

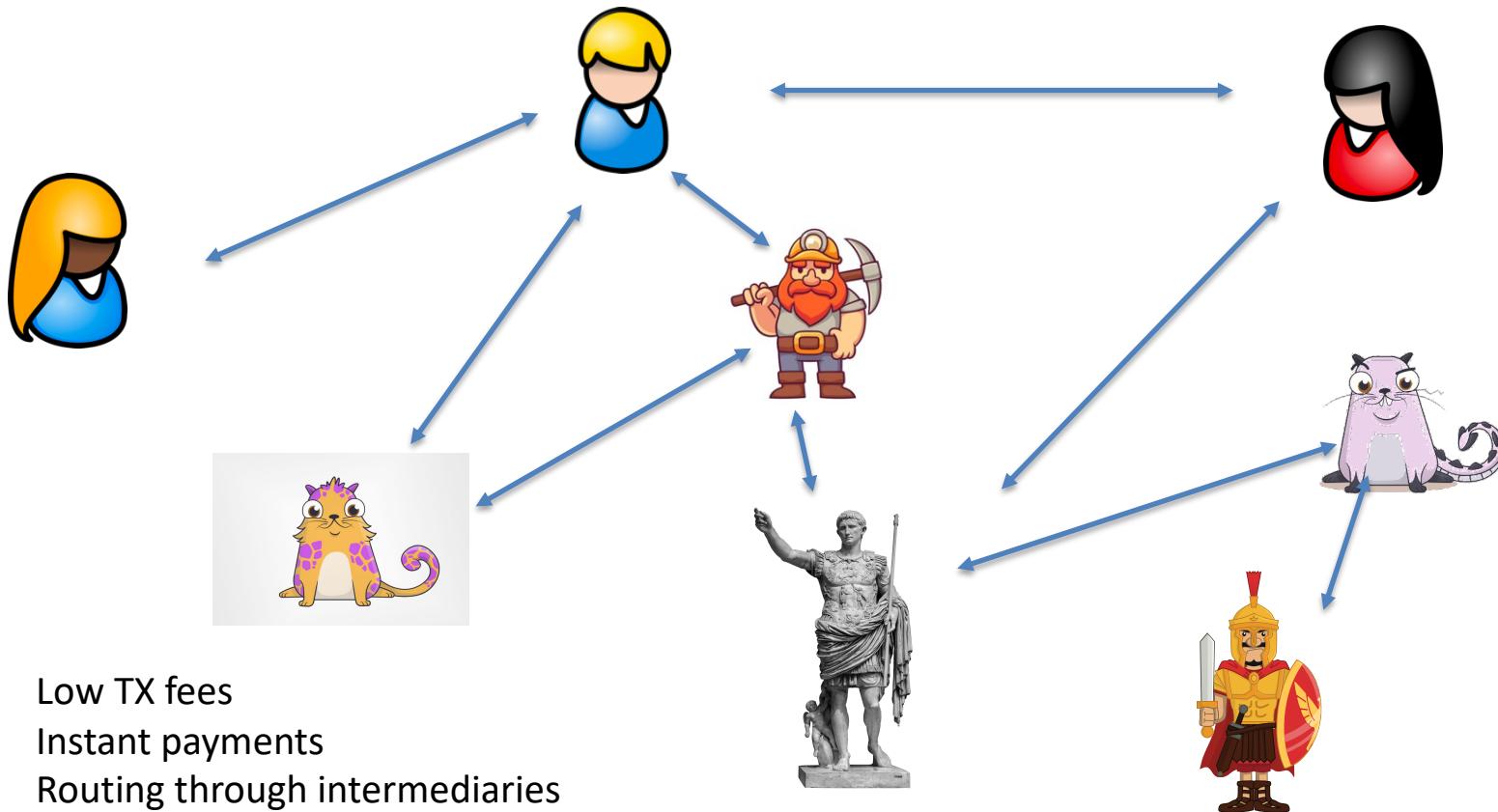
CS251 Fall 2021
(cs251.stanford.edu)



Scaling II: Rollup

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Lightning network



Downsides of Payment/State Channels

- Everyone needs to be online
 - Mitigated by watchtowers
 - Hubs need to be online
- Capital is locked up
 - Funds in one channel can't be used in different channel
 - If network is separated transactions are not possible
- Only Peer to Peer payments
 - No multi party contracts channels
- TX to fund/close

Blockchain Layers

Layer 3: user facing tools (cloud servers)

Layer 2: applications (DAPPs, smart contracts)

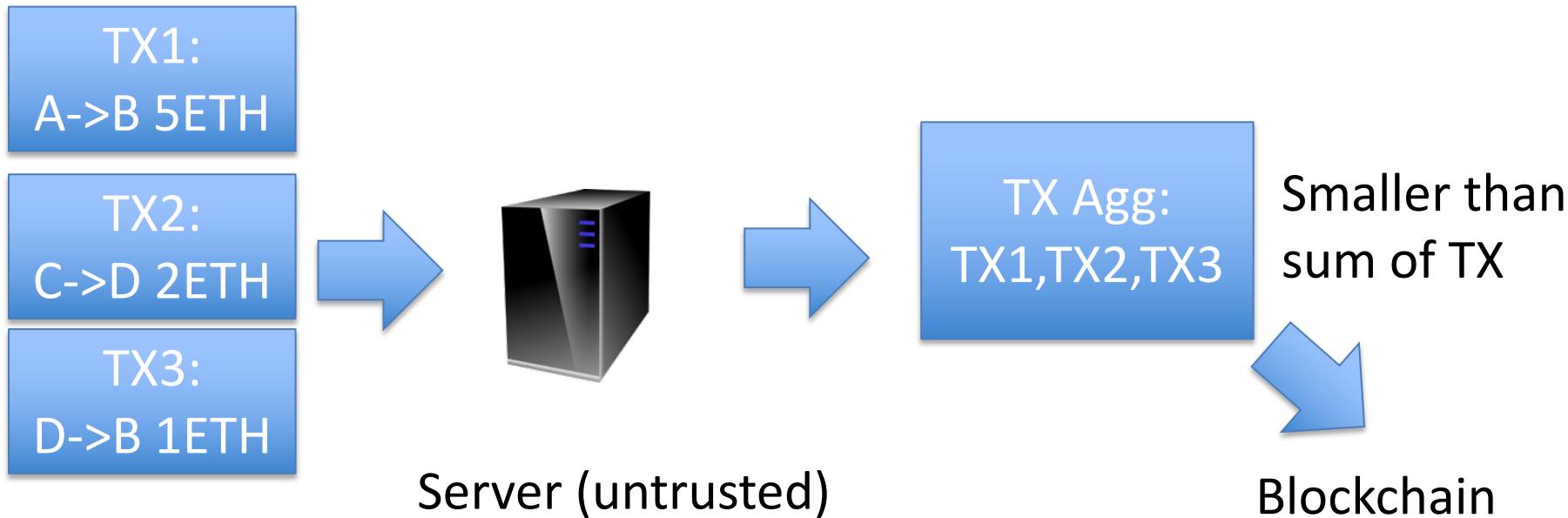
Layer 1.5: compute layer (blockchain computer)

Layer 1: consensus layer

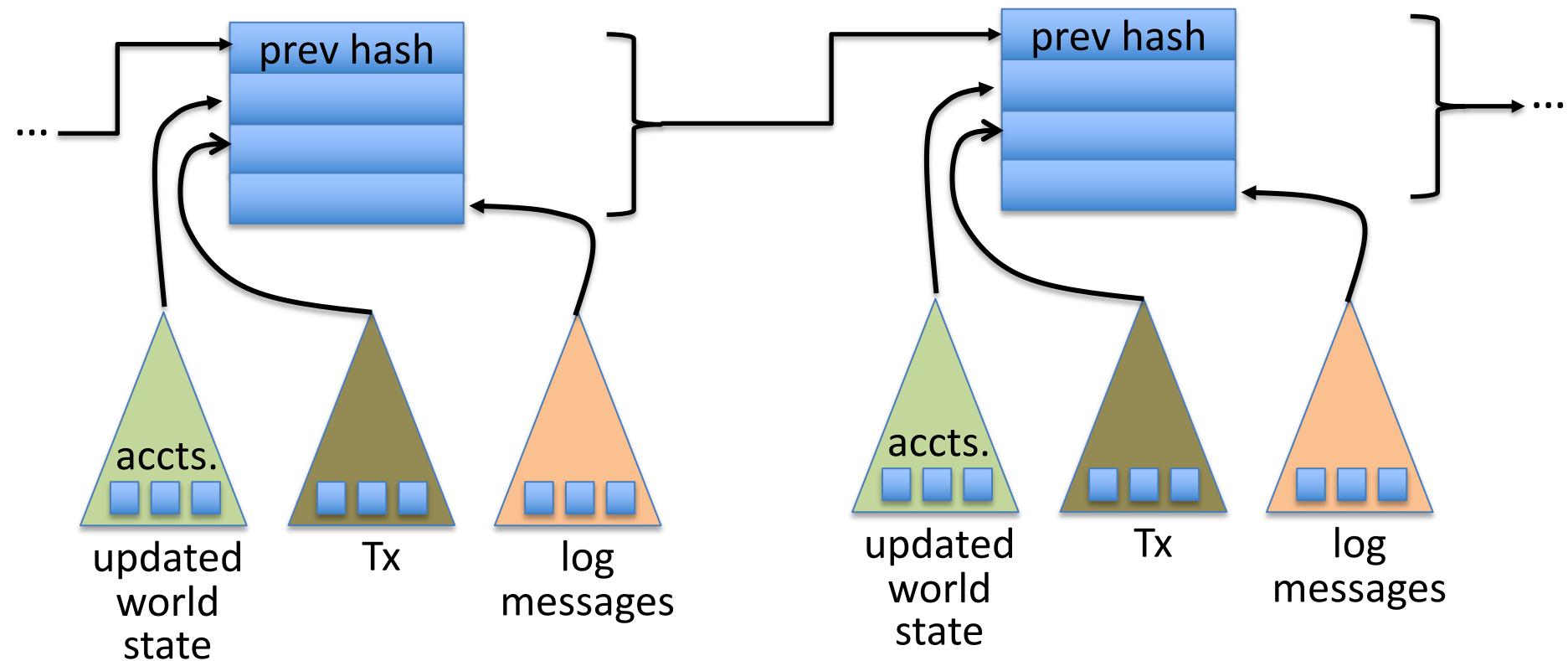
Bitcoin/Ethereum combine ordering (layer 1) and verification (1.5)
What if we can outsource verification? Makes consensus cheaper

Idea: Aggregate Transactions

- Payment channels move more transactions offchain
- Idea: Combine Transaction, Rollup Server verifies



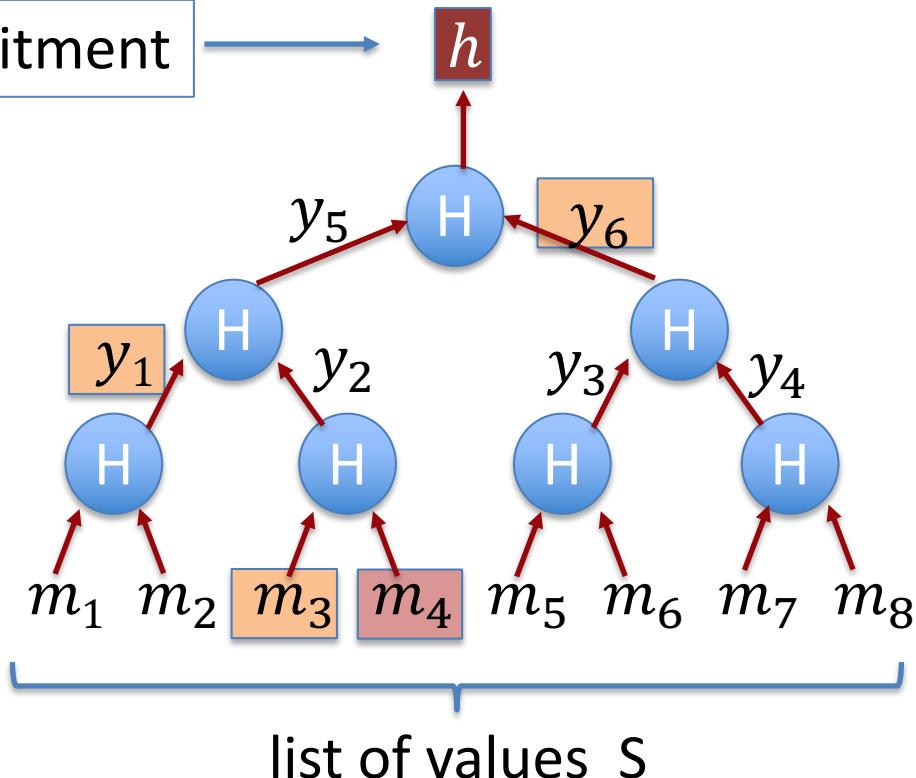
Recap: The Ethereum blockchain



Recap: Merkle tree

(Merkle 1989)

commitment



Goal:

- commit to list S
- Later prove $S[i] = m_i$

To prove $S[4] = m_4$,
proof $\pi = (m_3, y_1, y_6)$

length of π : $\log_2 |S|$

Recap State Commitment

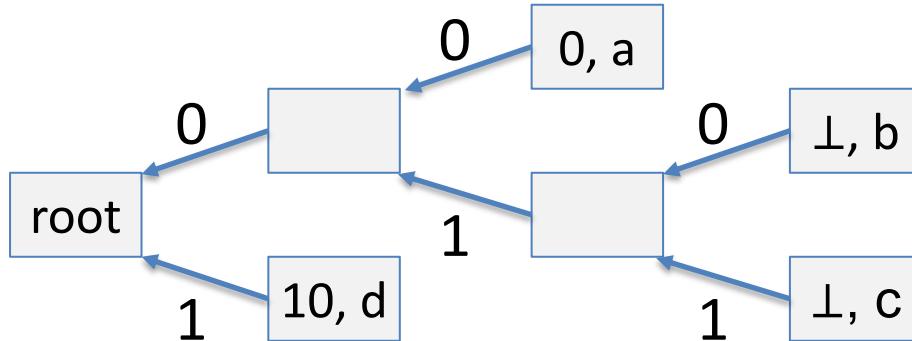
Every contract has an associated **storage array $S[]$** :

$S[0], S[1], \dots, S[2^{256}-1]$: each cell holds 32 bytes, init to 0.

Account storage root: **Merkle Patricia Tree hash of $S[]$**

- Cannot compute full Merkle tree hash: 2^{256} leaves

$S[000] = a$
 $S[010] = b$
 $S[011] = c$
 $S[110] = d$



time to compute
root hash:
 $\leq 2 \times |S|$

$|S| = \# \text{ non-zero cells}$

Merke (Patricia) Tree Proofs

- Logarithmic in tree height
- Given proof for $i \rightarrow$ Possible to update $S[i]$ and recompute root
- Given proof for i , proof for j and update of $S[j]$ it's possible to update proof for $S[i]$
- Exclusion proofs possible in Patricia Trees

Rollup



Users



Server

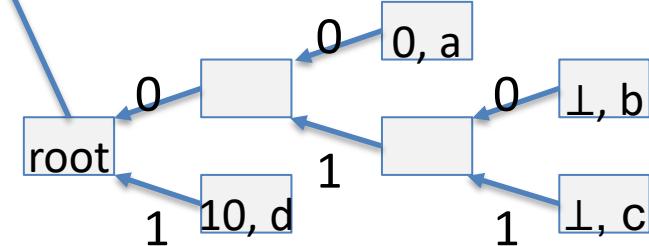
Rollup State S

$S[A's\ PK] = \{3\ ETH, nonce\}$
 $S[B's\ PK] = \{2\ ETH, nonce\}$
 $S[C's\ PK] = \{10\ ETH, nonce\}$
 $S[D's\ PK] = \{1\ ETH, nonce\}$



Rollup Smart Contract

Stores S



Rollup Deposit



Users

TX Deposit:

Proof that A's PK $\notin S$ given root

3 ETH transfer



Rollup Smart Contract root

1. Checks Proof
2. Updates root such that
 $S[A's\ PK] = \{3\ ETH, 0\}$

Rollup Withdraw



Users

TX Withdraw:

Proof that $S[A's\ PK] = \{3\ ETH, nonce\}$

given root

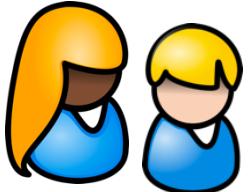
Destination Address NewA

Signature by A

Rollup Smart Contract root

1. Checks Proof
2. Checks Signature
3. Sends 3 ETH to NewA

Rollup Transfer



TX Transfer

Users

TX Transfer:

Proof that given root

$S[\text{A's PK}] = \{3 \text{ ETH}, 0\}$

$S[\text{B's PK}] = \{2 \text{ ETH}, 0\}$

Transfer amount 2 ETH

Signature by A



Rollup Smart Contract

root

1. Checks Proofs
2. Checks Signature
3. Set
 1. $S[\text{A's PK}] = \{1 \text{ ETH}, 1\}$
 2. $S[\text{B's PK}] = \{4 \text{ ETH}, 1\}$

Space saved but
no computation

SNARK

```
3     function validatePatriciaProof(
4         bytes32 rootHash,
5         bytes memory key,
6         bytes memory value,
7         bytes[] memory path
8     ) pure returns (bool accept) {
9         uint myKeyOffset = 0;
```



Provides Proof/SNARK that given given public inputs (rootHash, key, value) it knows private inputs (path) such that function outputs true

SNARK is short/easy to check

SNARK: a Succinct ARgument of Knowledge

A succinct preprocessing argument system is a triple (S, P, V) :

- $S(C) \rightarrow$ public parameters (S_p, S_v)



```
3   function validatePatriciaProof(  
4     bytes32 rootHash,  
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7     bytes[] memory path  
8   ) pure returns (bool accept) {  
9     uint walkKeyOffset = 0;
```

proof π ; $|\pi| = O(\log(|C|), \lambda)$

$|\pi| = 500$ bytes
 $\text{time}(V) = 500k$ Gas

verify ;

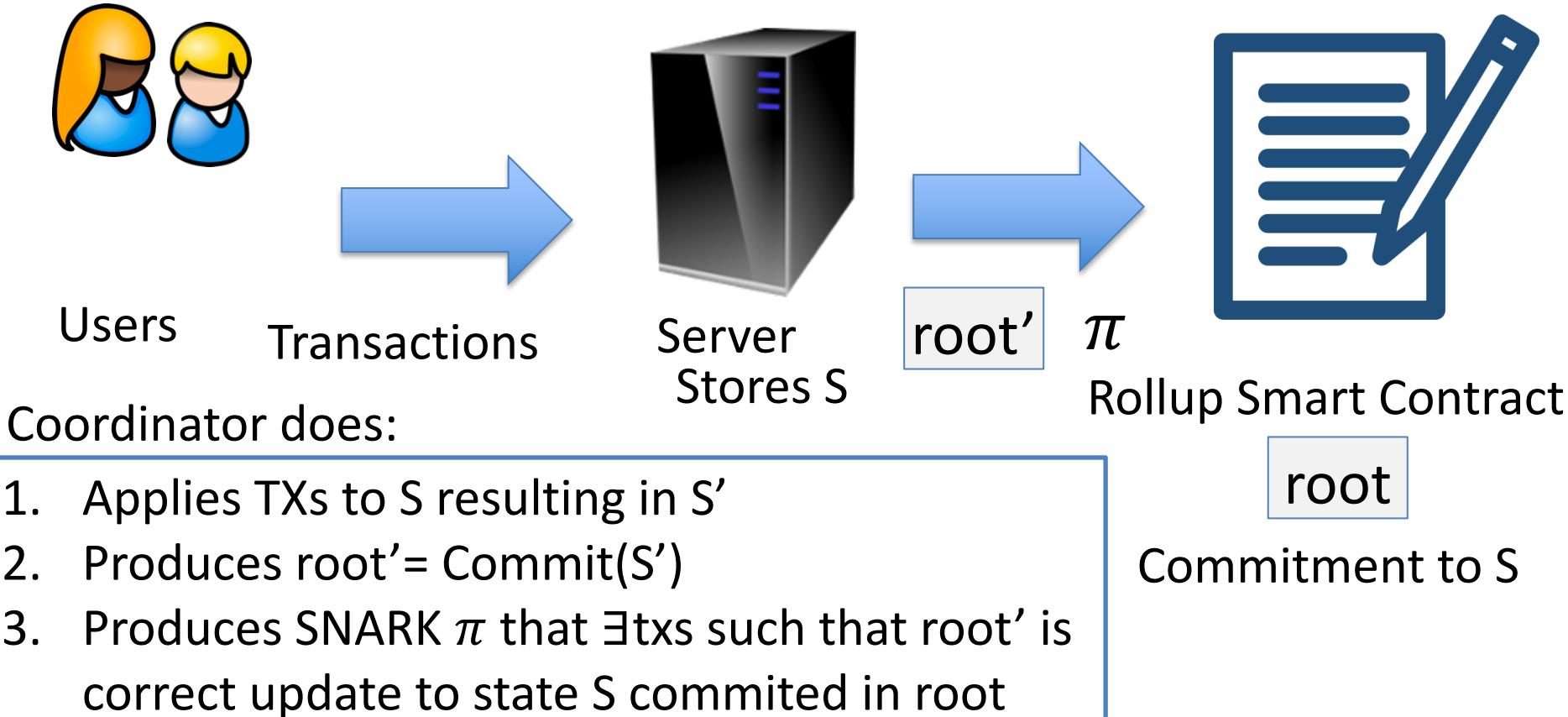
$\text{time}(V) = O(|x|, \log(|C|), \lambda)$

If (S, P, V) is **succinct** and **zero-knowledge** then we say that it is a **zk-SNARK**

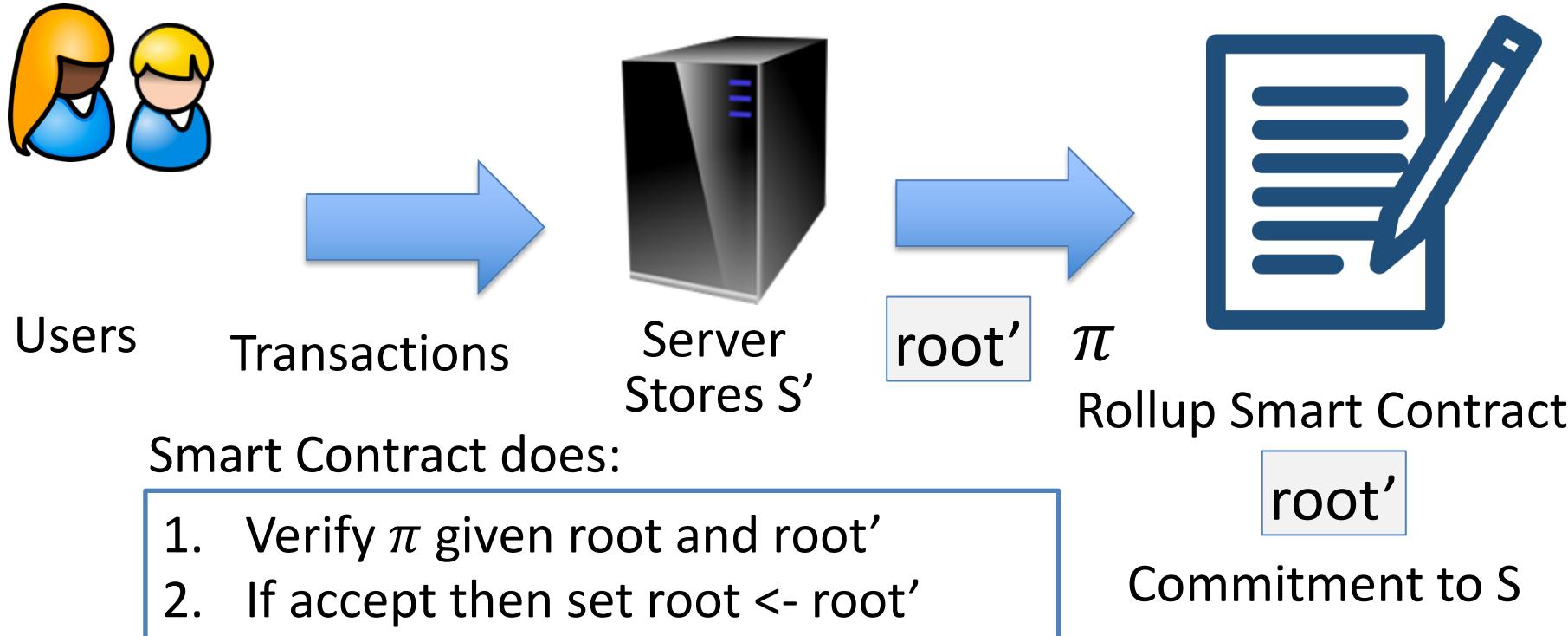
ZKRollup

- Merkleize Transactions
- SNARK proves that given transactions I know signatures such that state transition $S \rightarrow S'$ valid
- Publish transaction diff on chain.
- No signatures per transaction.
- 500k gas + data cost for on chain diff

ZKRollup (Validity Rollup)

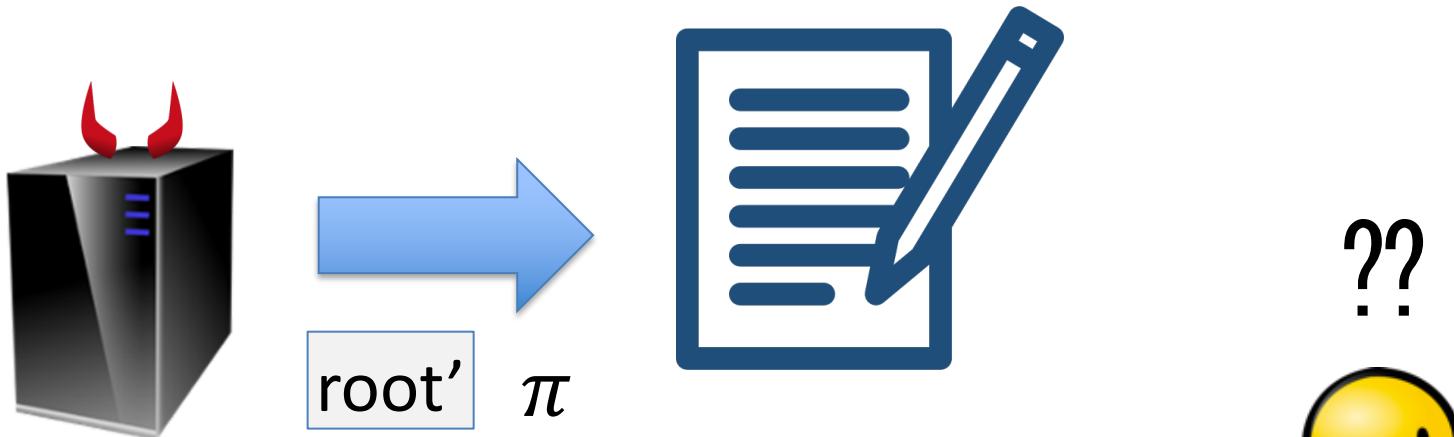


ZKRollup



Smart contract still allows “manual” withdrawals

Data Availability Problem

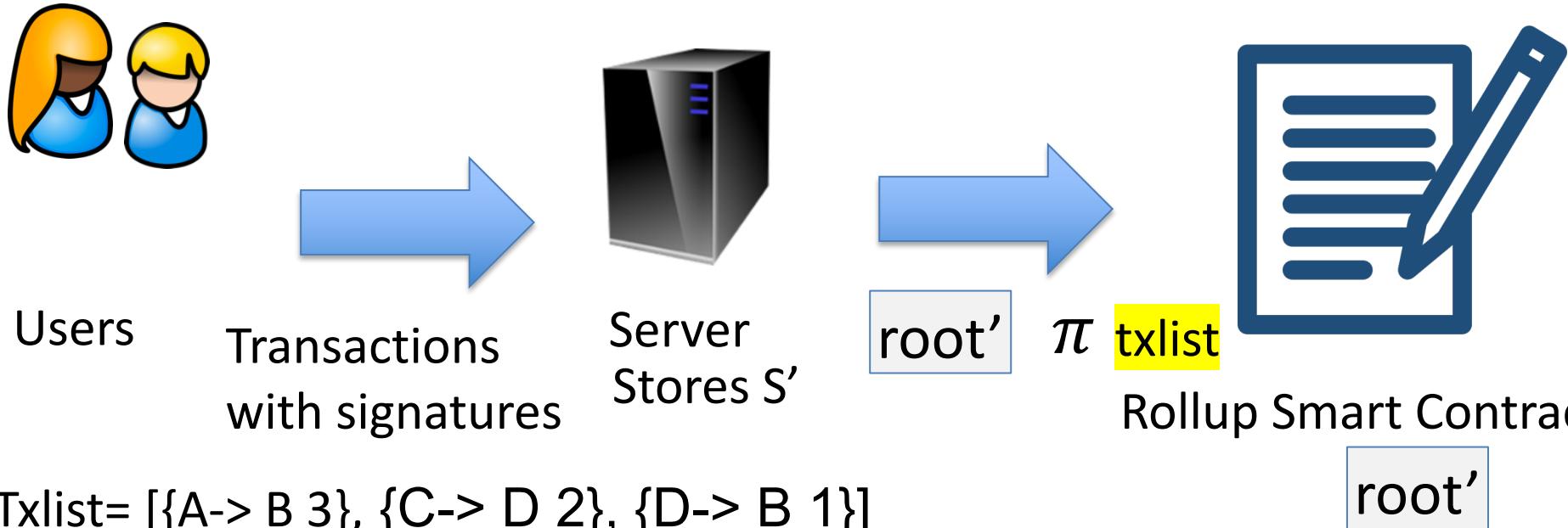


Update must be valid!

What if Server does not reveal
data?

Can't update Merkle proofs
Can't withdraw!

Publish diff on chain



$\text{Txlist} = [\{A \rightarrow B\ 3\}, \{C \rightarrow D\ 2\}, \{D \rightarrow B\ 1\}]$

No signatures, Sender, Receiver, Amount only in Calldata (not stored)

<100bytes per tx ~400 gas/tx, SNARK verification ~1500 gas/tx (if full)

Full Block 3600 rollup tx vs 570 normal tx (6x speedup)

zkRollup stats

- ZKRollup is cheaper than onchain tx
- Can scale to max ~300tx/s now, 1000tx/s soon
- Vs. max 40-50tx/s on mainnet
- Cost dominated by SNARK verification
 - Will get cheaper precompiles
- Finality ~ Blockchain finality (no instant transfer)

Multiple Assets

Very easy to support many assets

Simply add asset field to TX

Hardly increases SNARK complexity

Txlist= [{A-> B 3 ETH}, {C-> D 2 DAI}, {D-> B 1 BAT}]

1 byte → 256 assets

2 bytes → 65k assets

Transaction List/Atomic Swaps

Support transaction list that are executed together

Transactions need to be signed by all senders

Can't execute part of transaction only all together!

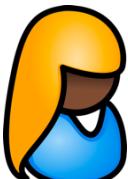
Enables atomic swaps: Alice swaps with Bob 3 ETH for 2 DAI

Txlist= [{A-> B 3 ETH and B-> A 2 DAI}, {D-> B 1 BAT}]

Exchanges



Buy 3 ETH for 5 DAI



Sell 3 ETH for 5 DAI



Exchanges match orders
Classical exchanges also store funds

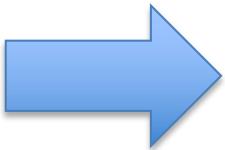
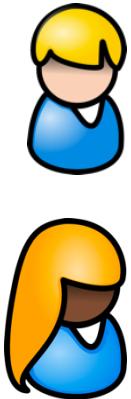
Order book

give

get

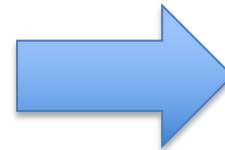
Alice	3	ETH	5	DAI
Bob	5	DAI	3	ETH
Carol	4	BAT	10	DAI

Rolled up Exchange



Submit orders

Has orderbook
Matches orders
Rolls up
transactions as
atomic swaps



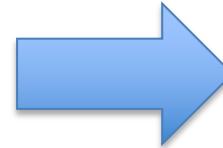
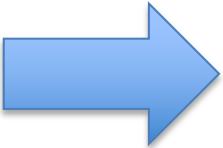
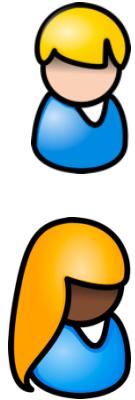
Txs Root, π

Verifies TX

Root of balance tree

Exchange trusted for
honest matching

Rolled up Exchange v2



Submit orders

Updates orderbook tree
on chain and proves
correct matching

Txs Root, π

Verifies TX

Root of balance tree
Root of orderbook tree

Benefit: No trust

Downside: Every order creates rollup TX, No instant matching

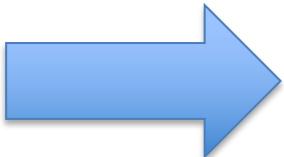
Rolling up Smart Contracts

- zkRollup works best for simple transfers
- zkRollup for the EVM?
 - Roll up generic smart contract transactions?
 - Create SNARK where the circuit implements the EVM
 - More expensive on the server
 - Soon to be a reality for a subset of the EVM (zkEVM)
- Can we support smart contract rollups today?

Optimistic Rollup



Users



Transactions
with signatures



Server
Stores S'



root'

π txlist



Rollup Smart Contract

root'

What if we remove the SNARK?

Idea: Instead of proving correctness, prove fraud!

New Role: Validator checks correctness, provides fraud proofs



Optimistic Rollup

- Server updates transaction root
- Server puts a large bond into escrow
- If transaction update is invalid users/validators provide *fraud proof*
- Successful fraud proof means bond gets *slashed*
 - Part to validator providing proof part gets burned
- Unsuccessful fraud proof costs validator money
- **How to proof fraud?**

Fraud Proofs



Server

root

Commits to state S

txlist

root'



Validator

1. Stores S agrees on root
2. Applies txlist to S to compute S'
3. Computes root'' from S'
4. If $\text{root}' \neq \text{root}''$ call “Fraud”

Problem: Validator doesn't know what's in root'

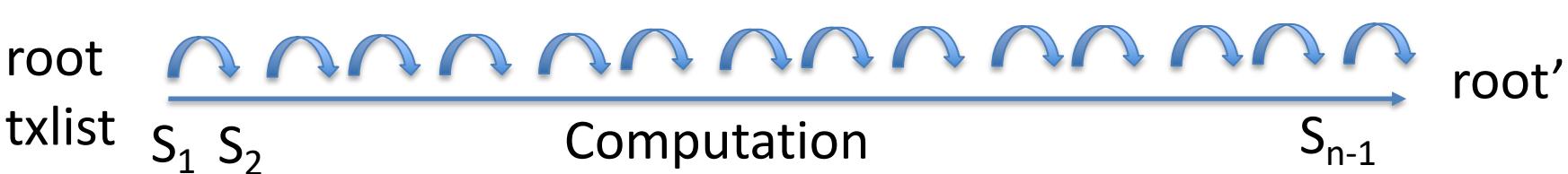
Referee Delegation

Idea: Server and Validator find first point of disagreement



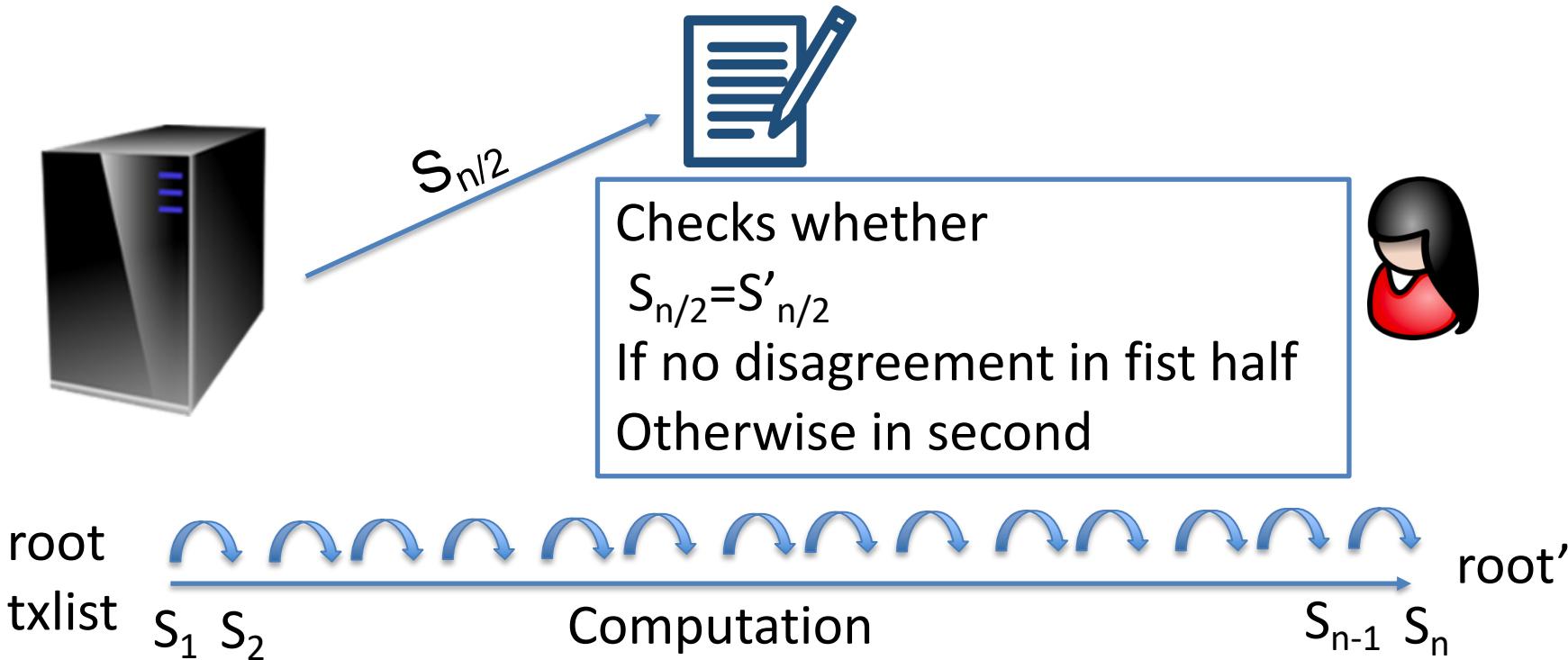
Break down computation of S' into small steps, e.g. cycles on a VM
Validator does the same

Let S_i be Server's intermediate states and S'_i the validator's



Referee Delegation

Server and Validator run interactive binary search



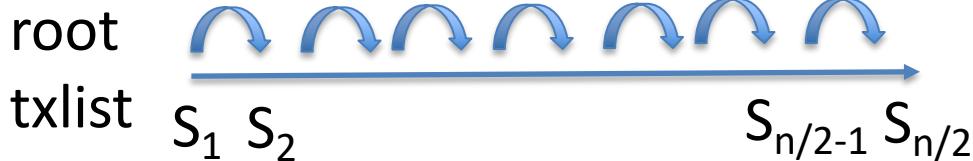
Referee Delegation



Repeat protocol for $\log_2(n)$ steps
End with agreement on S_i and
disagreement on S_{i+1} and S'_{i+1}



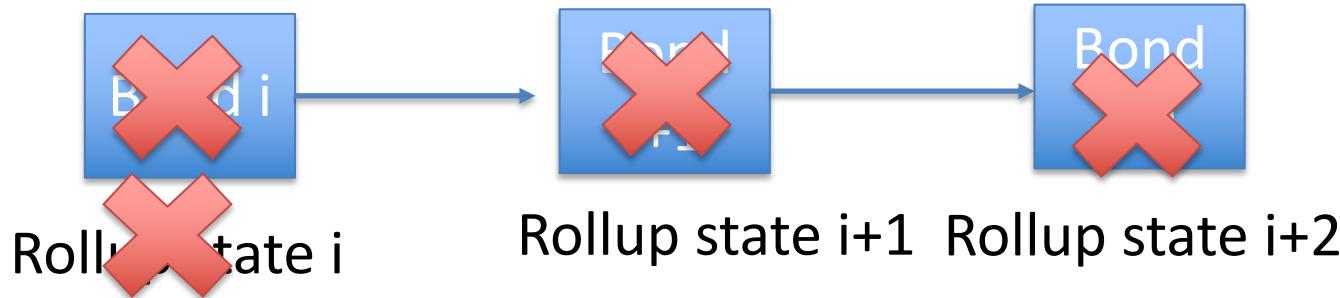
Smart Contract checks transition between S_i and S_{i+1} and declares winner



Problem: Checks take a long time

- $\log_2(n)$ messages (1 hash per message)
- 1 Verification step on smart contract
- If either party timeouts declares winner
- Looser gets *slashed*, Winner rewarded
- Problem: $\log_2(n)*\text{timeout}$
- No incentive to cheat
- But: Long wait till finalization! (7 days)

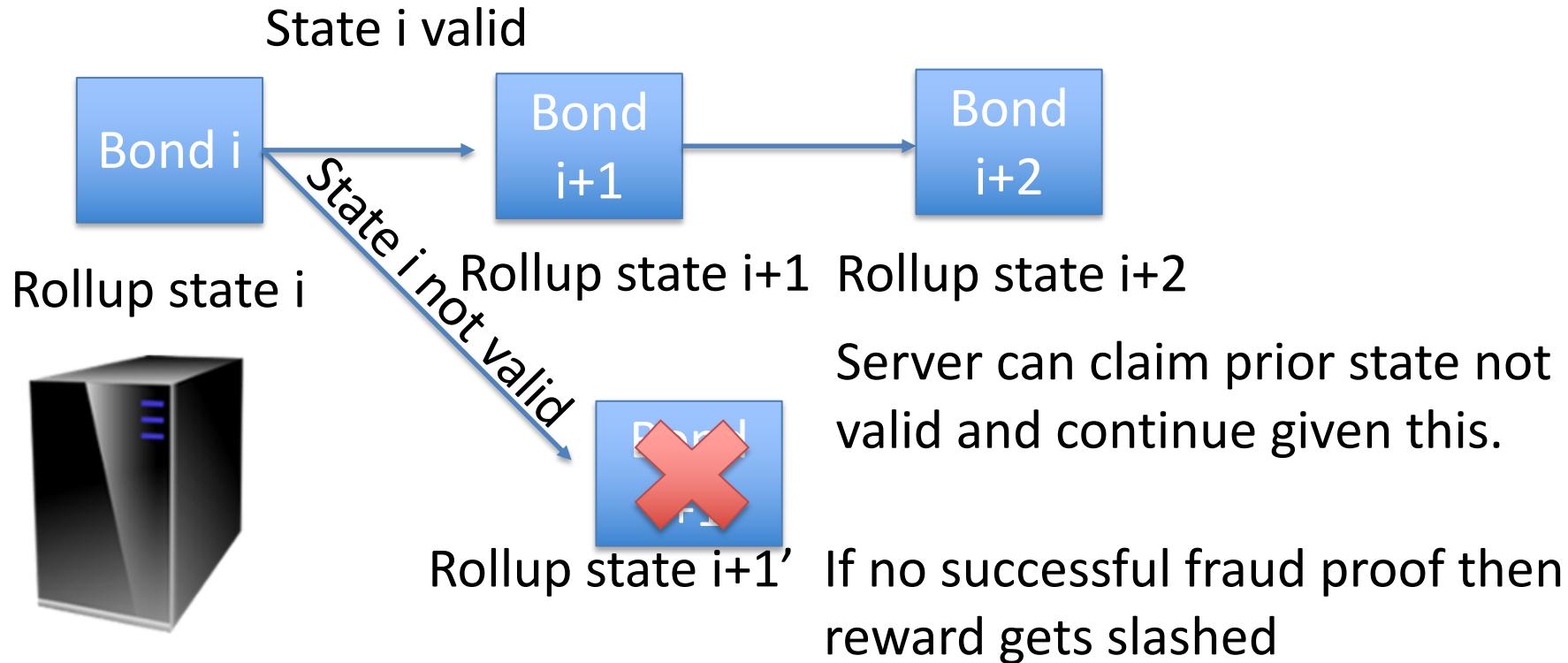
Pipelined Assertions



Server can build on states
before timeouts

If prior state invalid, all
subsequent bonds are slashed

Pipelined Assertions



Insurance of Rollup -> Instant Finality

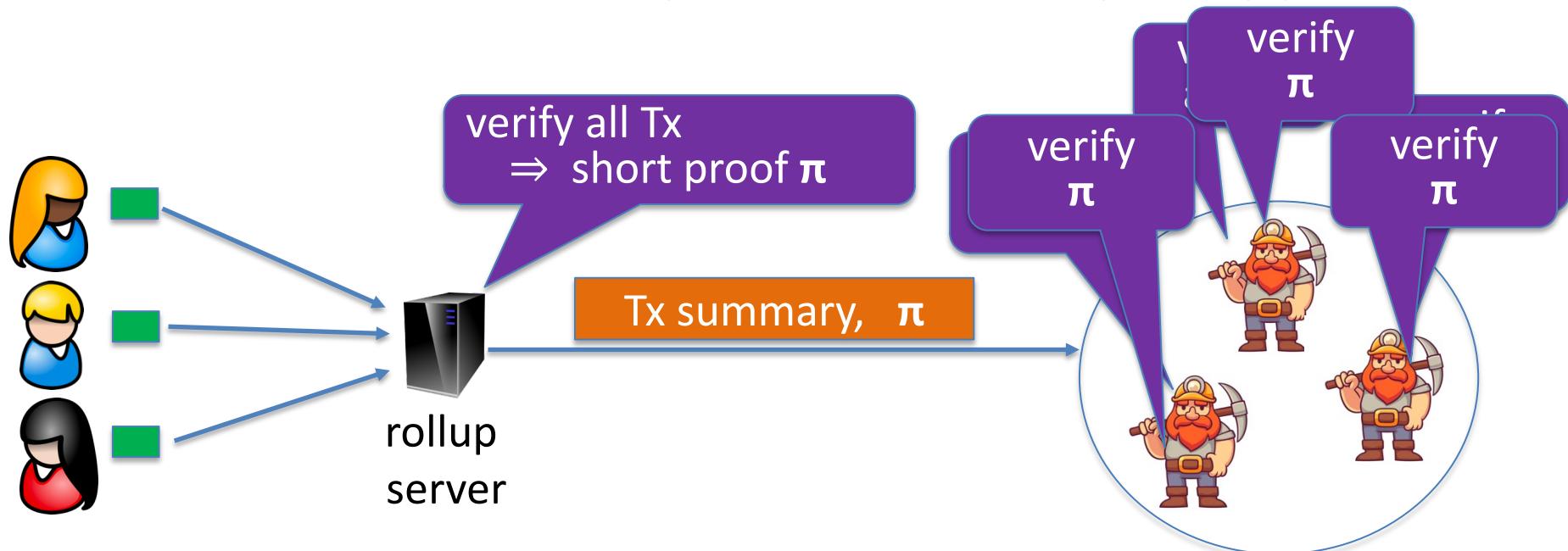
- Rollup is not instant (unlike lightning)
- But if server is trusted then giving them transaction -> finality
- Idea: Use insurance to achieve finality
- Server signs insurance
- If transaction not included in next (few) blocks insurance can be used to get insurance premium
- Works for zk and optimistic rollup
- Does not work for NFTs (directly)

Optimistic Rollup

- Live and implemented (Optimism and Arbitrum)
- You can port arbitrary smart contracts (OVM)
- Works well if honest rollup server
 - Fraud proofs protection if malicious server
- Up to ~4000 tx/s on ETH 1.0
- Important that one independent validator exists
- 7 day finality wait

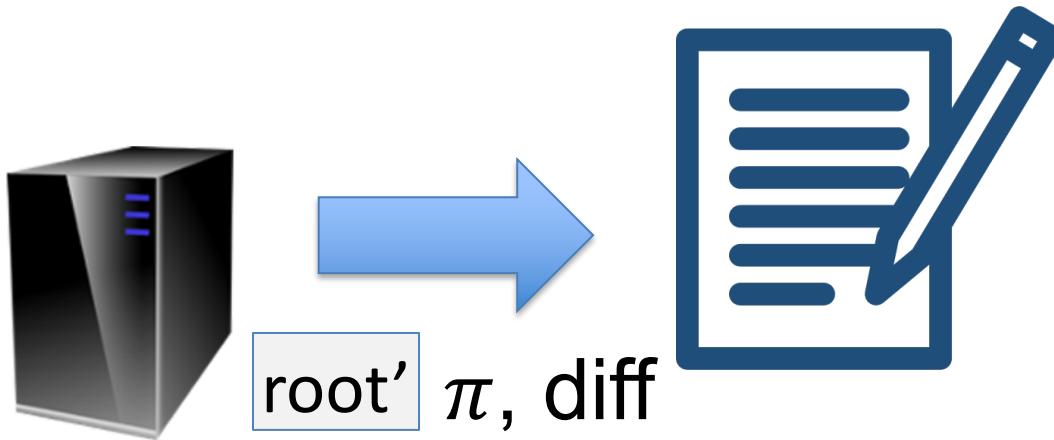
A combined view of rollups

Standard L1 chains: every miner must verify every posted Tx



Rollup server: compresses a thousand Tx into one on-chain proof (SNARK or Fraud)

Data Availability



Update must be valid!

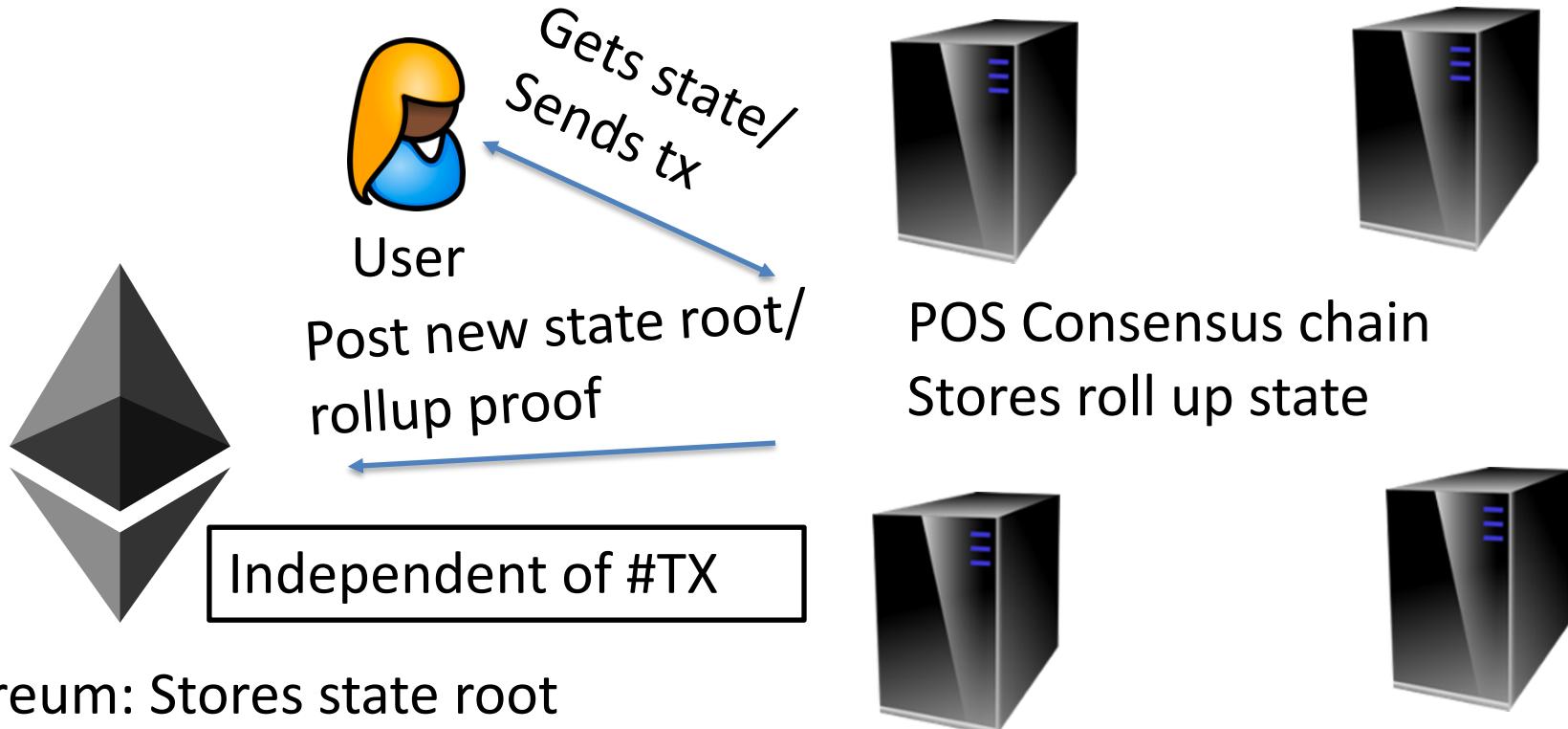
User must know state transition

Posting state diff on chain limits
rollup benefits

Can we keep the
data off chain?

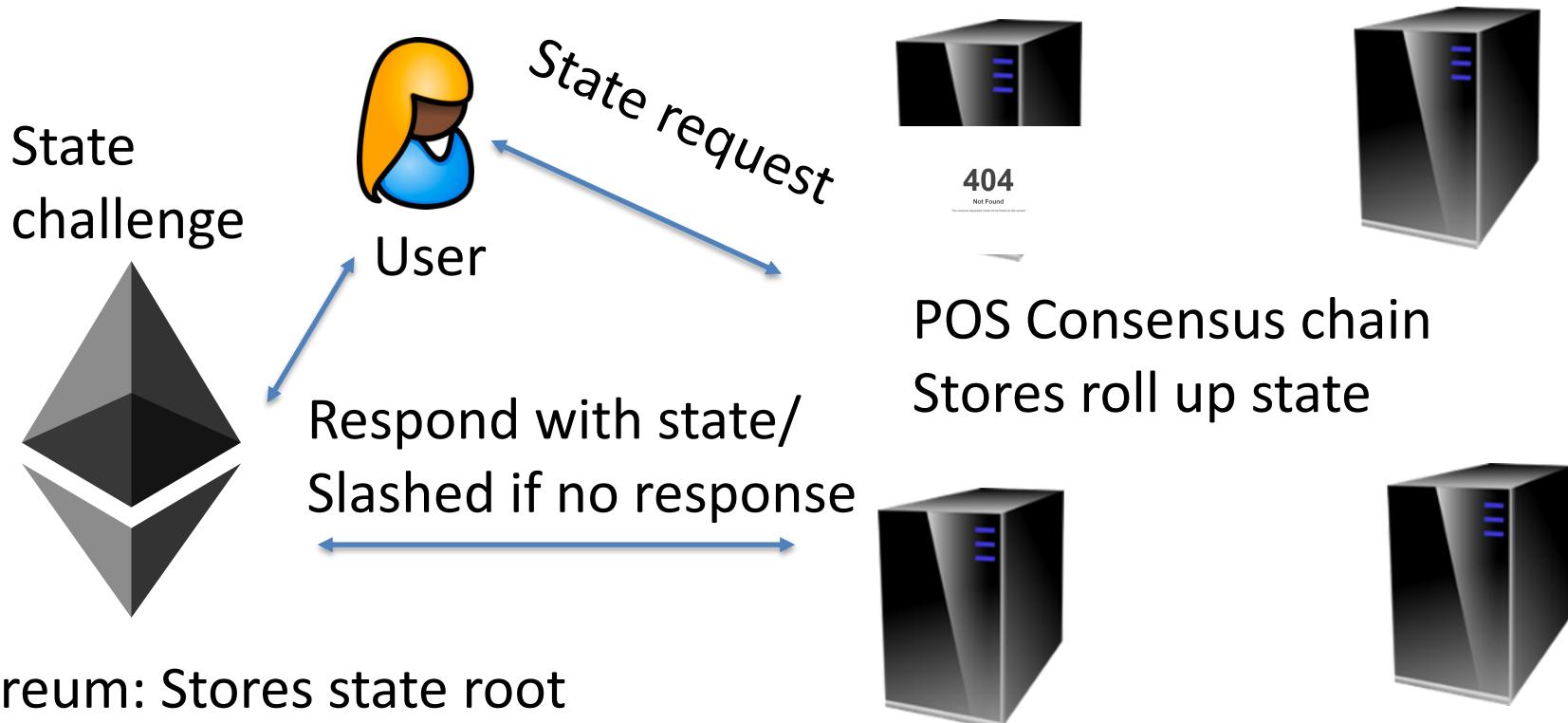
Off Chain Rollups (Validum and Plasma)

- Idea: Create a separate “cheap” chain for the data



Conflict Resolution: On Chain requests

- Idea: Create a separate “cheap” chain for the data



On Chain vs Off Chain Data availability

- Off Chain is much **cheaper** and independent of #tx
 - Only limitation is data consensus
- Data consensus **not trusted** for security
 - Can't steal your money
- Data consensus **is trusted** for availability
 - Can lock up your money (bribery attack)
 - Can increase fees
- Economic incentives can mitigate issues
- For high value transfer use on chain rollup for low value use off chain rollup

2 by 2 rollup

Scaling the blockchain: Payment channels and Rollups (L2 scaling)

security	SNARK validity proofs	Fraud proofs
availability	Tx summary on L1 chain	zkRollup blockchain finality, only simple transfers (now) optimistic Rollup 7 day finality Instant transfers
	Tx summary off chain	Vallidium large #tx but vulnerable to lock up attacks "Plasma" Largest #tx but lock up attacks and long finality

END OF LECTURE

Next lecture: Recursive SNARKs