Brian Petersen

This set of WeBWorK problems covers limits and continuity, material in sections 1.5 and 1.6 of Brief Calculus. WeBWorK assignment Set1 is due on 09/18/2012 at 10:00pm EDT.

1. (1 pt) Evaluate the limit

$$\lim_{a \to 1} \frac{a^3 - a}{a^2 - 1}$$

Answer(s) submitted:

• 1

(correct)

Correct Answers:

- 1
- 2. (1 pt) Evaluate the limit

$$\lim_{b \to 1} \frac{b^3 - 1}{b^2 - 1}$$

Answer(s) submitted:

• 3/2

(correct)

Correct Answers:

- 1.5
- 3. (1 pt) Evaluate the limit

$$\lim_{a \to 9} \frac{9 - a}{3 - \sqrt{a}}$$

Answer(s) submitted:

• 6

(correct)

Correct Answers:

- (
- **4.** (1 pt) Evaluate the limit

$$\lim_{x \to 7} \frac{\frac{1}{x} - \frac{1}{7}}{x - 7}$$

Answer(s) submitted:

-(1/49)

(correct)

Correct Answers:

-0.0204081632653061

5. (1 pt) Evaluate the limit

$$\lim_{b\rightarrow -18^-}\frac{|b+18|}{b+18}$$

Answer(s) submitted:

-1

(correct)

Correct Answers:

−1

6. (1 pt) Let
$$f(x) = x + 3$$
 if $x \le 2$ and $f(x) = 3$ if $x > 2$.

Sketch the graph of this function for yourself and find following limits if they exist (if not, enter N).

$$-1$$
. $\lim_{x \to 0} f(x)$

$$-2. \lim_{x \to 2^+} f(x)$$

$$3. \lim_{x \to 2}^{3} f(x)$$

Answer(s) submitted:

- 5
- 3
- N

(correct)

Correct Answers:

- 5
- 3
- N

7. (1 pt) Let
$$f(x) = 2$$
 if $x > 7$,

$$f(x) = 6 \text{ if } x = 7,$$

$$f(x) = -x + 8 \text{ if } -1 \le x < 7,$$

$$f(x) = 9 \text{ if } x < -1.$$

Sketch the graph of this function and find following limits if they exist (if not, enter DNE).

$$\underline{}$$
1. $\lim_{x \to \infty} f(x)$

$$2. \lim_{x \to 7^{+}} f(x)$$

$$\underline{}$$
3. $\lim_{x \to \infty} f(x)$

$$\underline{}$$
4. $\lim_{x \to \infty} f(x)$

$$-5. \lim_{x \to 1^{+}} f(x)$$

$$--6. \lim_{x \to -1}^{x} f(x)$$

Answer(s) submitted:

- 1
- 2
- DNE

- 9
- 9
- 9

(correct)

Correct Answers:

- 1
- 2
- DNE
- 9
- 9
- 9

8. (1 pt) Evaluate the limit

$$\lim_{h \to 0} \frac{1(6+h)^2 + 4(6+h) - (1 \cdot 6^2 + 4 \cdot 6)}{h}$$

Answer(s) submitted:

• 16

(correct)

Correct Answers:

- 16
- **9.** (1 pt) For what value of the constant c is the function f continuous on $(-\infty,\infty)$ where

$$f(x) = \begin{cases} x^2 - c & \text{if } x \in (-\infty, 2) \\ cx + 8 & \text{if } x \in [2, \infty) \end{cases}$$

Answer(s) submitted:

−4/3

(correct)

Correct Answers:

- **10.** (1 pt) The function f is given by the formula

$$f(x) = \frac{3x^3 + 15x^2 - 14x + 24}{x + 6}$$

when x < -6 and by the formula

$$f(x) = 6x^2 - 5x + a$$

when $-6 \le x$.

What value must be chosen for a in order to make this function continuous at -6?

a = _____

Answer(s) submitted:

-3 (-6) ^2+2 (-6) +4

(correct)

Correct Answers:

• -116

11. (1 pt)

Evaluate the following limits. If needed, enter INF for $+\infty$ and MINF for $-\infty$.

(a)

$$\lim_{x \to +\infty} \frac{5x+10}{8x^2-7x+8}$$

(b)

$$\lim_{x \to -\infty} \frac{5x + 10}{8x^2 - 7x + 8}$$

Answer(s) submitted:

- 0
- 0

(correct)

Correct Answers:

- 0
- 0

12. (1 pt)

Evaluate the following limits. If needed, enter INF for $+\infty$ and MINF for $-\infty$.

(a)

$$\lim_{x \to +\infty} \frac{\sqrt{3+4x^2}}{8+3x} =$$

(b)

$$\lim_{x \to -\infty} \frac{\sqrt{3+4x^2}}{8+3x} =$$

Answer(s) submitted:

- 2/3
- -2/3

(correct)

Correct Answers:

- 0.666666666666667
- -0.666666666666667

13. (1 pt)

Evaluate the following limits. If needed, enter INF for $+\infty$ and MINF for $-\infty$.

(a)

$$\lim_{x \to +\infty} \left(\sqrt{x^2 + 9x + 1} - x \right) =$$

(b)

$$\lim_{x \to -\infty} \left(\sqrt{x^2 + 9x + 1} - x \right) =$$

Answer(s) submitted:

- 9/2
- INF

(correct)

Correct Answers:

- 4.5
- INF

14. (1 pt)

Evaluate the following limits. If needed, enter INF for ∞ and MINF for $-\infty$.

$$\lim_{x \to \frac{11}{2}^+} \frac{31x}{11 - 2x} =$$

$$\lim_{x \to \frac{11}{2}^{-}} \frac{31x}{11 - 2x} =$$

Generated by ©WeBWorK, http://webwork.maa.org, Mathematical Association of America

Answer(s) submitted:

- MINF
- INF

(correct)

Correct Answers:

- MINF
- INF