## Homework 6

## 1 Minimum Spinning Tree

Finish question 1 on https://www.educoder.net/classrooms/9025/shixun\_homework/.

## 2 Coin changing

Consider the problem of making change for n cents using the fewest number of coins. Assume that each coin's value is an integer. We recommend to read the chapter 6 of book "Introduction to Algorithms" (3rd Edition).

- a. Describe a greedy algorithm to make change consisting of quarters, dimes, nickels and pennies. Please give the pseudocode, and prove that your algorithm yields an optimal solution.
- **b.** Suppose that the available coins are in the denominations that are powers of c, i.e., the denominations are  $c^0; c^1; \dots; c^k$  for some integers c > 1 and  $k \ge 1$ . Show that the greedy algorithm always yields an optimal solution.
- c. Give a set of coin denominations for which the greedy algorithm does not yield an optimal solution. Your set should include a penny so that there is a solution for every value of n.

## 3 Due

- 1. Due is Nov. 1st, 23:59.
- 2. Question 2 is a writing assignment, submit a PDF on the canvas.