

SEC 2.4 LINES

1. SLOPE: $\frac{\text{RISE}}{\text{RUN}} = \frac{\text{VERTICAL CHANGE}}{\text{HORIZONTAL CHANGE}} =$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

EXAMPLE: $P(2, 1)$ $Q(8, 5)$

$$m = \frac{5 - 1}{8 - 2} = \frac{4}{6} = \frac{2}{3}$$

2. POINT-SLOPE FORM

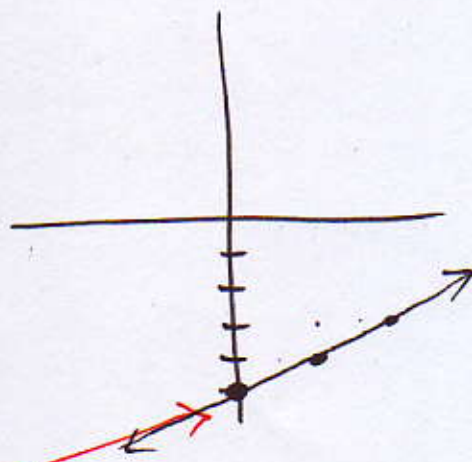
$$y - y_1 = m(x - x_1)$$

EX. $m = \frac{1}{2}$ $P(4, -3)$

$$y + (+3) = \frac{1}{2}(\overbrace{x - 4})$$

$$y + \cancel{3}^{-3} = \frac{1}{2}x - \cancel{2}^{-3}$$

$$\boxed{y = \frac{1}{2}x - 5}$$



3. SLOPE - INTERCEPT FORM

$$y = mx + b$$

SLOPE

y-INTERCEPT

$$m = \frac{1}{3}$$

SLOPE

$$b = \frac{2}{5}$$

y-INT.

$$y = \frac{1}{3}x + \frac{2}{5}$$

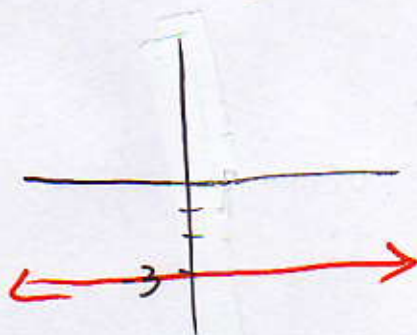
4. VERTICAL LINE $x = a$

$$x = 2$$



5. HORIZONTAL LINE $y = b$

$$y = -3$$



6. GENERAL FORM

$$Ax + By + C = 0$$

7. PARALLEL LINES

TWO NON-VERTICAL LINES ARE PARALLEL IF AND ONLY IF THEY HAVE THE SAME SLOPE.

EX

$$y = \frac{3}{5}x + 1$$

$$y = \frac{3}{5}x - 2$$

← SAME SLOPE

8. PERPENDICULAR LINES

TWO LINES ARE PERPENDICULAR IF AND ONLY IF $m_1 \cdot m_2 = -1$

EX. $7 \cdot -\frac{1}{7} = -1$

$-\frac{2}{3} \cdot \frac{3}{2} = -1$

OPPOSITE RECIPROALS

9. RATE OF CHANGE AS A SLOPE.

$$\frac{120 \text{ miles}}{5 \text{ gallons}}$$

=

$$\frac{24 \text{ mile}}{1 \text{ gallon}}$$

↑
DENOMINATOR SIMPLIFIES TO A 1.