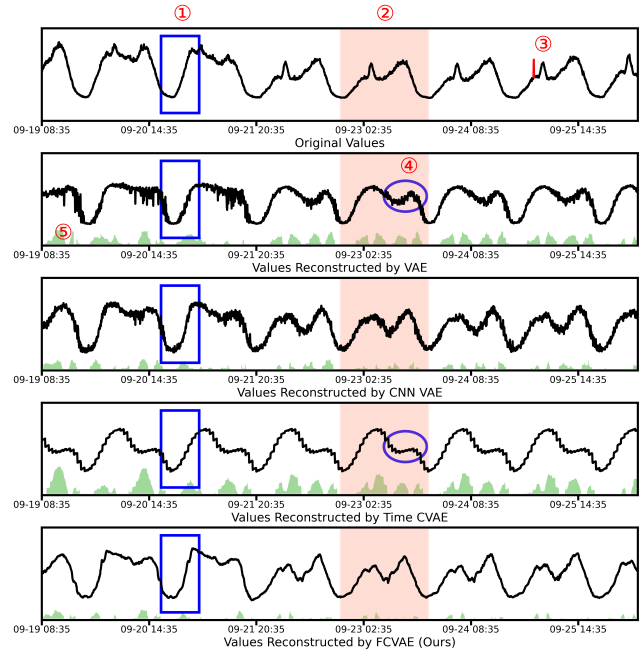
Time series anomaly detection (AD) is ubiquitous for web systems [8, 10, 13, 14, 16, 20, 32, 35, 49, 50]. Numerous web systems, such as online advertising systems, are monitored using a vast array of time series data (e.g., conversion rate) [52]. Deploying time series AD algorithms is essential for timely detecting anomalies and initiating subsequent diagnosis and remediation processes.

Anomalies are rare in real-world time series data [40], making it difficult to label them and train a supervised model for anomaly detection [50]. Instead, unsupervised machine learning techniques are commonly used [5, 7, 15, 17, 26, 33, 50, 55, 58–60]. These techniques can be divided into two categories: *prediction-based* [15, 17, 60] and *construction-based* [5, 26, 33, 50, 55]. Both types aim to identify normal values and compare them to actual values to detect anomalies. Prediction-based methods were originally developed for forecasting future data points, regardless of whether they were normal or anomalous. However, these methods may overfit to anomalous patterns and underperform. On the other hand, Variational AutoEncoders (VAEs) [22], the leading construction-based approach, encode raw time series into a lower-dimensional latent space and then reconstruct them back to their original dimensions. VAEs are well-suited for detecting anomalies, but existing VAE-based anomaly detection models have not yet reached theoretically optimal performance. In this paper, we aim to re-examine the VAE model and improve its effectiveness in anomaly detection.

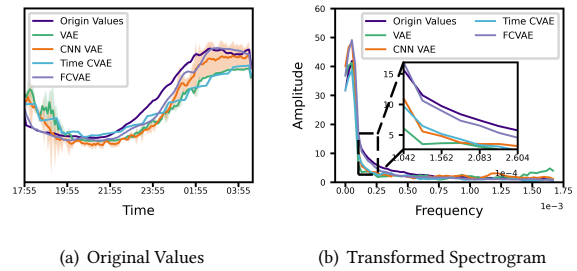
In order to more effectively demonstrate the challenges associated with VAE-based techniques, we provide an example in Figure 1. The original curve is displayed in the first sub-figure, with anomalies highlighted in red ③. The subsequent four sub-figures represent curves reconstructed by four distinct VAE-methods, including our proposed method (referred to as FCVAE). The reconstruction error is indicated by the green shaded area ⑤. To achieve superior AD performance, the reconstructed result should closely resemble the original curve for normal points, while deviating significantly for anomalous points ③. As evident in the figure, all VAE-based methods successfully disregard the anomalies during reconstruction. However, the reconstruction results for some normal points, particularly those marked by a blue rectangle ① and ellipse ④, are not satisfactory. This substantially impacts the overall performance, leading us to identify three key challenges that we address in the subsequent sections.

**Challenge 1: Capturing similar yet heterogeneous periodic patterns.** From Figure 1, periodic patterns can be observed in the curves, with one such period emphasized by the red shaded area ②. However, the shapes across different periods vary. As demonstrated by the blue ellipse, existing VAE-based methods (as shown in the second sub-figure) are unable to capture these heterogeneous patterns effectively. This observation naturally leads to the idea of utilizing conditional VAE to map data into distinct Gaussian spaces by considering the timestamp as a condition. Unfortunately, as illustrated in the fourth sub-figure (Time CVAE [26]), the results are unsatisfactory, which we will further discuss below.

**Challenge 2: Capturing detailed trends.** Reconstructing monotonous patterns (*i.e.*, trends) might appear straightforward at first glance. However, upon a closer examination of the local window (highlighted in a blue rectangle ① in Figure 1 and magnified in Figure 2(a)), it becomes evident that existing methods fail to restore detailed patterns within this time frame. In Figure 2(a), the two green lines initially overestimate the ground truth (purple curve) but subsequently underestimate it for the remainder of the window. This is primarily because existing methods aim to minimize the overall reconstruction error without focusing on



**Figure 1: Comparison of four KPI reconstruction methods presented in our paper, highlighting anomalies in red ③. The green shade ⑤ represents the difference between the reconstructed values and the original values, the red shade ② represents a long period, and the blue ellipse ④ indicates peaks and valleys that are not properly reconstructed, the blue rectangle ① will be magnified in Figure 2 for detailed comparison.**



**Figure 2: A detailed view of the region enclosed by a blue rectangle ① in Figure 1, where the shaded area represents the value range before applying a sliding window average.**

“point-to-point” dependencies, *e.g.*, the precise upward and downward ranges following a specific point. This omission results in fluctuating reconstruction outcomes (as seen in the second sub-figure). Although Convolutional Neural Network (CNN) attempts to model point-to-point dependencies within the window, it still produces coarse-grained fluctuations (visible in the third sub-figure in Figure 1). The reason of unsatisfactory result of CNN-CVAE lies

In this paper, we introduce a novel unsupervised anomaly detection algorithm, named FCVAE (Frequency-enhanced Conditional Variational AutoEncoder). Different from current VAE-based anomaly detection methods, FCVAE innovatively incorporates both global and local frequency information to guide the encoding-decoding procedures, that both heterogeneous periodic and detailed trend patterns can be effectively captured. This in turn enables more accurate anomaly detection. Our paper’s contributions can be summarized as follows:

- The replication package for this paper, including all our data, source code, and documentation, is publicly available online at [\*\*https://github.com/CSTCloudOps/FCVAE\*\*](https://github.com/CSTCloudOps/FCVAE).

## 2.1 Problem Statement

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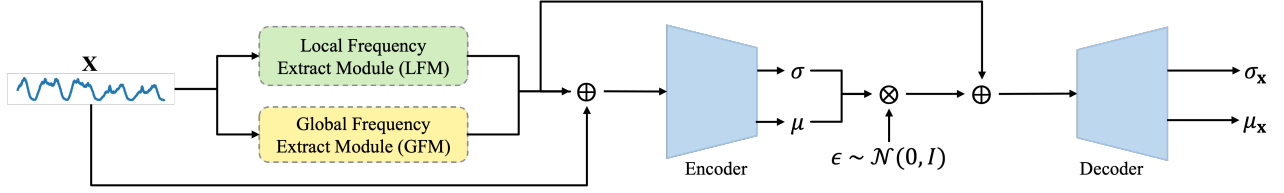


Figure 4: FCVAE Model Architecture.

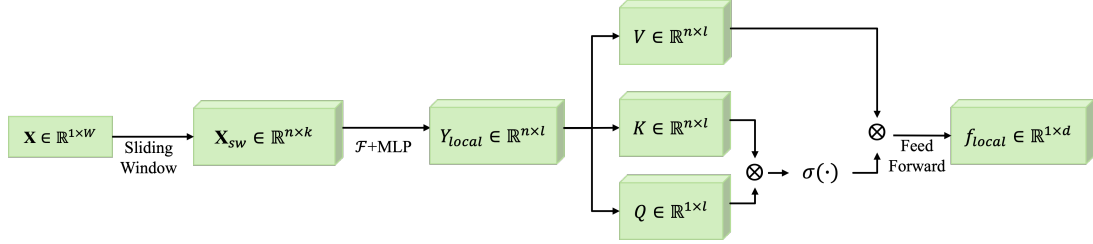


Figure 5: Architecture of LFM.

[26, 29, 50]. Therefore, we directly incorporate these techniques into our approach.

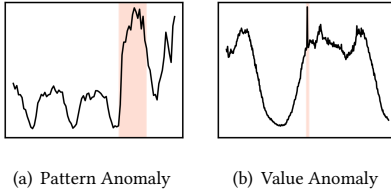


Figure 6: Examples of the two most frequent anomalies, where the red shaded area denotes the abnormal segments.

Previous data augmentation methods [25, 47, 54] often added normal samples, such as variations of data from the time domain or frequency domain. However, for our method, we train the model by incorporating all the time series from the dataset together, which provides sufficient pattern diversity. Furthermore, FCVAE has the ability to extract pattern information due to the addition of frequency information, so it can handle new patterns well. Nonetheless, even with the introduction of frequency information, anomalies are often challenging to be effectively addressed. For the model to learn how to handle anomalies, we primarily focus on abnormal data augmentation. In time series data, anomalies are mostly manifested as pattern mutations or value mutations (shown in Figure 6), so our data augmentation mainly targets to these two aspects. The augmentation on the pattern mutation is generated by combining two windows from different curves, with the junction acting as the anomaly. Value mutation refers to changing some points in the window to randomly assigned abnormal values. With the augmented anomaly data, M-ELBO in CVAE, which will be introduced in detail later, can perform well even in an unsupervised setting without true labels.

### 3.3 Network Architecture

The proposed FCVAE model is illustrated in Figure 4. It comprises three main components: encoder, decoder, and a condition extraction block that includes a global frequency information extraction module (GFM) and a local frequency information extraction module (LFM). Equation (3) illustrates how our model works.

$$\begin{aligned} \mu, \sigma &= \text{Encoder}(x, \text{LFM}(x), \text{GFM}(x)) \\ z &= \text{Sample}(\mu, \sigma) \\ \mu_x, \sigma_x &= \text{Decoder}(z, \text{LFM}(x), \text{GFM}(x)) \end{aligned} \quad (3)$$

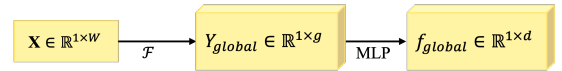


Figure 7: Architecture of GFM.

**3.3.1 GFM.** The GFM module (Figure 7) extracts the global frequency information using the FFT transformation ( $\mathcal{F}$ ). However, not all frequency information is useful. The frequencies resulted from the noise and anomalies in the time series data appear as long tails in the frequency domain. Therefore, we employ a linear layer after the FFT to filter out the useful frequency information that can represent the current window pattern. Moreover, we incorporate a dropout layer following Fedformer [61] to enhance the model's ability to learn the missing frequency information.

The  $f_{global} \in \mathbb{R}^{1 \times d}$  is calculated as (4), where  $d$  is the embedding dimension of the global frequency information and  $\mathcal{F}$  means FFT.

$$f_{global} = \text{Dropout}(\text{Dense}(\mathcal{F}(x))) \quad (4)$$

**3.3.2 LFM.** The attention mechanism [46] has been widely adopted in time series data processing due to its ability to dynamically process dependencies between different time steps and focus on important ones. Target attention, which is developed based on attention,

is widely used in the field of recommendation [4]. Specifically, target attention can weigh the features of the target domain, leading to more accurate domain adaptation.

The GFM module extracts the frequency information from the entire window, proving to be effective in reconstructing the data within the whole window. However, we use a window to detect whether the last point is abnormal, which poses a challenge because the GFM module does not provide sufficient attention to the last point. This can result in a situation where the reconstruction is satisfactory for part of the window but not for another part, especially when changes in system services lead to the concept drift in the time series data. Even in the absence of concept drift, GFM cannot capture local changes as it extracts the average frequency information from the entire window; hence, the reconstruction of the last key point may be unsatisfactory. Nonetheless, as previously mentioned, target attention can effectively address this issue, as it captures the frequency information of the entire window while paying a greater attention to the latest time point. Therefore, we propose the LFM that incorporates the target attention.

As depicted in Figure 5, the LFM module operates by sliding the entire window  $\mathbf{x}$  to obtain several small windows  $\mathbf{x}_{sw}$ . Subsequently, FFT and frequency information extraction are applied to each small window. The most recent small window is used as the query  $Q$  because it contains the last point that we want to detect. The remaining small windows are utilized as keys  $K$  and values  $V$  for target attention. Finally, a linear layer is employed to facilitate the model in learning to extract the most important and useful part of the local frequency information, and dropout is also applied to enhance the model's ability to reconstruct some of the local frequency information like GFM.

$$\begin{aligned} \mathbf{x}_{sw} &= \text{SlidingWindow}(\mathbf{x}) \\ Q &= \text{Select}(\text{Dense}(\mathcal{F}(\mathbf{x}_{sw}))) \\ K, V &= \text{Dense}(\mathcal{F}(\mathbf{x}_{sw})) \\ f_{local} &= \text{Dropout}(\text{FeedFawrd}((\sigma(Q \cdot K^T) \cdot V))) \end{aligned} \quad (5)$$

The calculation of  $f_{local} \in \mathbb{R}^{1 \times d}$  in LFM is given by (5), where  $d$  is the embedding dimension of the local frequency information, which is the same as that of GFM. Here,  $\mathbf{x}_{sw} \in \mathbb{R}^{n \times k}$  represents a group of small windows extracted from the original window, where  $k$  is the dimension of the small windows and  $n$  is the number of small windows. The Select function is employed to select the latest window as the query  $Q$  and the Dense function means dense neural network. The softmax function  $\sigma$  is used to calculate the attention weights for the small windows.

### 3.4 Training and Testing

The training process of FCVAE incorporates three key technologies: CVAE-based modified evidence lower bound (CM-ELBO), missing data injection, as well as the newly proposed **masking the last point**. As shown in (6), CM-ELBO is obtained by applying MELBO [50] to CVAE. Missing data injection [29, 50] is a commonly used technique in VAE that we directly apply. We observed that an anomalous point in time series data manifests as an outlier value in the time domain. However, when the data are transformed into the frequency domain, all frequency information is shifted, leading to a challenge. The impact of this issue will be amplified when the last point is abnormal, as we specifically aim to detect the last point

given the whole window. While we use the frequency enhancement method and frequency selection to mitigate this problem to some extent, we mask the last point as zero during the extraction of the frequency condition to address this issue further.

$$\mathcal{L} = \mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x}, \mathbf{c})} \left[ \sum_{w=1}^W \alpha_w \log p_\theta(\mathbf{x}_w | \mathbf{z}, \mathbf{c}) + \beta \log p_\theta(\mathbf{z}) - \log q_\phi(\mathbf{z} | \mathbf{x}, \mathbf{c}) \right] \quad (6)$$

While testing, FCVAE adopts the Markov Chain Monte Carlo (MCMC)-based missing imputation algorithm proposed in [38] and applied in [29] to mitigate the impact of missing data. Since our goal is to detect the last point of a window, the last point is set to missing for MCMC to obtain a normal value. This also allows for a better adaptation to the last point mask mentioned earlier. FCVAE further utilizes reconstruction probabilities as anomaly scores, which are defined in equation (7).

$$\text{AnomalyScore} = -\mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x}, \mathbf{c})} [\log p_\theta(\mathbf{x} | \mathbf{z}, \mathbf{c})] \quad (7)$$

## 4 EXPERIMENTS

### 4.1 Experiment Settings

**4.1.1 Datasets.** To evaluate the effectiveness of our proposed algorithm, we conducted experiments on four datasets. **Yahoo** [2] is an open data set for anomaly detection released by Yahoo lab. **KPI** [27] KPI is collected from five large Internet companies (Sougo, eBay, Baidu, Tencent, and Ali). **WSD** [1] Web service dataset (WSD) contains real-world KPIs collected from three top-tier Internet companies, Baidu, Sogou, and eBay, providing large-scale Web services. **NAB** [24] The Numenta Anomaly Benchmark (NAB) is an open dataset created by Numenta company for evaluating the performance of time series anomaly detection algorithms.

**4.1.2 Baseline Methods.** To benchmark our model FCVAE against existing methods, we chose the following approaches for evaluation: SPOT [42], SRCNN [37], TFAD [54], DONUT [50], Informer [60], Anomaly-Transformer [51], AnoTransfer [55], VQRAE [21]. SPOT represents a traditional statistical method rooted in extreme value theory. SRCNN and TFAD are supervised methods relying on high-quality labels. Donut, VQRAE, and AnoTransfer are unsupervised reconstruction-based methods utilizing VAE for normal value reconstruction. Informer is an unsupervised prediction-based method that endeavors to predict normal values using an attention mechanism. Anomaly-Transformer is an unsupervised anomaly detection method leveraging the transformer architecture.

**4.1.3 Evaluation Metrics.** In practical applications, operators tend to be less concerned with point-wise anomaly detection, i.e., whether each individual point is classified as anomalous or not, and focus more on detecting continuous anomalous segments in time series data. Moreover, due to the substantial impact of anomalous segments, operators aim to identify such segments as early as possible. To address these requirements, we adopt two metrics, best F1 and delay F1, which are based on the works of DONUT [50] and SRCNN [37], respectively.

Best F1 is obtained by traversing all possible thresholds for anomaly scores, and subsequently applying a point adjustment strategy to the prediction in order to compute the F1 score. Delay F1 is similar to best F1 but employs a delay point adjustment strategy to



**Table 1: Performance on test data. P means precision, R means recall, F1 means best F1 and F1\* means delay F1.**

Method	Yahoo						KPI						WSD						NAB					
	P	R	F1	P	R	F1*	P	R	F1	P	R	F1*	P	R	F1	P	R	F1*	P	R	F1	P	R	F1*
SPOT[42]	0.572	0.328	0.417	0.572	0.328	0.417	0.966	0.221	0.360	0.911	0.077	0.143	0.947	0.315	0.472	0.887	0.137	0.237	0.992	0.713	0.829	0.992	0.713	0.829
SRCNN[37]	0.268	0.236	0.251	0.219	0.181	0.198	0.673	0.944	0.786	0.617	0.753	0.678	0.093	0.903	0.170	0.028	0.361	0.053	0.825	0.832	0.828	0.460	0.766	0.575
DONUT[50]	0.381	0.150	0.215	0.381	0.150	0.215	0.378	0.569	0.454	0.328	0.407	0.364	0.263	0.195	0.224	0.199	0.131	0.158	0.933	0.937	0.935	0.821	0.774	0.797
VQRAE[21]	0.706	0.399	0.510	0.691	0.381	0.492	0.202	0.418	0.272	0.167	0.117	0.137	0.518	0.233	0.312	0.241	0.066	0.103	0.990	0.882	0.933	0.806	1.000	0.893
Anotransfer[55]	0.902	0.413	0.567	0.575	0.437	0.496	0.815	0.591	0.685	0.557	0.394	0.461	0.695	0.654	0.674	0.331	0.444	0.379	0.962	0.968	0.965	0.837	0.908	0.871
Informer[60]	0.747	0.671	0.707	0.731	0.619	0.671	0.927	0.910	<b>0.918</b>	0.801	0.845	<b>0.822</b>	0.532	0.583	0.557	0.402	0.385	0.393	0.971	0.974	<b>0.973</b>	0.878	0.907	0.892
TFAD[54]	0.884	0.739	<b>0.805</b>	0.883	0.734	<b>0.802</b>	0.684	0.834	0.752	0.650	0.714	0.680	0.541	0.750	0.628	0.431	0.482	<b>0.455</b>	0.749	0.719	0.734	0.265	0.233	0.248
Anomaly-Transformer[51]	0.588	0.179	0.274	0.054	0.020	0.029	0.930	0.814	0.868	0.622	0.240	0.346	0.861	0.630	<b>0.728</b>	0.144	0.129	0.137	0.944	1.000	0.971	0.891	0.932	<b>0.911</b>
FCVAE	0.897	0.821	<b>0.857</b>	0.897	0.792	<b>0.842</b>	0.930	0.924	<b>0.927</b>	0.906	0.772	<b>0.835</b>	0.786	0.881	<b>0.831</b>	0.705	0.571	<b>0.631</b>	0.953	1.000	<b>0.976</b>	0.925	0.909	<b>0.917</b>

truth	0	0	1	1	1	0	1	1	1	1
predict	1	0	0	1	1	0	0	0	1	1
adjusted	1	0	1	1	1	0	1	1	1	1
delay adjusted	1	0	1	1	1	0	0	0	0	0

**Figure 8: Illustration of the adjustment strategy.**

transform the prediction. The adjustment strategies are illustrated in Figure 8, with a delay set to 1 as an example. The detector misses the second anomalous segment because it takes two-time intervals to detect this segment, exceeding the maximum delay threshold we established. We configure the delay for all datasets to be 7, except for Yahoo, where it is set to 3, and NAB, where it is set to 150. This is because the anomaly segments in Yahoo are very short, while in NAB, they are typically much longer, often spanning several hundred data points.

**4.1.4 Implementation Details.** To guarantee the widespread applicability, all the experiments described below were conducted under entirely unsupervised conditions, without employing any actual labels (all labels are set to zero). For consistency across all methods, we trained a single model for all curves within a dataset. Regarding hyperparameters, we conducted a grid search to identify the most effective parameters for different datasets. Additionally, we later evaluated the sensitivity of these parameters to ensure robust performance.

## 4.2 Overall Performance

The performance of FCVAE and baseline methods across the four datasets is depicted in Table 1. Our method surpasses all baselines on four datasets regarding best F1 by 6.45%, 0.98%, 14.14% and 0.31%. In terms of delay F1, our method outperforms all baselines on four datasets by 4.98%, 1.58%, 38.68% and 0.65%.

The performance of various baseline methods on the datasets exhibits considerable variation. For instance, SPOT [42] does not excel on most datasets, as it erroneously treats extreme values as anomalies, whereas anomalies are not always manifested as such. SRCNN [37] is a reasonably proficient classifier, yet its performance falls short compared to most other models. This underscores the fact that implicitly extracting abnormal features is challenging. Informer [60] outperforms most other baselines across different datasets, as many anomalies exhibit notable value jumps, and prediction-based methods can effectively manage this situation. However, it

struggles with anomalies induced by frequency changes. Anomaly-Transformer [51] attains commendable results on most datasets in terms of best F1 but demonstrates a low delay F1. It detects anomalies based on the relationships with nearby points, and only when the anomalous point is relatively central within the window can it easily capture the correlation. Conversely, TFAD [54] achieves favorable results on various datasets but exhibits a certain delay in detection.

Moreover, our method surpasses DONUT [50] and VQRAE [21] in terms of reconstruction-based methods. Although VQRAE [21] introduces numerous modifications to the VAE, employing RNN to capture temporal relationships, our method still outperforms it. This finding implies that for UTS anomaly detection, it is imperative to incorporate only key information while avoiding overloading the model with superfluous data.

## 4.3 Different Types of Conditions in CVAE

We conduct experiments under identical settings to evaluate different types of conditions. The chosen conditions encompass information potentially useful for time series anomaly detection within the scope of our understanding, including timestamps [55], time domain information, and frequency domain information. To ensure consistency, we apply the same operation on the time domain information as we do on the frequency domain information.

As illustrated in Figure 9(a), the performance of employing the frequency information as a condition surpasses that using the timestamp or time domain information. This can be readily comprehended, as timestamps carry limited information and typically require one-hot encoding, resulting in sparse data representation. Time domain information is already incorporated in VAE, and utilizing it as a condition may lead to redundant information without significantly benefiting the reconstruction. Conversely, **frequency information, as a valuable and complementary prior, rendering it a more effective condition for anomaly detection.**

## 4.4 Frequency VAE and FACVAE

Is CVAE the optimal strategy for harnessing the frequency information in anomaly detection? In this study, we compare FCVAE with an improved frequency-based VAE (FVAE) model, in which the frequency information is integrated into VAE along with the input to reconstruct the original time series. As depicted in Figure 9(b), FCVAE surpasses FVAE. This outcome can be attributed to two primary reasons. Firstly, CVAE, due to its unique architecture that incorporates conditional information, intrinsically outperforms VAE

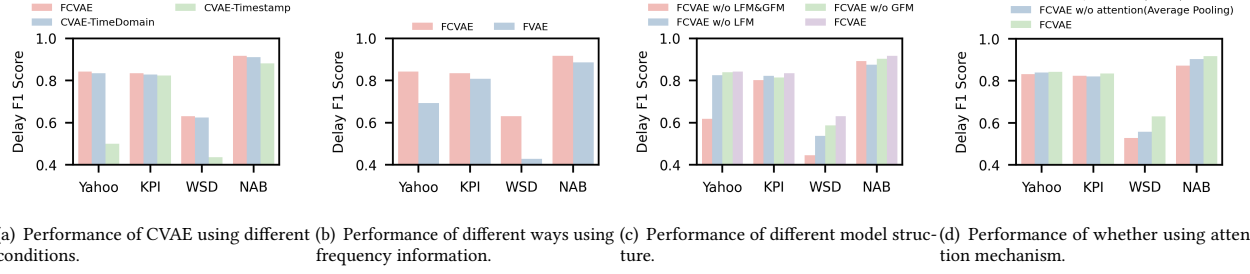


Figure 9: Delay F1 score of different settings.

in numerous applications. Secondly, FVAE does not fully exploit frequency information. Although it incorporates this additional information, it still lacks efficient utilization in practice, particularly in the decoder. Consequently, **the CVAE that incorporates the frequency information as a condition represents the most effective structure known to date.**

#### 4.5 GFM and LFM

We propose GFM and LFM to extract global and local frequency information, respectively. However, do these two modules achieve our intended effects through their designs? Additionally, it is worth noting that GFM and LFM may overlap to some degree. Thus, we would like to determine if combining the two can further enhance the performance.

We conduct experiments and the results are depicted in Figure 9(c). It can be observed that, across the four datasets, employing either LFM or GFM in FCVAE outperforms the VAE model under identical conditions of other settings except for NAB, where the frequent oscillation of data results in inconsistency between the information extracted from GFM and the data value of the current time. For all datasets, when both LFM and GFM modules are utilized concurrently, they synergistically enhance each other, resulting in superior performance. Consequently, **both global and local frequency information play a crucial role in detecting anomalies.**

#### 4.6 Attention Mechanism

It is crucial to discern whether the enhancement in LFM stems from the reduced window size or the attention mechanism. Thus, we perform experiments by excluding the attention operation from LFM while keeping GFM unaltered. Specifically, we utilized frequency information either from the latest small window in LFM (Latest) or from the average pooling of frequency information across all small windows in LFM (Average Pooling).

The findings in Figure 9(d) demonstrate that without attention, it is impossible to attain the original performance of FCVAE since it is not feasible to determine the specific weight of each small window in advance. However, **the attention mechanism effectively addresses this issue by assigning higher weights to more informative windows.**

We present a comprehensive explanation of the attention mechanism in LFM using a case. A specific data segment, denoted by the

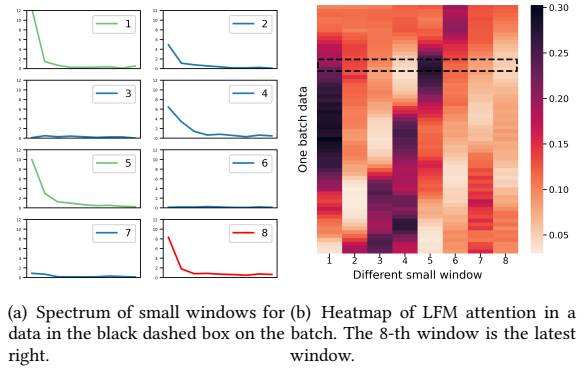


Figure 10: An example of attention mechanism in LFM.

black dashed box in Figure 10(b), is selected and all small windows produced by LFM’s sliding window module are transformed into the frequency domain to obtain their spectra. As illustrated in Figure 10(a), the 5-th (green) and the 8-th (red) windows exhibit the highest similarity, where the 8-th window serves as the query  $Q$  for our attention. Upon examining Figure 10(b), it can be observed that the heat value of the 5-th window is the highest, which corresponds with the findings in Figure 10(a).

#### 4.7 Key Techniques in Framework

In this section, we evaluate the effectiveness of our novel data augmentation technique, masking the last point, and the application of CM-ELBO on four distinct datasets. The results are presented in Table 2. Based on the results, it is clear that CM-ELBO plays the most crucial role in most datasets, which aligns with our expectations. This is because it can tolerate abnormal or missing data to a certain extent. Furthermore, masking the last point has a substantial impact on the results, as when an anomaly occurs at the last point of the window, it affects the entire frequency information. Effectively masking this point resolves the issue and improves the detection accuracy. Data augmentation, on the other hand, introduces some artificial anomalies to boost the performance of CM-ELBO, particularly in unsupervised settings.

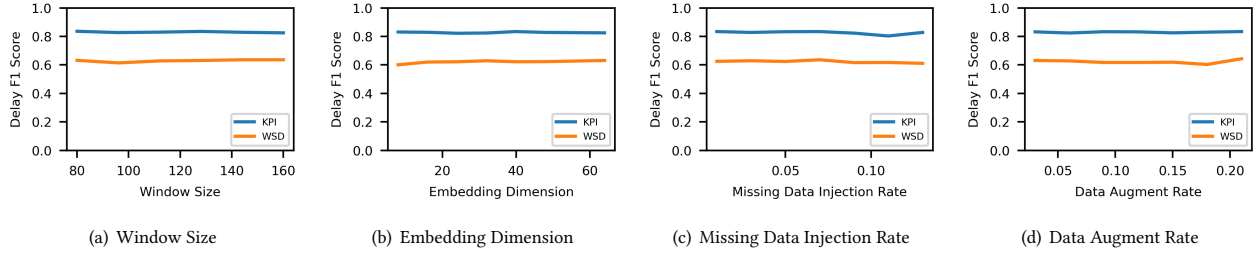


Figure 11: Delay F1 score of different settings.

Table 2: Delay F1 of different settings.

Variants	Yahoo	KPI	WSD	NAB
w/o data augment	0.841	0.825	0.626	0.904
w/o mask last point	0.835	0.830	0.534	0.877
w/o CM-ELBO	0.690	0.757	0.435	0.897
<b>FCVAE</b>	<b>0.842</b>	<b>0.835</b>	<b>0.631</b>	<b>0.917</b>

#### 4.8 Parameter Sensitivity

The stability of a model to different parameters is an important aspect to consider, and therefore we test the sensitivity of our model parameters on two datasets, KPI and WSD. We examine four aspects: the dimension of the condition, the window size, the proportion of missing data injection, and the proportion of data augmentation. The results, shown in Figure 11, indicate that our model can achieve stable and excellent results under different parameter settings.

### 5 PRODUCTION IMPACT AND EFFICIENCY

FCVAE has been incorporated as a crucial component in a large-scale cloud system that caters to millions of users globally [6, 18, 19]. The system generates billions of time series data points on a daily basis. The FCVAE detects anomalies in the cloud system, with the primary goal of identifying any potential regressions in the system that may indicate the occurrence of an incident[11, 13, 53, 58].

Table 3: Online performance of FCVAE in production compared to legacy detector. F1 and F1\* are defined in Table 1.

Baseline		FCVAE		Improvement		Inference efficiency [points/second]
F1	F1*	F1	F1*	F1	F1*	
0.66	0.63	0.73	0.69	10.9%	11.1%	1195.7

Table 3 presents the online performance improvement achieved by employing FCVAE over a period of one year. The experiments were conducted on a 24GB memory 3090 GPU. The results demonstrate substantial enhancements in both Best F1 and Delay F1 compared to the legacy detector. This underscores the effectiveness and robustness of our proposed method. Furthermore, our model is lightweight and highly efficient, capable of processing over 1000 data points within 1 second. This far exceeds the speed at which the system generates new temporal points.

## 6 RELATED WORK

**Traditional statistical methods** [31, 34, 36, 39, 44, 45, 57] are widely used in time series anomaly detection because of their great advantages in time series data processing. For example, SPOT [42] considers that some extreme values are abnormal, therefore, detects them through Extreme Value Theory [9].

**Supervised methods** [23, 30, 37, 58] mostly learn the features of anomalies and identify them through classifiers based on the features learned. Opprentice [30] efficiently combines the results of many detectors through random forest. Some methods [3, 54] obtain pseudo-labels through data augmentation to enhance the learning ability.

**Unsupervised methods** are mainly divided into reconstruction-based and prediction-based methods. Reconstruction-based methods [5, 7, 21, 26, 28, 50] learn low-dimensional representations and reconstruct the “normal patterns” of data and detect anomalies according to reconstruction error. Prediction-based methods [17, 41, 60] try to predict the normal values of metrics based on historical data and detect anomalies according to the prediction error. In recent years, transformer-based methods[51] have been widely proposed. Some methods [48, 61] have begun to solve some practical problems from the frequency domain. Moreover, many transfer learning methods have been proposed[12, 26, 55, 56].

## 7 CONCLUSION

Our paper presents a novel unsupervised method for detecting anomalies in UTS, termed FCVAE. At the model level, we introduce the frequency domain information as a condition to work with CVAE. To capture the frequency information more accurately, we propose utilizing both GFM and LFM to concurrently capture the features from global and local frequency domains, and employing the target attention to more effectively extract local information. At the architecture level, we propose several new technologies. We carry out experiments on four dataset and an online cloud system to evaluate our approach’s accuracy, and comprehensive ablation experiments to demonstrate the effectiveness of each module.

## 8 ACKNOWLEDGMENTS

This work was supported in part by the National Key Research and Development Program of China (No.2021YFE0111500), in part by the National Natural Science Foundation of China (No.62202445), in part by the State Key Program of National Natural Science Foundation of China under Grant 62072264.



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