Imitation and Inverse Reinforcement Learning

• Today:

Imitation and Inverse Reinforcement Learning

Today:

- What if you don't know the reward function and just want to act like an expert?
 - Imitation Learning
 - Inverse Reinforcement Learning

Trivia: When was the first car driven with a Neural Network?

2012 < 1998 1980

Trivia: When was the first car driven with a Neural Network?



Replying to @GTARobotics

GPU? Gez, ALVINN ran on 100 MFLOP CPU, ~10x slower than iWatch; Refrigerator-size & needed 5000 watt generator. @olivercameron

What's Hidden in the Hidden Layers?

The contents can be easy to find with a geometrical problem, but the hidden layers have yet to give up all their secrets

David S. Touretzky and Dean A. Pomerleau

AUGUST 1989 • B Y T E 231

tions, we fed the network road images taken under a wide variety of viewing angles and lighting conditions. It would be impractical to try to collect thousands of real road images for such a data set. Instead, we developed a synthetic roadimage generator that can create as many training examples as we need.

To train the network, 1200 simulated road images are presented 40 times each, while the weights are adjusted using the back-propagation learning algorithm. This takes about 30 minutes on Carnegie Mellon's Warp systolic-array supercomputer. (This machine was designed at Carnegie Mellon and is built by General Electric. It has a peak rate of 100 million floating-point operations per second and can compute weight adjustments for back-propagation networks at a rate of 20 million connections per second.)

Once it is trained, ALVINN can accurately drive the NAVLAB vehicle at about 3½ miles per hour along a path through a wooded area adjoining the Carnegie Mellon campus, under a variety of weather and lighting conditions. This speed is nearly twice as fast as that achieved by non-neural-network algorithms running on the same vehicle. Part of the reason for this is that the forward pass of a back-propagation network can be computed quickly. It takes about 200

milliseconds on the Sun-3/160 workstation installed on the NAVLAB.

The hidden-layer representations AL-VINN develops are interesting. When trained on roads of a fixed width, the net-

work chooses a representation in which hidden units act as detectors for complete roads at various positions and orientations. When trained on roads of variable



Photo 1: The NAVLAB autonomous navigation test-bed vehicle and the road used for trial runs.

Trivia: When was the first car driven with a Neural Network?



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Photo 1: The NAVLAB autonomous navigation test-bed vehicle and the road used for trial runs.

1995: 2797/2849 miles (98.2%)





Behavioral Cloning

Behavioral Cloning

$$\max_{\substack{ heta \ -}} \max_{(s,a) \in D} \pi_{ heta}(a \mid s)$$

Behavioral Cloning

$$\max_{ heta} \prod_{(s,a) \in D} \pi_{ heta}(a \mid s)$$

Problem: Cascading Errors

How did ALVINN do it?

3.2. TRAINING "ON-THE-FLY" WITH REAL DATA

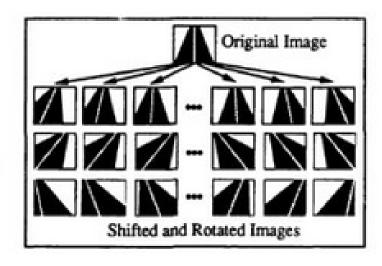


Figure 3.4: The single original video image is shifted and rotated to create multiple training exemplars in which the vehicle appears to be at different locations relative to the road.

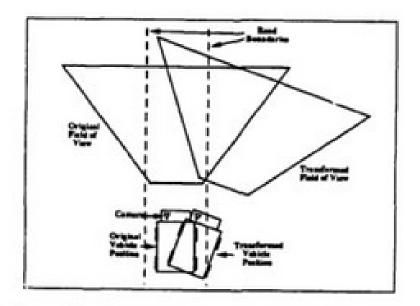
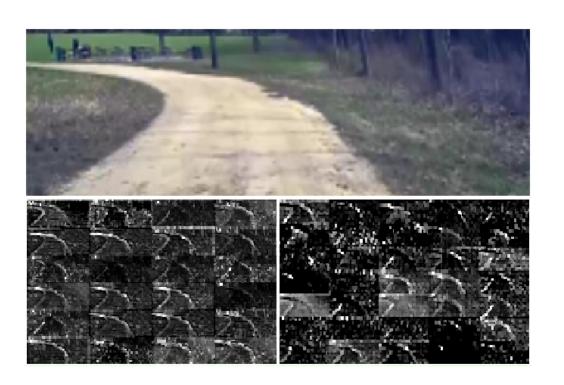


Figure 3.5: An aerial view of the vehicle at two different positions, with the corresponding sensor fields of view. To simulate the image transformation that would result from such a change in position and orientation of the vehicle, the overlap between the two field of view trapezoids is computed and used to direct resampling of the original image.

How did NVIDIA do it in 2016?



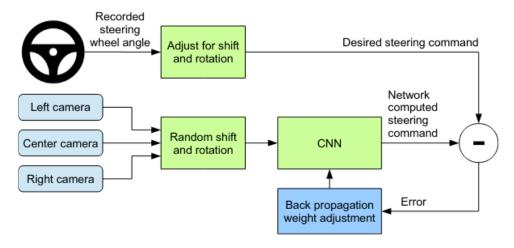


Figure 2: Training the neural network.

```
function optimize(M::DataSetAggregation, D, θ)
    P, bc, k_max, m = M.P, M.bc, M.k_max, M.m
     d, b, \pi E, \pi \theta = M.d, M.b, M.\pi E, M.\pi \theta
     \theta = \text{optimize}(bc, D, \theta)
     for k in 2:k_max
          for i in 1:m
               s = rand(b)
              for j in 1:d
                    push!(D, (s, \pi E(s)))
                    a = rand(\pi\theta(\theta, s))
                    s = rand(P.T(s, a))
               end
          end
          \theta = \text{optimize}(bc, D, \theta)
     end
     return θ
end
```

```
function optimize(M::DataSetAggregation, D, θ)
     \mathcal{P}, bc, k_max, m = M.\mathcal{P}, M.bc, M.k_max, M.m
      d, b, \pi E, \pi \theta = M.d, M.b, M.\pi E, M.\pi \theta
      \theta = \text{optimize}(bc, D, \theta)
      for k in 2:k_max
           for i in 1:m
                 s = rand(b)
                 for j in 1:d
                       push!(D, (s, \pi E(s)))

a = rand(\pi \theta(\theta, s))

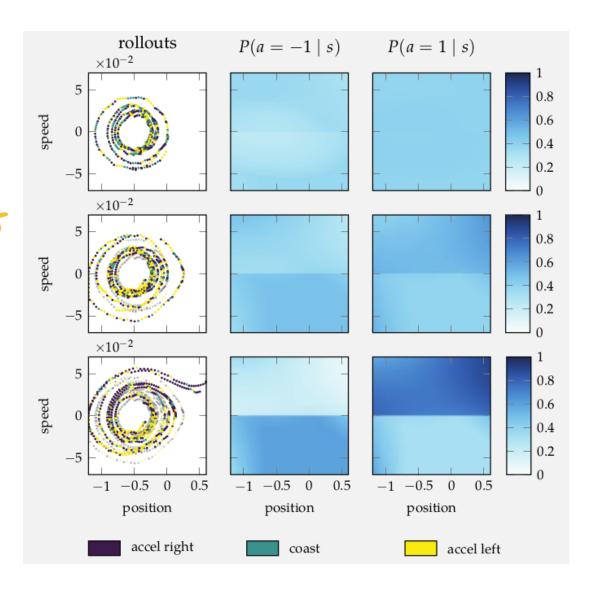
s = rand(\mathcal{P}.T(s, a))
                 end
            end
            \theta = \text{optimize}(bc, D, \theta)
      end
      return θ
end
```

```
function optimize(M::DataSetAggregation, D, θ)
     P, bc, k_max, m = M.P, M.bc, M.k_max, M.m
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                 s = rand(b)
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a = rand(\pi \theta(\theta, s))

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                 end
            end
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     for k in 2:k_max
           for i in 1:m
                 s = rand(b)
                 for j in 1:d
                       push!(D, (s, \pi E(s)))
a = rand(\pi \theta \theta, s))
                 end
           end
           \theta = \text{optimize}(bc, D, \theta)
     end
     return θ
end
```



```
function optimize(M::SMILe, θ)
     \mathcal{P}, bc, k_max, m = M.\mathcal{P}, M.bc, M.k_max, M.m
     d, b, \beta, \pi E, \pi \theta = M.d, M.b, M.\beta, M.\pi E, M.\pi \theta
     \mathcal{A}, T = \mathcal{P}.\mathcal{A}, \mathcal{P}.T
     \theta s = []
     \pi = s \rightarrow \pi E(s)
     for k in 1:k_max
           # execute latest \pi to get new data set D
           D = []
          for i in 1:m
                s = rand(b)
                for j in 1:d
                      push!(D, (s, \pi E(s)))
                     a = \pi(s)
                      s = rand(T(s, a))
                end
           end
           # train new policy classifier
           \theta = \text{optimize}(bc, D, \theta)
           push!(\thetas, \theta)
           # compute a new policy mixture
           P\pi = \text{Categorical}(\text{normalize}([(1-\beta)^{(i-1)} \text{ for } i \text{ in } 1:k],1))
           \pi = s \rightarrow begin
                if rand() < (1-\beta)^{k-1}
                     return πE(s)
                else
                      return rand(Categorical(\pi\theta(\theta s[rand(P\pi)], s)))
                end
           end
     end
     Ps = normalize([(1-\beta)^{(i-1)} \text{ for } i \text{ in } 1:k_max],1)
     return Ps, θs
end
```

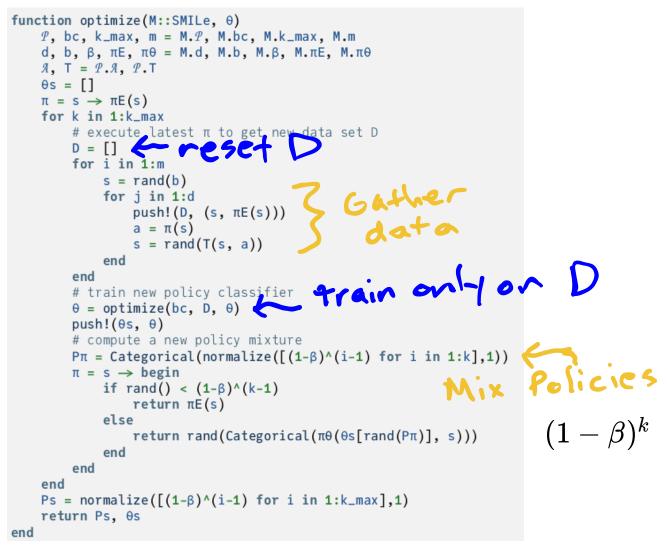
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function optimize(M::SMILe, θ)
     \mathcal{P}, bc, k_max, m = M.\mathcal{P}, M.bc, M.k_max, M.m
     d, b, \beta, \pi E, \pi \theta = M.d, M.b, M.\beta, M.\pi E, M.\pi \theta
     \mathcal{A}, T = \mathcal{P}.\mathcal{A}, \mathcal{P}.T
     \theta s = []
    \pi = s \rightarrow \pi E(s)
     for k in 1:k_max
          # execute latest \pi to get new data set D
          for i in 1:m
               s = rand(b)
               for j in 1:d
                     push!(D, (s, \pi E(s)))
                     a = \pi(s)
                     s = rand(T(s, a))
               end
          end
          # train new policy classifier
          \theta = \text{optimize}(bc, D, \theta)
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                else
                     return rand(Categorical(\pi\theta(\theta s[rand(P\pi)], s)))
                end
          end
     end
     Ps = normalize([(1-\beta)^{(i-1)}] for i in 1:k_max],1)
     return Ps, θs
end
```

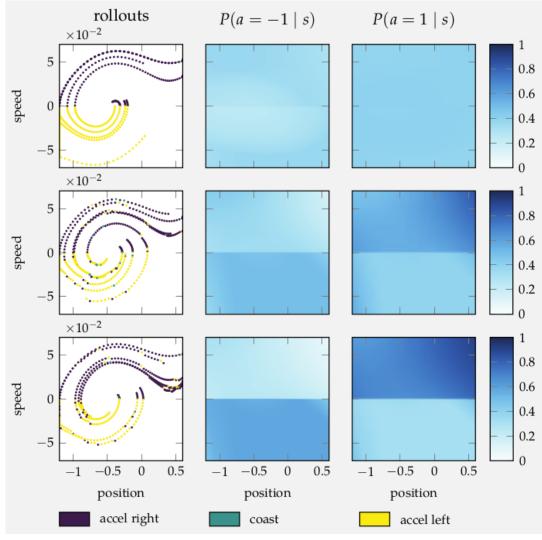
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     \mathcal{P}, bc, k_max, m = M.\mathcal{P}, M.bc, M.k_max, M.m
     d, b, \beta, \pi E, \pi \theta = M.d, M.b, M.\beta, M.\pi E, M.\pi \theta
     A, T = P.A, P.T
     \theta s = []
    \pi = s \rightarrow \pi E(s)
     for k in 1:k_max
          # execute latest \pi to get new data set D
          for i in 1:m
               s = rand(b)
               for j in 1:d
                    s = rand(T(s, a))
               end
          end
          # train new policy classifier
          \theta = \text{optimize}(bc, D, \theta)
          push!(\thetas, \theta)
          # compute a new policy mixture
          P\pi = Categorical(normalize([(1-\beta)^{(i-1)} for i in 1:k],1))
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               if rand() < (1-\beta)^{(k-1)}
                    return πE(s)
               else
                    return rand(Categorical(\pi\theta(\theta s[rand(P\pi)], s)))
               end
          end
     end
     Ps = normalize([(1-\beta)^{(i-1)} \text{ for } i \text{ in } 1:k_max],1)
     return Ps, θs
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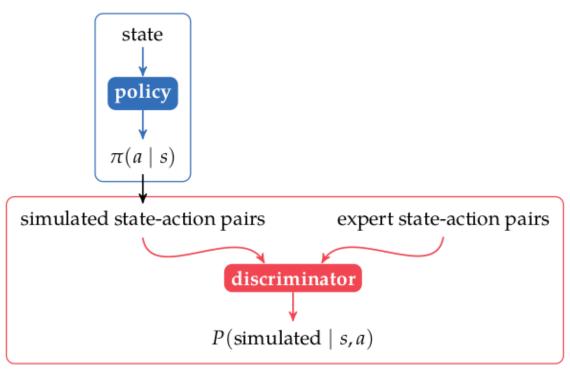
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    A, T = P.A, P.T
    \theta s = []
    \pi = s \rightarrow \pi E(s)
    for k in 1:k_max
         # execute latest π to get new data set D
         for i in 1:m
             s = rand(b)
             for j in 1:d
                  s = rand(T(s, a))
              end
        # train new policy classifier Train on O
         push!(\thetas, \theta)
         # compute a new policy mixture
         P\pi = Categorical(normalize([(1-\beta)^{(i-1)} for i in 1:k],1))
         \pi = s \rightarrow begin
             if rand() < (1-\beta)^{(k-1)}
                  return πE(s)
              else
                  return rand(Categorical(\pi\theta(\theta s[rand(P\pi)], s)))
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    end
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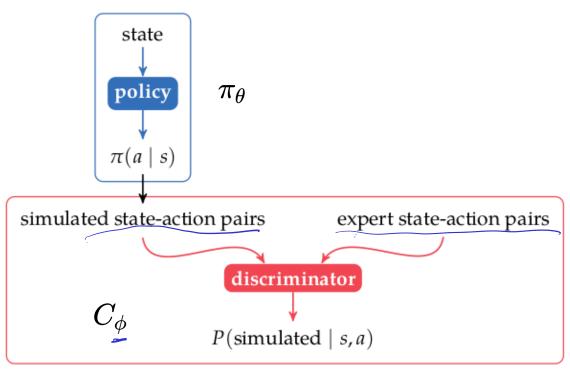
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    for k in 1:k_max
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              else
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              end
         end
    end
    Ps = normalize([(1-\beta)^{(i-1)}] for i in 1:k_max],1)
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    A, T = P.A, P.T
    \theta s = []
    \pi = s \rightarrow \pi E(s)
    for k in 1:k_max
        # execute latest π to get new data set D
        for i in 1:m
            s = rand(b)
                 s = rand(T(s, a))
             end
        push!(\thetas, \theta)
        # compute a new policy mixture
        P\pi = Categorical(normalize([(1-\beta)^{(i-1)} for i in 1:k],1))
        \pi = s \rightarrow begin
            if rand() < (1-\beta)^{k-1}
                 return πE(s)
             else
                                                                         (1-\beta)^k
                 return rand(Categorical(\pi\theta(\theta s[rand(P\pi)], s)))
             end
        end
    end
    Ps = normalize([(1-\beta)^{(i-1)}] for i in 1:k_max],1)
    return Ps, θs
end
```

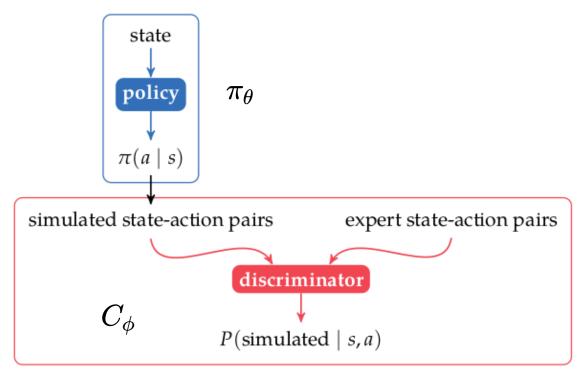








$$\max_{\mathbf{\Phi}} \min_{\mathbf{\theta}} \mathbb{E}_{(s,a) \sim \pi_{\mathbf{\theta}}} \left[\log(C_{\mathbf{\Phi}}(s,a)) \right] + \mathbb{E}_{(s,a) \sim \mathcal{D}} \left[\log(1 - C_{\mathbf{\Phi}}(s,a)) \right]$$



GANs are frighteningly good at generating believable synthetic things

$$\max_{\mathbf{\Phi}} \min_{\mathbf{\theta}} \mathbb{E}_{(s,a) \sim \pi_{\mathbf{\theta}}} \left[\log(C_{\mathbf{\Phi}}(s,a)) \right] + \mathbb{E}_{(s,a) \sim \mathcal{D}} \left[\log(1 - C_{\mathbf{\Phi}}(s,a)) \right]$$

Concretive Adversarial Imitation g (GAIL)

simula max min

GANs are frighteningly good at generating believable synthetic things

What if we know the dynamics, but not the reward?

What if we know the dynamics, but not the reward?

Reinforcement Learning

Inverse Reinforcement Learning

Input

Output

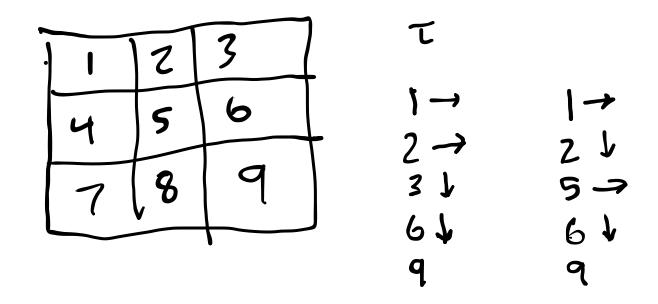
What if we know the dynamics, but not the reward?

Reinforcement Learning	Inverse Reinforcement Learning
------------------------	--------------------------------

Input Environment (S, A, T, R) $S, A, T, \{\tau\}$

Output π^*

Exercise



1		
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	4 (
		47
	1	+70

What is the reward function?

$$R_{\mathbf{\Phi}}(s, a) = \mathbf{\Phi}^{\top} \mathbf{\beta}(s, a)$$

$$R_{oldsymbol{\Phi}}(s,a) = oldsymbol{\Phi}^{ op} oldsymbol{eta}(s,a)$$
 $eta(s,a) \in \{0,1\}^n$

$$R_{oldsymbol{\phi}}(s,a) = oldsymbol{\phi}^{ op} oldsymbol{eta}(s,a)$$
 $eta(s,a) \in \{0,1\}^n$ $\|oldsymbol{\phi}\|_2 \le 1$

$$R_{\mathbf{\Phi}}(s, a) = \mathbf{\Phi}^{\top} \mathbf{\beta}(s, a)$$

$$\beta(s, a) \in \{0, 1\}^n$$

$$\|\mathbf{\Phi}\|_2 \le 1$$

$$\mathbb{E}_{s \sim b}[\underline{U(s)}] = \mathbb{E}_{\tau} \left[\sum_{k=1}^{d} \gamma^{k-1} R_{\mathbf{\Phi}}(s^{(k)}, a^{(k)}) \right]$$

$$= \mathbb{E}_{\tau} \left[\sum_{k=1}^{d} \gamma^{k-1} \mathbf{\Phi}^{\top} \beta(s^{(k)}, a^{(k)}) \right]$$

$$= \mathbf{\Phi}^{\top} \left(\mathbb{E}_{\tau} \left[\sum_{k=1}^{d} \gamma^{k-1} \beta(s^{(k)}, a^{(k)}) \right] \right)$$

$$= \mathbf{\Phi}^{\top} \mathbf{\mu}_{\pi}$$

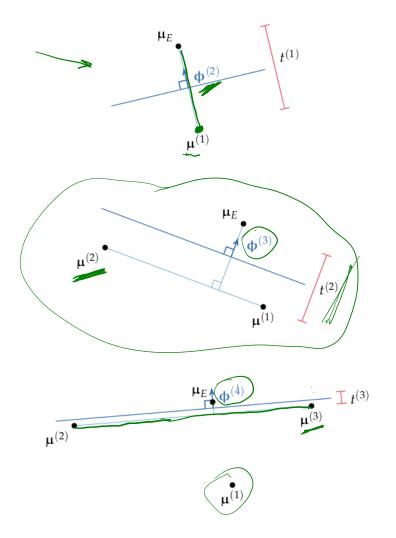
Maximum Margin Inverse Reinforcement Learning

$$R_{oldsymbol{\Phi}}(s,a) = oldsymbol{\Phi}^{ op}oldsymbol{eta}(s,a)$$
 $eta(s,a) \in \{0,1\}^n$ $\|oldsymbol{\Phi}\|_2 \leq 1$

$$\begin{split} \mathbb{E}_{s \sim b}[U(s)] &= \mathbb{E}_{\tau} \left[\sum_{k=1}^{d} \gamma^{k-1} R_{\Phi}(s^{(k)}, a^{(k)}) \right] \\ &= \mathbb{E}_{\tau} \left[\sum_{k=1}^{d} \gamma^{k-1} \Phi^{\top} \beta(s^{(k)}, a^{(k)}) \right] \\ &= \Phi^{\top} \left(\mathbb{E}_{\tau} \left[\sum_{k=1}^{d} \gamma^{k-1} \beta(s^{(k)}, a^{(k)}) \right] \right) \\ &= \Phi^{\top} \mu_{\pi} \\ &= \Phi^{\top} \mu_{\pi} \end{split}$$

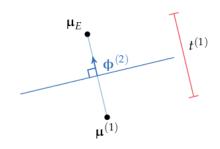
maximize
$$t$$
 subject to $\mathbf{\Phi}^{\top} \mathbf{\mu}_{E} \geq \mathbf{\Phi}^{\top} \mathbf{\mu}^{(i)} + t$ for $i = 1, \dots, k-1$ $\|\mathbf{\Phi}\|_{2} \leq 1$

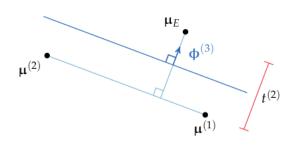
Maximum Margin Inverse Reinforcement Learning

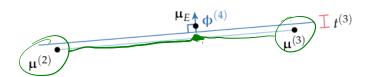


maximize
$$t$$
subject to $\Phi^{\top} \underline{\mu}_{E} \geq \Phi^{\top} \underline{\mu}^{(i)} + t$ for $i = 1, ..., k-1$
 $\|\Phi\|_{2} \leq 1$

Maximum Margin Inverse Reinforcement Learning







maximize
$$t$$
 subject to $\mathbf{\Phi}^{\top} \mathbf{\mu}_{E} \geq \mathbf{\Phi}^{\top} \mathbf{\mu}^{(i)} + t \text{ for } i = 1, \dots, k-1$ $\|\mathbf{\Phi}\|_{2} \leq 1$

$$\begin{array}{ll} \text{minimize} & \|\mu_E - \mu_\lambda\|_2 \\ \text{subject to} & \lambda \geq 0 \\ & \|\lambda\|_1 = 1 \end{array}$$

$$\underbrace{P_{\mathbf{\Phi}}(\tau)}_{} = \underbrace{\frac{1}{Z(\mathbf{\Phi})}}_{} \exp(R_{\mathbf{\Phi}}^{\checkmark}(\underline{\tau}))$$

$$P_{\mathbf{\Phi}}(\tau) = \frac{1}{Z(\mathbf{\Phi})} \exp(R_{\mathbf{\Phi}}(\tau))$$
 $Z(\mathbf{\Phi}) = \sum_{\tau} \exp(R_{\mathbf{\Phi}}(\tau))$

$$P_{\mathbf{\Phi}}(\tau) = \frac{1}{Z(\mathbf{\Phi})} \exp(R_{\mathbf{\Phi}}(\tau)) \qquad Z(\mathbf{\Phi}) = \sum_{\tau} \exp(R_{\mathbf{\Phi}}(\tau))$$

$$\max_{\mathbf{\Phi}} f(\mathbf{\Phi}) = \max_{\mathbf{\Phi}} \sum_{\tau \in \mathcal{D}} \log P_{\mathbf{\Phi}}(\tau)$$

$$\max_{\mathbf{\Phi}} f(\mathbf{\Phi}) = \max_{\mathbf{\Phi}} \sum_{\tau \in \mathcal{D}} \log P_{\mathbf{\Phi}}(\tau)$$

$$\begin{aligned} \max_{\mathbf{\Phi}} f(\mathbf{\Phi}) &= \max_{\mathbf{\Phi}} \sum_{\tau \in \mathcal{D}} \frac{\log P_{\mathbf{\Phi}}(\tau)}{T} \\ f(\mathbf{\Phi}) &= \sum_{\tau \in \mathcal{D}} \log \frac{1}{Z(\mathbf{\Phi})} \exp(R_{\mathbf{\Phi}}(\tau)) \\ &= \left(\sum_{\tau \in \mathcal{D}} R_{\mathbf{\Phi}}(\tau)\right) - |\mathcal{D}| \log Z(\mathbf{\Phi}) \\ &= \left(\sum_{\tau \in \mathcal{D}} R_{\mathbf{\Phi}}(\tau)\right) - |\mathcal{D}| \log \sum_{\tau} \exp(R_{\mathbf{\Phi}}(\tau)) \end{aligned}$$

$$\max_{\mathbf{\Phi}} f(\mathbf{\Phi}) = \max_{\mathbf{\Phi}} \sum_{\tau \in \mathcal{D}} \log P_{\mathbf{\Phi}}(\tau)$$

$$\begin{split} f(\mathbf{\phi}) &= \sum_{\tau \in \mathcal{D}} \log \frac{1}{Z(\mathbf{\phi})} \exp(R_{\mathbf{\phi}}(\tau)) \\ &= \left(\sum_{\tau \in \mathcal{D}} R_{\mathbf{\phi}}(\tau)\right) - |\mathcal{D}| \log Z(\mathbf{\phi}) \\ &= \left(\sum_{\tau \in \mathcal{D}} R_{\mathbf{\phi}}(\tau)\right) - |\mathcal{D}| \log \sum_{\tau} \exp(R_{\mathbf{\phi}}(\tau)) \end{split}$$

$$\underline{\nabla_{\Phi} f} = \left(\sum_{\tau \in \mathcal{D}} \nabla_{\Phi} R_{\Phi}(\tau)\right) - \frac{|\mathcal{D}|}{\sum_{\tau} \exp(R_{\Phi}(\tau))} \sum_{\tau} \exp(R_{\Phi}(\tau)) \nabla_{\Phi} R_{\Phi}(\tau)
= \left(\sum_{\tau \in \mathcal{D}} \nabla_{\Phi} R_{\Phi}(\tau)\right) - |\mathcal{D}| \sum_{\tau} P_{\Phi}(\tau) \nabla_{\Phi} R_{\Phi}(\tau)
= \left(\sum_{\tau \in \mathcal{D}} \nabla_{\Phi} R_{\Phi}(\tau)\right) - |\mathcal{D}| \sum_{s} b_{\gamma, \Phi}(s) \sum_{a} \pi_{\Phi}(a \mid s) \underline{\nabla_{\Phi} R_{\Phi}(s, a)}$$
(18.15)

$$\max_{\mathbf{\Phi}} f(\mathbf{\Phi}) = \max_{\mathbf{\Phi}} \sum_{\tau \in \mathcal{D}} \log P_{\mathbf{\Phi}}(\tau)$$

$$\begin{split} f(\mathbf{\phi}) &= \sum_{\tau \in \mathcal{D}} \log \frac{1}{Z(\mathbf{\phi})} \exp(R_{\mathbf{\phi}}(\tau)) \\ &= \left(\sum_{\tau \in \mathcal{D}} R_{\mathbf{\phi}}(\tau)\right) - |\mathcal{D}| \log Z(\mathbf{\phi}) \\ &= \left(\sum_{\tau \in \mathcal{D}} R_{\mathbf{\phi}}(\tau)\right) - |\mathcal{D}| \log \sum_{\tau} \exp(R_{\mathbf{\phi}}(\tau)) \end{split}$$

$$\underline{\nabla_{\Phi} f} = \left(\sum_{\tau \in \mathcal{D}} \nabla_{\Phi} R_{\Phi}(\tau)\right) - \frac{|\mathcal{D}|}{\sum_{\tau} \exp(R_{\Phi}(\tau))} \sum_{\tau} \exp(R_{\Phi}(\tau)) \nabla_{\Phi} R_{\Phi}(\tau)$$

$$= \left(\sum_{\tau \in \mathcal{D}} \nabla_{\Phi} R_{\Phi}(\tau)\right) - |\mathcal{D}| \sum_{\tau} P_{\Phi}(\tau) \nabla_{\Phi} R_{\Phi}(\tau)$$

$$= \left(\sum_{\tau \in \mathcal{D}} \nabla_{\Phi} R_{\Phi}(\tau)\right) - |\mathcal{D}| \sum_{s} b_{\gamma, \Phi}(s) \sum_{a} \pi_{\Phi}(a \mid s) \nabla_{\Phi} R_{\Phi}(s, a)$$
(18.16)

Discounted visitation probability

Optimal policy under R_ϕ

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