# An Automata Based Approach for Verification of Information Flow Properties

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Granting, restricting & controlling the flow of information

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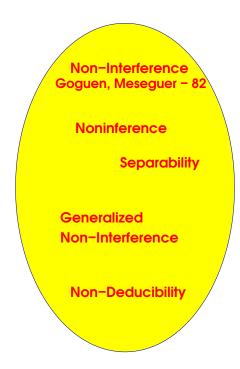
Goguen, Meseguer, '82 - Non-Interference

"What one group of users does has no effect on what other group of users does"

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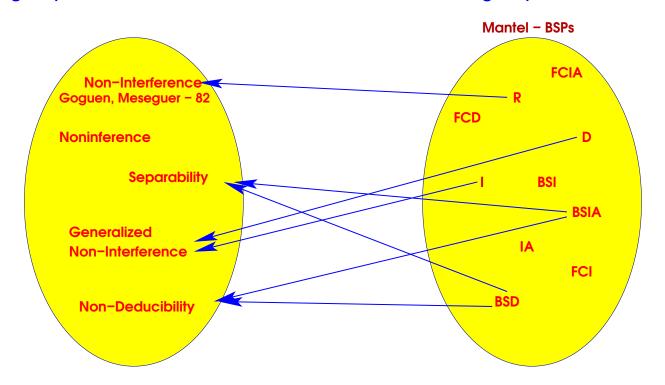
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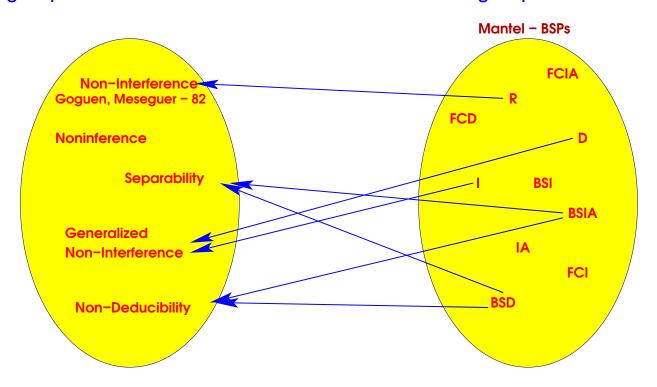
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Can we automate Verification of Security?

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Trace based information flow properties in BSPs

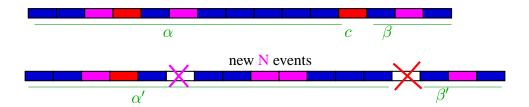
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BSP Deletion (D)



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BSP Insertion (I)



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BSP Insert X-Admissible ( $IA^X$ )



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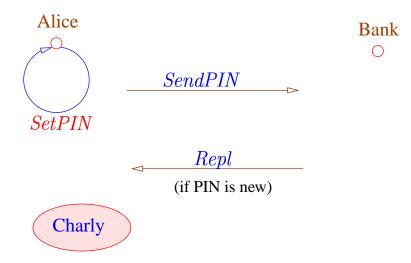
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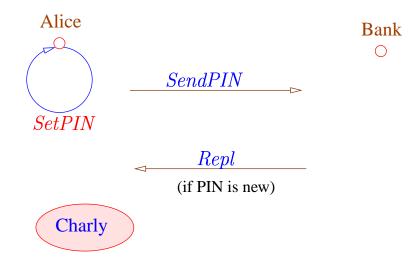
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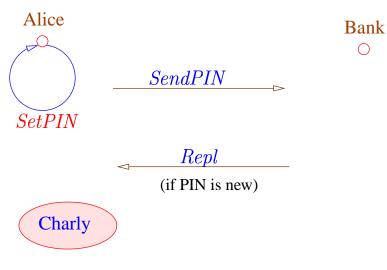
Generalized Non-Interference - I and D

Noninference - R

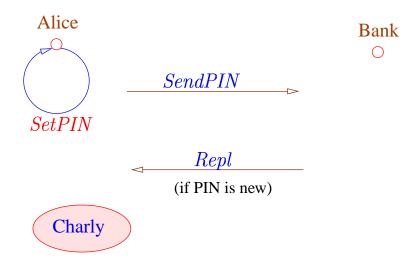




```
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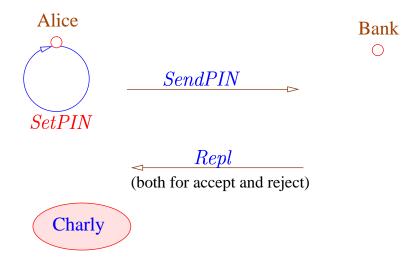


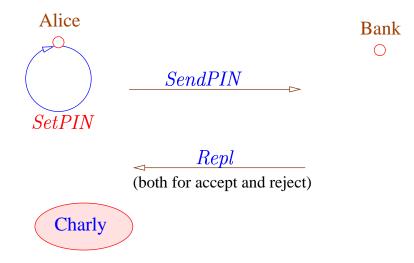
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Confidentiality compromised. BSP Deletion fails

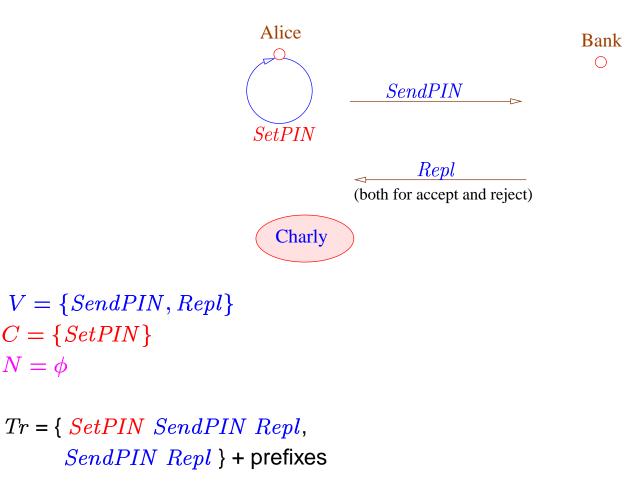


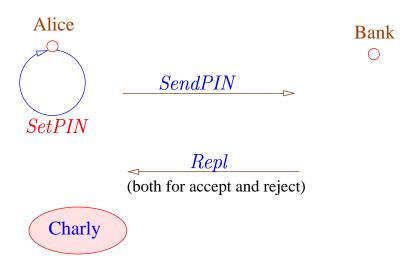


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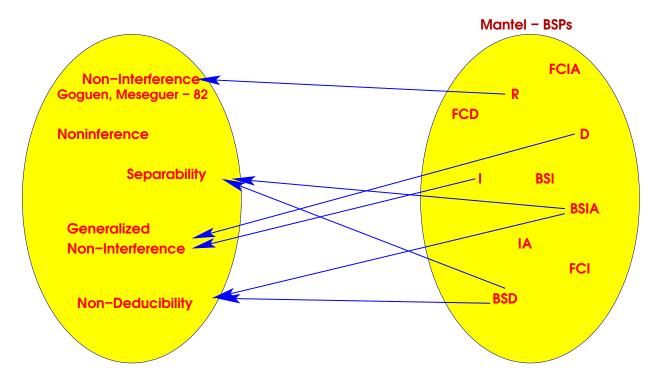
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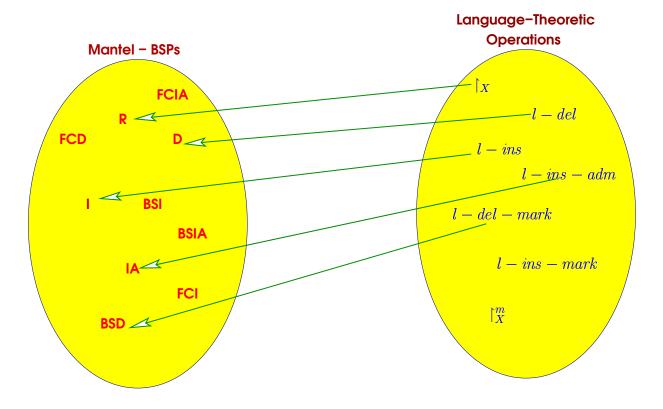
Automated Verification technique - BSP on Finite State Automaton

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 $I\text{-del}(L) := \{\alpha\beta \mid \alpha c\beta \text{ in } L, \text{ no } C \text{ events in } \beta\}$  deletes the last occurring C-event

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*I-ins-adm*<sup>X</sup>(L):= { $\alpha c\beta \mid \alpha\beta$  in L, no C events in  $\beta$ , there exists  $\gamma c$  in L,  $\gamma = \bar{\chi} \alpha$ }

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- Removal R iff  $L \upharpoonright_V \subseteq_N L$ .
- Deletion D iff I-del $(L) \subseteq_N L$ .
- Insertion I iff I-ins $(L) \subseteq_N L$ .
- Strict Removal SR iff  $L \upharpoonright_{\overline{C}} \subseteq L$ .
- Strict Deletion SD iff I- $del(L) \subseteq L$ .

Any  $\tau$  in I-del(L)

Any  $\tau$  in *I-del*(L)

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au' equivalent to au modulo  $extit{N}$ -corrections

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$$L\!\upharpoonright_{\!X}$$

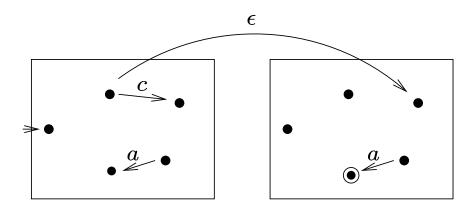
by replacing transitions  $p \xrightarrow{a} q$ , with  $a \notin X$ , in A, by an  $\epsilon$ -transition  $p \xrightarrow{\epsilon} q$ 

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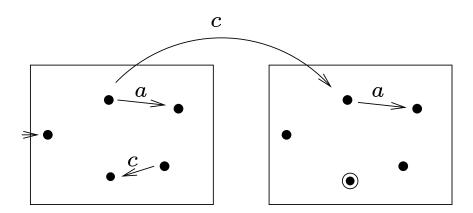


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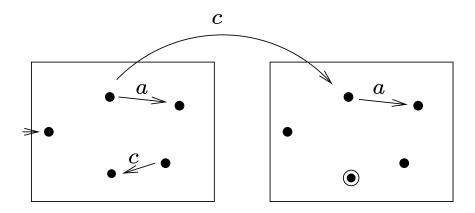


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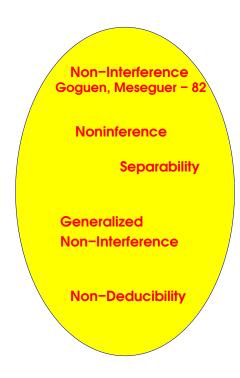
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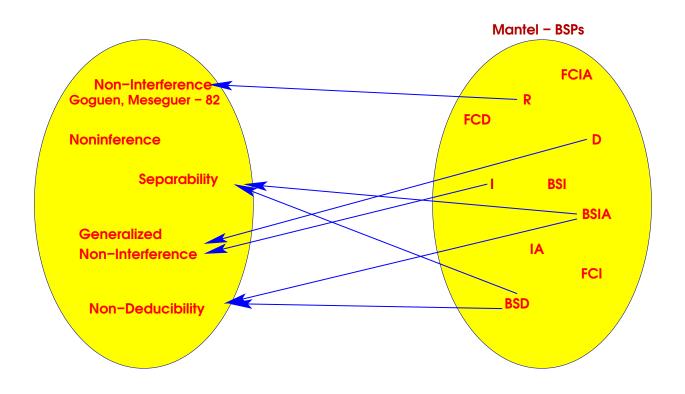
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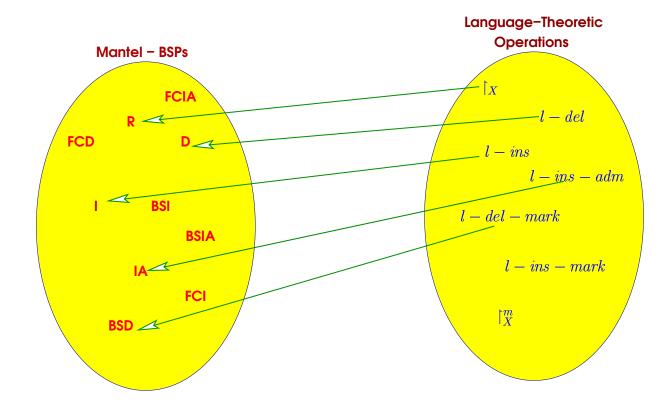
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For infinite state systems?

# Thank You