

# Metareasoning about Security Protocols using Distributed Temporal Logic

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## Motivation

- Formal methods for security protocol analysis
- Most problems due to communication and distribution, rather than cryptography
- Many models, many simplifications, many assumptions

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- Formal methods for security protocol analysis
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## Goal

- Use a protocol independent distributed temporal logic
- Formalize different models, protocols and security goals
- Prove the correctness of modeling and reasoning simplification techniques

## Plan

- Overview of distributed temporal logic
- A simple network model
- Protocol modeling and security goals
- Metareasoning examples
  - Secrecy lemma
  - One intruder is enough
  - The predatory intruder

# Distributed temporal logic

K. Lodaya, R. Parikh, R. Ramanujam, and P.S. Thiagarajan.

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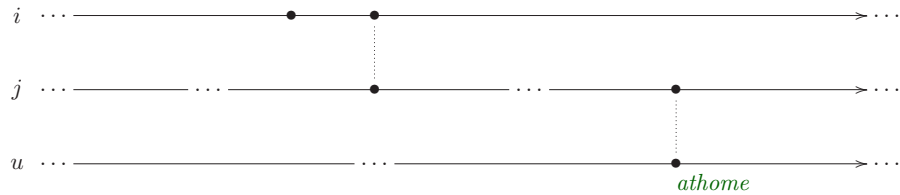
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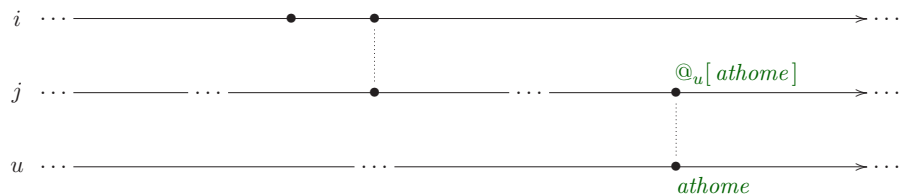
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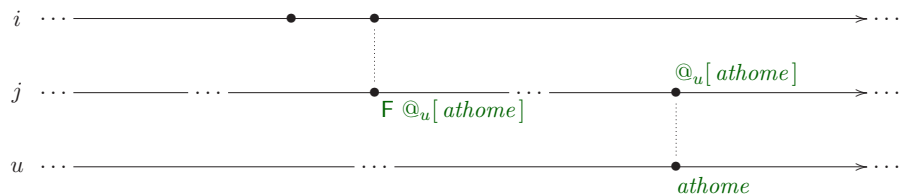


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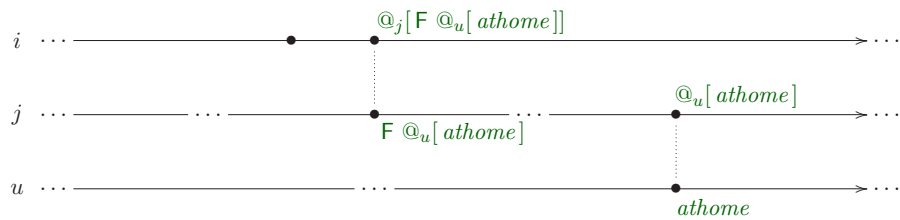
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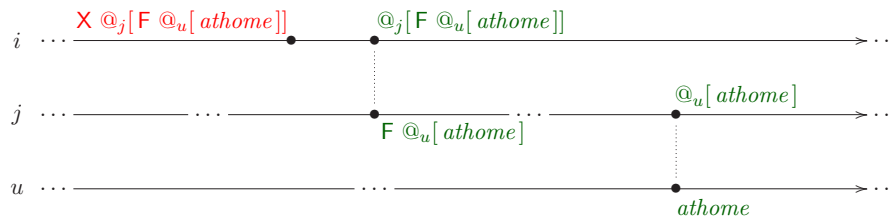
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# Syntax

**Distributed signature**  $\Sigma = \langle Id, \{Act_i\}_{i \in Id}, \{Prop_i\}_{i \in Id} \rangle$

$Id$  finite set of **agent identifiers**

each  $Act_i$  is a set of **local action symbols**

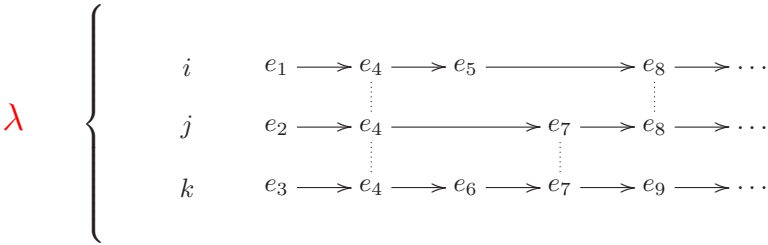
each  $Prop_i$  is a set of **local state propositions**

$$\mathcal{L} ::= @_i[\mathcal{L}_i] \mid \perp \mid \mathcal{L} \Rightarrow \mathcal{L}$$

$$\mathcal{L}_i ::= Act_i \mid Prop_i \mid \perp \mid \mathcal{L}_i \Rightarrow \mathcal{L}_i \mid \mathcal{L}_i \cup \mathcal{L}_i \mid \mathcal{L}_i \text{ S } \mathcal{L}_i \mid @_j[\mathcal{L}_j]$$

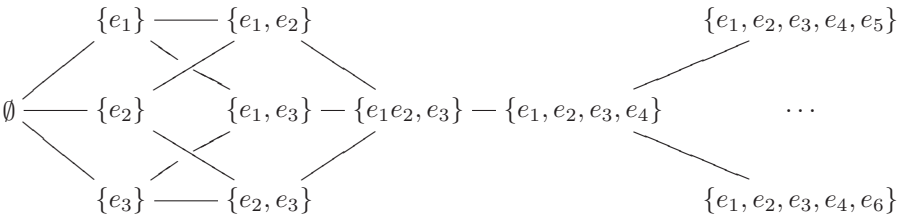
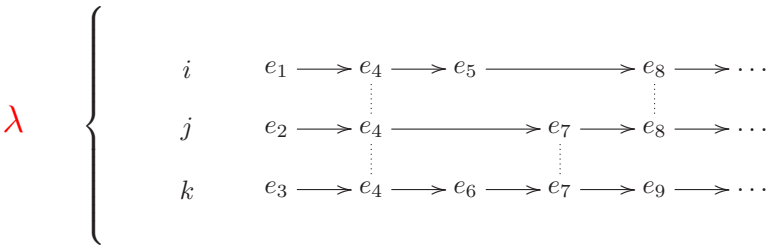
# Models

$\mu = \langle \lambda, \alpha, \pi \rangle$



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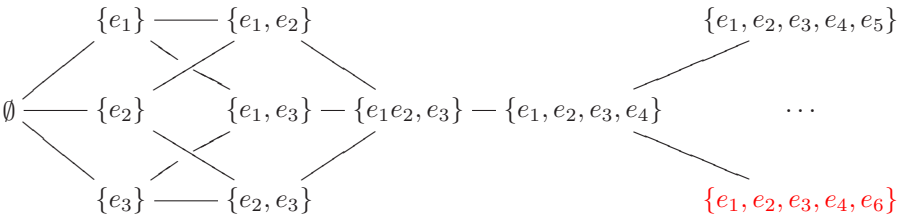
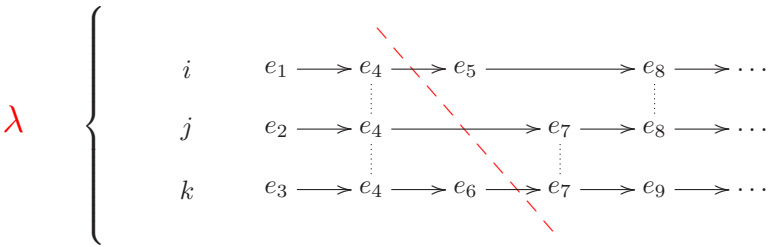
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Global configurations  $\Xi$

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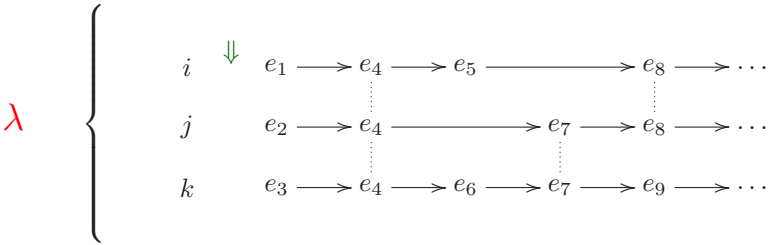
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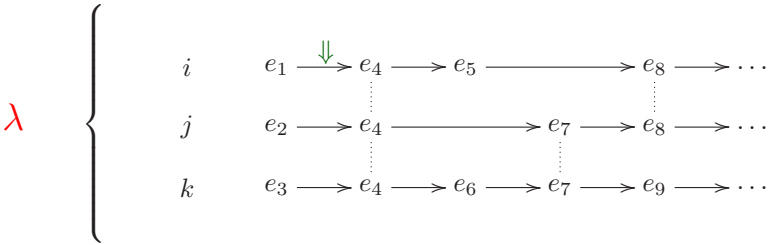
$\emptyset$

Local configurations  $\Xi_i$



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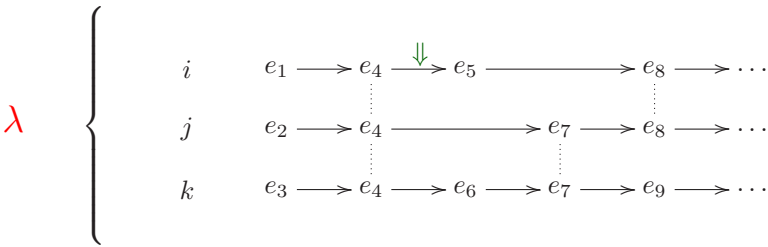


$\emptyset \longrightarrow \{e_1\}$

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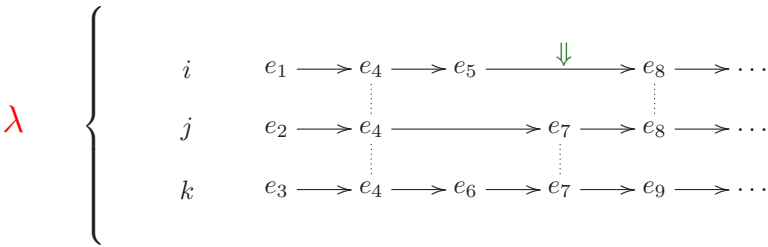


$\emptyset \longrightarrow \{e_1\} \longrightarrow \{e_1, e_4\}$

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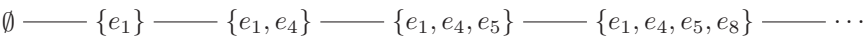
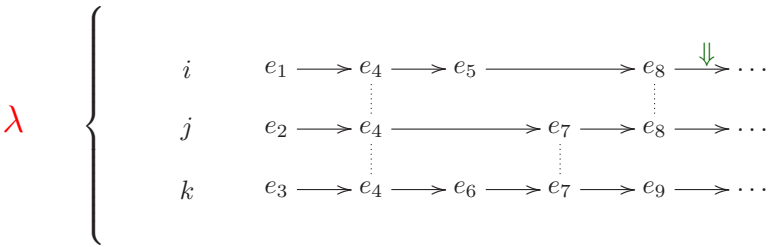


$\emptyset \longrightarrow \{e_1\} \longrightarrow \{e_1, e_4\} \longrightarrow \{e_1, e_4, e_5\}$

Local configurations  $\Xi_i$

# Models

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Local configurations  $\Xi_i$

# Models

$\mu = \langle \lambda, \alpha, \pi \rangle$

$\lambda \left\{ \begin{array}{lll} i & e_1 \longrightarrow e_4 \longrightarrow e_5 \longrightarrow e_8 \longrightarrow \dots \\ & \vdots \\ j & e_2 \longrightarrow e_4 \longrightarrow e_7 \longrightarrow e_8 \longrightarrow \dots \\ & \vdots \\ k & e_3 \longrightarrow e_4 \longrightarrow e_6 \longrightarrow e_7 \longrightarrow e_9 \longrightarrow \dots \end{array} \right.$

$\alpha = \{\alpha_i\}_{i \in Id}$ , each  $\alpha_i : Ev_i \rightarrow Act_i$

$\pi = \{\pi_i\}_{i \in Id}$ , each  $\pi_i : \Xi_i \rightarrow 2^{Prop_i}$

$\pi_i(\emptyset) \xrightarrow{\alpha_i(e_1)} \pi_i(\{e_1\}) \xrightarrow{\alpha_i(e_4)} \pi_i(\{e_1, e_4\}) \xrightarrow{\alpha_i(e_5)} \pi_i(\{e_1, e_4, e_5\}) \xrightarrow{\alpha_i(e_8)} \dots$

# Satisfaction

The **global satisfaction** relation at a given global configuration  $\xi$  of  $\mu$  is:

- $\mu, \xi \Vdash @_i[\varphi]$  if  $\mu, \xi|_i \Vdash_i \varphi$ ;
- $\mu, \xi \not\Vdash \perp$ ; and  $\mu, \xi \Vdash \gamma \Rightarrow \delta$  if  $\mu, \xi \not\Vdash \gamma$  or  $\mu, \xi \Vdash \delta$ , where

the **local satisfaction** relations at given local configurations are:

- $\mu, \xi_i \Vdash_i act$  if  $\xi_i \neq \emptyset$  and  $\alpha_i(last(\xi_i)) = act$ ;
- $\mu, \xi_i \Vdash_i p$  if  $p \in \sigma_i(\xi_i)$ ;
- $\mu, \xi_i \not\Vdash_i \perp$ ; and  $\mu, \xi_i \Vdash_i \varphi \Rightarrow \psi$  if  $\mu, \xi_i \not\Vdash_i \varphi$  or  $\mu, \xi_i \Vdash_i \psi$ ;
- $\mu, \xi_i \Vdash_i \varphi \cup \psi$  if there exists  $\xi_i'' \in \Xi_i$  with  $\xi_i \subsetneq \xi_i''$  such that  $\mu, \xi_i'' \Vdash_i \psi$ , and  $\mu, \xi_i' \Vdash_i \varphi$  for every  $\xi_i' \in \Xi_i$  with  $\xi_i \subsetneq \xi_i' \subsetneq \xi_i''$ ;
- $\mu, \xi_i \Vdash_i \varphi \text{ S } \psi$  if there exists  $\xi_i'' \in \Xi_i$  with  $\xi_i'' \subsetneq \xi_i$  such that  $\mu, \xi_i'' \Vdash_i \psi$ , and  $\mu, \xi_i' \Vdash_i \varphi$  for every  $\xi_i' \in \Xi_i$  with  $\xi_i'' \subsetneq \xi_i' \subsetneq \xi_i$ ; and
- $\mu, \xi_i \Vdash_i @_j[\varphi]$  if  $\xi_i \neq \emptyset$ ,  $last(\xi_i) \in Ev_j$  and  $\mu, (last(\xi_i) \downarrow)|_j \Vdash_j \varphi$ .

As usual  $\mu \Vdash \gamma$  if  $\mu, \xi \Vdash \gamma$  for every global configuration  $\xi$ .

# A simple network model

*Princ* set of principals

*Name* =  $\{Name_A\}_{A \in Princ}$  pairwise disjoint sets of names

*Id* =  $Princ \uplus \{Ch\}$

*Msg* build by composition and encryption, from *Name*, *Nonce* and *Key*

For  $A \in Princ$

*Act*<sub>A</sub> : *send*(*M*, *B'*), *rec*(*M*), *spy*(*M*), and *nonce*(*N*)

*Prop*<sub>A</sub> : *knows*(*M*)

For the channel

*Act*<sub>Ch</sub> : *in*(*M*, *A'*), *out*(*M*, *A'*), and *leak*

*Prop*<sub>Ch</sub> : none

## Network axioms

### Knowledge axioms for principals

(K1)  $@_A[knows(M_1; M_2) \Leftrightarrow (knows(M_1) \wedge knows(M_2))];$

(K2)  $@_A[(knows(M) \wedge knows(K)) \Rightarrow knows(\{M\}_K)];$

(K3)  $@_A[(knows(\{M\}_K) \wedge knows(K^{-1})) \Rightarrow knows(M)];$

(K4)  $@_A[knows(M) \Rightarrow G_o knows(M)];$

(K5)  $@_A[rec(M) \Rightarrow knows(M)];$

(K6)  $@_A[spy(M) \Rightarrow knows(M)];$  and

(K7)  $@_A[nonce(N) \Rightarrow knows(N)].$

### Fresh nonce generation

(N1)  $@_A[nonce(N) \Rightarrow Y \neg knows(M_N)];$  and

(N2)  $@_A[nonce(N)] \Rightarrow \bigwedge_{B \in Princ \setminus \{A\}} @_B[\neg knows(M_N)].$



# Network axioms

## Behaviour and communication axioms for the channel

$$(C1) \ @_{Ch}[in(M, A') \Rightarrow \bigvee_{B \in Princ} @_B[send(M, A')]];$$

$$(C2) \ @_{Ch}[out(M, A') \Rightarrow P \ in(M, A')]; \text{ and}$$

$$(C3) \ @_{Ch}[out(M, A') \Rightarrow @_A[rec(M)]].$$

## Behaviour and communication axioms for principals

$$(P1) \ @_A[send(M, B') \Rightarrow Y(knows(M) \wedge knows(B'))];$$

$$(P2) \ @_A[send(M, B') \Rightarrow @_{Ch}[in(M, B')]];$$

$$(P3) \ @_A[rec(M) \Rightarrow @_{Ch}[\bigvee_{A' \in Name_A} out(M, A')]];$$

$$(P4) \ @_A[spy(M) \Rightarrow @_{Ch}[leak \wedge P \ \bigvee_{B' \in Name} in(M, B')]];$$

$$(P5) \ @_A[\bigwedge_{B \in Princ \setminus \{A\}} \neg @_B[\top]]; \text{ and}$$

$$(P6) \ @_A[nonce(N) \Rightarrow \neg @_{Ch}[\top]].$$

# Protocol modeling

Protocols described as a series of steps of the form

$$(\text{step}_q) \quad x_s \rightarrow x_r : (n_{q_1}, \dots, n_{q_t}). M$$

**Hon** - honest principals follow the rules of the protocol and use only one name

**Intr** - dishonest principals are potential “intruders”

Given a protocol with  $j$  distinct roles, and an instantiation with names

$A'_1, \dots, A'_j$  of principals  $A_1, \dots, A_j$

$$\text{step}_q^i = \begin{cases} \langle \text{nonce}(N_{q_1}) \dots \text{nonce}(N_{q_t}).\text{send}(M, A'_r) \rangle & \text{if } i = s \\ \langle \text{rec}(M) \rangle & \text{if } i = r \\ \langle \rangle & \text{otherwise} \end{cases}$$

Each  $\text{run}_A^i = \langle \text{act}_1 \dots \text{act}_n \rangle$  is characterized by

$$\text{role}_A^i = \text{act}_n \wedge \text{P}(\text{act}_{n-1} \wedge \text{P}(\dots \wedge \text{P} \text{act}_1) \dots).$$

## Security goals

$$\text{secre}_S(A_1, \dots, A_j)$$

secrecy goal for  $S$  among honest participants  $A_1, \dots, A_j$

$$\bigwedge_{i=1}^j @_{A_i}[\text{P} \circ \text{role}_{A_i}^i] \Rightarrow \bigwedge_{B \in \text{Princ} \setminus \{A_1, \dots, A_j\}} \bigwedge_{M \in S} @_B[\neg \text{knows}(M)]$$

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$$\text{auth}_{A,B}^{i,j,q}$$

authentication goal for honest  $A$  in role  $i$  wrt some  $B$  in role  $j$

$$@_A[\text{role}_A^i] \Rightarrow @_B[\text{P} \circ \text{send}(M, A)], \text{ if } B \text{ is honest}$$

$$@_A[\text{role}_A^i] \Rightarrow \bigvee_{C \in \text{Intr}} @_C[\text{P} \circ \text{send}(M, A)], \text{ if } B \text{ is dishonest}$$

assuming that  $\text{step}_q$  requires  $x_j$  to send message  $M$  to  $x_i$

## Metareasoning: secret data lemma

Given  $S \subseteq \text{Msg}$ ,  $\text{Msg}_S$  are the  $S$ -secure messages, that is, messages where items from  $S$  can only appear under the scope of an encryption with a key whose inverse is also in  $S$

### Protocol independent secret data lemma

$G \subseteq \text{Princ}$ ,  $\mu$  network model such that

$\mu \Vdash \bigwedge_{A \in G} @_A[\neg \text{send}(M, C')]$  for every  $M \notin \text{Msg}_S$  and every name  $C'$ , and

$\mu \Vdash \bigvee_{A \in G} @_A[* \Rightarrow \text{F nonce}(N)]$  for every nonce  $N \in S$ .

If it is the case that

- $\mu, \xi \Vdash \bigwedge_{B \in \text{Princ} \setminus G} @_B[\neg \text{knows}(M)]$  for every  $M \notin \text{Msg}_S$ ,

then also

- $\mu, \xi \Vdash \bigwedge_{B \in \text{Princ} \setminus G} @_B[G_\circ \neg \text{knows}(M)]$  for every  $M \notin \text{Msg}_S$ .

## Metareasoning: secrecy lemma

$$\text{secr}_F = \bigwedge_{i=1}^j @_{A_i} [\text{P} \circ \text{role}_{A_i}^i] \Rightarrow \bigwedge_{B \in \text{Princ} \setminus \{A_1, \dots, A_j\}} \bigwedge_{M \in F} @_B [\neg \text{knows}(M)].$$

### Secrecy lemma

A protocol guarantees  $\text{secr}_F$  for a protocol instantiation with honest participants  $A_1, \dots, A_j$ , provided that all the messages ever sent by  $A_1, \dots, A_j$  in any protocol run are  $(\{K_{A_1}^{-1}, \dots, K_{A_j}^{-1}\} \cup F)$ -secure.

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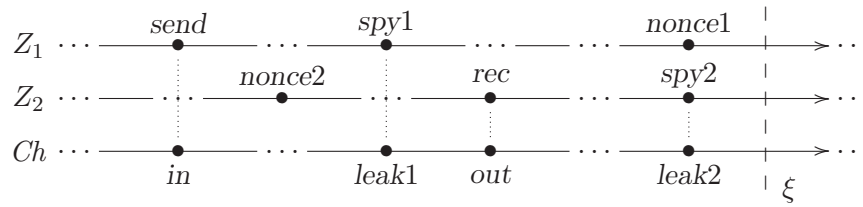
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J.Millen, H.Ruess - Protocol independent secrecy, 2000

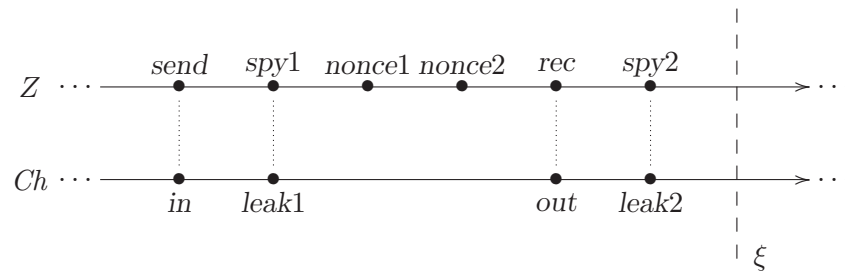
Discreteness

Avoiding artificial notions like spells

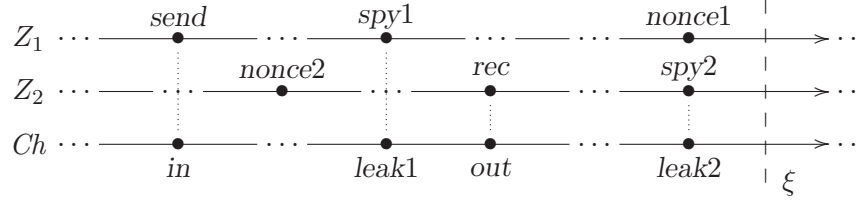
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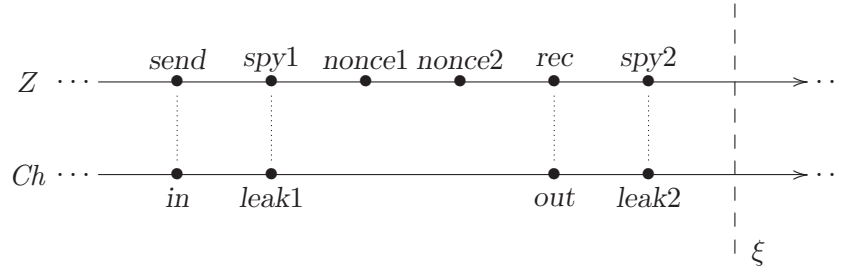
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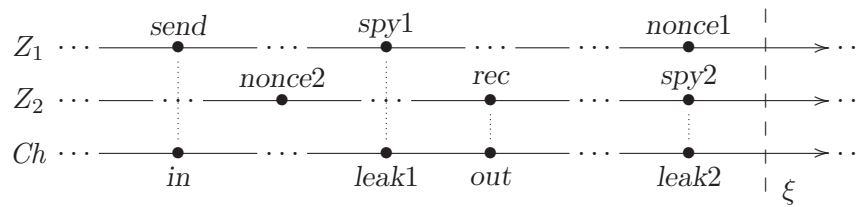
$\mu, \xi \Vdash @_A[\varphi]$  iff  $\mu', \xi \Vdash @_A[\varphi]$  for  $A \in Hon$ ,  $\varphi \in \mathcal{L}_A$  without  $@$

$\mu, \xi \Vdash \bigvee_{A \in Intr} @_A[P \circ act]$  iff  $\mu', \xi \Vdash @_Z[P \circ act]$

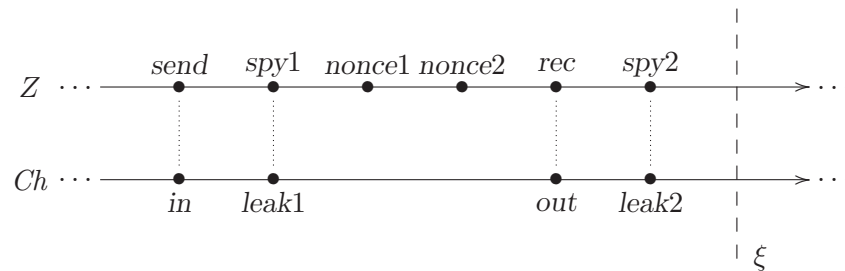
if  $\mu, \xi \Vdash \bigvee_{A \in In} @_A[knows(M)]$  then  $\mu', \xi \Vdash @_Z[knows(M)]$



# Metareasoning: one intruder is enough



can be reduced to



H. Comon-Lundh, V. Cortier - Security properties: two agents are sufficient, 2003  
Intruders part of the model

## Metareasoning: the predatory intruder

- $Z$  spies every message sent by an honest principal immediately after it arrives to the channel, and that is all the spying he does

$$@_{Ch}[@_Z[\textit{spy}(M)] \Leftrightarrow \bigwedge_{A \in Hon} @_A[\bigvee_{B' \in Name} \textit{send}(M, B')]]$$

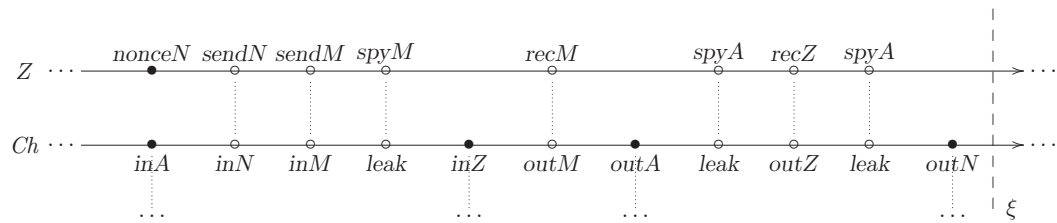
- $Z$  never bothers receiving messages (he has already spied them)

$$@_Z[\neg \textit{rec}(M)]$$

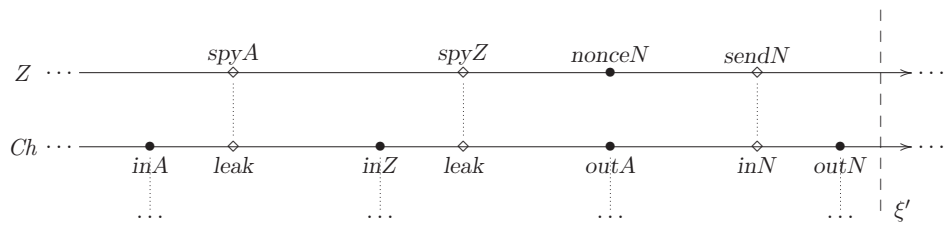
- $Z$  only sends messages to honest principals, and just immediately before the honest principal gets them

$$@_Z[\neg \textit{send}(M, Z')] \quad \text{and} \quad @_Z[\textit{send}(M, A) \Rightarrow @_Ch[\neg @_A[\textit{rec}(M)]]]$$

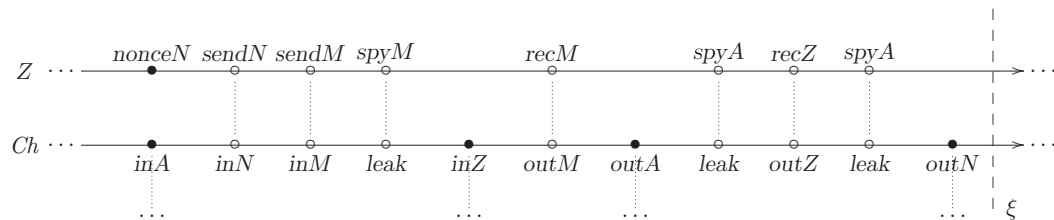
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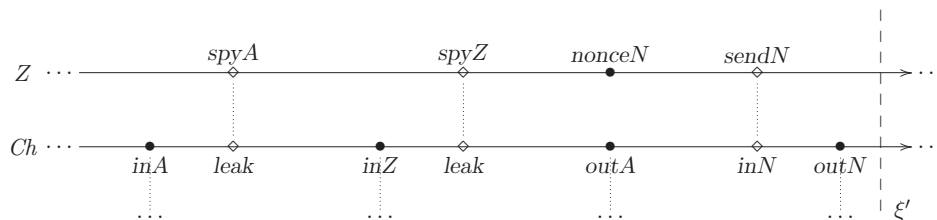
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# Metareasoning: the predatory intruder



can be reduced to



Towards justifying the linearization of distributed communication in trace models

Corollary: the intruder only needs to send messages according to the protocol

## Conclusion and further work

- Distributed temporal logic as a tool for security protocol model analysis
- A few of its potentialities
- **Further work**
  - Other widely used reductions: bounds on the number of honest principals, step compression
  - Nicer conditions for secrecy, and its relationship to authentication
  - New meaningful partial order reductions
  - Protocol compositionality

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**Thank you!**