

# ACCOUNTING FOR JOB-TO-JOB TRANSITIONS: WAGES VERSUS VALUES

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# MOTIVATION

- Job-to-job transitions are an important part of labor reallocation
  - 60% of new hires come directly from other jobs
  - 10% of workers each year make an EE transition
- Moving jobs is a common way of obtaining earnings increases
- Yet there appears to be a substantial amount of wage cuts
- Wage cuts are not necessarily puzzling from a dynamic perspective if they are associated with increases in *value*
- Key question: are these wage cuts associated with positive or negative changes in *value*?
- Important for understanding efficiency of the labor market, risk over the life cycle, policy design
  - Motivations for switching jobs affect the allocation of workers to firms and determine which features should be included in models
  - Link between labor market fluidity and welfare

# MOTIVATIONS FOR WAGE AND VALUE CHANGES

	- Wage	+ Wage
+ Value	Accept wage cut now in exchange for future wage growth: Postel-Vinay and Robin (2002)	Good move for both immediate wages and future wages
- Value	Non-wage amenities, forced moves: Sorkin (2018), Hall and Mueller (2018), Moscarini and Postel-Vinay (2019)	Borrowing constraints: Lise (2012), Luo and Mongey (2019)

1. Refine measurement of job-to-job transitions
  - Made possible by high frequency administrative data from Denmark
  - Precise pinpointing of transition and clear wage measures
2. Compute wage change CDFs for stayers and switchers
3. Semi-parametric estimation of value of a job for a worker
  - Nest value functions in commonly used search models
4. Analyze the joint distribution of wage changes and value changes for job-to-job transitions
  - With model, we assign a change in value associated with every wage change we observe
  - Quantify value cuts, toward an understanding of who is taking them and why

## Measurement

- About half of job-to-job transitions feature a wage cut, but only a quarter of these are more than 10%
- But it makes a difference how you measure these!

## Wages vs. values

- Changes in *value* are typically smaller in magnitude than wage changes
- 60% of wage cuts also feature declines in value
- Motivations for EE switches tend to be related to *unobservable* match + job characteristics
- Lots of variation as to whether future wages or future transitions are quantitatively responsible for the value changes

Measurement and Motivating Facts

Model of Job Values

Results

## MEASUREMENT AND MOTIVATING FACTS

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## Danish administrative registry data

- Entire Danish population from 2008 to 2017
- Monthly payroll records reported by employers
- Total pay each month, firm ID, contractual hours, occupation, industry, demographics,...
- Public transfers database for unemployment and OLF states

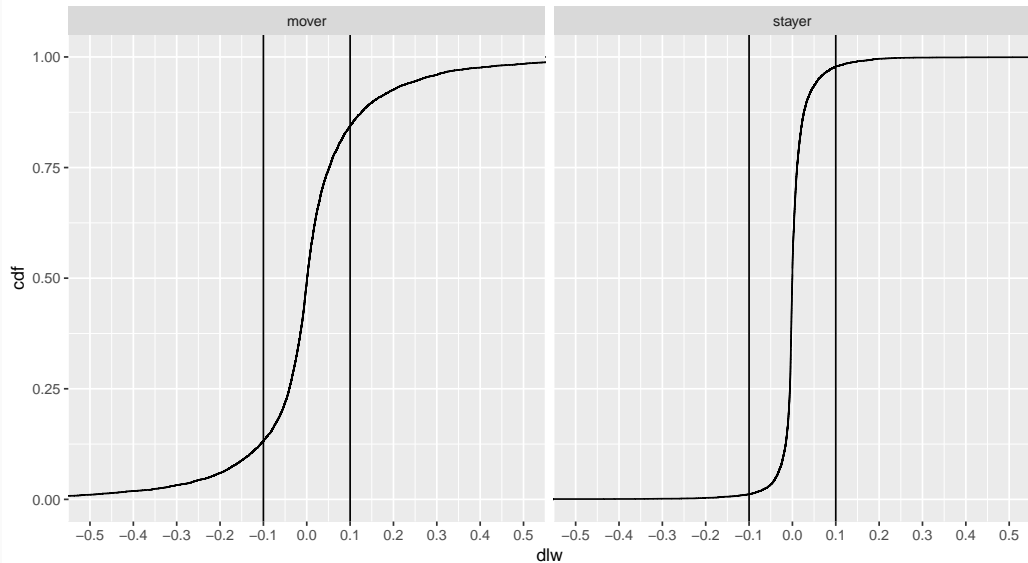
## What is a job?

- Firm  $\times$  2-digit occupation
- Why? Wages in same firm differ across occupation, relevant for model
- Cells under 1000 person-quarter observations are grouped by 4-digit industry  $\times$  2-digit occupation

Quarterly aggregation to keep model tractable, but still can track moves through U



# DISTRIBUTION OF WAGE GROWTH



# HOW TO MEASURE WAGES

Construct measure of base real wage

- Issue: spikes during the last month, representing payouts from holiday fund
- Drop last wage observation + calculate 12-month centered moving average

Sample: full-time workers who are attached to the labor force

- Only consider jobs with contractual hours within 2% of 160 hours per month (full-time)
- Ensures measured wage change during job switch not driven by hours

## WAGE GROWTH FOR SWITCHERS: ALTERNATE MEASUREMENTS

	Decrease > 10%	Increase > 10%
Baseline	0.13	0.14
Fail to drop last wage obs.	0.19	0.14
Looser hours restriction	0.17	0.18
Previous two combined	0.26	0.16

- Our adjustments reduce the noise present in the original data
- Careful measurement matters, especially at the tails

## MODEL OF JOB VALUES

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# OBJECTIVES

- Want to translate our wage changes into *value* changes
- PDV of future wages in a job consists of:
  1. Wage stream in that job
  2. Transition rates to other jobs
- Need a model for
  1. Predicting wages for any worker in any job
  2. Predicting transitions between jobs for any worker
- Approach
  1. Define worker and job types
  2. Define state variables
  3. Estimate wage and transition as function of state variables by type
- How to pick state variables? Guided by theory. Today: a variant of the wage posting model of Burdett and Mortensen (1998)

## Workers

- Workers can be one of  $i \in I$  types (will drop  $i$  subscripts)
- Type-specific component of earnings:  $g$
- Live from  $a = 1, 2, \dots, A$
- Age profile of earnings differs across types:  $h(a)$

## Jobs

- Workers transition between  $J$  jobs
- This set also includes non-employment states
- Piece-rate in each job:  $\omega(j)$

**Wages:**  $\omega(j)h(a)gz$

- $z$ : match-specific productivity

## Matches

- When matched to a job, workers have a match-specific productivity  $z$ 
  - Helps match the wage changes of job switchers
- After moving  $j \rightarrow k$ , draw new  $z'$  from a distribution that depends on  $(j, k, z)$ 
  - $z'$  revealed if the match is created
  - Allow for persistence in  $z$  when workers switch between jobs
  - Productivity in new job may depend on the identity of the old job
- Stayers' wages are subject to i.i.d. mean 0 shocks  $\varepsilon$ 
  - Helps match stayers' wage growth
- Contact rate from job  $j$  to  $k$ :  $\lambda_k(a, j, z)$ 
  - Workers may be more likely to leave lower-paying jobs or jobs at which they're not productive

$$v(a, j, z) = \overbrace{\omega(j) h(a) g z}^{\text{today's wages}} + \beta \left[ \sum_k \underbrace{\lambda_k(a, j, z) \mathbb{I}_{\{d(a, j, k, z)=1\}} \mathbb{E}_{z \times \varepsilon} v(a+1, k, z' \varepsilon')}_{\text{expected value of switching from job } j \text{ to job } k} + \underbrace{\Lambda(a, j, z) \mathbb{E}_{\varepsilon} v(a+1, j, z \varepsilon')}_{\text{expected value of staying at job } j} \right]$$

- Burdett-Mortensen: constant job-specific wage piece rate, probability of moving to other jobs depends on current job, no renegotiation in response to outside offers
- Generalizations: life-cycle, match-specific productivity, i.i.d. shocks to stayers' wages
- Instead of computing equilibria of structural model, calculate ingredients needed to solve for  $v(a, j, z)$



Ingredients:  $\omega(j)$ ,  $h(a)$ ,  $g, z$ ,  $\lambda_k(a, j, z)$ , expectations over  $z'$  for switchers

## Worker types

- Correspond to 4 fixed education  $\times$  gender categories

## Job types $j$

- 6019 employment states (about half correspond to firm  $\times$  occupation; other half corresponds to industry  $\times$  occupation)
- 10 non-employment states: short- and long-term unemployment, retirement, maternity leave, sick leave, etc. that we observe transfers for

## Age profile $h(a)$

- $w(j), z$  constant within match  $\rightarrow$  average wage change between  $a$  and  $a + 1$  for stayers
- Pool across jobs and over time, take cumulative sum of earnings changes

## WAGE PREMIA $\omega(j)$

Separate each component of earnings:  $w_n(a, j, z) = \omega(j)h(a)gz$

- Selection issue: what if workers' mobility decisions are based on  $z$ ?
- Averaging earnings within jobs and worker types would give biased estimates of  $\omega(j)$
- Assumption: while unemployed,  $z$  is low enough such that all workers accept any job offer  $\implies$  their distribution of  $z$  is the same across jobs

With  $g$  in hand, for jobs with enough hires from  $U$ ,  $\omega(j)$  is: [How to estimate  \$g\(i\)\$](#)

$$\frac{1}{U_j} \sum_{n=1}^{U_j} \frac{w_n(a_n, j_n, z_n)}{h(a_n)g_n} = \frac{1}{U_j} \sum_{n=1}^{U_j} \frac{\omega(j)h(a)g\mathbb{E}[z]}{h(a)g} = \omega(j) \quad \forall n : j_n = j$$

- Key: expectation over  $z$  is the same as the unconditional, normalized to 1 for all  $j$
- For jobs less workers hired from  $U$ , impute  $\omega(j)$  via statistical methods [Details](#) [Scatter plot](#)

## MATCH-SPECIFIC PRODUCTIVITY

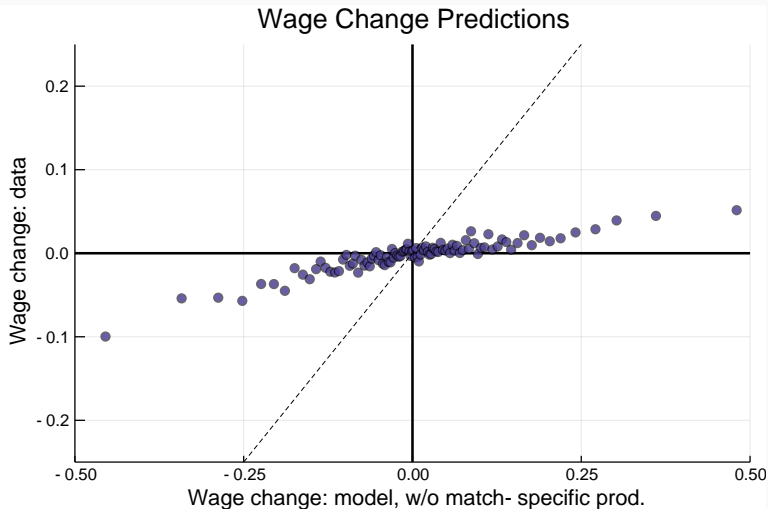
- Match-specific productivity  $z_n$  in data:

$$z_n = \frac{w_n(a_n, j_n, z_n)}{\omega(j_n)h(a_n)g_n}$$

- Necessary step for computing values: law of motion for  $z'$
- Want to generate accurate wage predictions *at the individual level* so we can trust value predictions!
  - Model with and without  $z$  fit the overall CDF of wage changes well
- For job switchers from  $j$  to  $k$ , want to forecast  $z'$  as a function of the model's state variables:  $z' = f(a, j, k, z)$
- Specification that yields the best forecast is:

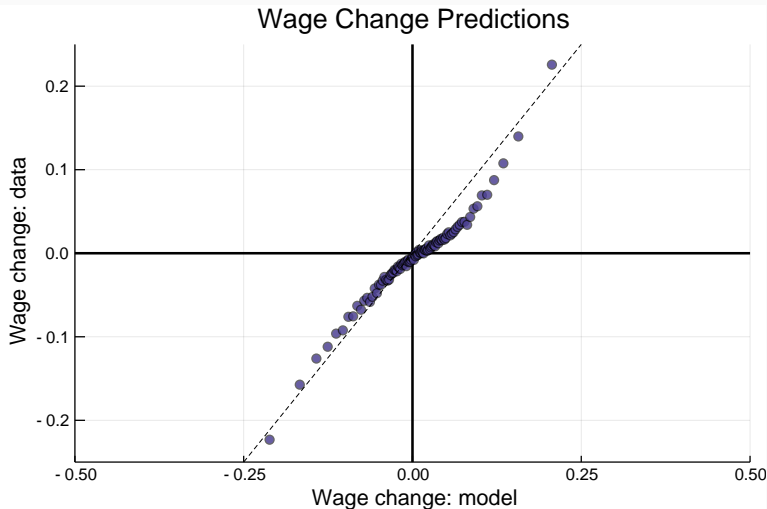
$$\begin{aligned}\log z'_i = & \bar{z} + \rho \log z_i + \beta_1 \log \omega_i + \beta_2 \log \omega'_i + \beta_3 \text{mean}(z|\omega_i) + \beta_4 \text{mean}(z|\omega'_i) \\ & + \beta_5 \text{var}(z|\omega_i) + \beta_6 \text{var}(z|\omega'_i) + \eta_i\end{aligned}$$

## EE WAGE CHANGE PREDICTIONS: WITHOUT MATCH-SPECIFIC PRODUCTIVITY



- On their own, piece rates do not do well at predicting individual wage changes

## EE WAGE CHANGE PREDICTIONS: WITH MATCH-SPECIFIC PRODUCTIVITY $z$



- Incorporating  $z$  into the model helps to better match individual wage changes

Observed  $z$

- Transition probabilities:  $\lambda_k(a, j, z)$ 
  - Use observed transitions among the whole set of jobs in the data
  - Workers at better paying jobs or with higher  $z$  may be less willing to leave
  - Group  $a$  into 3 age bins and  $z$  into 4 quartiles
- Distribution of  $z$  for UE transitions
  - Comes from variance of  $z$  in the data for workers hired out of U
- Distribution of  $\varepsilon$ 
  - Comes directly from variance of wage changes for stayers

## RESULTS

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# DENSITIES OF WAGE AND VALUE CHANGES

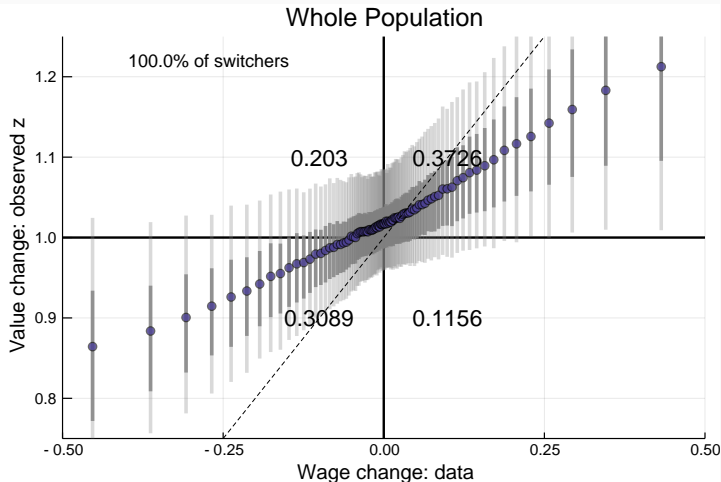


- Value changes smaller in magnitude than wage changes

Histograms

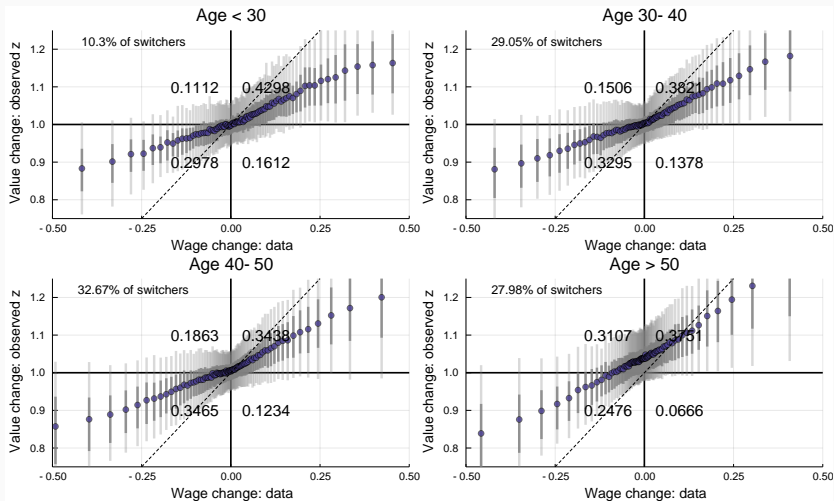


# MAJORITY OF MOVES RESULT IN VALUE INCREASE



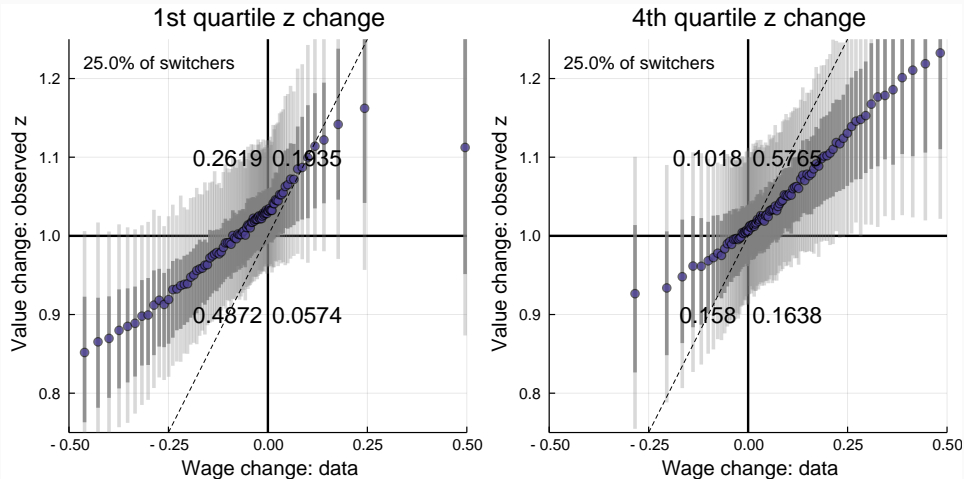
- $\Pr(\text{value increase} \mid \text{wage cut}) = 39.6\%$ ;  $\Pr(\text{value cut} \mid \text{wage increase}) = 23.8\%$
- No major differences within fixed worker groups (gender  $\times$  education)

# YOUNGER WORKERS TEND TO INCREASE $w$ ; OLDER WORKERS TEND TO INCREASE $v$



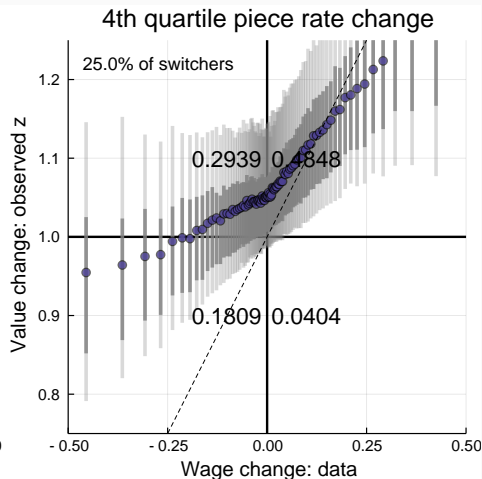
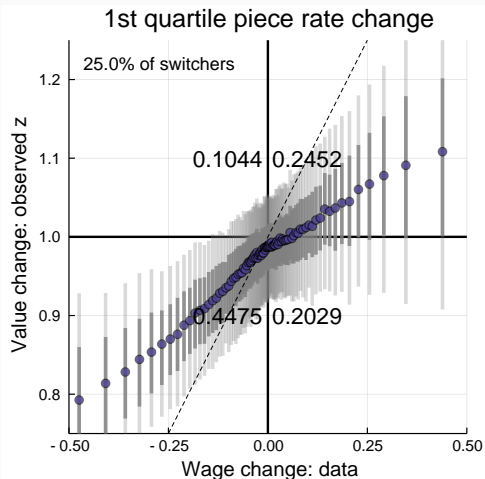
- Younger workers more likely borrowing constrained
- Older workers tend to take more wage cuts that result in higher values

# BETTER MATCHES TEND TO INCREASE BOTH WAGES AND VALUE



- Increasing z is likely to be good for both wages and values

# STILL LOTS OF WAGE CUTS FOR MOVES TO HIGHER-PAYING JOBS



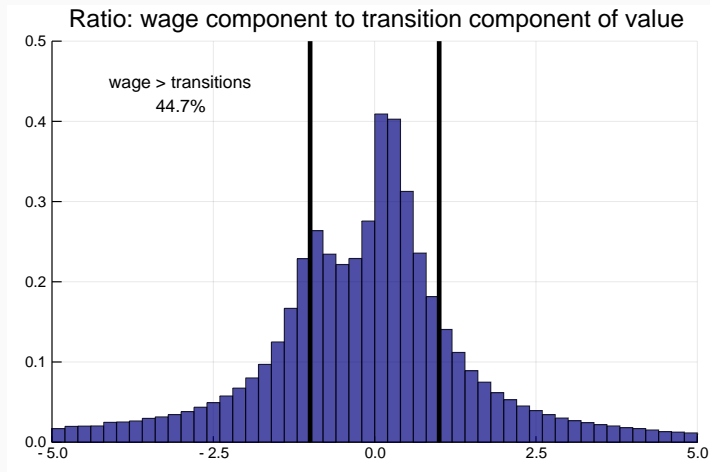
- In contrast to  $z$ , moving up in  $\omega(j)$  is more closely tied to increases in *value*
- Piece rate  $\neq$  wage  $\neq$  value

Initial wage

Initial omega

Initial z

# TRANSITION RATES ARE AN IMPORTANT COMPONENT OF VALUE



- Decompose the change in value from  $(j, z)$  to  $(k, z')$  into 2 components, coming from wages and transition rates
- Value changes come from all different mixes

## CONCLUSION AND FUTURE WORK

- Developed a methodology for assigning values associated with job-to-job transitions
- Findings
  - Careful measurement for documenting features of EE switches
  - Significant mass in all quadrants of wage change/value change plane
  - Unobserved heterogeneity is key for determining values behind each switch
- Next steps
  1. Better understand the motivations behind the transitions
    - Recover distribution of non-wage amenities or reallocation shocks that rationalize negative value switches
    - See if switches coincide with family events, geographic moves, changes in wealth or consumption, etc.
  2. Further develop the model
    - Allow for other forms of worker and job heterogeneity
    - Extend to Postel-Vinay and Robin (2002) setting

### Measurement

- Nominal wage changers for *stayers*: Grigsby, Hurst, Yildirmaz (2020)
- Wage changes using administrative data: Kurmann and McEntarfer (2018), Jardim et al. (2019)

### Reasons for wage cuts

- Future wage growth, transitions to other jobs: Postel-Vinay and Robin (2002)
- Non-wage amenities: Sorkin (2018), Hall and Mueller (2018)
- “Godfather” shocks: Moscarini and Postel-Vinay (2019) and lots of others

## TYPE-SPECIFIC PREMIA $g(i)$

- Let  $U_{ij}$  be the number of workers of type  $i$  hired into job  $j$  from unemployment
- For jobs with  $U_{ij} \geq 25$ , compute the following:

$$\frac{1}{U_{ij}} \sum_{n=1}^{U_{ij}} \frac{w_n(a_n, j_n, z_n)}{h(i_n, a_n)} = \frac{1}{U_{ij}} \sum_{n=1}^{U_{ij}} \frac{\omega(j)h(i, a)g(i)\mathbb{E}[z]}{h(i, a)} = \omega(j)g(i) \quad \forall n : j_n = j$$

- Key: expectation over  $z$  is the same as the unconditional, assumed to be 1 for all  $j$
- Set  $g(i) = 1$  for baseline group, weighted average of  $g(i)\omega(j)$  over  $j$ , and compare to weighted average of  $\omega(j)$  for baseline group



## WAGE PREMIA $\omega(j)$ : FOR JOBS WITH FEWER OBSERVATIONS

1. For jobs with few observations, first compute naive  $\tilde{\omega}(j)$  using *all* hires:

$$\tilde{\omega}(j) = \frac{1}{N_j} \sum_{n=1}^{N_j} \frac{w_n(a_n, j_n, z_n)}{h(i_n, a_n)g(i_n)}$$

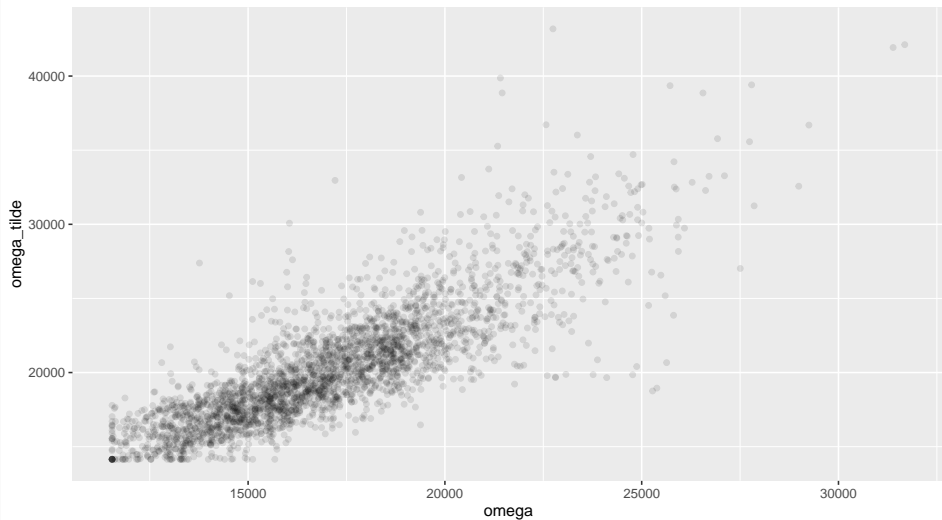
2. For jobs with  $U_{ij} \geq 10$  estimate the following:

$$\log \omega(j) = \beta_0 + \beta_1 \log \tilde{\omega}(j) + \beta_2 \mathbf{X}_j + \epsilon_j$$

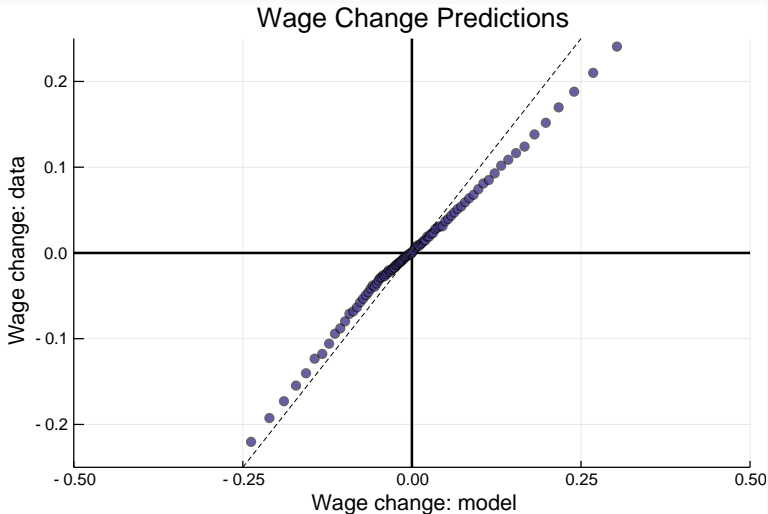
$\mathbf{X}_j$  contains firm size, occupation, industry

3. Use this relationship to impute a  $\omega(j)$  for jobs with less than 10 hires from unemployment

# RELATIONSHIP BETWEEN $\omega(j)$ AND $\tilde{\omega}(j)$

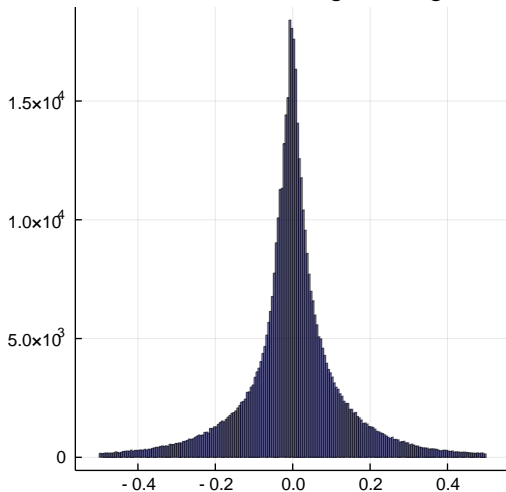


## EE WAGE CHANGE PREDICTIONS: WITH *OBSERVED* MATCH-SPECIFIC PRODUCTIVITY $z$

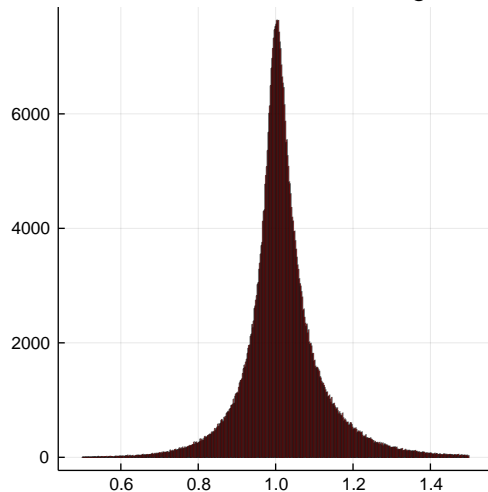


# DENSITIES OF WAGE AND VALUE CHANGES

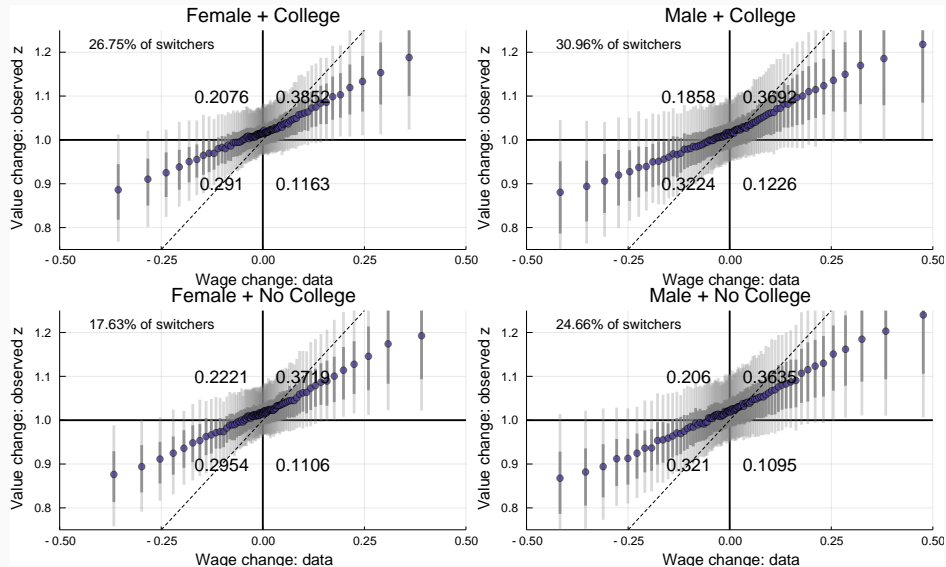
Distribution of wage changes

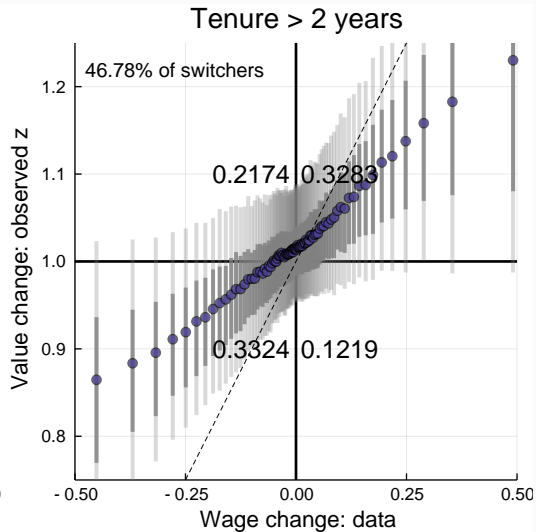
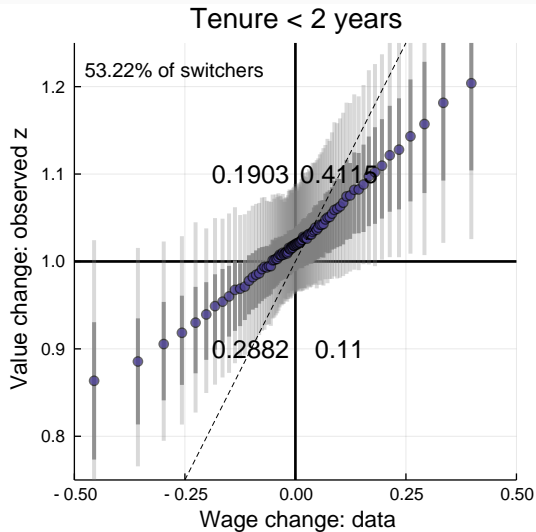


Distribution of value changes

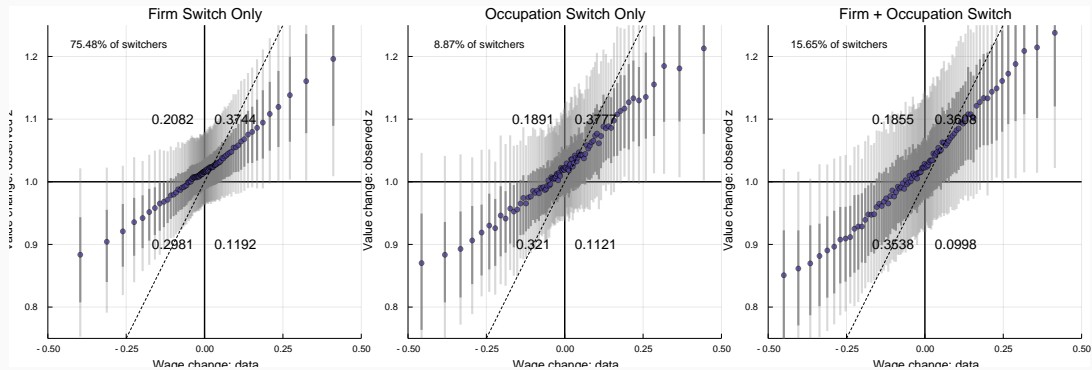


# EDUCATION × GENDER



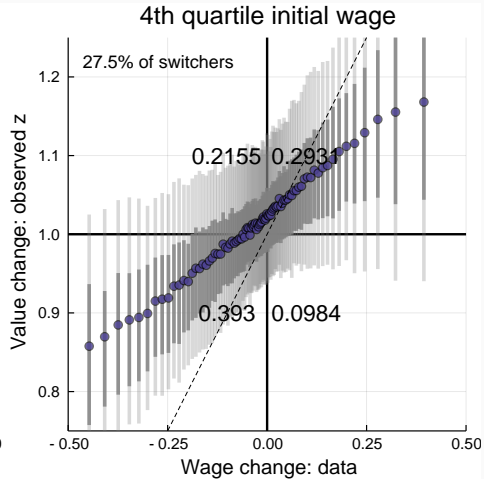
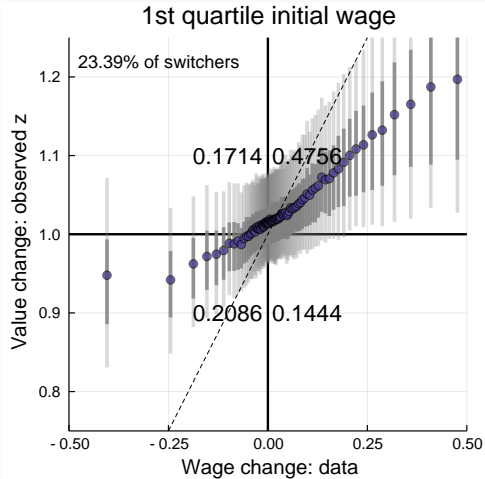


# FIRM AND OCCUPATION SWITCHES



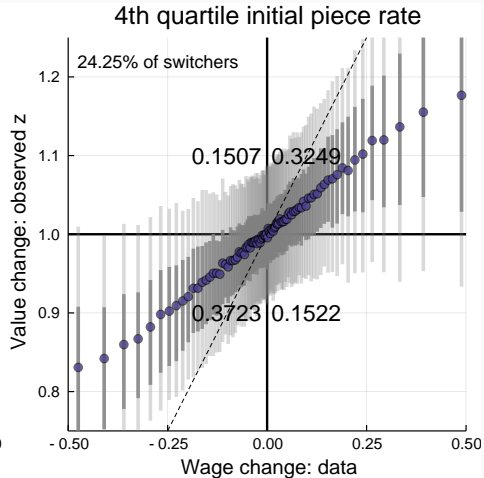
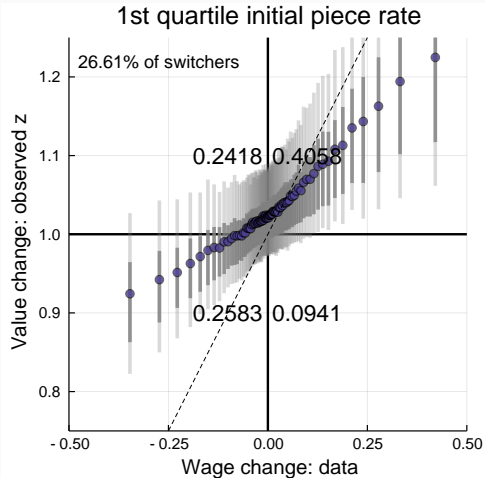
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# INITIAL WAGE

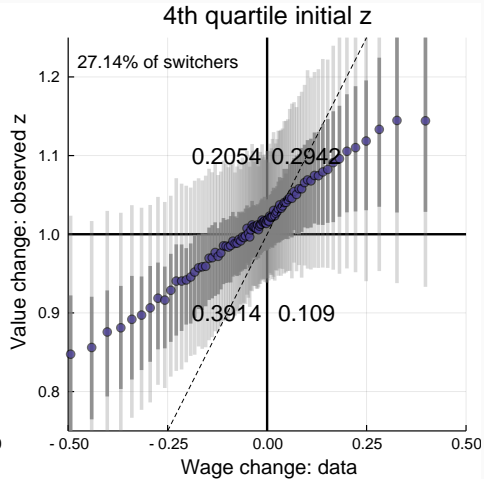
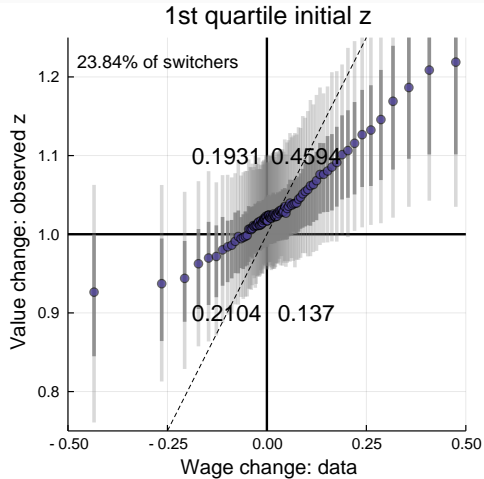




# INITIAL PIECE RATE



# INITIAL Z



# DECOMPOSITION BY QUADRANT

