# Literature Review: Machine Learning Applied to Dynamic Physial System

## I. ABSTRACT

This survery is on recent advancements in the intersection of physical modelling and machine learning.

## II. INTRODUCTION

Understanding of physical process from data when there is no first prinicple solution is very hard. The abundance of data in both natural and physical sciences has enabled the use of machine learning models to understand governing dynamics of many complex processes. There are different ways in which physical modeling and machine learning methods have been used together. There are works in the problem of understanding pysical process from data, classifying or predicting complex physical process, using physics to generate simulation data, using machine learning to control non-linear dynamical systems, using machine learning to do fault detection in dynamical systems, etc.

This survey is on all the different areas where there has been an amalgation of machine learning and physics. The application on which we focus is on time series modeling, non-linear control, motor control, and fault detection.

## III. BACKGROUND

The background section is divided in to the following subsections; first is modeling of physical systems, second is on non-linear control, third is on motor control, and fourth is on fault detection.

# A. Modeling of physical systems

HMM or Kalman filter are able to learn linear dynamic models, for non-linear dynamics accommodating nonlinearity into HMM is very hard. In [?] a new method called sufficient posterior representation is presented which can be used to model nonlinear dynamic behaviors using many nonlinear supervised learning algorithms such as neural networks, boosting and SVM in a simple and unified fashion.

PDEs can describe complex phoenomena. We don't always have PDEs for a given problem, but we may have a large amount of data available. In [?] a data driven method is proposed to learn governing PDEs of a given system from time series data. Sparse regression is used to learn the coefficients and an iterative method is used to get most suitable coefficients. Experiments on Navier-Stokes equation is shown.

In [?] modeling of time invariant nonlinear systems is addressed. A multi-layered network architecture with a control input signal called Hidden Control Neural Network (HCNN) is presented which can model signals generated by nonlinear dynamical systems with restricted time variability.

Reinforcement learning has also been used for physial modelling. In [?] a Temporal Difference learning algorithm for continuous-time, continuous-state, nonlinear control problems is presented. Kernel regression method is used to learn a nonlinear auto-regressive model.

[?] uses machine learning to optimize physical dynamic systems.

Most of the methods of data driven learning of dynamic systems deal with sequential data. In [?] method is presented to learn dynamics from non-sequential data.

Computing hidden system paramters from measurable quantities of complex physical systems using invertible neural network(INN) is presented in [?].

In [?] a deep learning appraoch for discovering nonlinear partial differential equations from scattered and potentially noisy observations is presented. Two deep neural networks are used to approximate solution and nonlinear dynamics.

In [?] a data driven approach of approximating nonlinear dynamics to a linear one using deep neural networks has been present. Koopman operators are learned from data for coordinate transformation of nonlinear system to linear one.

In [?], [?] a physics-guided neural networ(PGNN) is presented which leverages the output of physics-based model simulations along with observational features to generate predictions using a neural network. The model predictions not only show lower errors on the training data but are also consistent with the system dynamics.

There are systems where dynamics change with time and some dynamics may not have been seen before. It will be usefull to identify new dynamics. [?] uses neural networks to identify new phayics.

- [?] have trained three deep neural network structures on sequential data and have shown detailed analysis on how DNNs are able to model the underlying dynamical systems.
- [?] has shown how physics can be used to do better data driven discoveries. Theory guided design, learning, refinement of machine learning model has been presented.

In [?] a multi-layered neural networks called Hidden Control Neural Network(HCNN) is presented to model nonlinear dynamical systems with restricted time variability. The mapping of NN changes with time as a function of an aditional control input signal.

Using recurrent network to create mixture of expertes for modelling and controlling dynamical systems is presented in [?].

- IN [?] a dynamical system is first modeled using recurrent neural network(RNN). Then the dynamic response of the system is controlled using another RNN. Disturbance cancelling is performed using an adtitional RNN.
- In [?] a recurrent neural network architecture called Simoid Diagonal Recurrent Neural Network(SDRNN) is used for adaptive control of nonlinear dynamical systems.
- In [?] a feedforward neural network is used to control an unkown stochastic nonlinear dynamical system.
- In [?] recurrent neural network is used to control nonlinear plants. Approach is used in controlin landing of a commercial aircraft in difficult wind conditions.

In []

C. Motor Control

D. Fault Detection

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