

SEC 4.2 DIVIDING POLYNOMIAL

1. LONG DIVISION:

$$\begin{array}{r}
 \text{FOCUS} \\
 \text{DIVISOR } 3x+1 \overline{) 6x^3 + 2x^2 + 22x + 0} \\
 \underline{-6x^3} \\
 15x \\
 \underline{-15x} \\
 0 \\
 \underline{-0} \\
 0
 \end{array}$$

QUOTIENT: $2x^2 + 7x + 5$

REMAINDER: $7x - 5$

Handwritten notes: $3x(2x^2+5)$, $1(2x^2+5)$

$$\begin{array}{ccccccc}
 P(x) & = & D(x) & \cdot & Q(x) & + & R(x) \\
 \uparrow & & \uparrow & & \uparrow & & \uparrow \\
 \text{DIVIDEND} & & \text{DIVISOR} & & \text{QUOTIENT} & & \text{REMAINDER}
 \end{array}$$

$$P(x) = (2x^2+5)(3x+1) + (7x-5)$$

EX. $(x+2) \overline{) 3x^3 - 6x^2 + 4x - 1}$

$$\begin{array}{r}
 3x^2 - 12x + 28 \\
 (x+2) \overline{) 3x^3 - 6x^2 + 4x - 1} \\
 \underline{-3x^3 + 6x^2} \\
 -12x^2 + 4x - 1 \\
 \underline{+12x^2 + 24x} \\
 28x - 1 \\
 \underline{-28x + 56} \\
 -57
 \end{array}$$

Handwritten notes: $3x^2(x+2)$, $-12x(x+2)$, $28(x+2)$

$$P(x) = (x+2)(3x^2 - 12x + 28) + (-57)$$

2. SYNTHETIC DIVISION : (FAST WAY TO DO LONG DIVISION)

BUT DIVISOR MUST BE OF THE FORM $x - c$.

$$\underline{3x^3 - 6x^2 + 4x - 1}$$

$$\begin{array}{l} x+2 \\ (x - (-2)) \\ x - c \end{array}$$

-2		3	-6	4	-1
		↓	-6	24	-56
		3	-12	28	-57

$$P(x) = \underset{\substack{\uparrow \\ D(x)}}{(x+2)} (3x^2 - 12x + 28) + \underset{R(x)}{-57}$$

$Q(x)$

3. REMAINDER THEOREM :

IF THE POLYNOMIAL $P(x)$ IS DIVIDED BY $(x-c)$, THEN THE REMAINDER IS THE VALUE $P(c)$

$$P(x) = 3x^5 + 5x^4 - 4x^3 + 7x + 3$$

$$P(-2) = 3(-2)^5 + 5(-2)^4 - 4(-2)^3 + 7(-2) + 3$$

$$3 \cdot (-32) + 5 \cdot 16 - 4(-8) + 7(-2) + 3$$

$$-96 + 80 + 32 - 14 + 3$$

$$-16 + 32 - 14 + 3$$

$$16 - 14 + 3$$

$$2 + 3$$

$-2 \mid$	3	5	-4	0	7	<div style="border: 1px solid black; padding: 2px; display: inline-block;">5</div>
	\downarrow	-6	2	4	-8	2
	3	-1	-2	4	-1	<div style="border: 1px solid black; padding: 2px; display: inline-block;">5</div>

$(-2, 5)$ POINT ON THE GRAPH

4. FACTOR THEOREM : c IS A ZERO $P(c)=0$
 AND $x-c$ IS A FACTOR OF
 THE POLYNOMIAL



REMAINDER

EX. $P(x) = x^3 - 7x + 6$

DIRECT SUBSTITUTION

$$\begin{aligned} 1^3 - 7 \cdot 1 + 6 \\ 1 - 7 + 6 \\ -6 + 6 \\ 0 \end{aligned}$$

$P(1)$
 BY SYNTHETIC DIVISION

$$\begin{array}{r|rrrr} 1 & 1 & 0 & -7 & 6 \\ & \downarrow & 1 & 1 & -6 \\ \hline & 1 & 1 & -6 & 0 \end{array}$$

$x^2 + 1x - 6$ 0 ← REMAINDER

$\{1\}$ ZERO

$(x-1)$ FACTOR

$(1,0)$ x-int.

$x^2 + x - 6$

$(x+3)(x-2)(x-1)$

ZEROS: $\{-3, 2, 1\}$

