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$$(\ln 2)^x \xrightarrow{x \cdot \ln 2} x \cdot \ln 2$$

$$\frac{d}{dx} 2^x = \underbrace{(e^{\ln 2})^x}_2 = e^{x \cdot \ln 2}$$

$$\frac{d}{dx} e^{(x \cdot \ln 2)} = e^{x \cdot \ln 2} \cdot \ln 2 = 2^x \cdot \ln 2$$

$$\frac{d}{dx} e^{x^2} = e^{x^2} \cdot 2x$$

$$\begin{aligned} \frac{d}{dx} a^x &: \lim_{h \rightarrow 0} \left(\frac{a^{x+h} - a^x}{h} \right) = \frac{a^x a^h - a^x}{h} = \frac{a^x (a^h - 1)}{h} \\ &= a^x \left(\lim_{h \rightarrow 0} \frac{a^h - 1}{h} \right) \end{aligned}$$

$\ln 2$

$$\frac{d}{dx} a^x \text{ at } x=0$$

$$z^x = e^{x(\ln z)}$$

$$a^x = e^{x \cdot \ln a}$$

$$(e^{\ln a})^x \nearrow$$

$$P(t) = P_0 e^{kt}$$

$$P'(t) = P_0 e^{kt} \cdot k = k P(t)$$

instantaneous
rate
of change

$\therefore k \cdot \text{current value}$

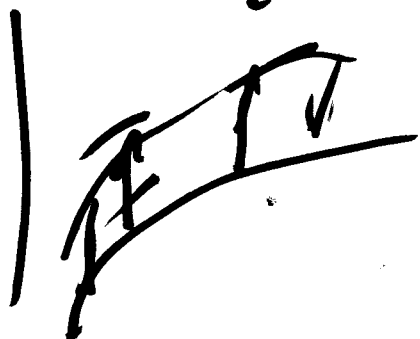
$$f(x) = \ln(x) \quad f'(x) = x^{-1} = \left(\frac{1}{x}\right)'$$

$$f(x) = \ln(x^2) \quad f'(x) = \frac{1}{x^2} \cdot 2x = 2 \cdot \frac{1}{x}$$

$$\underline{2 \ln(x)} \Rightarrow f'(x) = 2 \cdot \frac{1}{x} = \frac{2}{x}$$

$$f(x) = \ln(5x) \quad f'(x) = \frac{1}{5x} \cdot 5 = \frac{1}{x}$$

$$\underline{\underline{\ln(x) + \ln(5)}} \quad f'(x) = \frac{1}{x} + 0$$



$$f(x) = x^x$$

$$f(2) = 4 = 2^2$$

$$f(3) = 27 = 3^3$$

$$f(4) = 256$$

$$f'(x) =$$

$$f(x) = (e^{\ln x})^x = e^{x \cdot \ln x}$$

$$f'(x) = e^{x \ln x} \cdot \left[1 \cdot \ln x + x \cdot \frac{1}{x} \right]$$

$$= x^x [\ln x + 1]$$

$$\underline{g(x)} = \underline{\ln(f(x))}$$

$$\underline{g'(x)} = \frac{1}{f(x)} \cdot f'(x) = \underline{\frac{f'(x)}{f(x)}}$$

$$\underline{f'(x)} = \underline{f(x)} \cdot g'(x)$$

$$= f(x) \cdot \frac{d}{dx} \ln(f(x))$$

$$f(x) = x^x$$

$$f'(x) = x^x \cdot \frac{d}{dx} [\underline{x \ln x}]$$

$$f(x) = \frac{(x^2+3x)^5 (\sqrt{x+3})^6}{\left(x+\frac{1}{x}\right)^2 (x-3)^{\frac{1}{2}}}$$

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$$\underline{f'(x)} = \underline{f(x)} \cdot (\ln f(x))'$$

$$f'(x) = \frac{(x^2+3x)^5 (\sqrt{x+3})^6}{\left(x+\frac{1}{x}\right)^2 (x-3)^{\frac{1}{2}}} \left[\frac{5 \cdot 2x}{x^2+3x} + \frac{3}{x+3} - 2 \left(\frac{1-\frac{1}{x^2}}{x+\frac{1}{x}} \right) - \frac{1}{2} \frac{1}{x-3} \right]$$

$$\ln f(x) = 5 \ln(x^2+3x) + 3 \ln(x+3) - 2 \ln\left(x+\frac{1}{x}\right) - \frac{1}{2} \ln(x-3)$$