Trajectory Simulation Package

version

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CUSF 6DOF Rocket Trajectory Simulation documentation

Guide

Run the example file .:

```
python example.py
>>Running simulation
>>t=0.00 s alt=0.00 km (h=6.782383938042269e-09 s). Step number 0
>>t=8.61 s alt=1.41 km (h=0.10479235692442031 s). Step number 100
>>t=20.29 s alt=6.65 km (h=0.15804273091835203 s). Step number 200
>>Burnout at t=24.78 s
>>t=78.04 s alt=11.95 km (h=1.1551712462768395 s). Step number 300
```

Technical Documentation

Full technical documentation can be found here

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Trajectory Package

Trajectory Package

Core Functions

6DOF Trajectory Simulator

Contains the classes and functions for the core trajectory simulation

Example

A small, single stage rocket can be found in examples, to run

\$ python example/example.py

Notes

SI units unless stated otherwise Coordinate systems: $x_b, y_b, z_b = Body$ coordinate system (origin on rocket, rotates with the rocket) $x_i, y_i, z_i = I$ lnertial coordinate system (does not rotate, origin at centre of the Earth) $x_i, y_j, z_i = I$ Launch site coordinate system (origin has the launch site's longitude and latitude, but is at altitude = 0). Rotates with the Earth.

Directions are defined below.

• Body:

y points east and z north at take off (before rail alignment is accounted for) x up. x is along the "long" axis of the rocket.

• Launch site:

z points perpendicular to the earth, y in the east direction and x tangential to the earth pointing south

• Inertial:

Origin at centre of the Earth z points to north from centre of earth, x aligned with launchsite at start and y orthogonal

 ${\tt trajectory.main.r_earth}$

Radius of Earth/m

Type: float

trajectory.main.e_earth

Eccentricity of the Earth, currently set to zero to simplify calculations (i.e. spherical Earth model is being used)

Type: float

trajectory.main.ang_vel_earth

The angular velocity of the Earth

Type: float

class trajectory.main.LaunchSite (rail_length, rail_yaw, rail_pitch, alt, longi, lat, wind=[0, 0, 0])

Bases: object

Object holding the launch site information

Parameters:

- rail_length (float) Length of launch rail /m
- rail_yaw (float) Angle of rotation (using a right hand rule) about the launch site z-axis /degrees. Examples: rail_yaw = 0 points South, rail_yaw = 90 points East.
- rail_pitch (float) Angle between the rail and the launch site z-axis (i.e. angle to the vertical) /degrees. Example: rail_pitch = 0 points up.
- alt (float) Altitude /m
- longi (float) Londditude /degrees
- lat (float) Latitude /degrees
- wind (*list, optional*) Wind vector at launch site. Defaults to [0,0,0]. Will increase completness/complexity at some point to include at least altitude variation.

rail_length

Length of launch rail /m

Type: float

rail_yaw

Angle of rotation about the z axis (north pointing) /rad

Type: float

rail_pitch

Angle of rotation about "East" pointing y axis - in order to simplify calculations below this needs to be measured in the yaw then pitch order rad

Type: float

alt

Altitude /m

Type: float

longi

Londditude /degrees

Type: float

lat

Latitude /degrees

Type: float

wind

Wind vector at launch site. Defaults to [0,0,0]. Will increase completness/complexity at some point to include at least altitude variation.

Type: list, optional

class trajectory.main.Motor (motor_time_data, prop_mass_data, cham_pres_data, throat_data, gamma_data,
nozzle_efficiency_data, exit_pres_data, area_ratio_data)

Bases: object

Object holding the performance data for the engine

Parameters:

- motor_time_data (list) Time since ignition (with times corresponding to the other input lists) /s
- prop_mass_data (list) Propellant mass /kg
- cham_pres_data (list) Chamber Pressure /Pa
- throat_data (list) Throat diameter /m
- gamma_data (list) Nozzle inlet gamma (ratio of specific heats)
- nozzle_efficiency_data (list) Nozzle efficiency
- exit_pres_data (list) Exit pressure /Pa
- area_ratio_data (list) Area ratio

motor_time_data

Time since ignition (with times corresponding to the other input lists) /s

Type: list

prop_mass_data

Propellant mass /kg

Type: list

cham_pres_data

Chamber Pressure /Pa

Type: list

throat_data

Throat diameter /m

Type: list

gamma_data

Nozzle inlet gamma (ratio of specific heats)

Type: list

nozzle_efficiency_data

Nozzle efficiency

Type: list

exit_pres_data

Exit pressure /Pa

Type: list

area_ratio_data

Area ratio

Type: list

class trajectory.main.RasAeroData (file_location_string, area=0.0305128422)

Bases: object

Object holding aerodynamic data from a RasAero II 'Aero Plots' export file

Note

Relies on an axially symetric body

Parameters:

- file_location_string (string) Location of RASAero file
- area (float, optional) Reference area used to normalise coefficients, defaults to 0.0305128422 /m^2

area

Referance area used to normalise coefficients, /m^2

Type: float, optional

COP

Centre of pressure at time after ignition, when called interpolates to desired time /m

Type: Scipy Interpolation Function

CA

Axial coefficient of drag, when called interpolates to desired time /

Type: Scipy Interpolation Function

CN

Normal coefficient of drag, when called interpolates to desired time /

Type: Scipy Interpolation Function

class trajectory.main.Rocket (mass_model, motor, aero, launch_site, h=0.01, variable=False, rtol=1e-07,
atol=1e-14)

Bases: object

The rocket and key simulation components

Parameters:

- mass_model (Mass Model Object) Mass model object, must have mass, ixx, iyy, izz, cog class methods which return them at time
- motor (Motor Object) Motor object that stores performace parameters over time
- aero (Aero Object) Most have area, cop, cn and ca class methods which return that at time
- launch_site (Launch site object) Stores launch site parameters
- h (float, optional) Timestep for integration (only required when variable is off), defaults ot 0.01 /s
- variable (bool, optional) Adaptive timesteps?, defaults to False
- rtol (float) Relative error tollerance for integration /
- atol (float) Absolute error tollerance for integration /

mass_model

Mass model object, must have mass, ixx, iyy, izz, cog class methods which return them at time

Type: Mass Model Object

motor

Motor object that stores performace parameters over time

Type: Motor Object

aero

Most have area, cop, cn and ca class methods which return that at time

Type: Aero Object

launch_site

Stores launch site parameters

Type: Launch site object

h

Timestep for integration (only required when variable is off) /s

Type: float, optional

variable

Adaptive timesteps?, defaults to False

Type: bool, optional

rtol

Relative error tollerance for integration /

Type: float

atol

Absolute error tollerance for integration /

Type: float

b2i

Specifies the rotation from the body to inertial frame

Type: Scipy Rotation Object

i2b

Specifies the rotation from the inertial to body frame

Type: Scipy Rotation Object

pos_i

Position of the rocket in the inertial coordinate system [x,y,z] /m

Type: numpy array

vel_i

Velocity of the rocket in the inertial coordinate system [x,y,z] /m/s

Type: numpy array

w_b

Angular velocity of the body coordinate system in the inertial frame [x,y,z]/rad/s

Type: numpy array

alt

Altitude of the rocket (height abover surface in the launchsite frame) /m

Type: float

on_rail

Rocket still on rail? Initialises to True

Type: bool

burn_out

Engine burned out? Initialises to False

Type: bool

accelerations (pos i, vel i, b2i, w b, time)

Gathers the foces on the rocket and returns translational and rotational accelerations on the rocket

Parameters:

- pos_i (numpy array) Position of the rocket in the inertial coordinate system [x,y,z] /m
- vel_i (numpy array) Velocity of the rocket in the inertial coordinate system [x,y,z] /m/s
- **b2i** (*scipy rotation object*) Defines the orientation of the body frame to the inertial frame
- w_b (numpy array) Angular velocity of the body in the body frame [x,y,z] /rad/s
- time (float) Time since ignition /s

Returns: Translational accleration in inertial frame, and rotational acceleration using the body

coordinate system

Return type: numpy array

aero_forces (pos_i, vel_i, b2i, w_b, time)

Returns aerodynamic forces (in the body reference frame and the distance of the centre of pressure (COP) from the front of the vehicle.)

Note

-This currently ignores the damping moment generated by the rocket is rotating about its long axis -Unsure if the right angles for calculating CN as the angles of attack vary (same for CA as angles of attack vary) -Not sure if using the right density for converting between force coefficients and forces

Parameters:

- pos_i (numpy array) Position of the rocket in the inertial coordinate system [x,y,z] /m
- vel_i (numpy array) Velocity of the rocket in the inertial coordinate system [x,y,z] /m/s
- b2i (scipy rotation object) Defines the orientation of the body frame to the inertial frame
- w_b (numpy array) Angular velocity of the body in the body frame [x,y,z] /rad/s
- time (float) Time since ignition /s

Returns: numpy array – Aerodynamic forces on the rocket in the body frame [x,y,z] /N float – Distance from the front of the rocket that the forces act through /m

altitude (pos_i)

Returns the altitude (height from surface in launch frame)

Note

-Uses a spherical Earth model

Parameters: pos_i (numpy array) – Position of the rocket in the inertial coordinate system [x,y,z] /m

Returns: Altitude /m
Return type: float

check_phase (debug=False)

Checks phase of flight between steps

Notes

-Since this only checks between steps there may be a very short period where the rocket is still orientated as if its still on the rail when it is not -May look like the rocket leaves the rail at an altitude greater than the rail length for this reason

Parameters: verbose (bool, optional) – Outputs progress messages if True

Returns: List of events that happened in this step for log

Return type: list

fdot (time, fn)

Returns the rate of change of the Rocket's state array, f

Notes

-'fdot' here is the same as 'ydot' in the 2P1 (2nd Year) Engineering Lagrangian dynamics notes RK4 section

Parameters:

• time (float) - Time since ignition /s

fn (list) - [pos_i[0], pos_i[1], pos_i[2],vel_i[0], vel_i[1], vel_i[2], w_b[0], w_b[1], w_b[2], xb[0], xb[1], xb[2], yb[0], yb[1], yb[2], zb[0],zb[1],zb[2]]

Returns: [vel_i[0], vel_i[1], vel_i[2], acc_i[0], acc_i[1], acc_i[2], w_bdot[0], w_bdot[1], w_bdot[2],

xbdot[0], xbdot[1], xbdot[2], ybdot[0], ybdot[1], ybdot[2], zbdot[0], zbdot[1], zbdot[2]]

Return type: numpy array

gravity (pos_i, vel_i, b2i, w_b, time)

Returns the gravity force, as a vector in inertial coordinates.

Note

-Uses a spherical Earth gravity model

Parameters:

- pos_i (numpy array) Position of the rocket in the inertial coordinate system [x,y,z] /m
- vel_i (numpy array) Velocity of the rocket in the inertial coordinate system [x,y,z] /m/s
- **b2i** (scipy rotation object) Defines the orientation of the body frame to the inertial frame
- w_b (numpy array) Angular velocity of the body in the body frame [x,y,z] /rad/s

• time (float) - Time since ignition /s

Returns: Gravitational force on rocket in inertial frame [x,y,z] /N

Return type: numpy array

run (max_time=300, debug=False, to_json=False)

Runs the rocket simulation

Notes

-Uses the scipy DOP853 O(h^8) integrator

Parameters:

- max_time (int, optional) Maximum simulation runtime, defaults to 300 /s
- debug (bool, optional) Output more progress messages/warnings, defaults to False
- to_json (str, optional) Export a .JSON file containing the data to the directory given, "False" means nothing will be exported.

Returns: Record of simulation, contains interial position and velocity, angular velocity in body

coordinates, orientation and events (e.g. parachute). Most information can be derived from this in post processing. "time" arrayList of times that all the data corresponds to /s "pos_i" arrayList of inertial position vectors [x, y, z] /m "vel_i" arrayList of inertial velocity vectors [x, y, z] /m/s "b2imat" array:List of rotation matrices for going from the body to inertial coordinate system (i.e. a record of rocket orientation) "w_b" array:List of angular velocity vectors, in body coordinates [x, y, z] /rad/s "events" array:List of useful events

Return type: pandas array

thrust (pos_i, vel_i, b2i, w_b, time, vector=[1, 0, 0])

Returns thrust and moments generated by the motor, in body frame.

Note

-Mainly derived from Joe Hunt's NOVIS Simulation

Parameters:

- pos_i (numpy array) Position of the rocket in the inertial coordinate system [x,y,z] /m
- vel_i (numpy array) Velocity of the rocket in the inertial coordinate system [x,y,z] /m/s
- **b2i** (*scipy rotation object*) Defines the orientation of the body frame to the inertial frame
- w_b (numpy array) Angular velocity of the body in the body frame [x,y,z] /rad/s
- time (float) Time since ignition /s
- vector (numpy array, optional) Thrust direction in the body coordinate system models misalignment or thrust vector control. Defaults to [1,0,0]

Returns: Thrust forces on the rocket in the body frame [x,y,z] /N

Return type: numpy array

trajectory.main.from_json (directory)
Imports simulation data from a JSON file

Parameters: directory (string) – The directory of the simulation data .JSON file

Returns: Record of simulation, contains interial position and velocity, angular velocity in body

coordinates, orientation and events (e.g. parachute). Most information can be derived from this in post processing. "time"arrayList of times that all the data corresponds to /s "pos_i"arrayList of inertial position vectors [x, y, z] /m "vel_i"arrayList of inertial velocity vectors [x, y, z] /m/s "b2imat"array:List of rotation matrices for going from the body to inertial coordinate system (i.e. a record of rocket orientation) "w_b"array:List of angular velocity

vectors, in body coordinates [x, y, z] /rad/s "events" array: List of useful events

Return type: pandas array

trajectory.main.warning_on_one_line (message, category, filename, lineno, file=None, line=None)

Constants

Mass Models

Mass Models

Stores mass models

class trajectory.mass.CylindricalMassModel (mass, time, I, r)

Bases: object

Simple cylindrical model of the rockets mass and moments of inertia.

Note

Assumes the rocket is a solid cylinder, constant volume, which has a mass that reduces with time (i.e. the density of the cylinder reduce)

Parameters:

- mass (list) Masses of the rocket at time after ignition /kg
- time (list) Corresponding time for the mass /s
- I (float) Length of rocket (cylinder) /m
- r (float) Radius of rocket (cylinder) /m

mass

Masses of the rocket at time after ignition, when called interpolates to desired time /kg

Type: Scipy Interpolation Function

time

Corresponding time for the mass /s

Type: list

1

Length of rocket (cylinder) /m

Type: float

r

Radius of rocket (cylinder) /m

Type: float

cog (time)

Returns the centre of gravity at some time after igition

Parameters: time (float) - Time since ignition /s

Returns: Centre of gravity /m

Return type: float

ixx (time)

Returns the xx moment of inertia at some time after igition

Parameters: time (float) - Time since ignition /s

Returns: xx moment of inertia /kgm^2

Return type: float

iyy (time)

Returns the yy moment of inertia at some time after igition

Parameters: time (float) – Time since ignition /s

Returns: yy moment of inertia /kgm^2

Return type: float

izz (time)

Returns the zz moment of inertia at some time after igition

Parameters: time (float) - Time since ignition /s

Returns: zz moment of inertia /kgm^2

Return type: float

mass (time)

Returns the mass at some time after igition

Note

Do not include the self parameter in the Parameters section.

Parameters: time (float) - Time since ignition /s

Returns: Mass interpolated at time /lg

Return type: float

Plotting

6DOF Trajectory Simulator

Various useful plots of the outputted data

```
trajectory.plot.animate_orientation (simulation_output, frames=500)
```

frames: number of animation frames in total - less means that the animations runs faster

```
trajectory.plot.get_velocity_magnitude (df)
```

trajectory.plot.plot_aero_forces (simulation_output)

```
trajectory.plot.plot_altitude_time (simulation_output, rocket)
```

Plots the following, against time where applicable: ground track, altitude, speed (in the launch frame) and vertical velocity (in the launch frame)

Parameters:

- **simulation_output** (*pandas array*) Simulation output from a Rocket.run() method. Should contain the following data:
- rocket (trajectory.Rocket object) The rocket object that was used to produce the simulation data. Is needed to calculate coordinate system changes.

```
trajectory.plot.plot_inertial_trajectory_3d (simulation_output, show_orientation=False)
Plots the trajectory in 3D, given the simulation_output
```

trajectory.plot.plot_launch_trajectory_3d (simulation_output, rocket, show_orientation=False, arrow_frequency=0.02)

Plots the trajectory in 3D, given the simulation_output and the rocket

Parameters:

- **simulation_output** (*pandas array*) Simulation output from a Rocket.run() method. Should contain the following data:
- rocket (trajectory.Rocket object) The rocket object that was used to produce the simulation data. Is needed to calculate coordinate system changes.

```
trajectory.plot.plot_position (simulation_output)
```

```
trajectory.plot.plot_quat_i2b (simulation_output)
```

trajectory.plot.plot_quat_i2bdot (simulation_output)

trajectory.plot.plot_velocity (simulation_output)

trajectory.plot.plot_w_b (simulation_output)

trajectory.plot.plot_wdot_b (simulation_output)

trajectory.plot.plot_ypr (simulation_output)

```
trajectory.plot.set_axes_equal (ax)
```

Make axes of 3D plot have equal scale so that spheres appear as spheres, cubes as cubes, etc.. This is one possible solution to Matplotlib's ax.set_aspect('equal') and ax.axis('equal') not working for 3D.

Source: https://stackoverflow.com/questions/13685386/matplotlib-equal-unit-length-with-equal-aspect-ratio-z-axis-is-not-equal-to

Input

ax: a matplotlib axis, e.g., as output from plt.gca().

Transforms

trajectory.transforms.direction_i21 (vector, launch_site, time)
Converts position in launch frame to position in inertial frame.

Note

-Problem in the yaw pitch conversions, unexplained negative sign needed

Parameters:

- vector (numpy array) Vector in the inertial frame [x,y,z] /m/s
- launch_site (LaunchSite object) Holds the launch site parameters
- time (float) Time since ignition /s

Returns: Vector in the launch frame

Return type: numpy array

trajectory.transforms.direction_12i (vector, launch_site, time)
Converts position in launch frame to position in inertial frame.

Note

-Problem in the yaw pitch conversions, unexplained negative sign needed

Parameters:

- vector (numpy array) Vector in the launch frame [x,y,z] /m/s
- launch_site (LaunchSite object) Holds the launch site parameters
- time (float) Time since ignition /s

Returns: Vector in the launch frame

Return type: numpy array

trajectory.transforms.pos_i21 (position, launch_site, time)
Converts position in launch frame to position in inertial frame.

spherical coordinates to

Calculus/Book%3A_Calculus_(OpenStax)/12%3A_Vectors_in_Space/12.7%3A_Cylindrical_and_Spherical_Coordinates#:~:text=To%20

Parameters:

- position (numpy array) Position in the inertial frame [x,y,z] /m
- launch_site (LaunchSite object) Holds the launch site parameters
- time (float) Time since ignition /s

Returns: Position in the launch frame

Return type: numpy array

trajectory.transforms.pos_12i (pos_I, launch_site, time)
Converts position in launch frame to position in inertial frame.

spherical coordinates to

Calculus/Book%3A_Calculus_(OpenStax)/12%3A_Vectors_in_Space/12.7%3A_Cylindrical_and_Spherical_Coordinates#:~:text=To%20

Parameters:

• pos_I (numpy array) – Position in the launch site frame [x,y,z] /m

• launch_site (LaunchSite object) - Holds the launch site parameters

• time (float) - Time since ignition /s

Returns: Position in the inertial frame

Return type: numpy array

trajectory.transforms.vel_i2l (vel_i, launch_site, time)
Converts position in launch frame to position in inertial frame.

Note

 $-v = w \times r$ for a rigid body, where v, w and r are vectors

Parameters:

• vel_i (numpy array) - Velocity in the inertial frame [x,y,z] /m/s

• launch_site (LaunchSite object) - Holds the launch site parameters

• time (float) - Time since ignition /s

Returns: Velocity in the launch frame

Return type: numpy array

trajectory.transforms.vel_l2i (vel_I, launch_site, time)
Converts position in launch frame to position in inertial frame.

Note

 $-v = w \times r$ for a rigid body, where v, w and r are vectors

Parameters:

vel_i (numpy array) – Velocity in the launch frame [x,y,z] /m/s

• launch_site (LaunchSite object) - Holds the launch site parameters

• time (float) - Time since ignition /s

Returns: Velocity in the inertial frame

Return type: numpy array

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