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[https://cs.unibuc.ro/~crusu/ps/Procesarea_Semnalelor_\(PS\)_-Laborator_07.ipynb](https://cs.unibuc.ro/~crusu/ps/Procesarea_Semnalelor_(PS)_-Laborator_07.ipynb)

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[illegible]

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    "\\n",
    "*Atenție*:  $x$  reprezintă informație în domeniul timpului,  $y$  în domeniul frecvenței.\\n",
    "\\n",
    "2. Comprimați imaginea cu ratoul de mai sus prin atenuarea frecvențelor înalte până la un prag SNR autoimpus.\\n",
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