Experiment 6

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Branch: IT **Section/Group: 22BET_IOT-701/A**

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Subject Name: AP Lab - 2 **Subject Code: 22ITP-351**

1. Aim:

To develop efficient Dynamic Programming (DP) solutions for optimization problems, including counting paths, maximizing sums and products, determining reachability, and finding optimal subsequences, while analyzing and improving time and space complexity.

i.) Climbing Stairs
ii.) Maximum Subarray
iii.) House Robber
iv.) Jump Game
v.) Unique Paths
vi.) Coin Change
vii.) Longest Increasing Subsequence
viii.) Maximum Product Subarray
ix.) Decode Ways

2. Objective:

- Apply Dynamic Programming (DP) to solve optimization and sequence-based problems efficiently.
- Understand state transitions and recurrence relations in problems like Climbing Stairs and Coin Change.
- Optimize subarray and subsequence problems such as Maximum Subarray, Maximum Product Subarray, and Longest Increasing Subsequence.
- Determine feasibility in Jump Game and Decode Ways using greedy and DP approaches.
- Compute unique paths and optimal strategies in problems like Unique Paths and House Robber.
- Analyze and improve time and space complexity, comparing $O(n^2)$ DP vs. $O(n \log n)$ methods.

3. Code:

Problem 1: Climbing Stairs

```
class Solution {
public:
    int climbStairs(int n) {
        if (n == 1) return 1;
```

```
        if (n == 2) return 2;
        int prev1 = 2, prev2 = 1, current;
        for (int i = 3; i <= n; i++) {
            current = prev1 + prev2;
            prev2 = prev1;
            prev1 = current;
        }
        return current;
    }
};
```

Problem 2: Maximum Subarray

```
class Solution {
public:
    int maxSubArray(vector<int>& nums) {
        int maxSum = INT_MIN, currentSum = 0;
        for (int num : nums) {
            currentSum += num;
            maxSum = max(maxSum, currentSum);
            if (currentSum < 0) currentSum = 0;
        }
        return maxSum;
    }
};
```

Problem 3: House Robber

```
class Solution {
public:
    int rob(vector<int>& nums) {
         if (nums.empty()) return 0;
        if (nums.size() == 1) return nums[0];
        int prev1 = 0, prev2 = 0;
        for (int num : nums) {
            int temp = max(prev1, prev2 + num);
            prev2 = prev1;
            prev1 = temp;
        }
        return prev1;
    }
};
```

Problem 4: Jump Game

```
class Solution {
public:
    bool canJump(vector<int>& nums)
         int maxReach = 0;
        int n = nums.size();
        for (int i = 0; i < n; i++) {
```

```
            if (i > maxReach) return false;  // Can't move forward
            maxReach = max(maxReach, i + nums[i]);  // Update max reachable index
            if (maxReach >= n - 1) return true;  // Early exit if last index is reachable
        }
        return true;
    }
};
```

Problem 5: Unique Paths

```
class Solution {
public:
    int uniquePaths(int m, int n) {
        vector<int> dp(n, 1);  // Initialize first row with 1
        for (int i = 1; i < m; i++) {  // Start from row 1
            for (int j = 1; j < n; j++) {
                dp[j] += dp[j - 1];  // Update current cell
            }
        }
        return dp[n - 1];
    }
};
```

6: Coin Change

```
class Solution {
public:
    int coinChange(vector<int>& coins, int amount) {
        vector<int> dp(amount + 1, amount + 1);
        dp[0] = 0;
        for (int i = 1; i <= amount; i++) {
            for (int coin : coins) {
                if (i >= coin) {
                    dp[i] = min(dp[i], 1 + dp[i - coin]);
                }
            }
        }
        return (dp[amount] == amount + 1) ? -1 : dp[amount];
    }
};
```

Problem 7: Longest Increasing Subsequence

```
class Solution {
public:
    int lengthOfLIS(vector<int>& nums) {
        int n = nums.size();
        vector<int> dp(n, 1);  // Initialize all values to 1
        int maxLength = 1;
        for (int i = 1; i < n; i++) {
            for (int j = 0; j < i; j++) {
```

```
                if (nums[j] < nums[i]) {
                    dp[i] = max(dp[i], dp[j] + 1);
                }
            }
            maxLength = max(maxLength, dp[i]);
        }
        return maxLength;
    }
};
```

Problem 8: Maximum Product Subarray

```
class Solution {
public:
    int maxProduct(vector<int>& nums) {
        int n = nums.size();
        int maxProd = nums[0], minProd = nums[0], result = nums[0];
        for (int i = 1; i < n; i++) {
            if (nums[i] < 0) swap(maxProd, minProd);  // Swap when encountering negative
            maxProd = max(nums[i], nums[i] * maxProd);
            minProd = min(nums[i], nums[i] * minProd);
            result = max(result, maxProd);  // Update global max
        }
        return result;
    }
};
```

Problem 9: Decode Ways

```
class Solution {
public:
    int numDecodings(string s) {
        int n = s.size();
        if (s[0] == '0') return 0; // Cannot start with zero

        vector<int> dp(n + 1, 0);
        dp[0] = 1; // Empty string has one way
        dp[1] = 1; // First character (if not '0') has one way

        for (int i = 2; i <= n; i++) {
            if (s[i - 1] != '0') {
                dp[i] += dp[i - 1]; // Single digit decoding
            }
            int twoDigit = stoi(s.substr(i - 2, 2)); // Get last two digits
            if (twoDigit >= 10 && twoDigit <= 26) {
                dp[i] += dp[i - 2]; // Two-digit decoding
            }
        }
        return dp[n];
    }
};
```

4. Output:

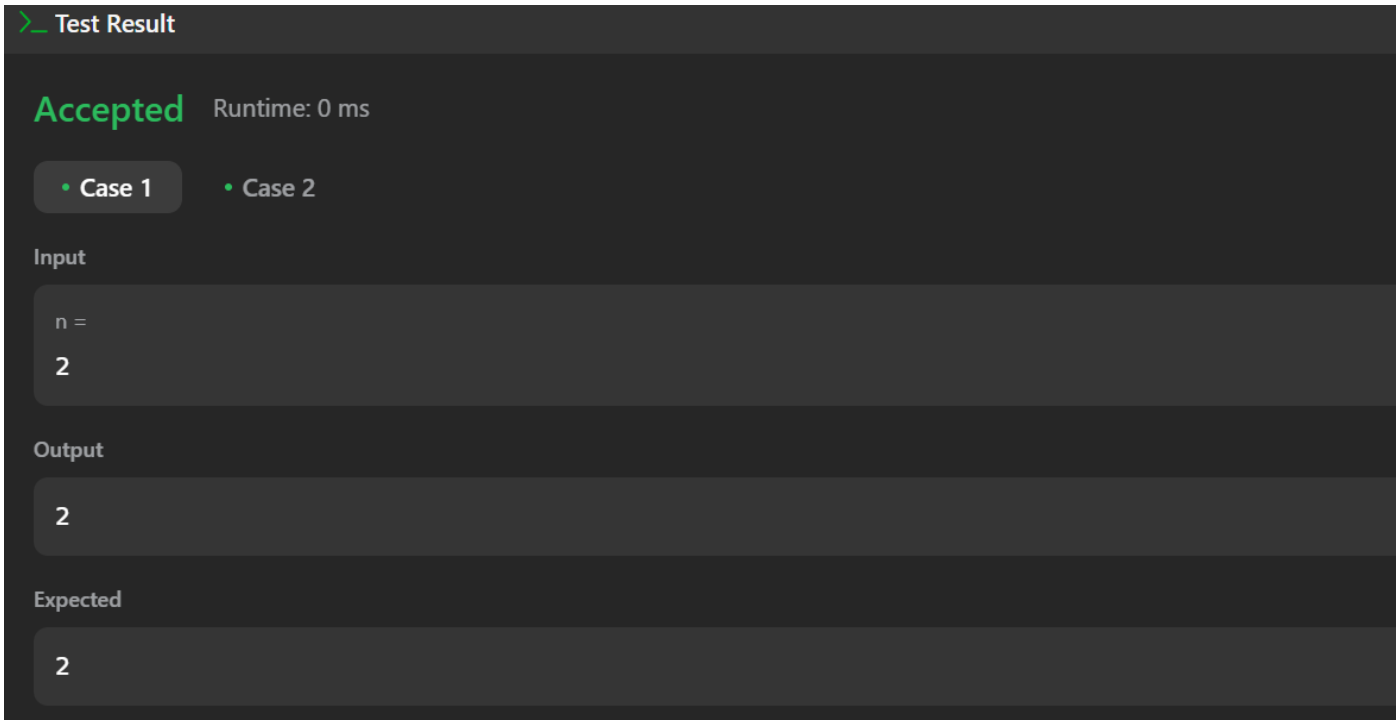

Fig 1. Climbing Stairs

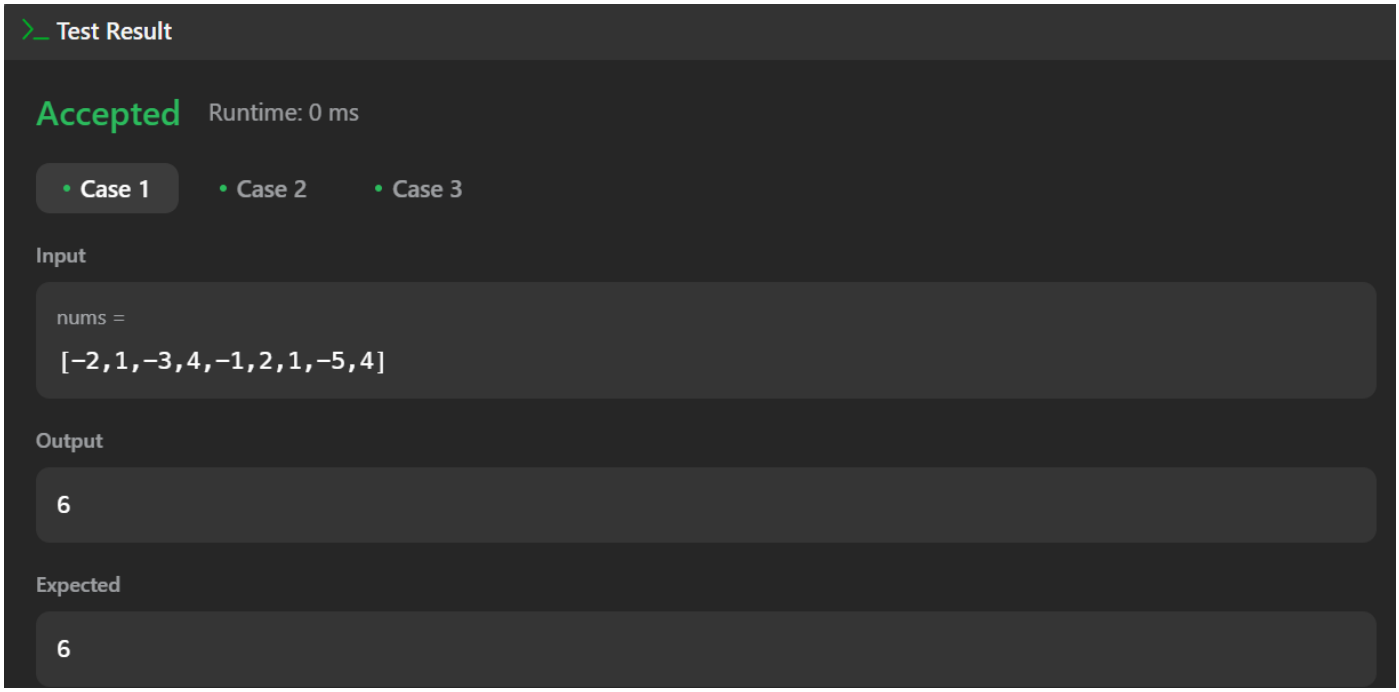

Fig 2. Maximum Subarray

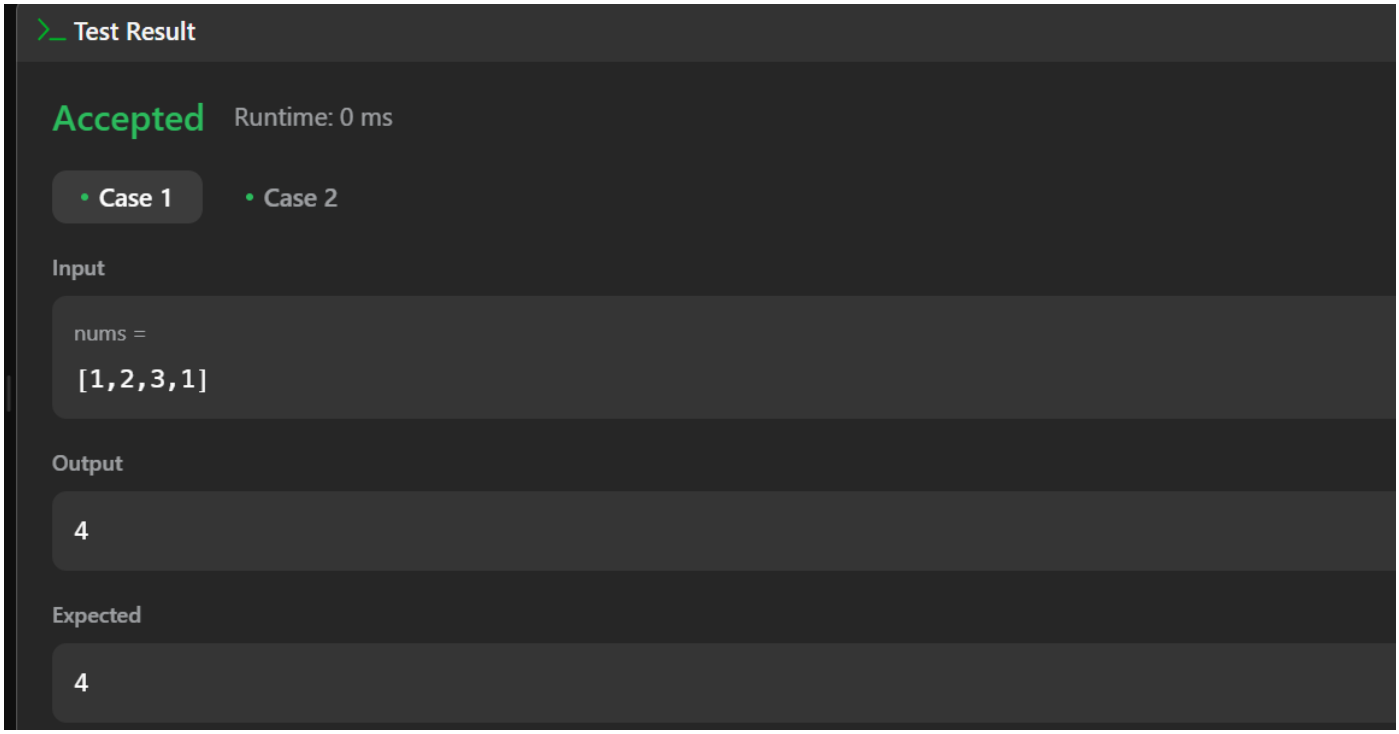

Fig 3. House Robber

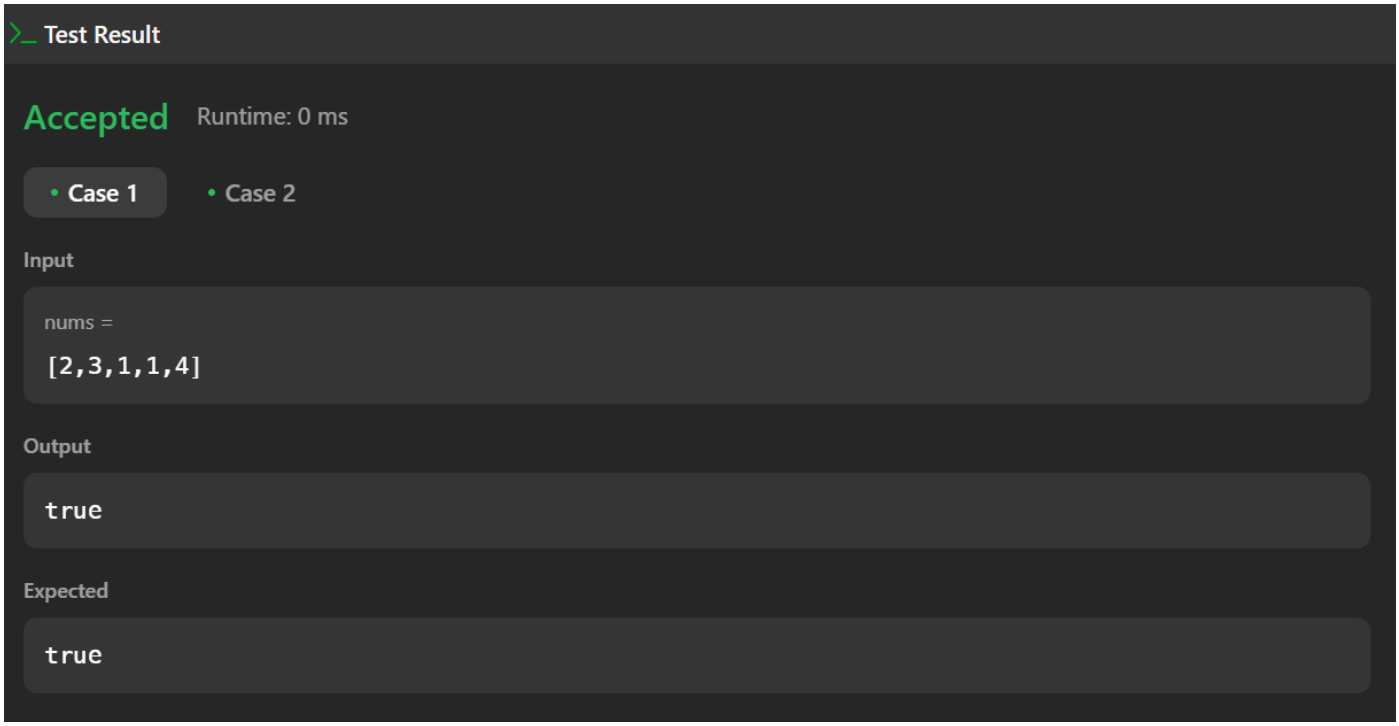

Fig 4. Jump Game

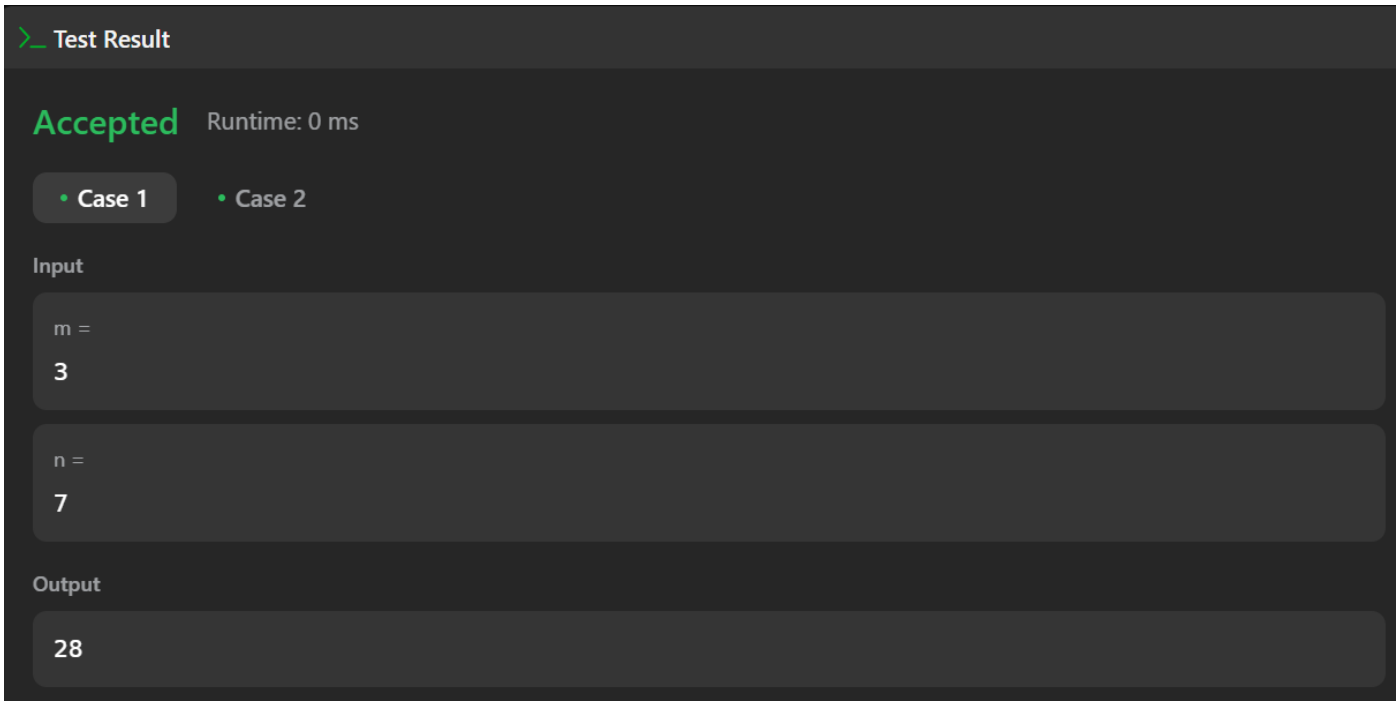

Fig 5. Unique Paths

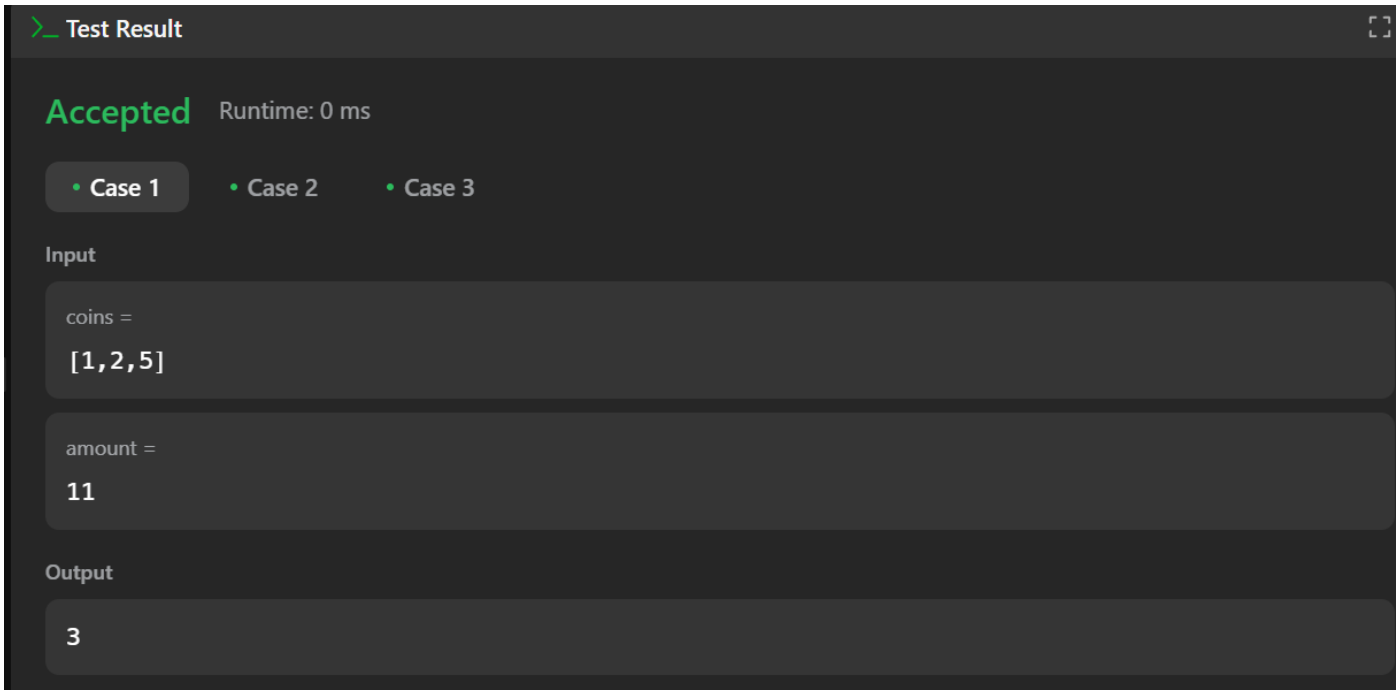

Fig 6. Coin Change

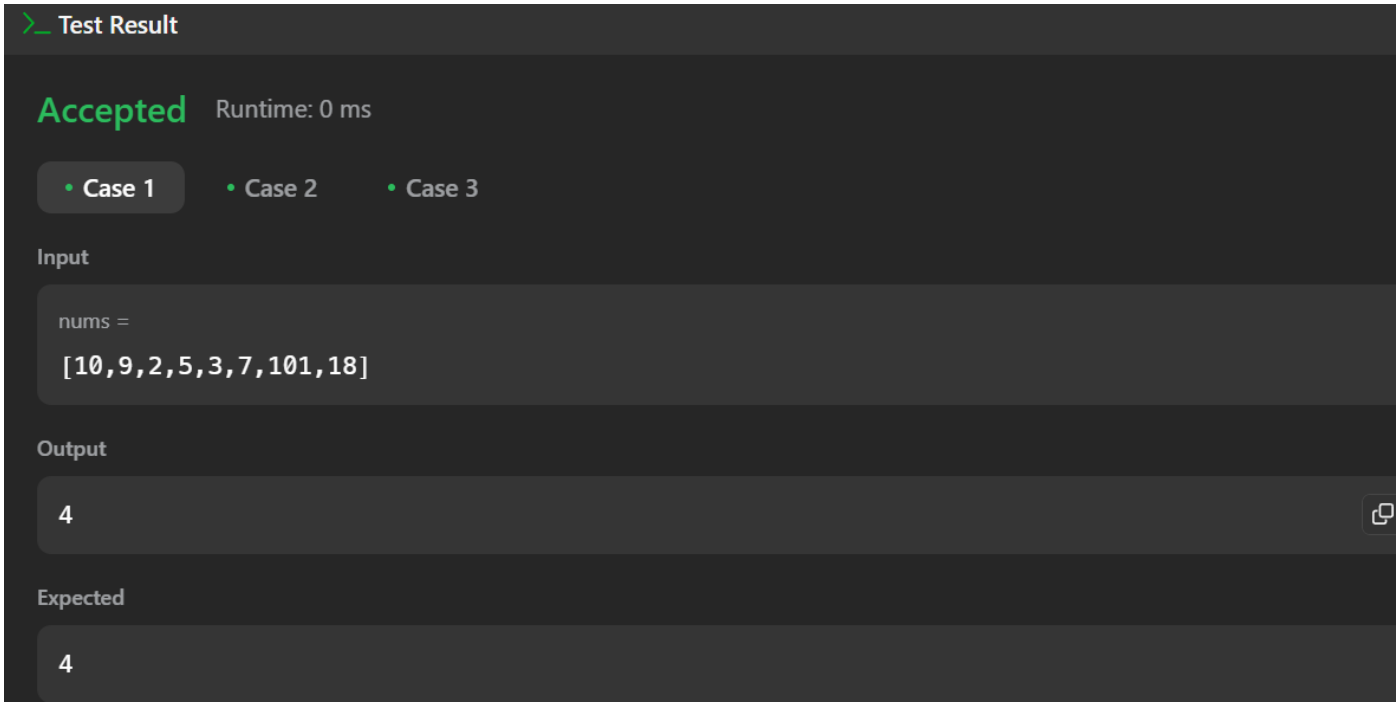

Fig 7. Longest Increasing Subsequence

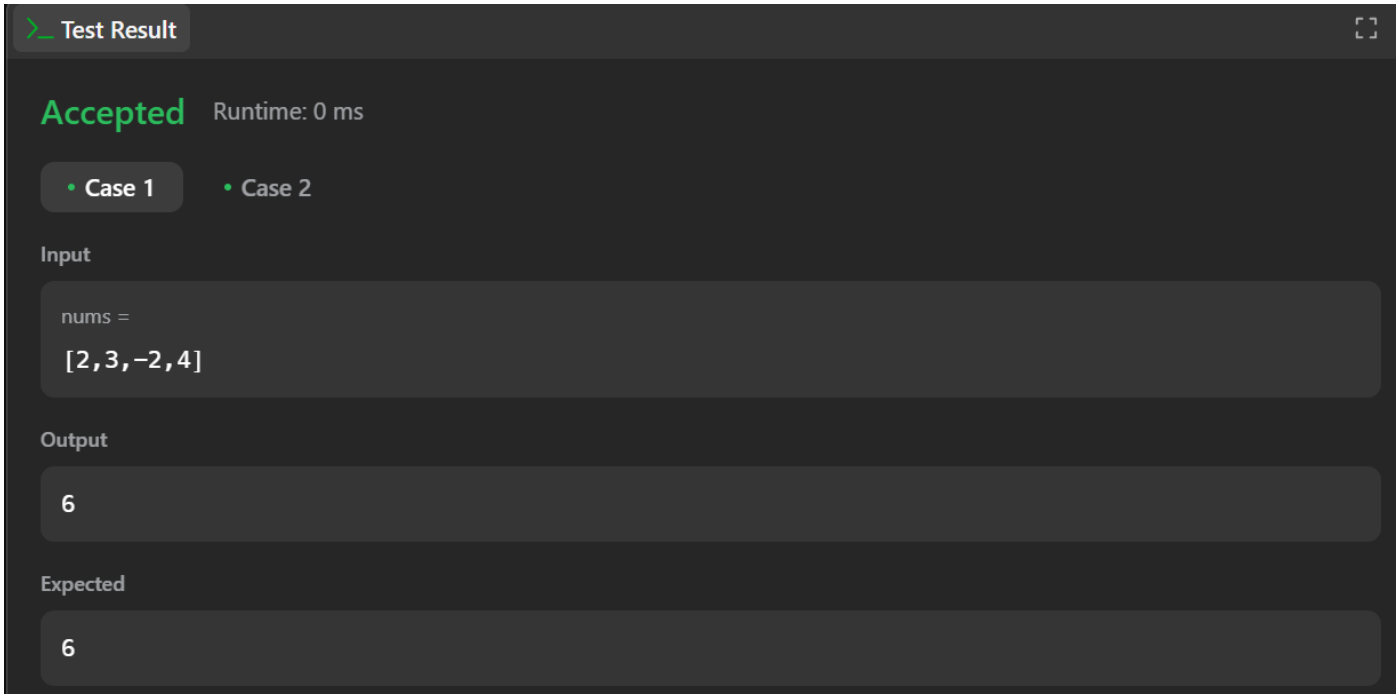

Fig 8. Maximum Product Subarray

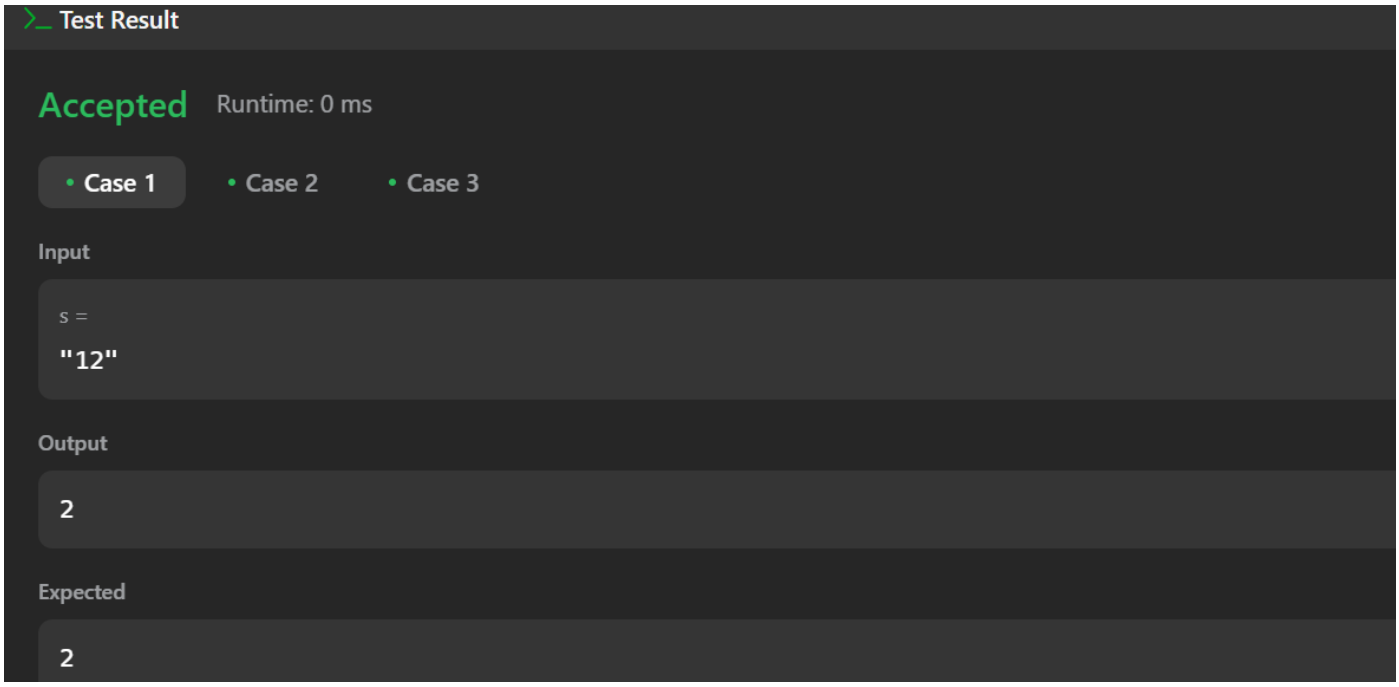

Fig 9. Decode Ways

5. Learning Outcomes:

- Gain a strong understanding of Dynamic Programming (DP) to efficiently solve optimization problems.
- Learn how to manage subproblems and overlapping substructure using a bottom-up DP approach.
- Implement state transitions and recurrence relations in classic problems like Coin Change, Longest Increasing Subsequence (LIS), and Word Break.
- Analyze and optimize solutions by comparing $O(n^2)$ DP methods with O(n log n) approaches.
- Leverage HashSets and Binary Search to improve efficiency in word segmentation and sequence-related problems.