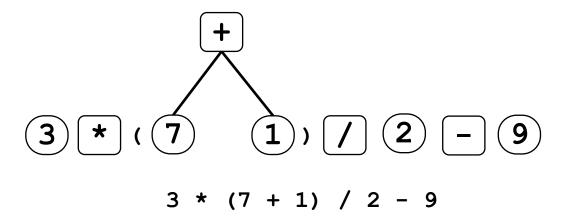
高级数据结构上机课

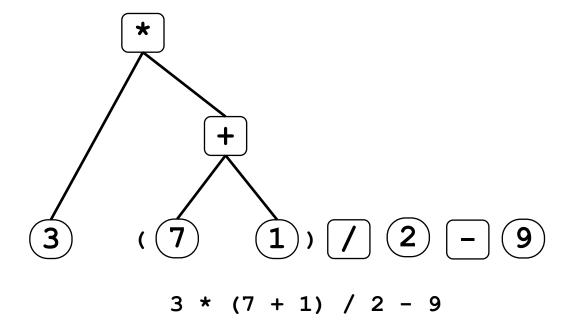
- 双周周二 16:00~18:00, 软件学院 3-101
- 负责: 董明凯 (dmkaplony@sjtu.edu.cn)
- 内容:
 - Mini Basic (30%)
 - LSM K/V Store (40%)
 - Graph (15%)
 - Balanced Search Tree (15%)
- 助教: 江学强、张孝东

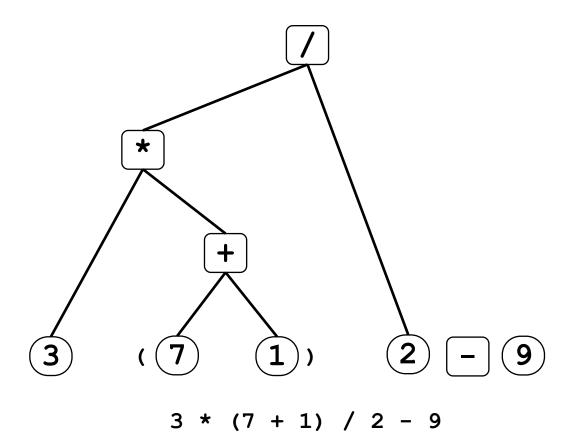
时间安排

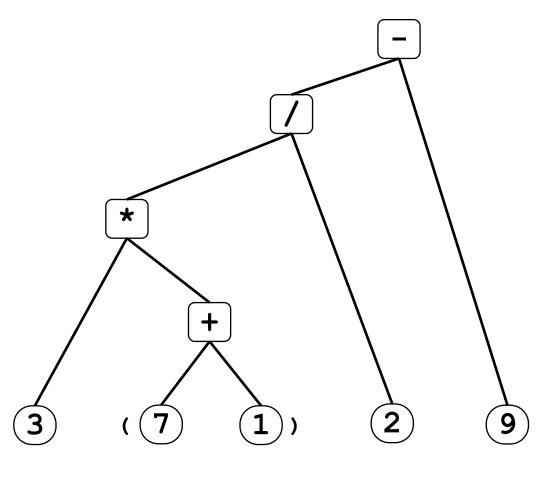
| Week 1 | |
|---------|---|
| Week 2 | Project 1: MiniBasic |
| Week 3 | |
| Week 4 | Q/A |
| Week 5 | |
| Week 6 | Q/A + Graph |
| Week 7 | |
| Week 8 | DDL: Project 1 (答辩) Project 2: LSM Tree |
| Week 9 | |
| Week 10 | Q/A + Tree |
| Week 11 | |
| Week 12 | Q/A |
| Week 13 | |
| Week 14 | Q/A |
| Week 15 | |
| Week 16 | DDL: Project 2 LSM 答辩 |

Expression Trees & Parsing & Evaluation

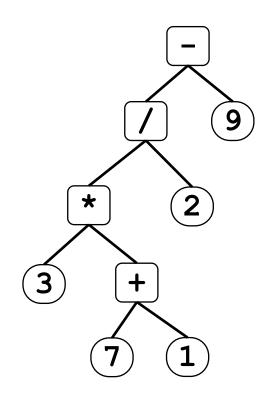


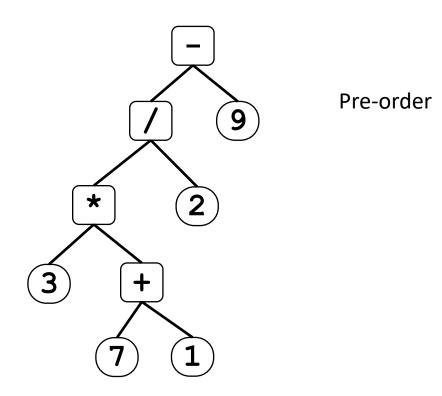


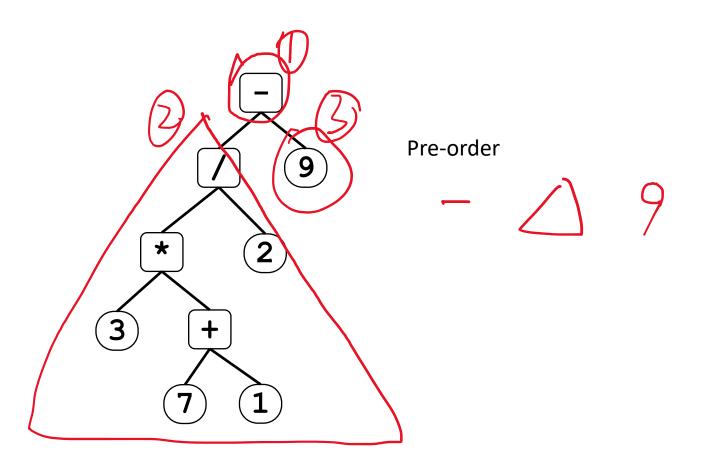


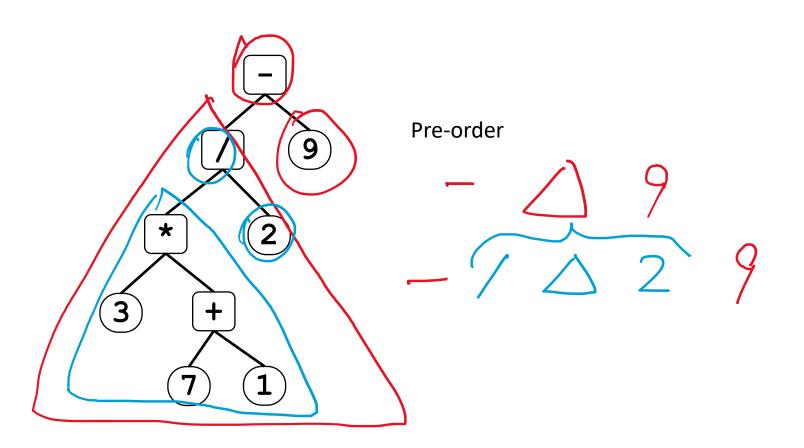


3 * (7 + 1) / 2 - 9

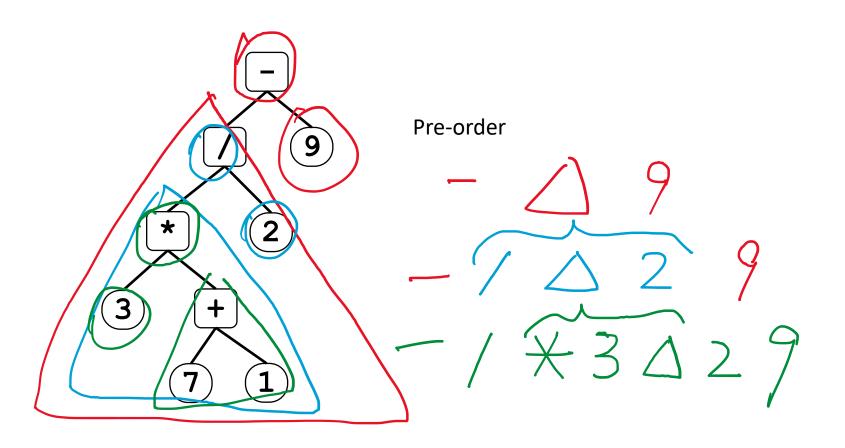


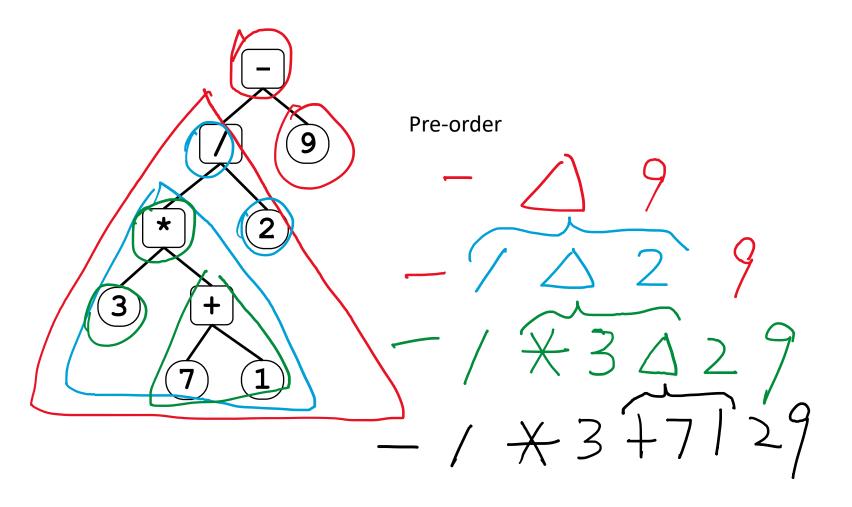




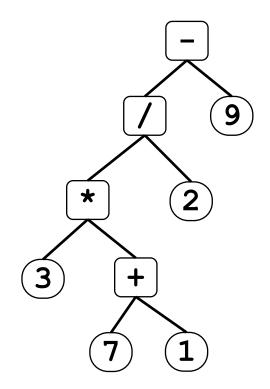


$$3 * (7 + 1) / 2 - 9$$





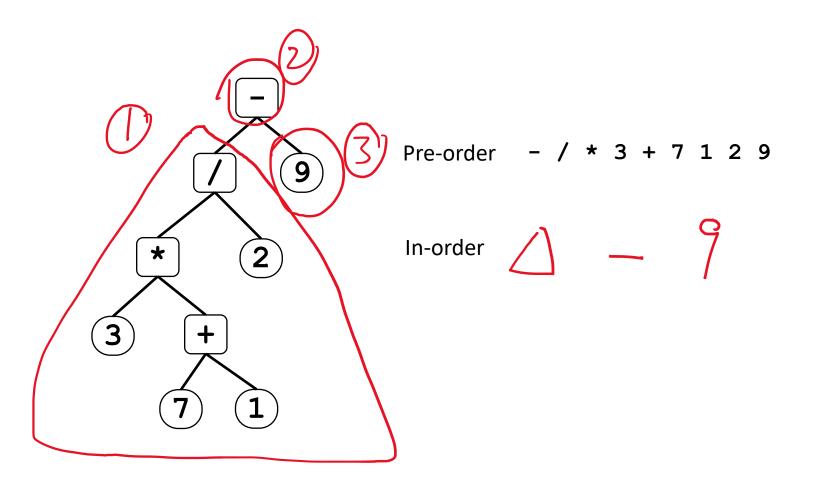
$$3 * (7 + 1) / 2 - 9$$



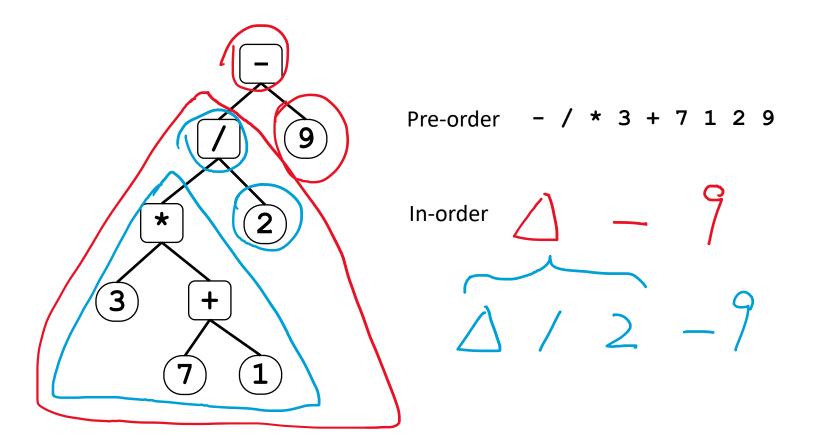
Pre-order - / * 3 + 7 1 2 9

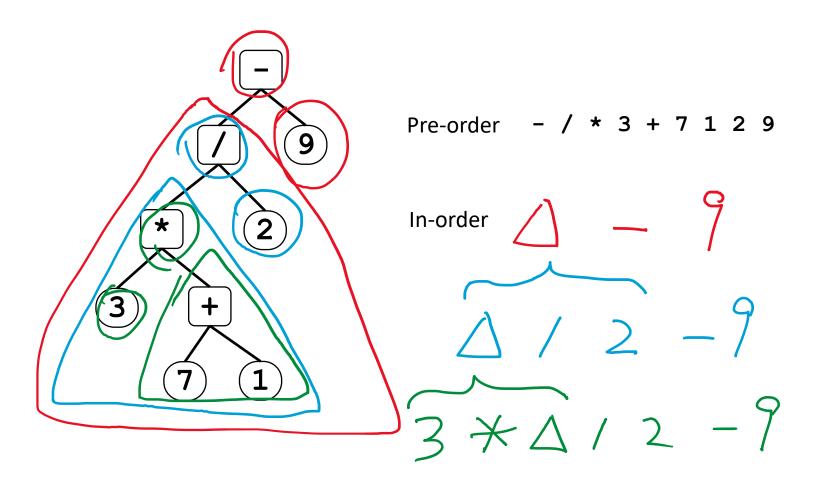
$$-/ \times 3 + 7/29$$

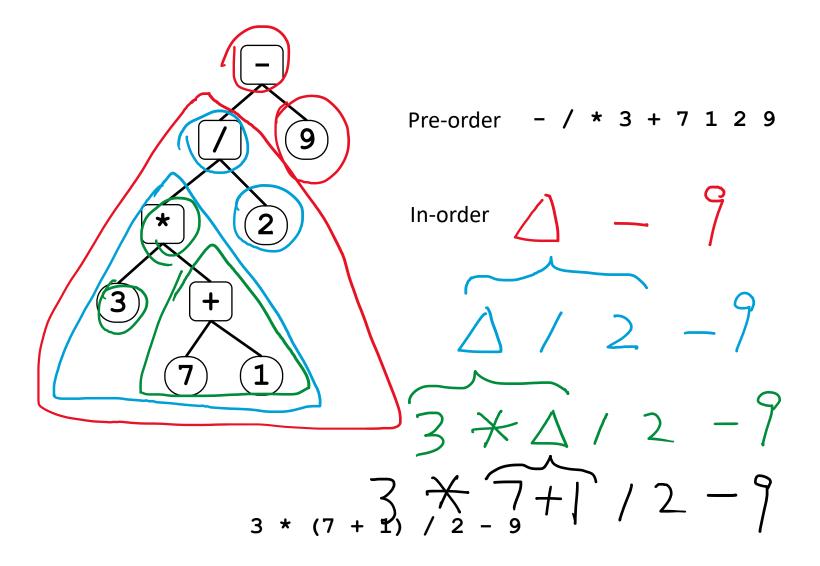
$$3 * (7 + 1) / 2 - 9$$

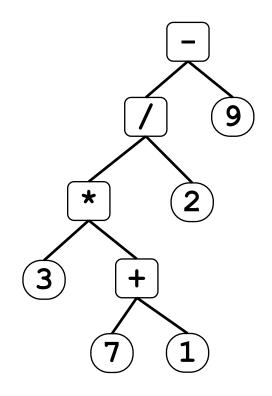


$$3 * (7 + 1) / 2 - 9$$



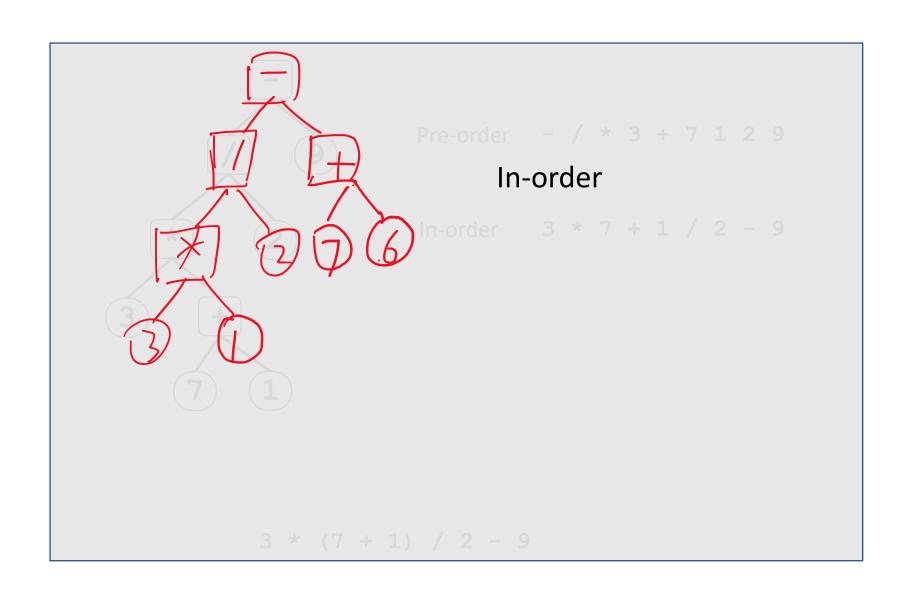


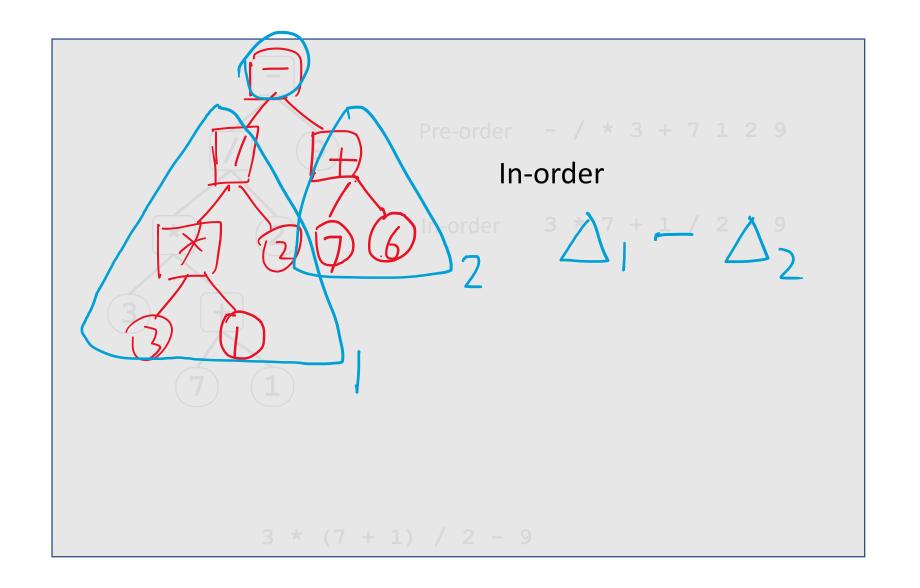


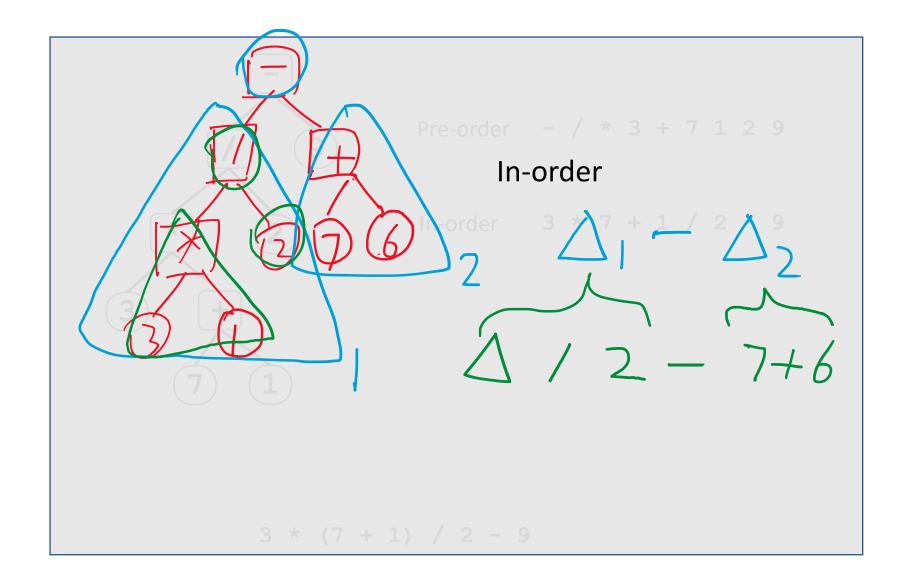


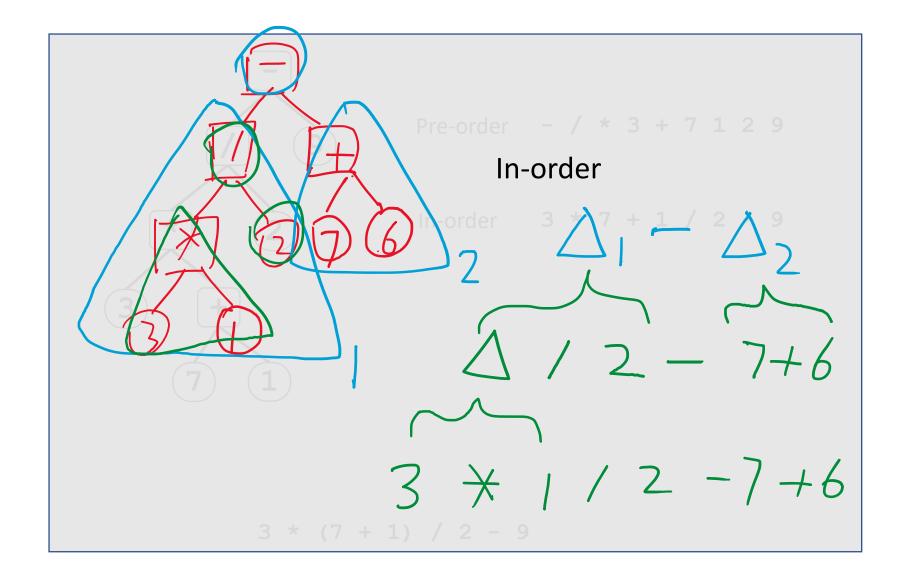
In-order
$$3 * 7 + 1 / 2 - 9$$

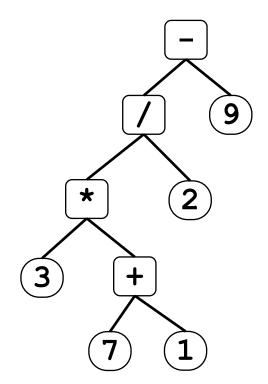
$$\frac{3 \times 7 + 1}{3 \times (7 + 1) / 2 - 9} + \frac{1}{2} - \frac{9}{2}$$

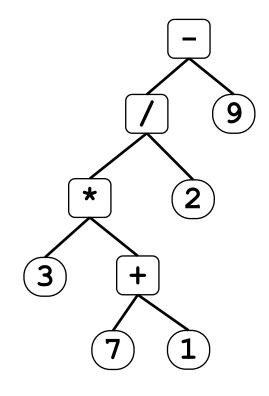












Pre-order

Prefix form - / * 3 + 7 1 2 9
Polish Notation

In-order 3 * 7

3 * 7 + 1 / 2 - 9

Infix form

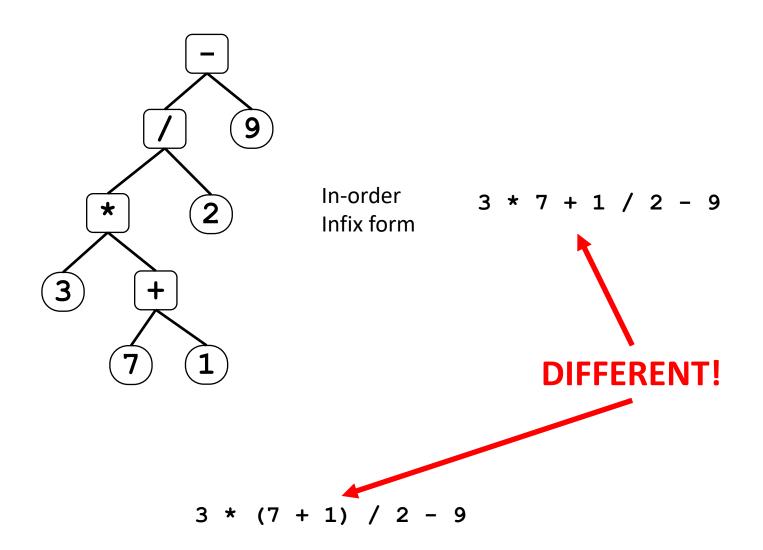
Post-order

Postfix form

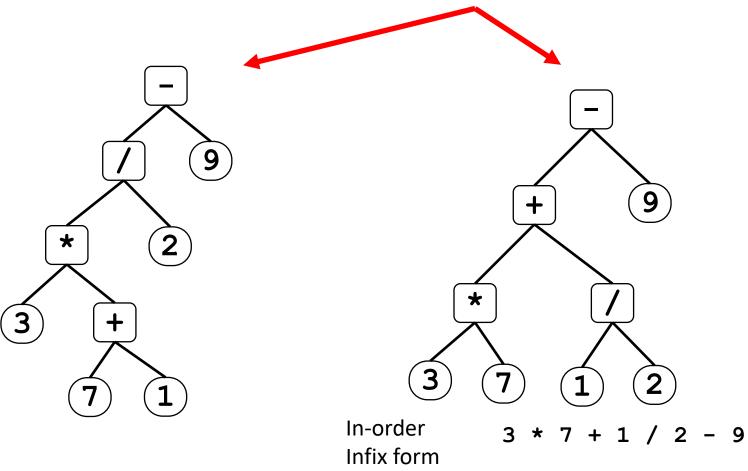
3 7 1 + * 2 / 9 -

Reverse Polish Notation

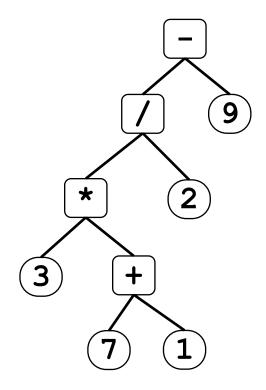
$$3 * (7 + 1) / 2 - 9$$



Same infix form, DIFFERENT shapes!



$$3 * (7 + 1) / 2 - 9$$



Pre-order

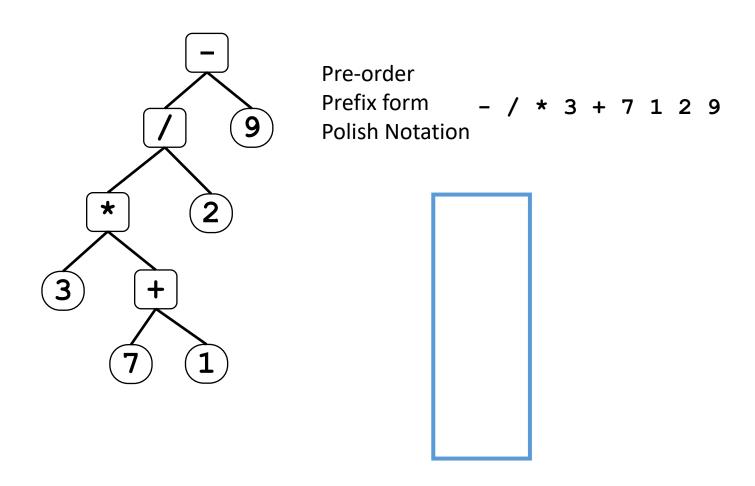
Prefix form - / * 3 + 7 1 2 9

Polish Notation

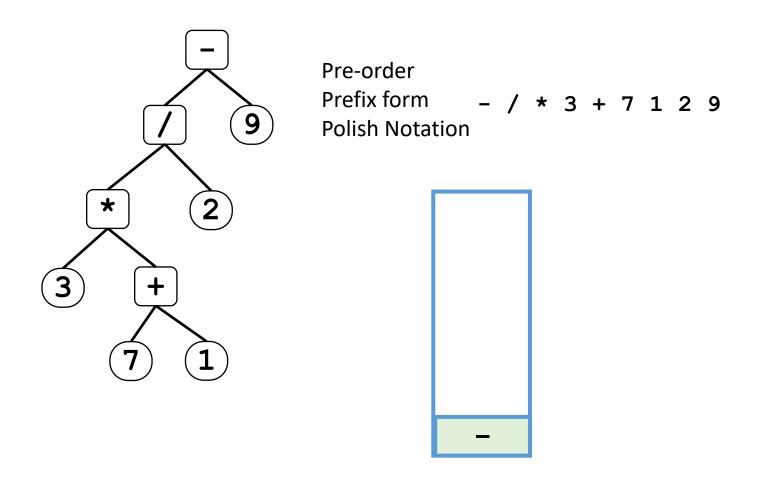
Post-order
Postfix form

3 7 1 + * 2 / 9 Reverse Polish Notation

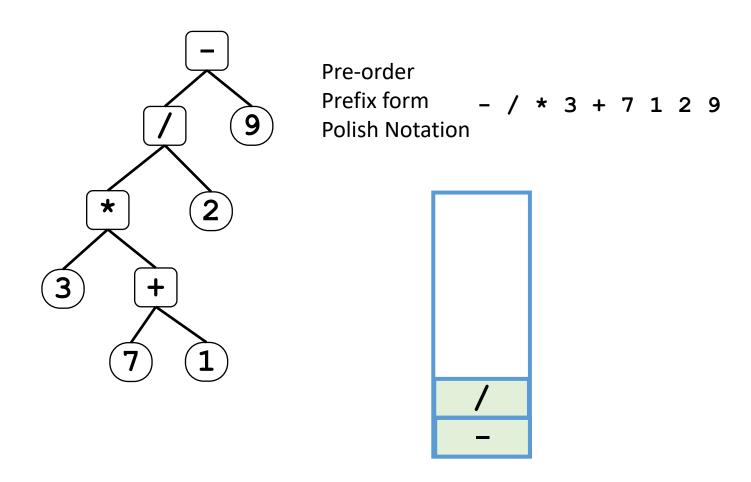
$$3 * (7 + 1) / 2 - 9$$

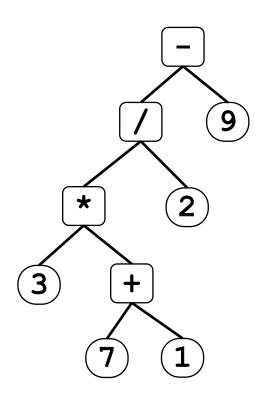


3 * (7 + 1) / 2 - 9



3 * (7 + 1) / 2 - 9

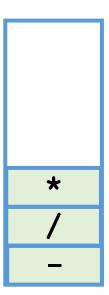


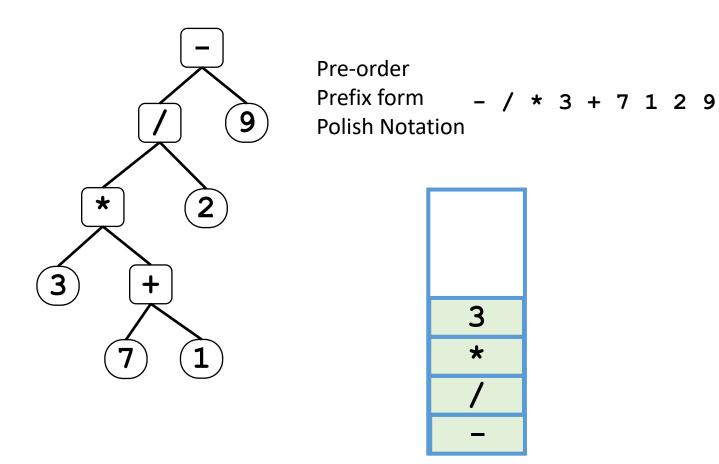


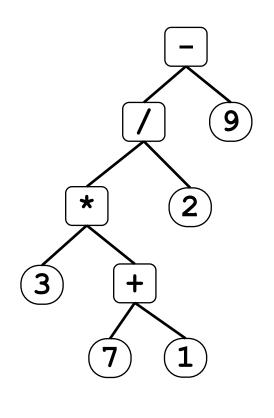
Pre-order

Prefix form - / * 3 + 7 1 2 9

Polish Notation





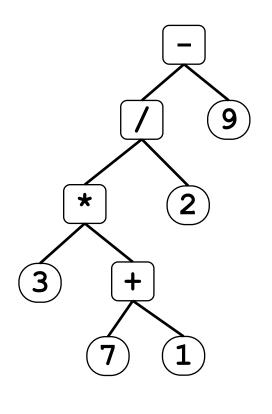


Pre-order

Prefix form - / * 3 + 7 1 2 9

Polish Notation





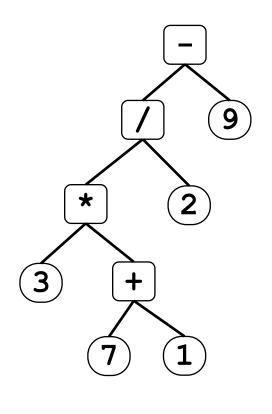
Pre-order

Prefix form - / * 3 + 7 1 2 9

Polish Notation



$$3 * (7 + 1) / 2 - 9$$

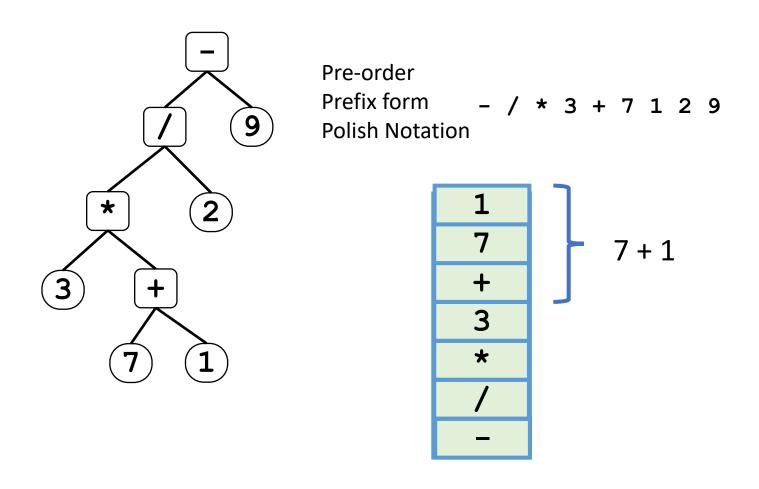


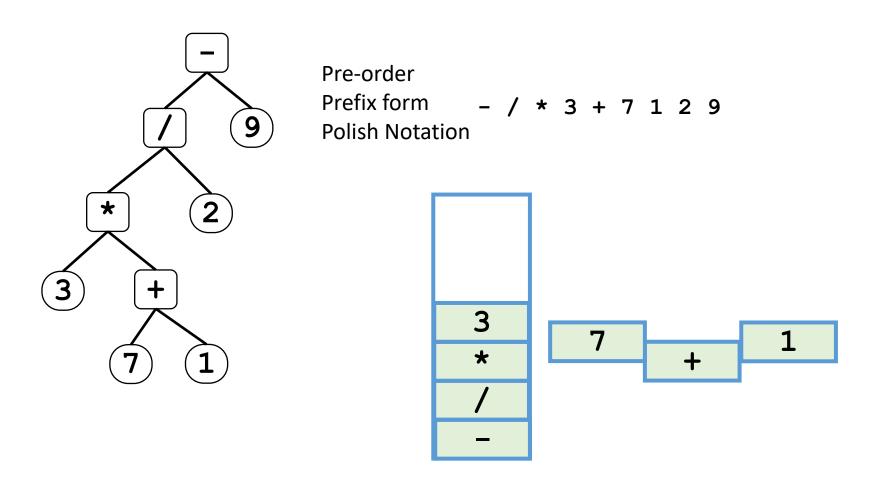
Pre-order

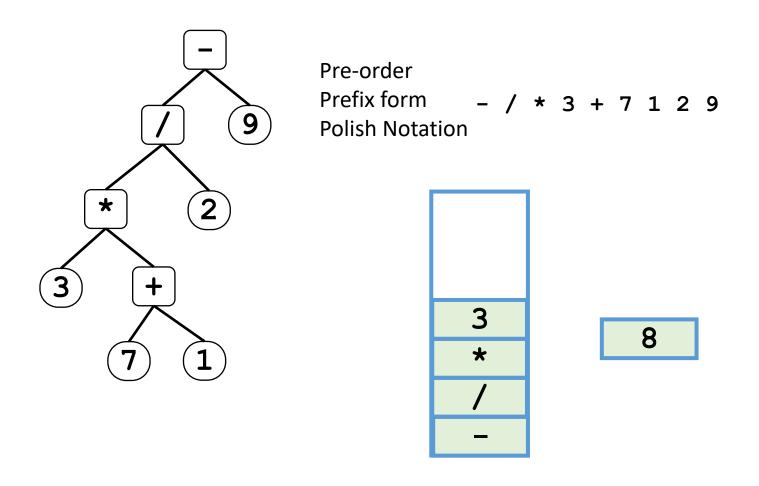
Prefix form - / * 3 + 7 1 2 9

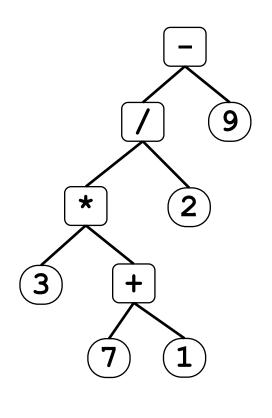
Polish Notation











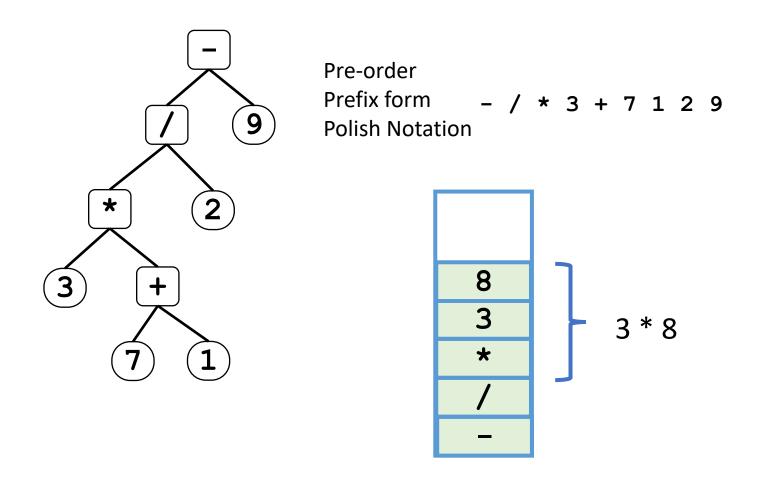
Pre-order

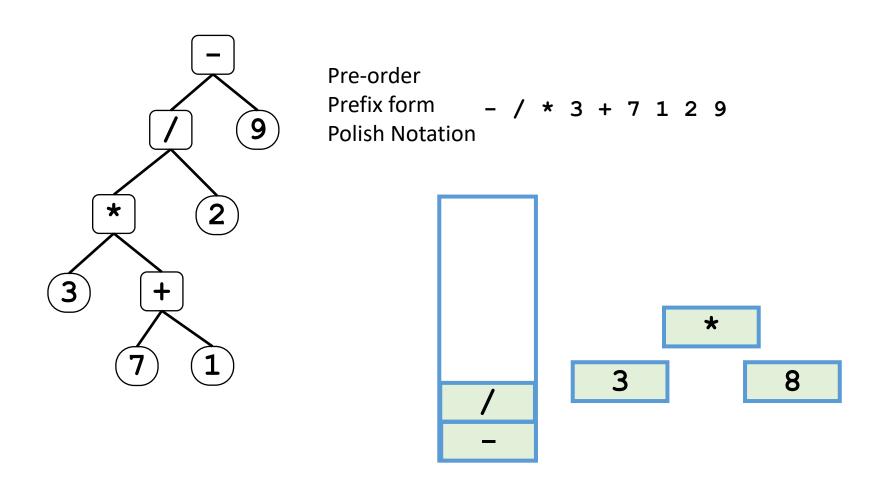
Prefix form - / * 3 + 7 1 2 9

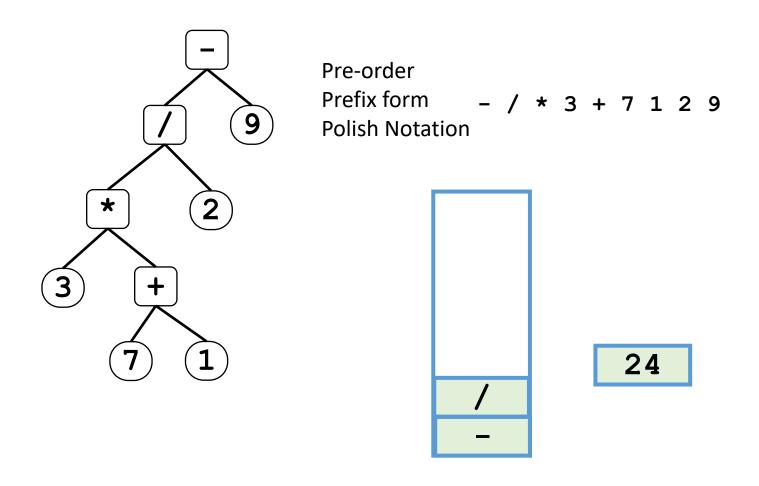
Polish Notation

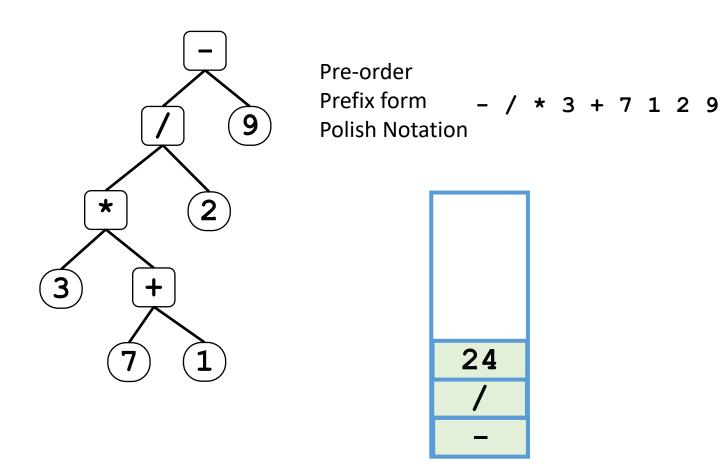


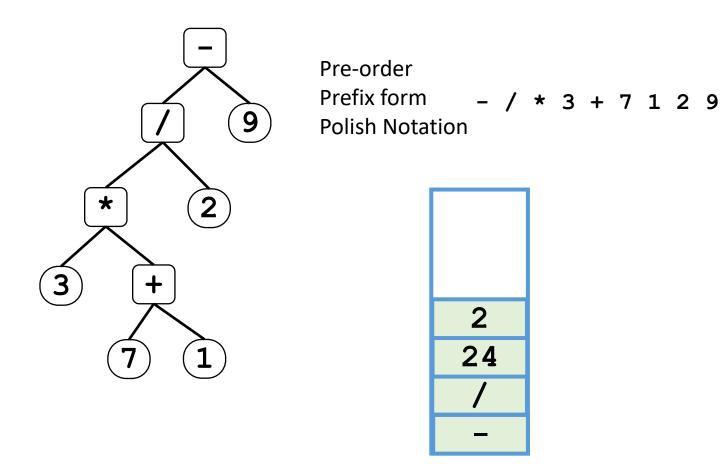
$$3 * (7 + 1) / 2 - 9$$

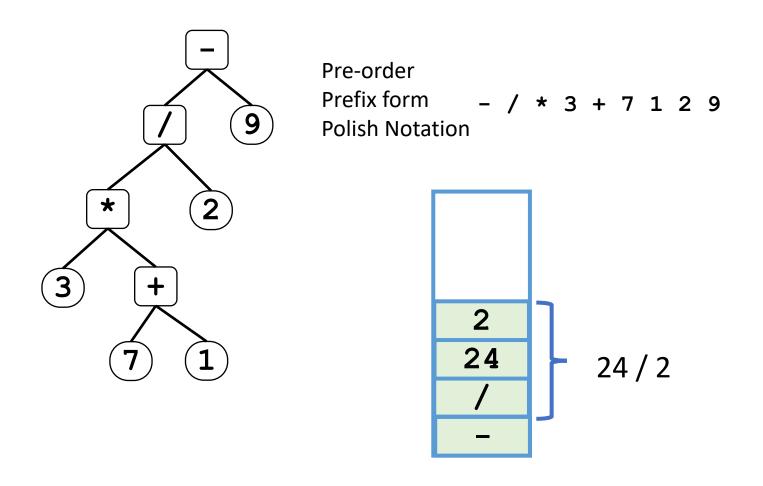


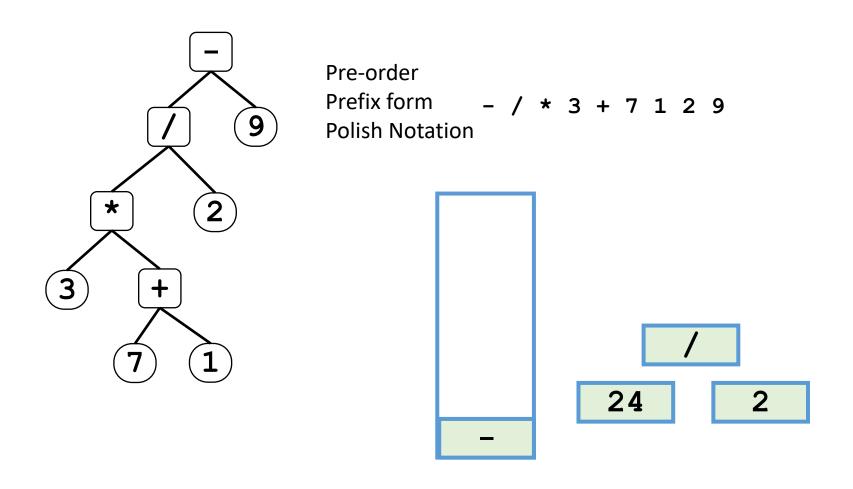


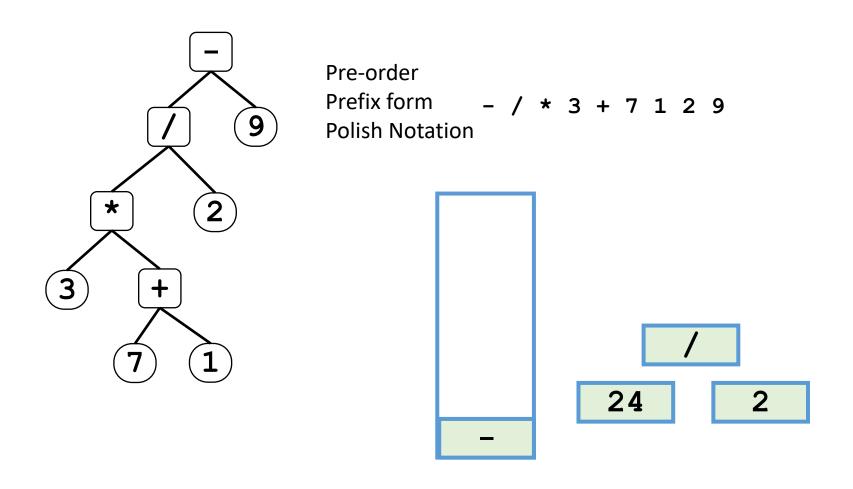


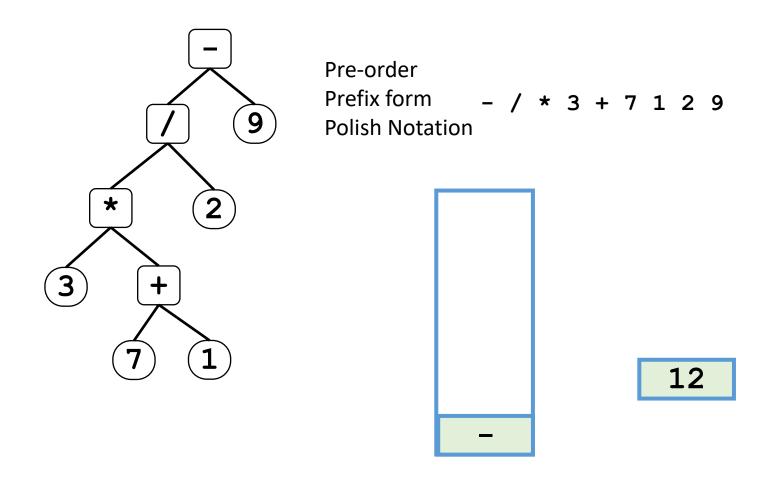


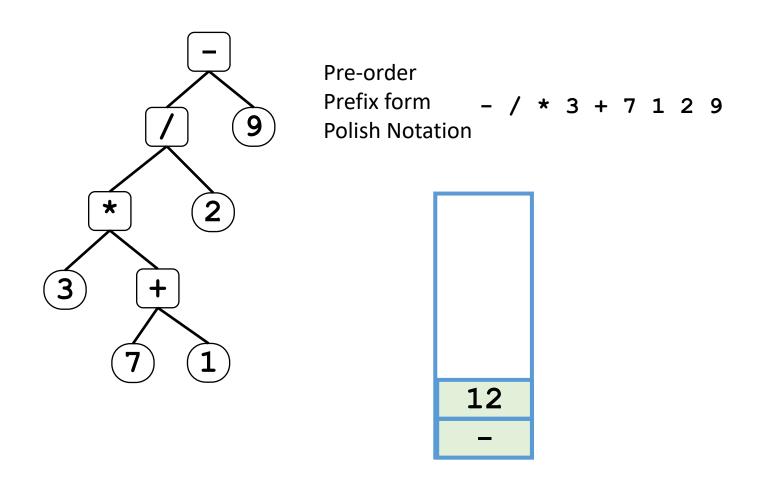


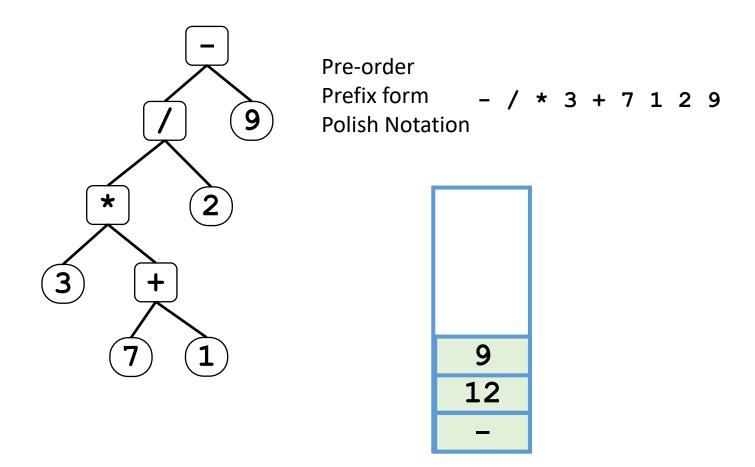


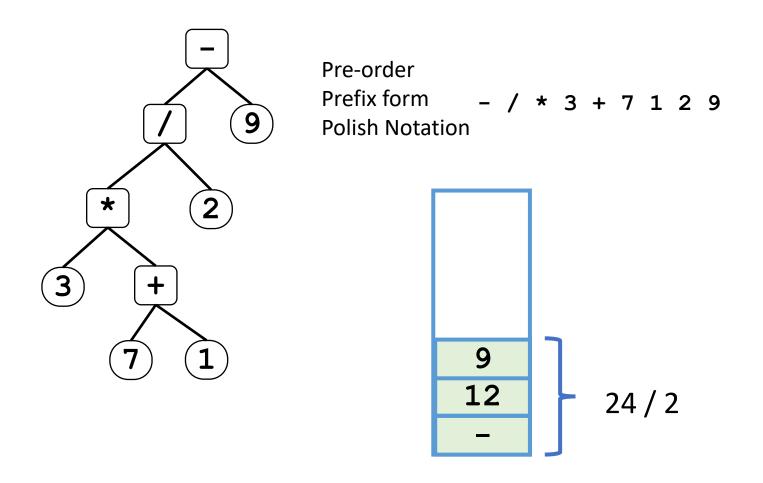


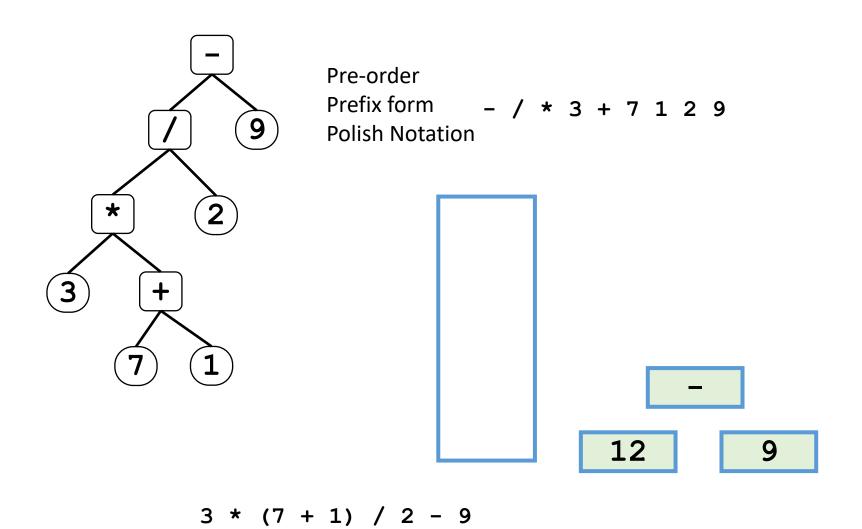


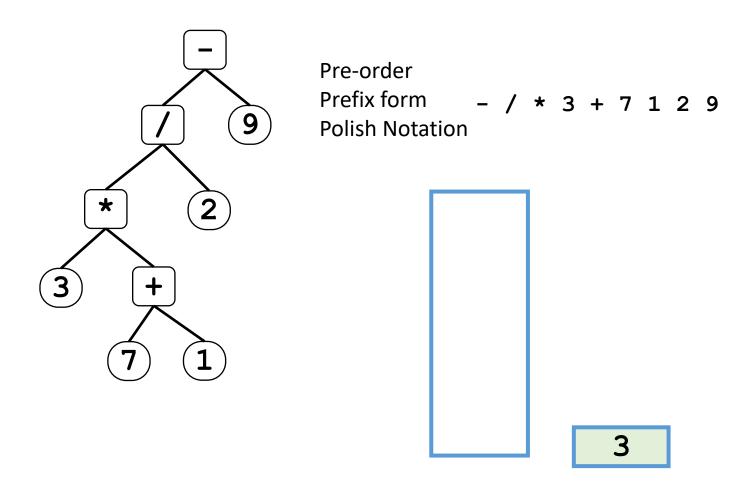


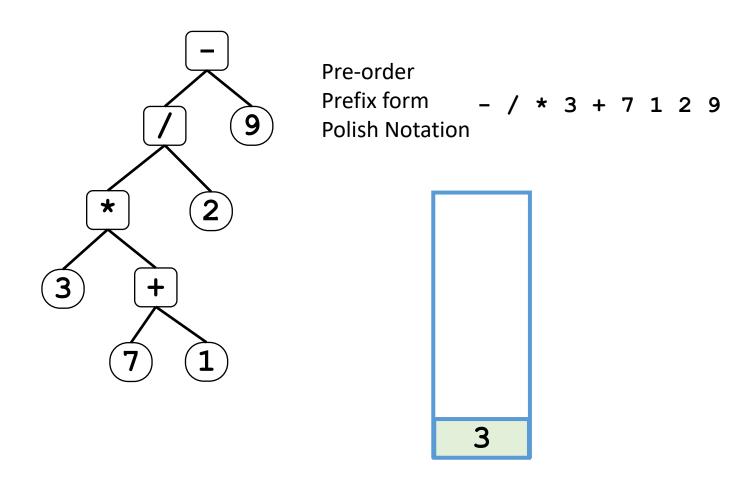


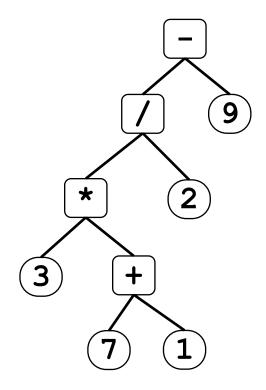












Pre-order

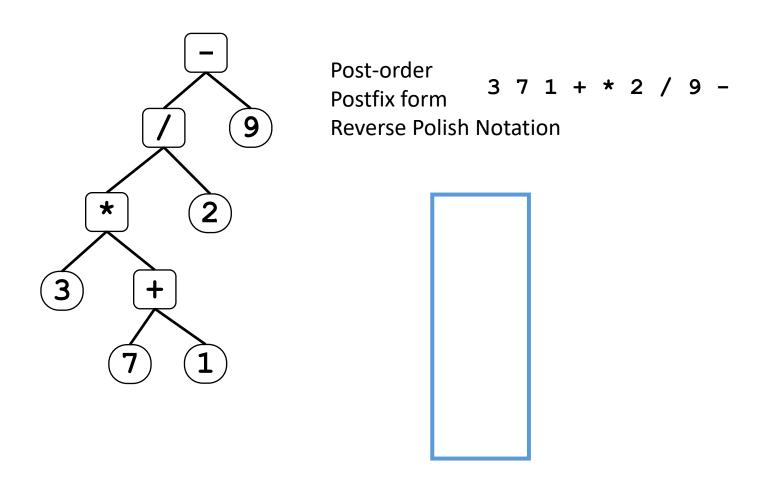
Prefix form - / * 3 + 7 1 2 9

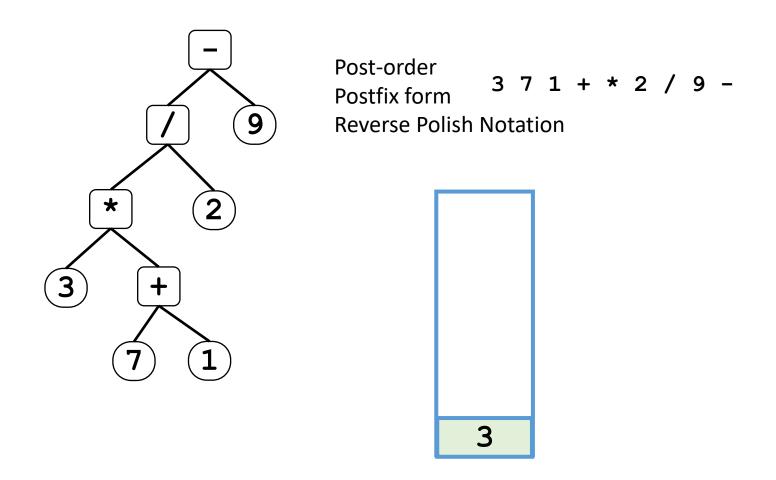
Polish Notation

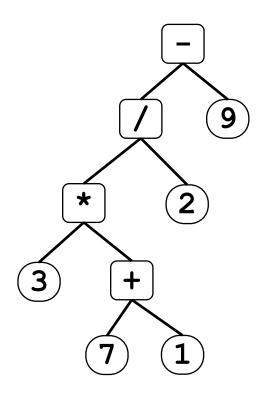
Post-order
Postfix form

3 7 1 + * 2 / 9 Reverse Polish Notation

$$3 * (7 + 1) / 2 - 9$$





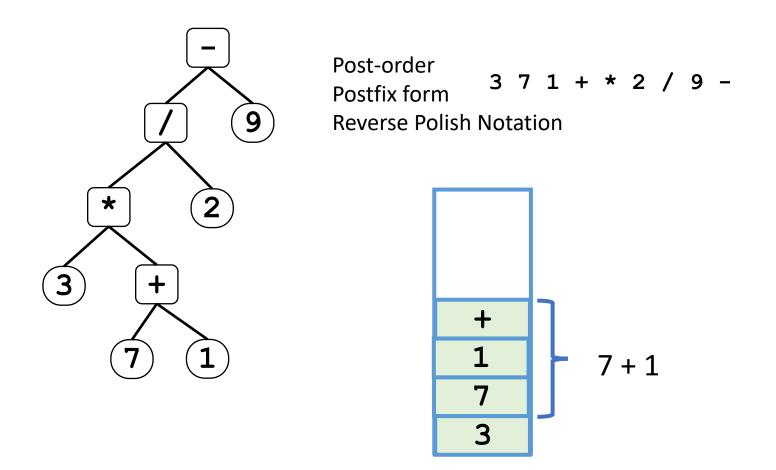


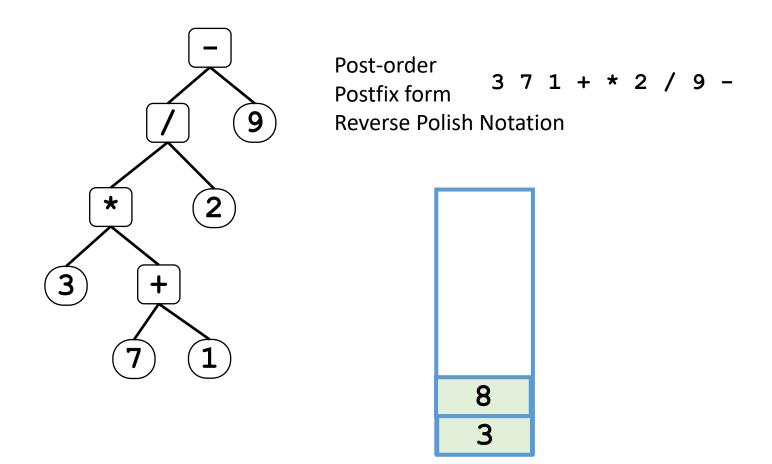
Post-order Postfix form

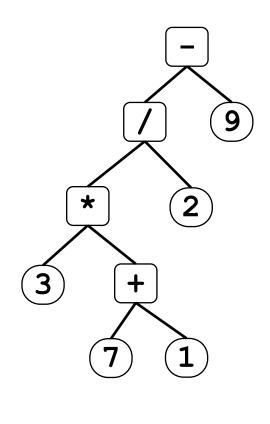
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Reverse Polish Notation

$$3 * (7 + 1) / 2 - 9$$

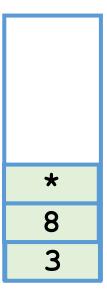




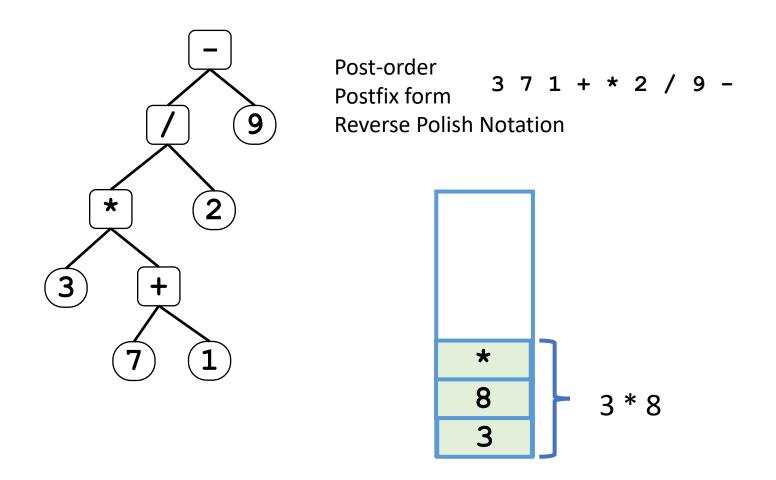


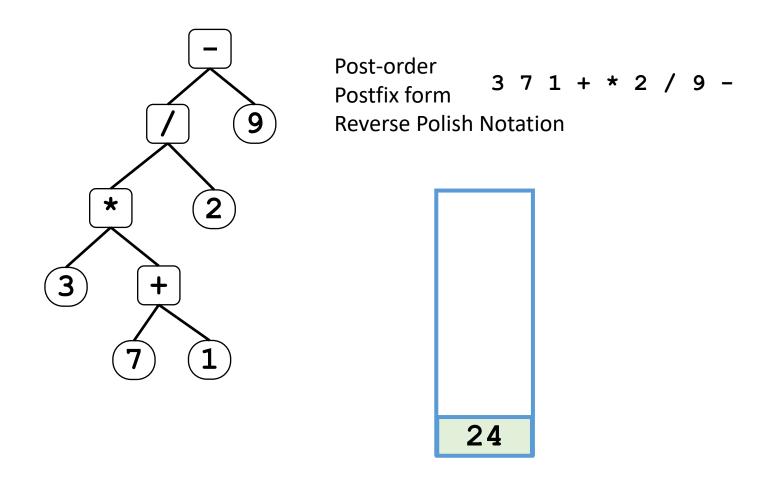
Post-order
Postfix form

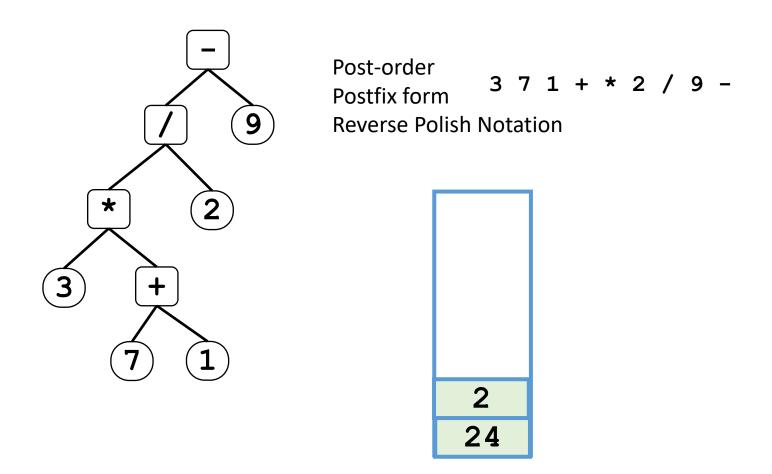
3 7 1 + * 2 / 9 Reverse Polish Notation

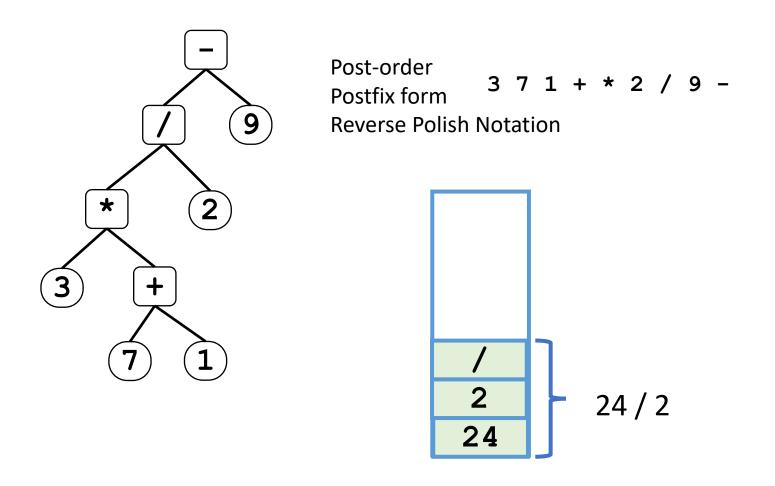


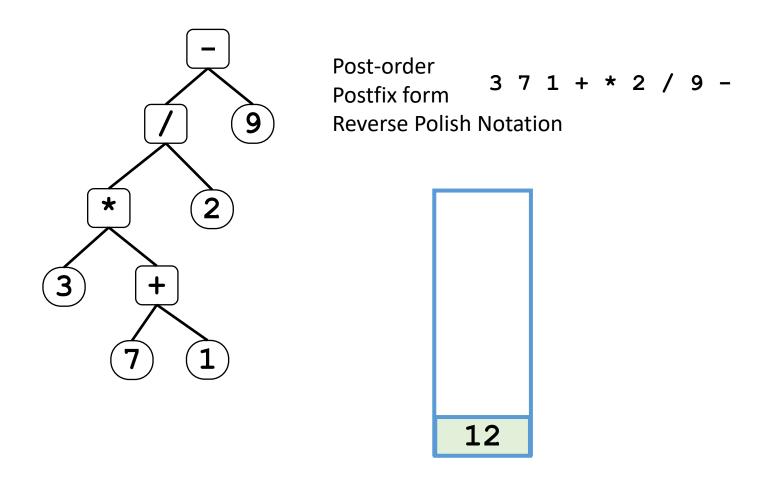
$$3 * (7 + 1) / 2 - 9$$

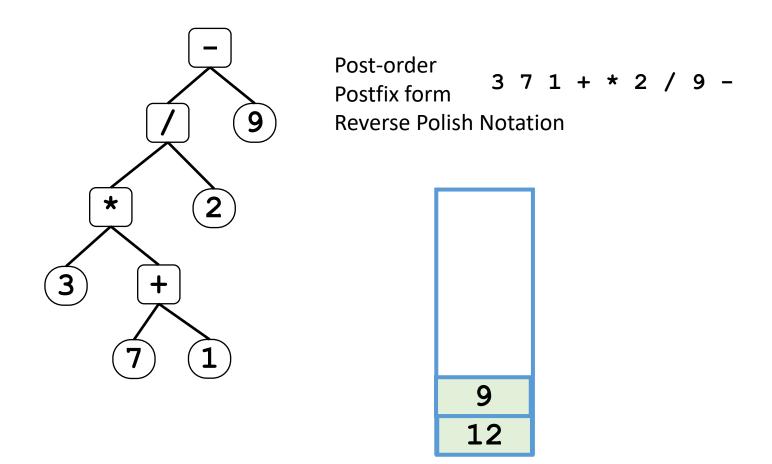


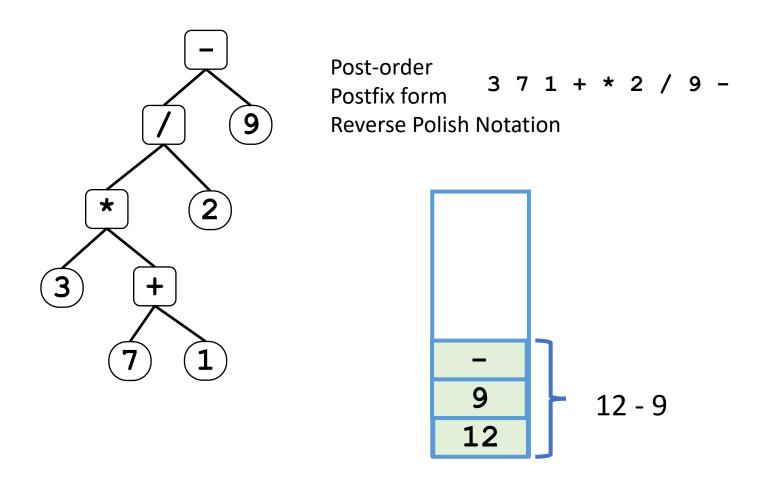


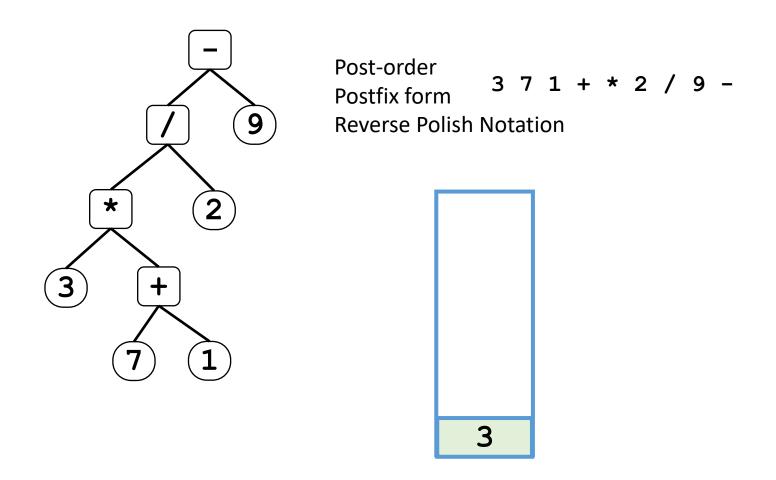












Recursive Structure of Expressions

- In most programming languages, an *expression* is a recursive structure that can contain subexpressions.
- Every expression can have one of the following forms:
 - An integer constant
 - A variable name that holds an integer value
 - Two expressions joined by an operator
 - An expression enclosed in parentheses
- The rules for forming an expression can be expressed in the form of a *grammar*, as follows:

```
E \rightarrow constant 1024

E \rightarrow identifier temp

E \rightarrow E \ op \ E temp + 1024

E \rightarrow (E) (temp + 1024)
```

A Two-Level Grammar

- The problem of parsing an expression can be simplified by changing the grammar to one that has two levels:
 - An expression is either a term or two expressions joined by an operator.
 - A term is either a constant, an identifier, or an expression enclosed in parentheses.
- This design is reflected in the following revised grammar.

$$\mathbf{E} \to \mathbf{T}$$
 $\mathbf{E} \to \mathbf{E} \ op \ \mathbf{E}$

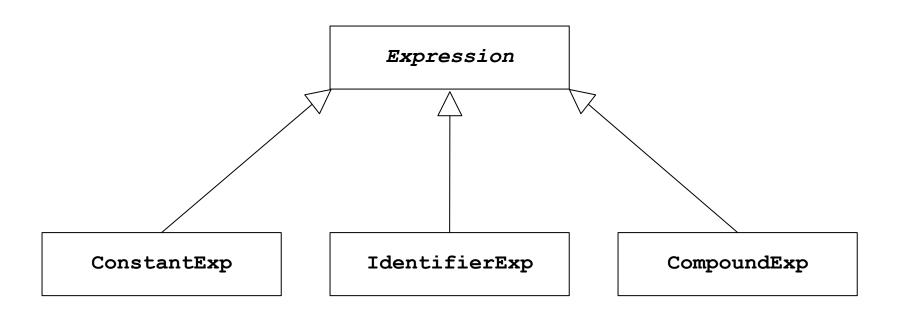
$$T \rightarrow constant$$

$$T \rightarrow identifier$$

$$T \rightarrow (E)$$

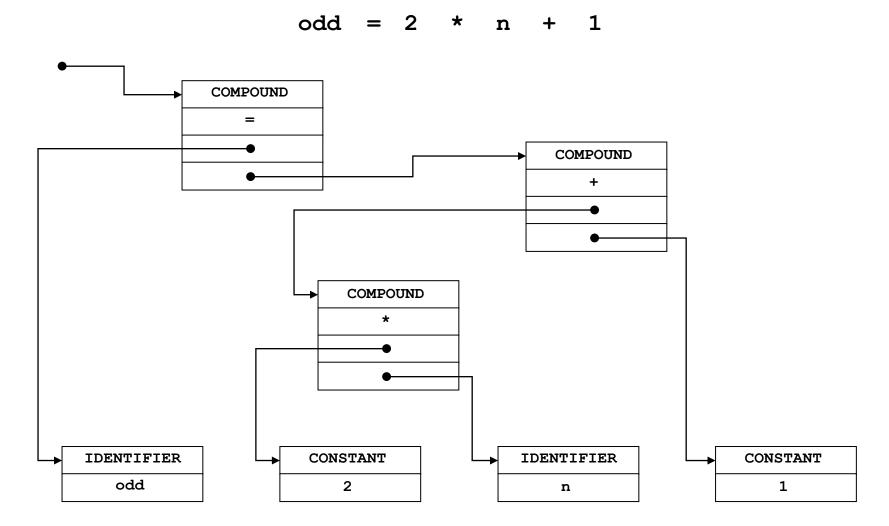
The **Expression** Class Hierarchy

• Because expressions have more than one form, a C++ class that represents expressions can be represented most easily by a class hierarchy in which each of the expression types is a separate subclass, as shown in the following diagram:



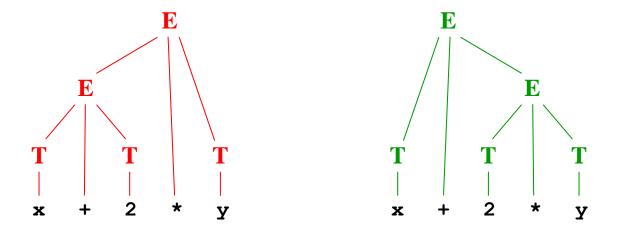
Parsing an Expression

• Parsing: Convert the string representation to an internal form



Ambiguity in Parse Structures

• Although the two-level grammar from the preceding slide can recognize any expression, it is *ambiguous* because the same input string can generate more than one parse tree.



• Ambiguity in grammars is typically resolved by providing the parser with information about the *precedence* of the operators.

Precedence

| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |

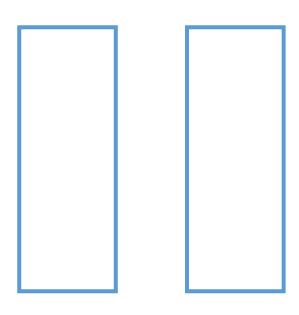
Parsing an expression

- Several approaches
 - Recursive parsing
 - Infix parsing using stacks

Example: Parsing using stacks

$$Odd = 1 + n * (2 - x) / 2$$

| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |

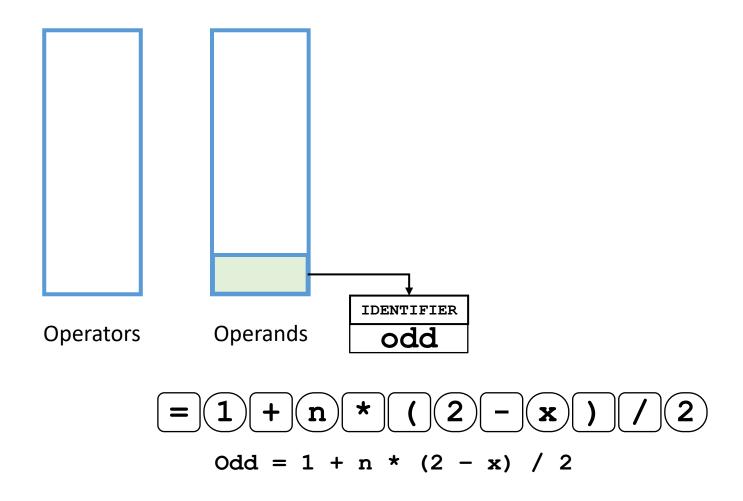


Operators Operands

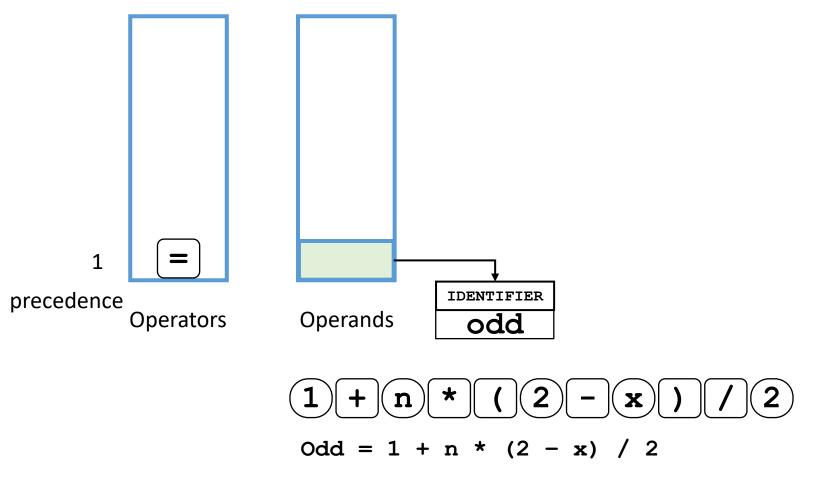
odd = 1 + n * (2 - x) / 2

$$0dd = 1 + n * (2 - x) / 2$$

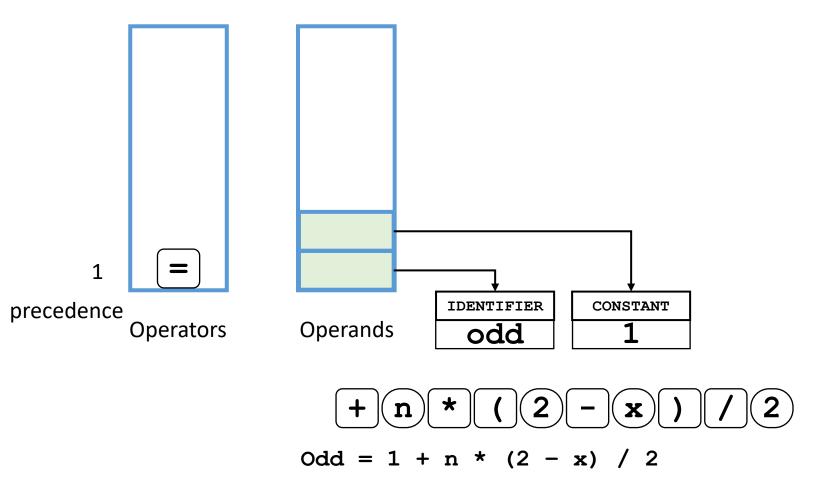
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



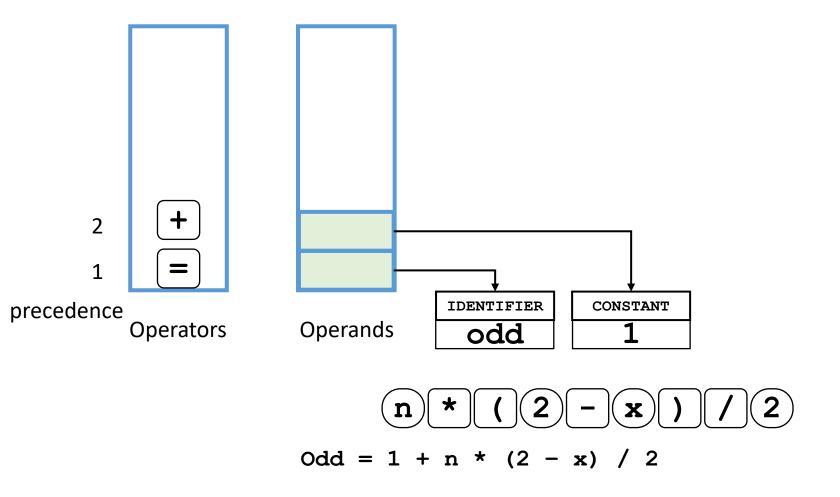
| precedence | operators |
|------------|-----------|
| 3 | */ |
| 2 | + - |
| 1 | = |



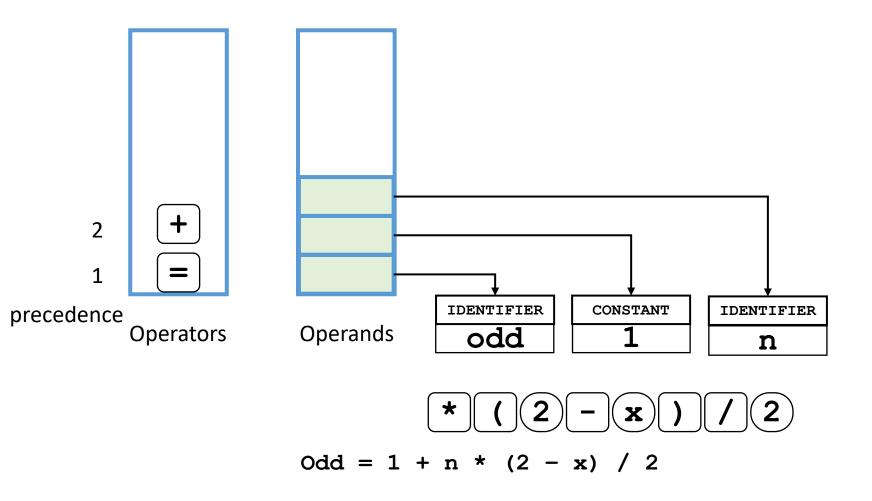
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



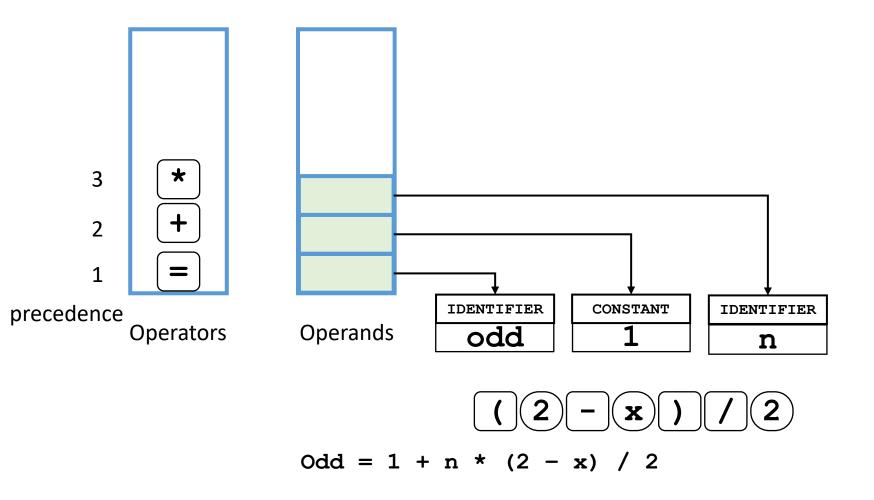
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



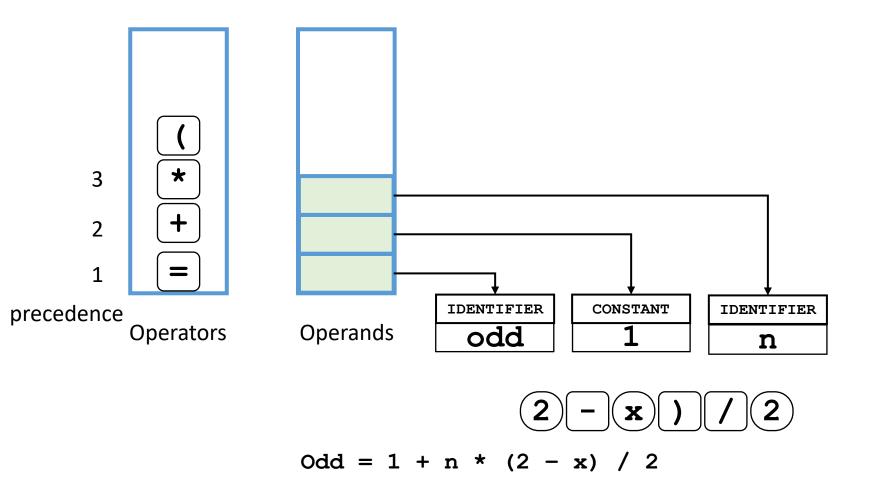
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



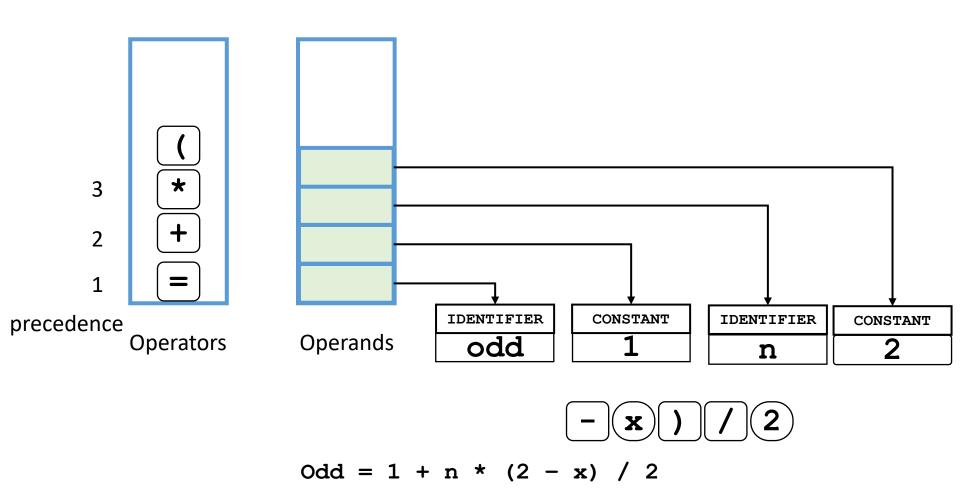
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



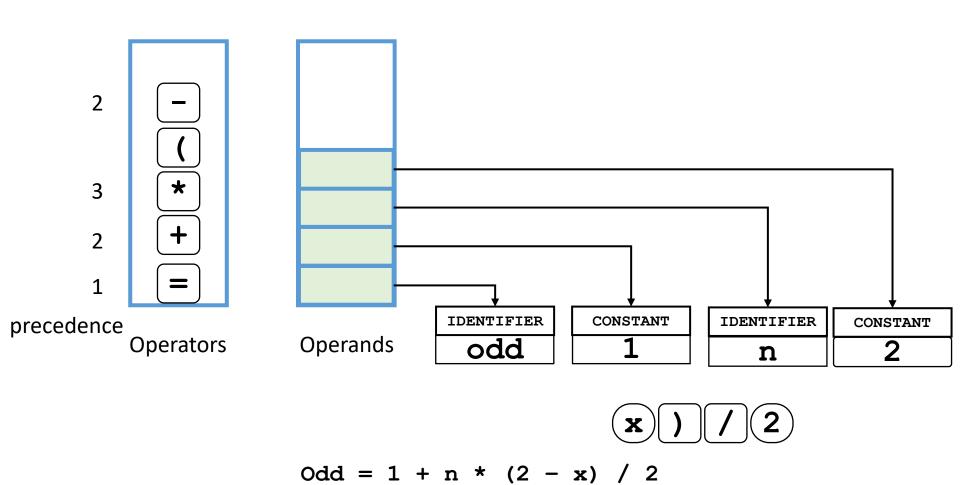
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



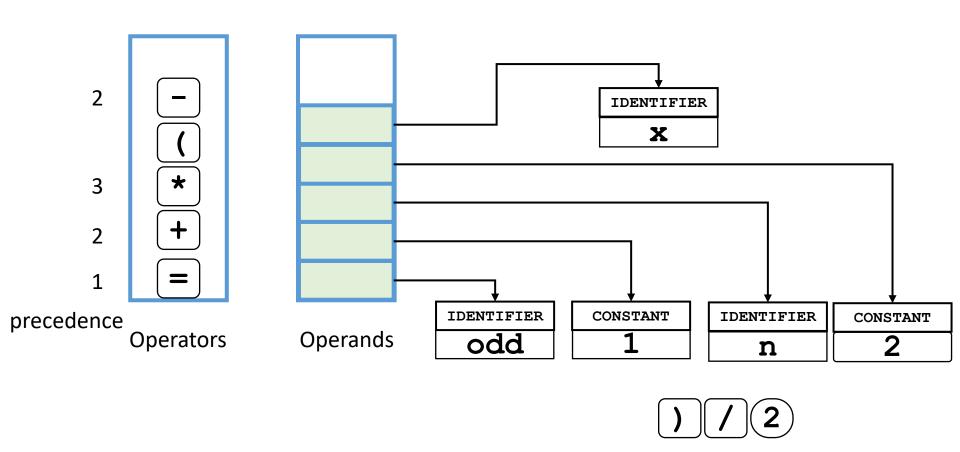
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



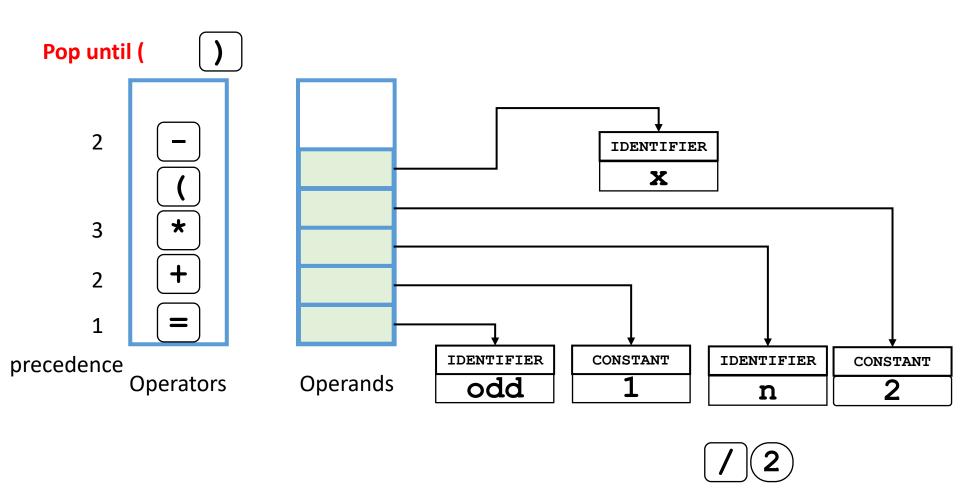
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |



| precedence | operators |
|------------|-----------|
| 3 | */ |
| 2 | + - |
| 1 | = |

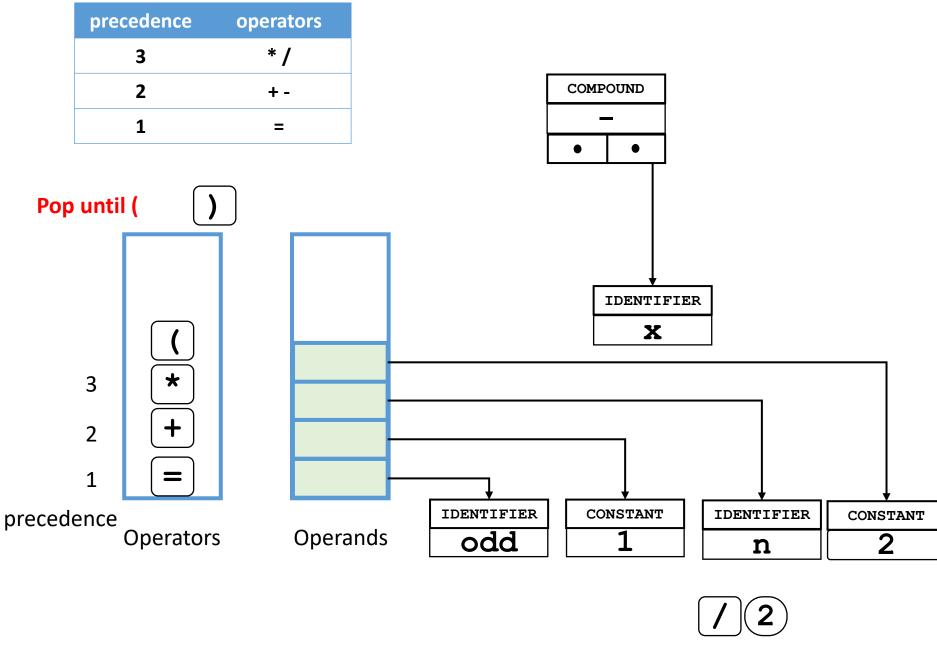


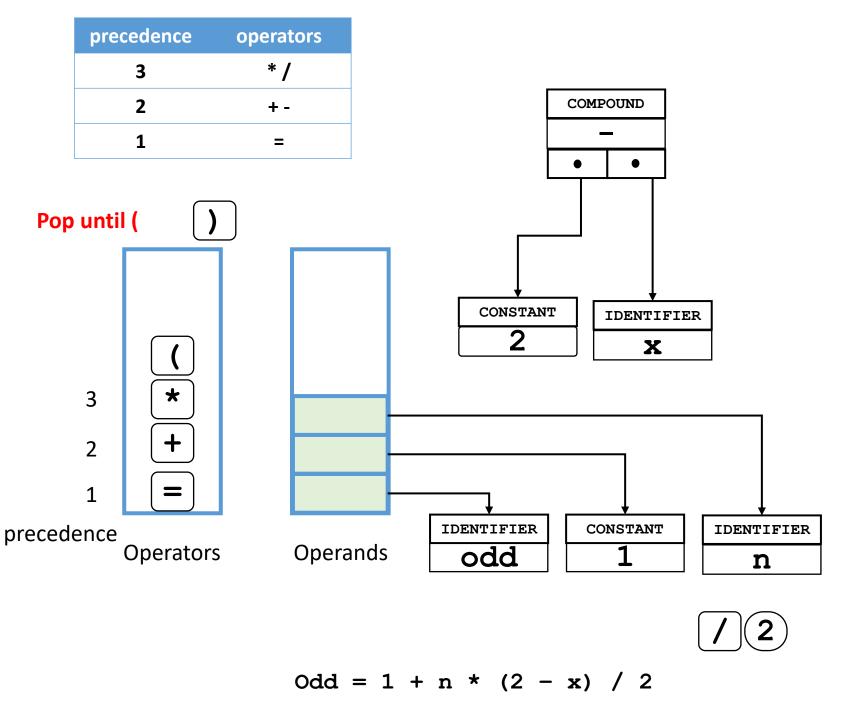
| precedence | operators |
|------------|-----------|
| 3 | * / |
| 2 | + - |
| 1 | = |

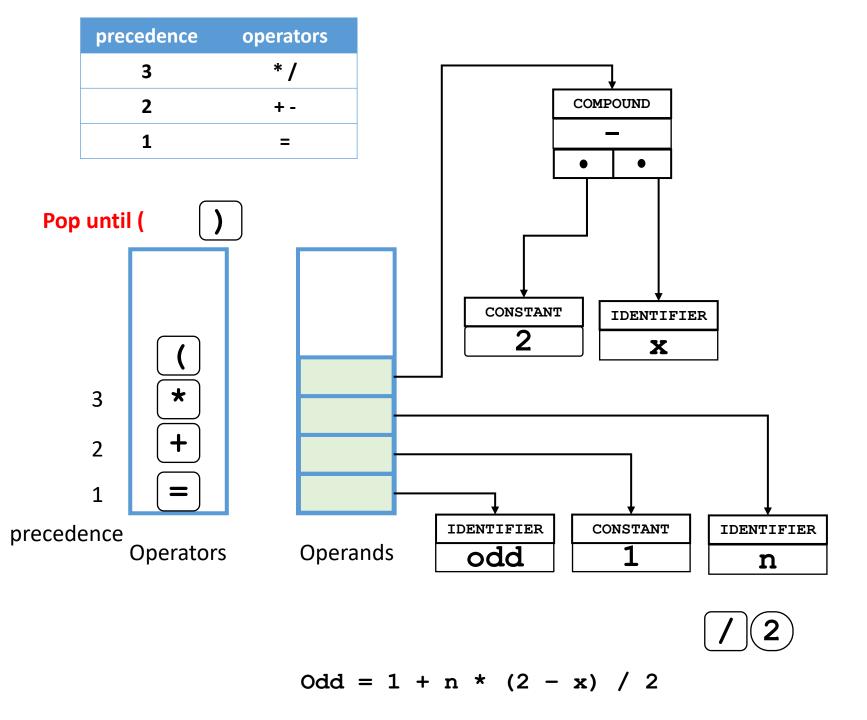


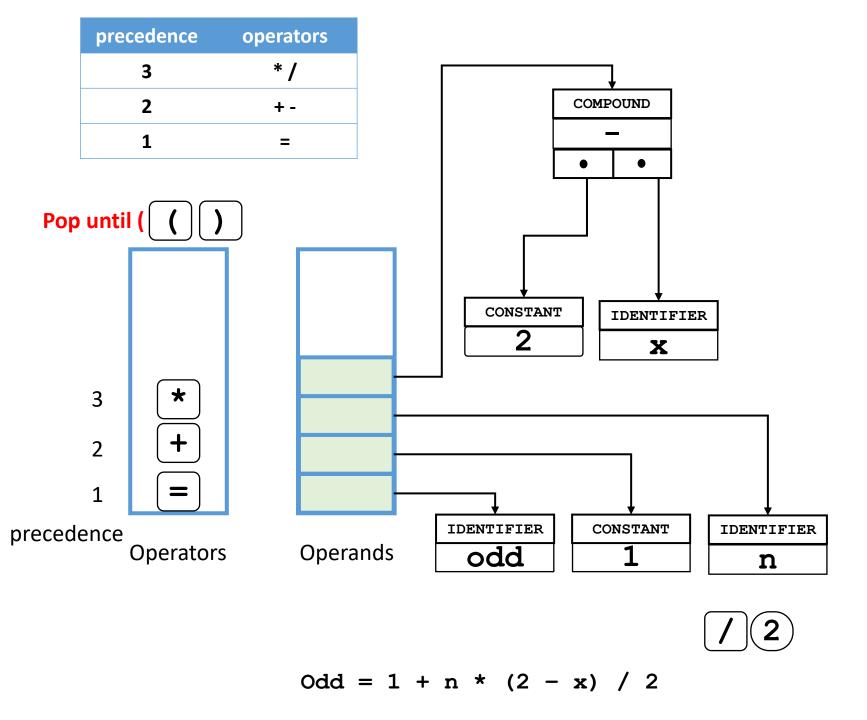
$$Odd = 1 + n * (2 - x) / 2$$

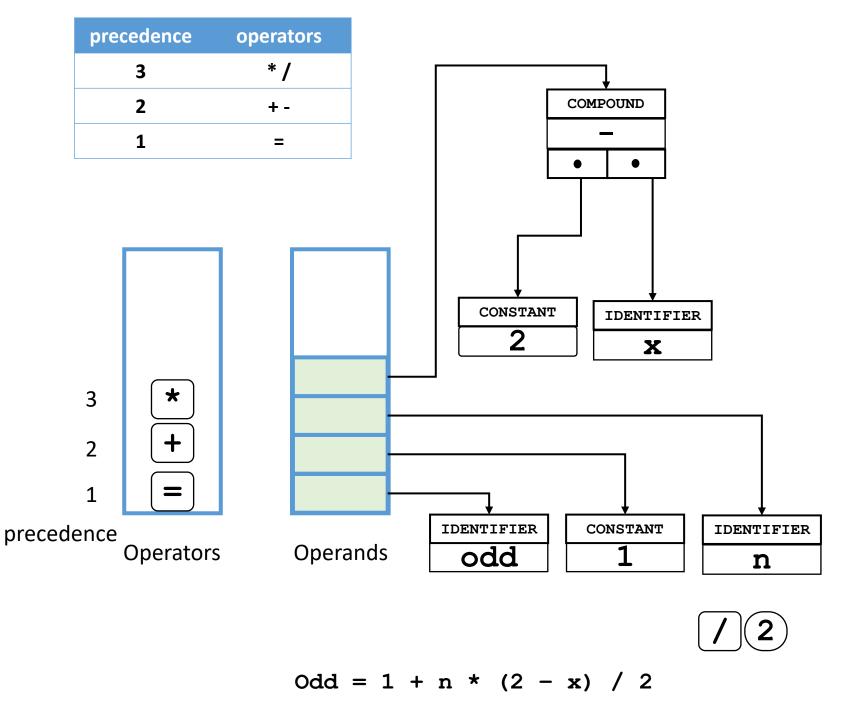
| | precedence | operators | | | | |
|---------|----------------------------------|-----------|----|-------------|--------------|--------|
| | 3 | * / | | | | |
| | 2 | + - | cc | OMPOUND | | |
| | 1 | = | | _ - | | |
| Pop | until (| | | | | |
| | | | | identifier | : | |
| | 3 * 2 + 1 = | | | | | |
| precede | | s Opera | | CONSTANT 1 | identifier n | consta |
| | | | | | /2 | |

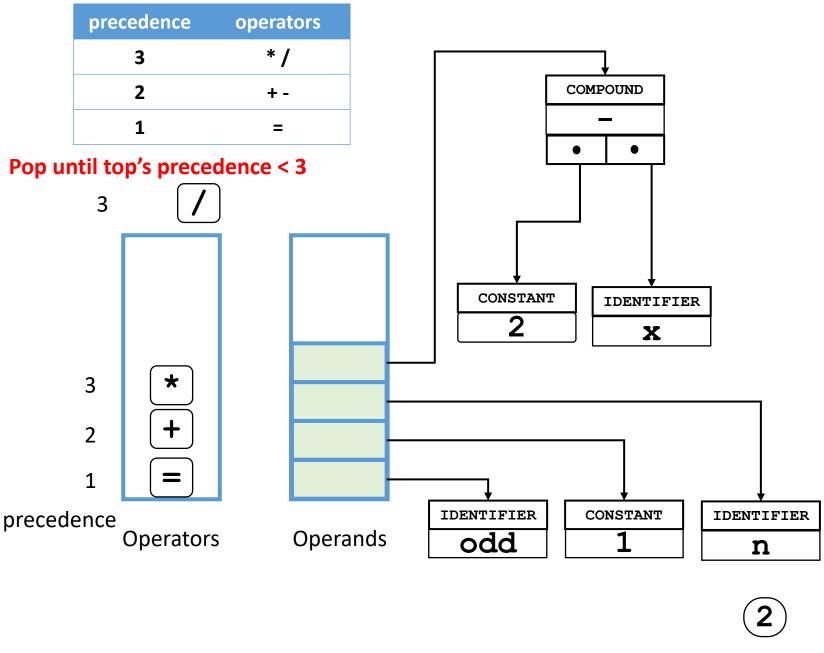


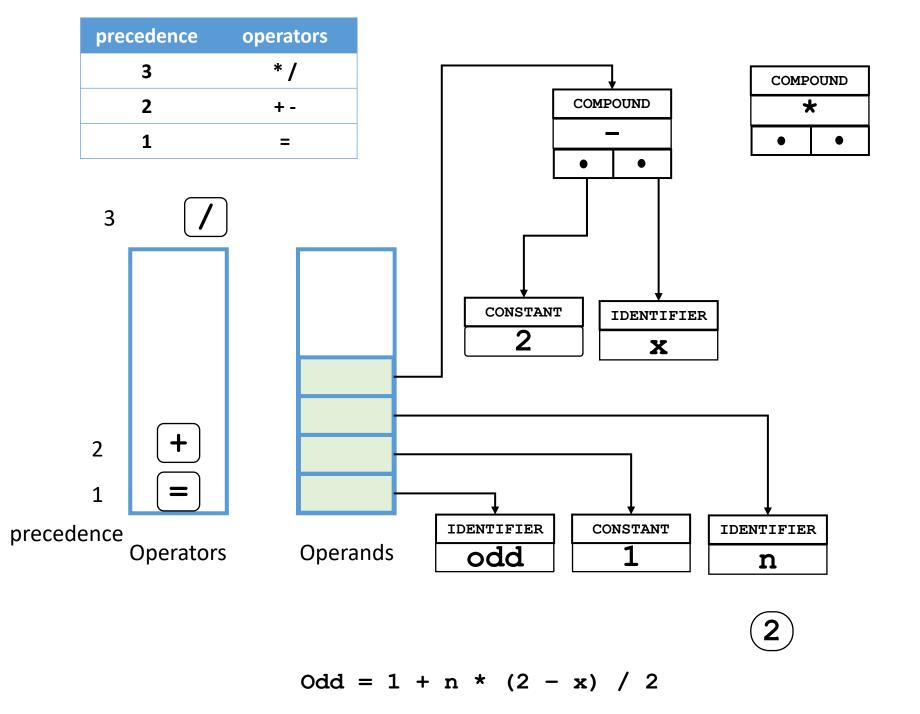


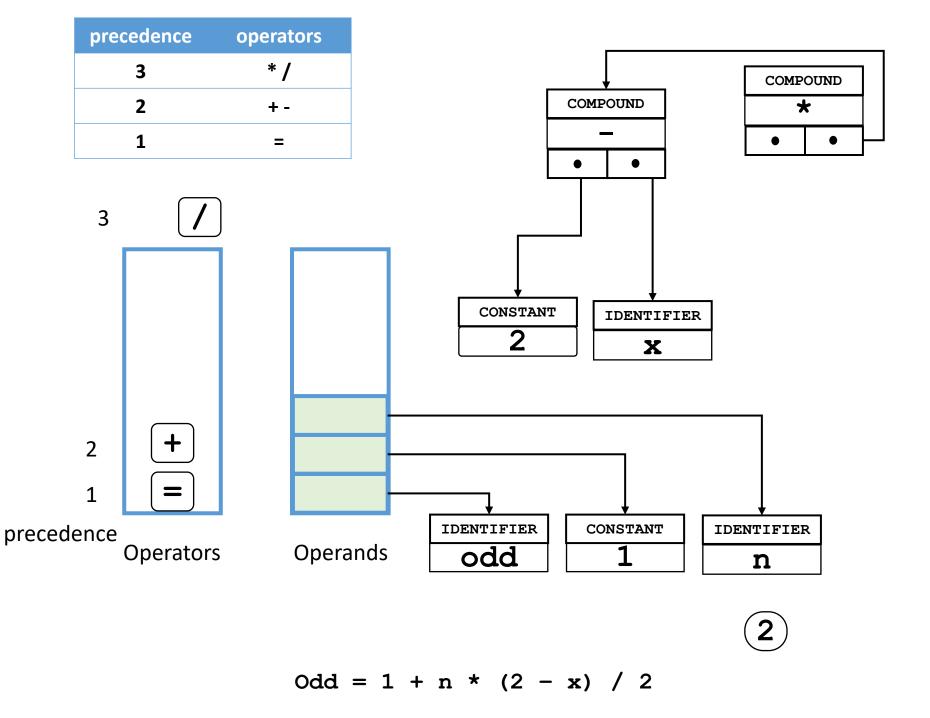


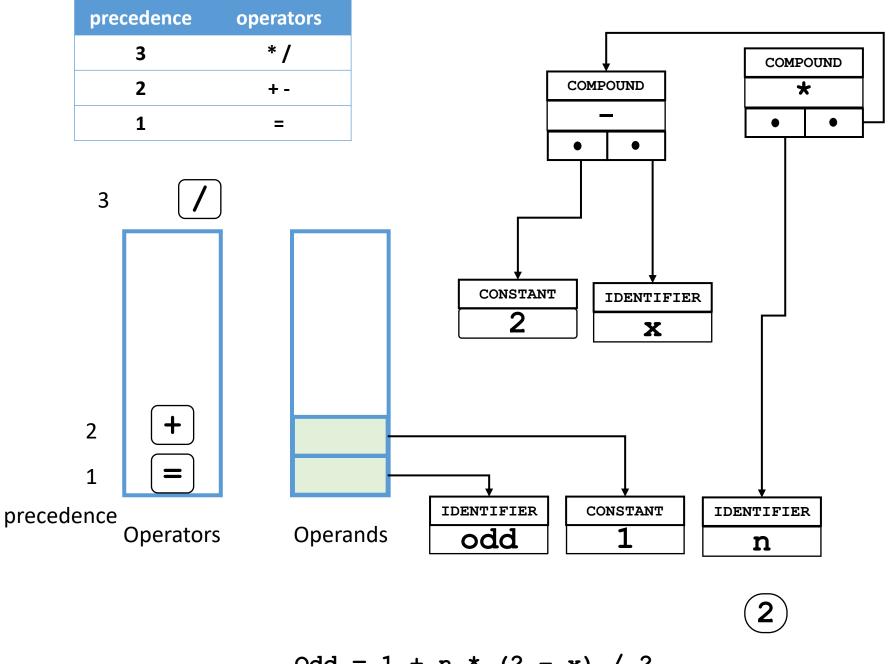


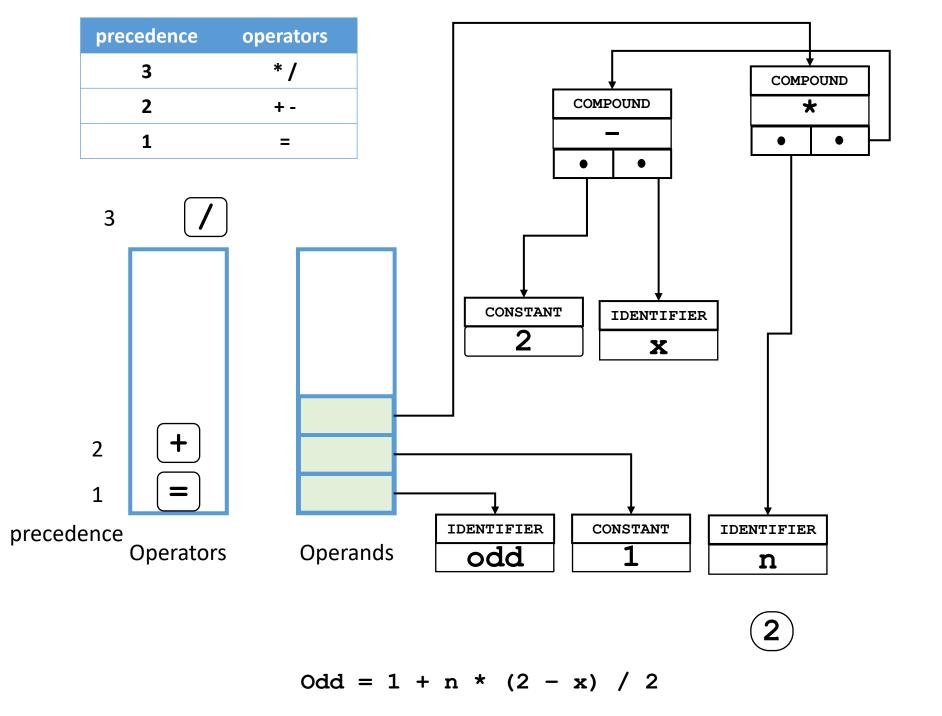


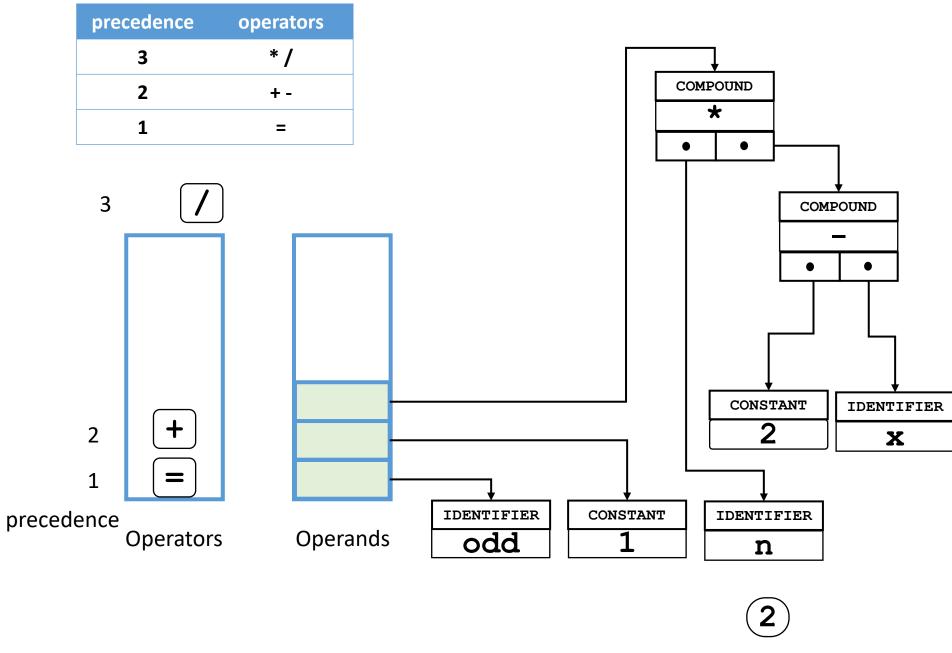


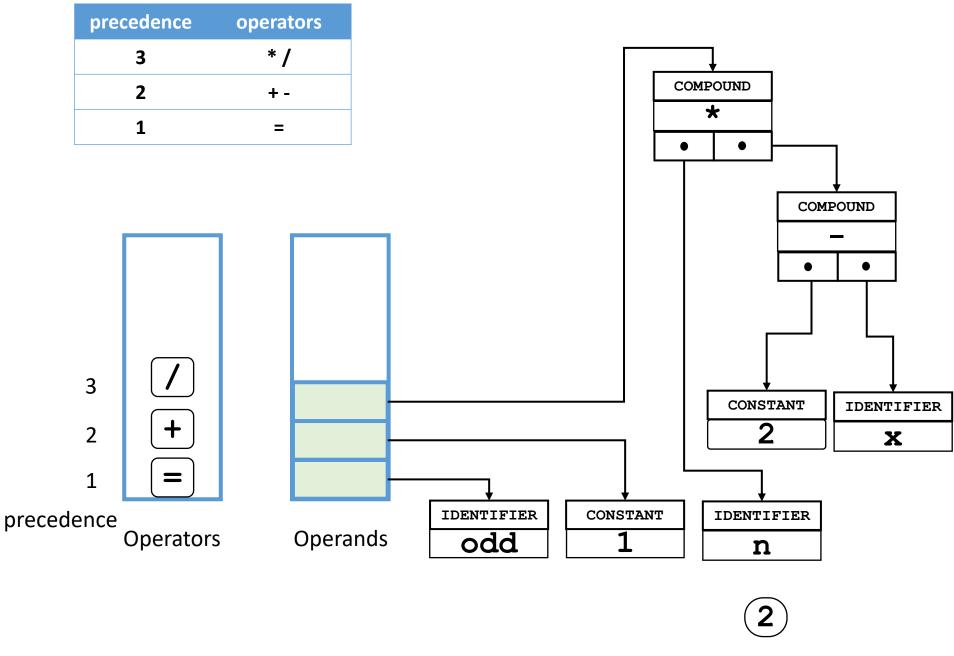


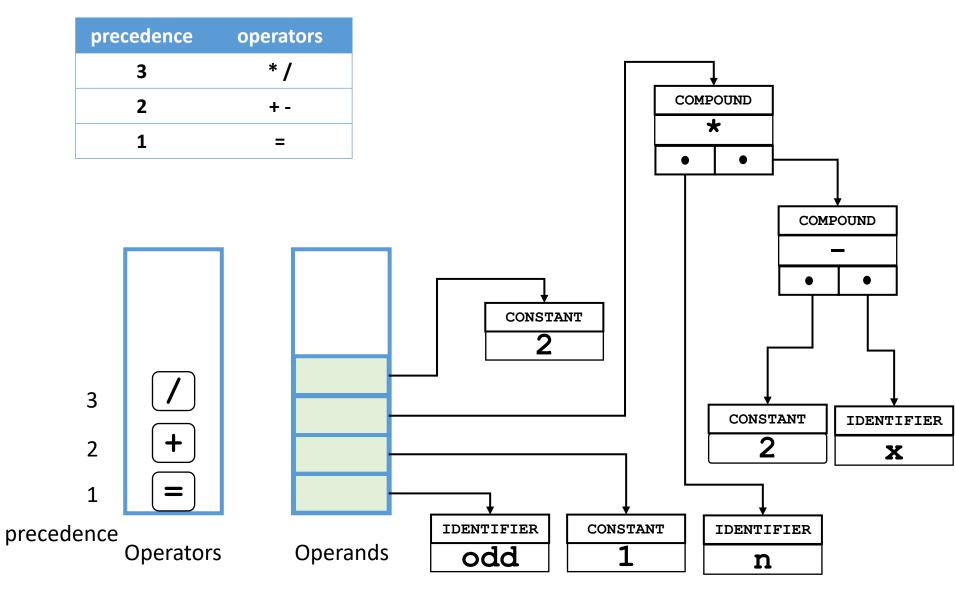




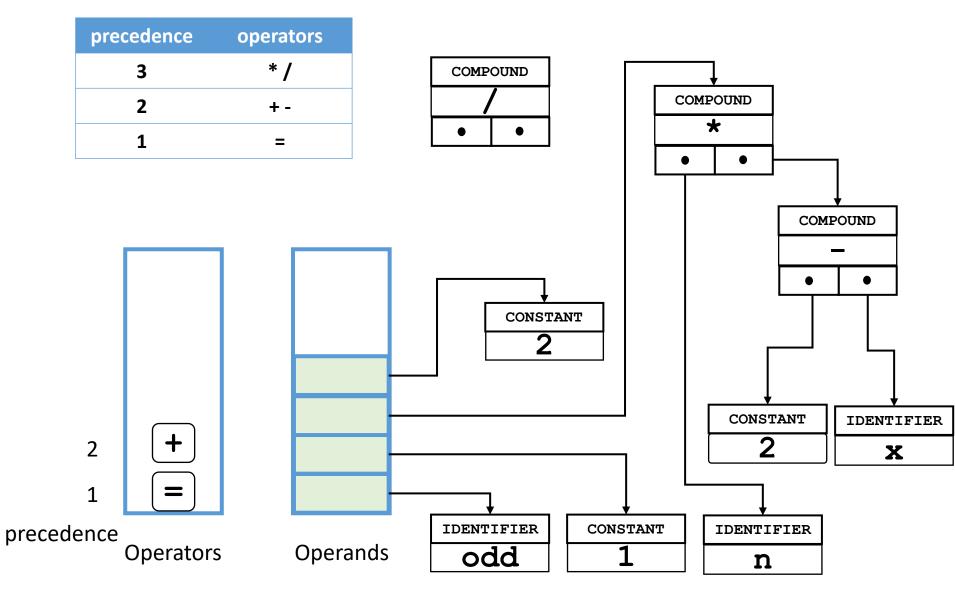




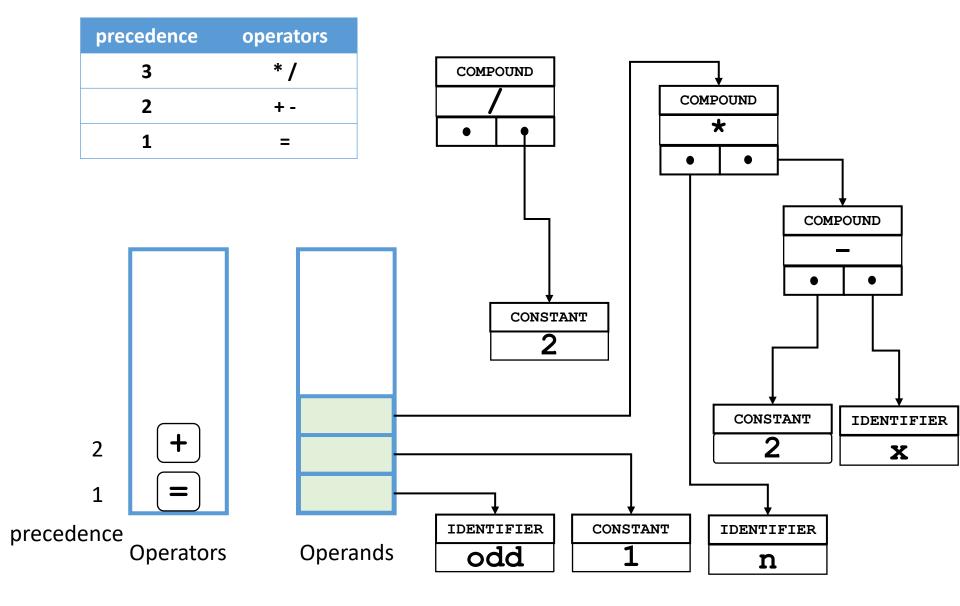




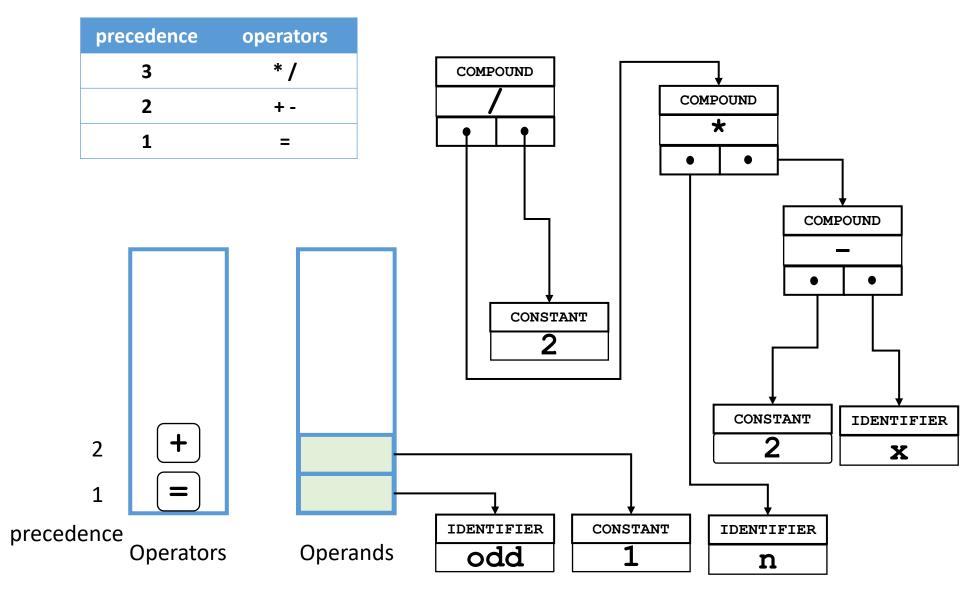
$$Odd = 1 + n * (2 - x) / 2$$



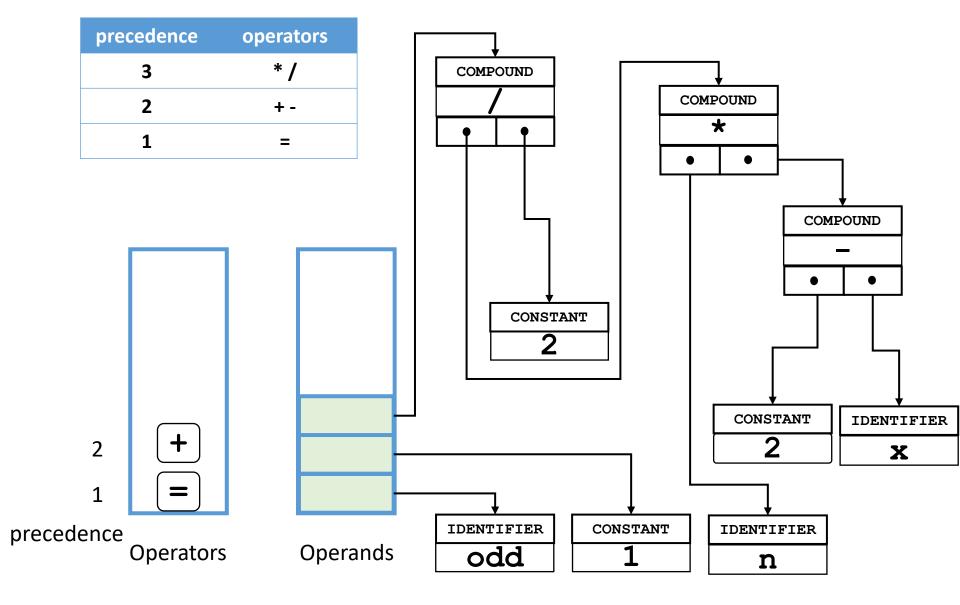
$$Odd = 1 + n * (2 - x) / 2$$



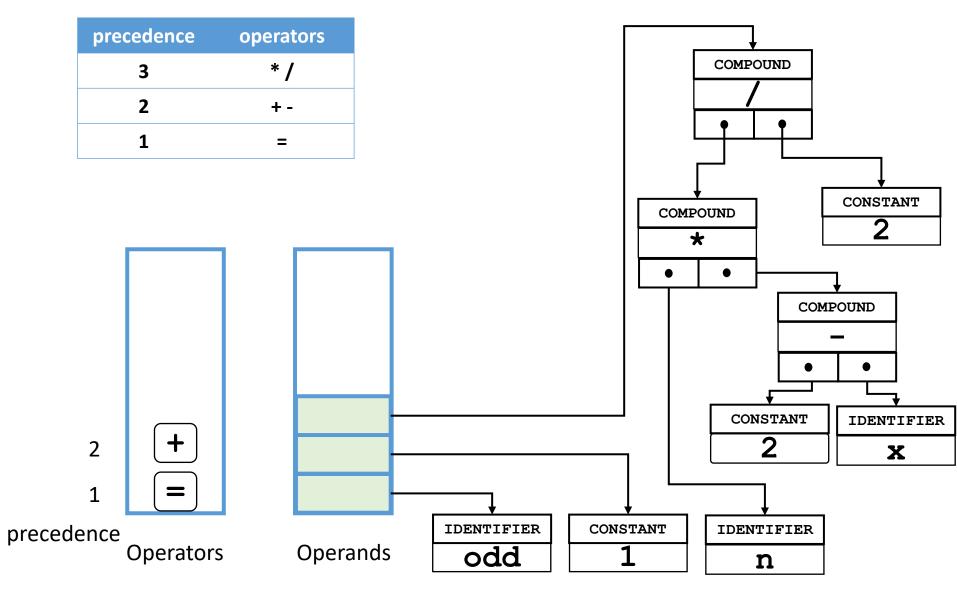
$$Odd = 1 + n * (2 - x) / 2$$



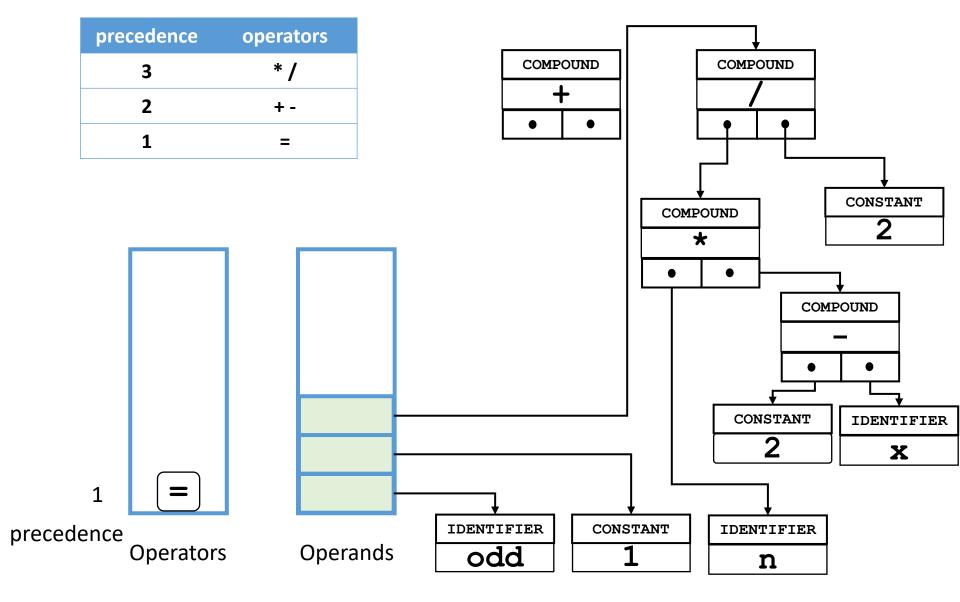
$$Odd = 1 + n * (2 - x) / 2$$



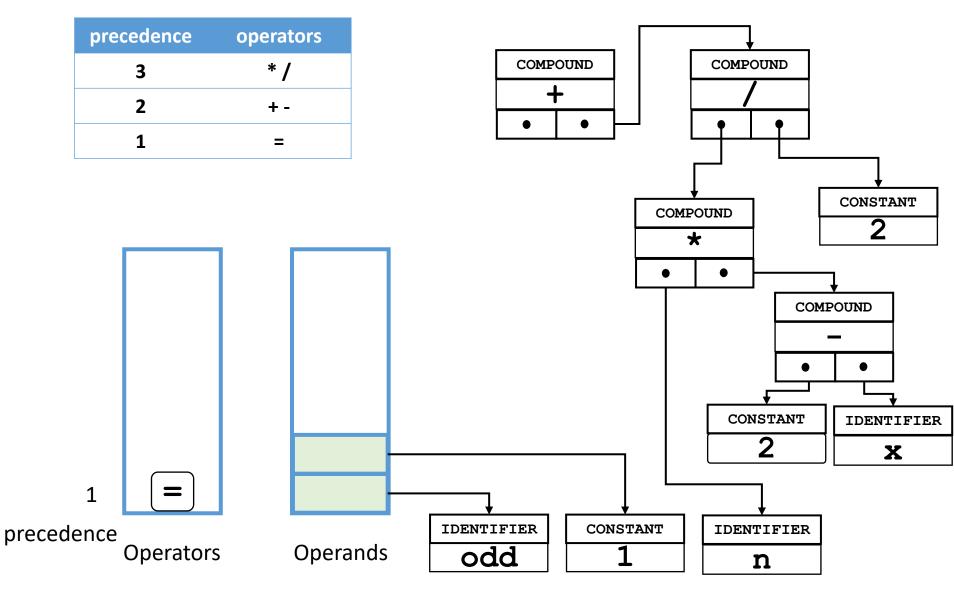
$$Odd = 1 + n * (2 - x) / 2$$



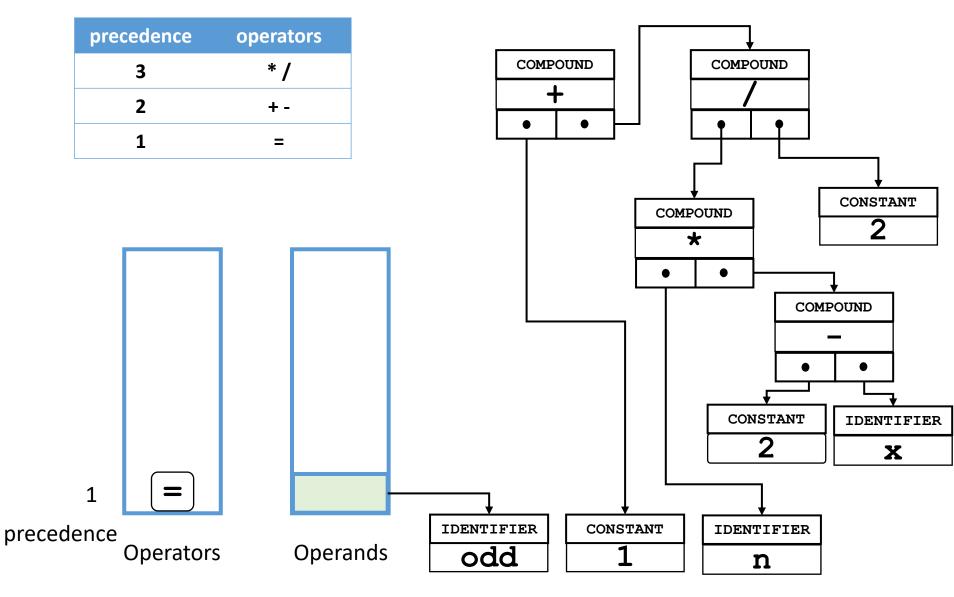
$$Odd = 1 + n * (2 - x) / 2$$



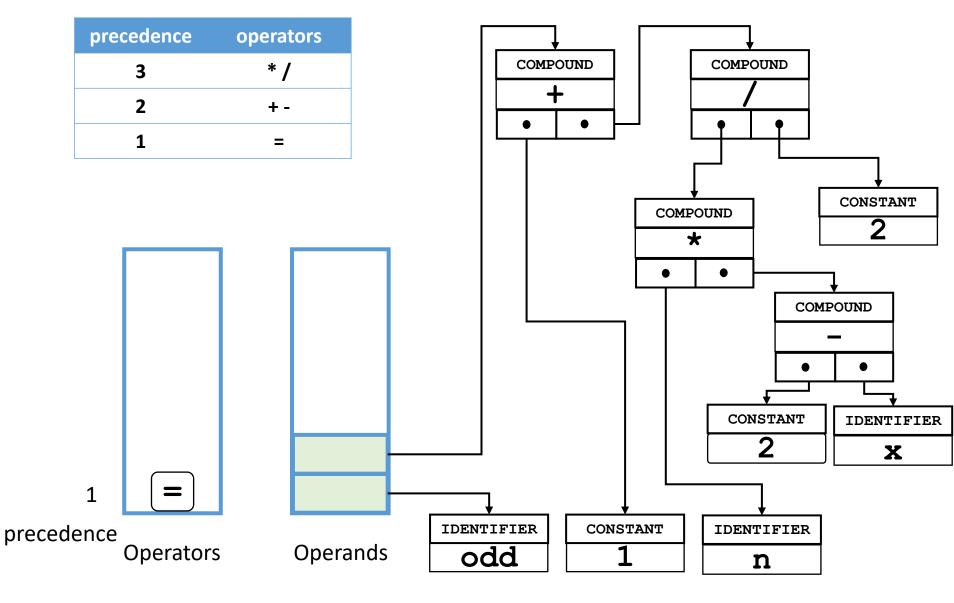
$$Odd = 1 + n * (2 - x) / 2$$



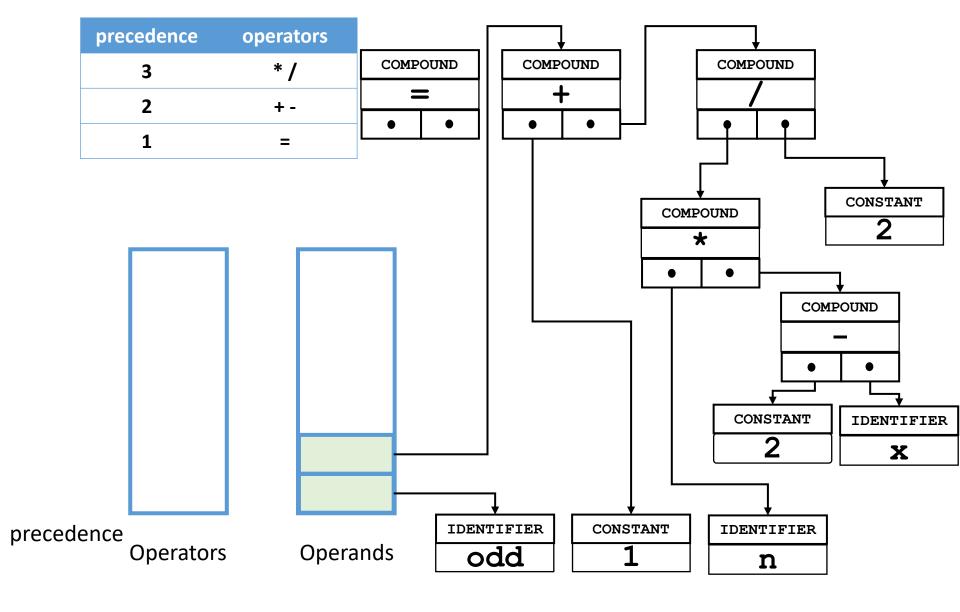
$$Odd = 1 + n * (2 - x) / 2$$



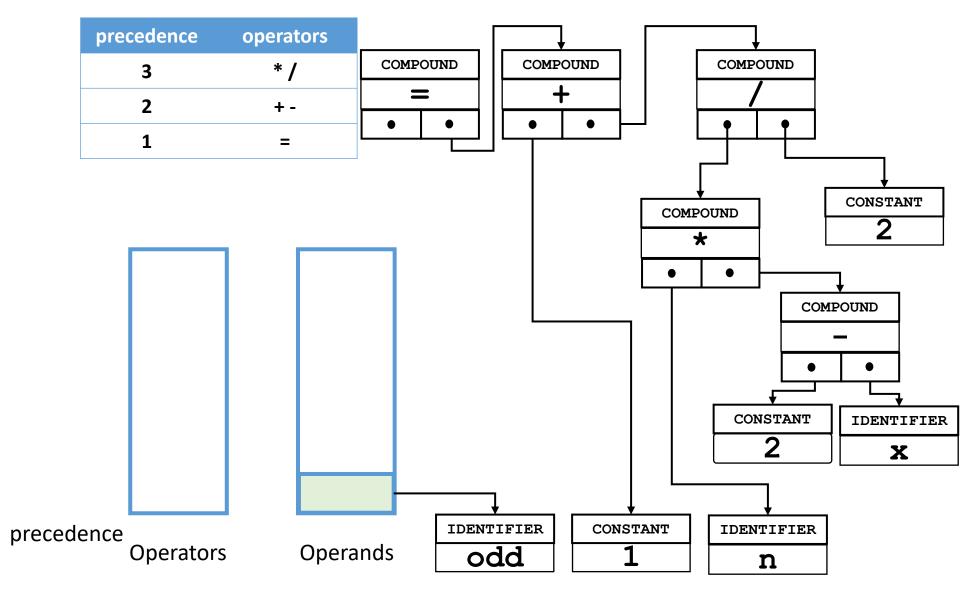
$$Odd = 1 + n * (2 - x) / 2$$



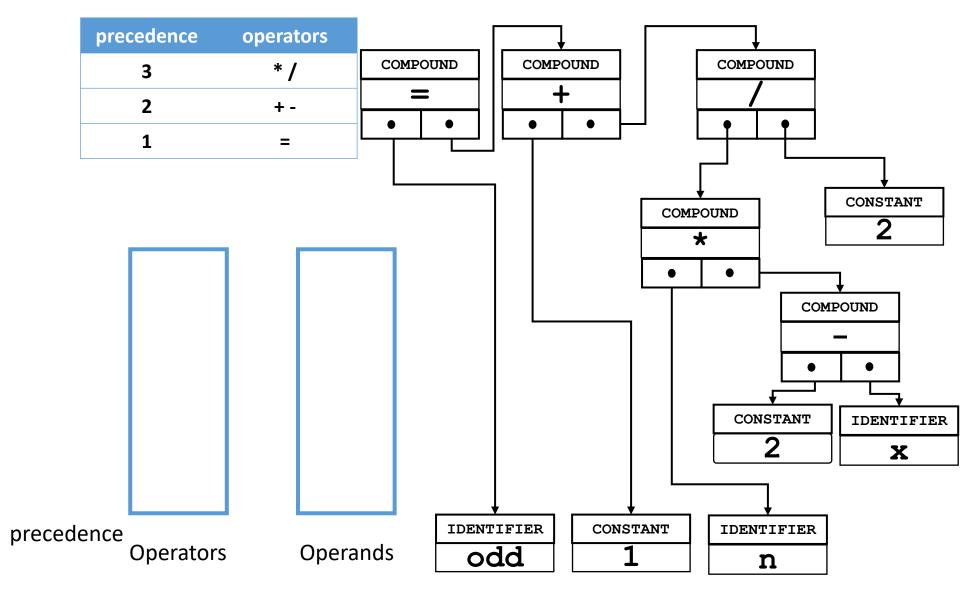
$$Odd = 1 + n * (2 - x) / 2$$



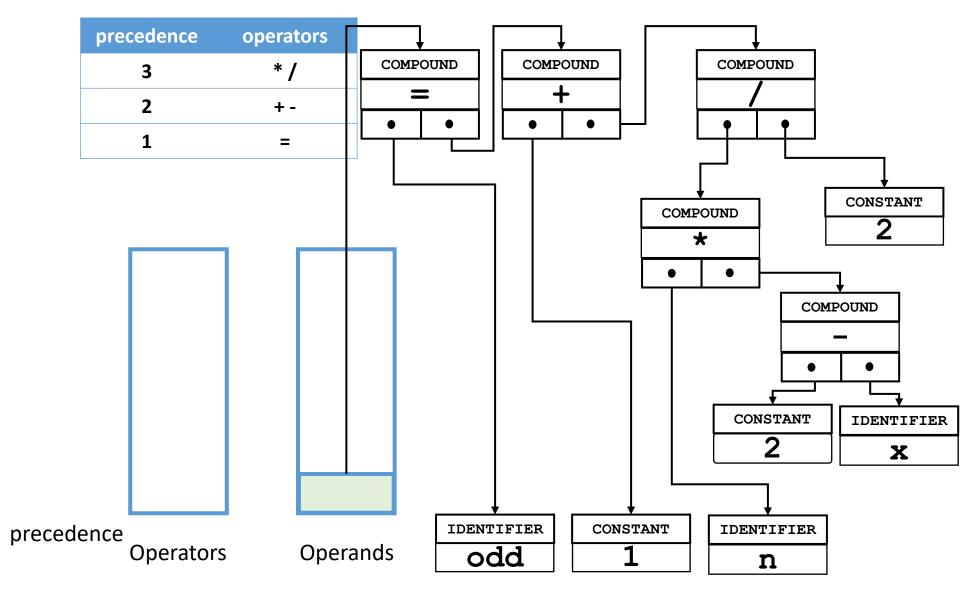
$$Odd = 1 + n * (2 - x) / 2$$



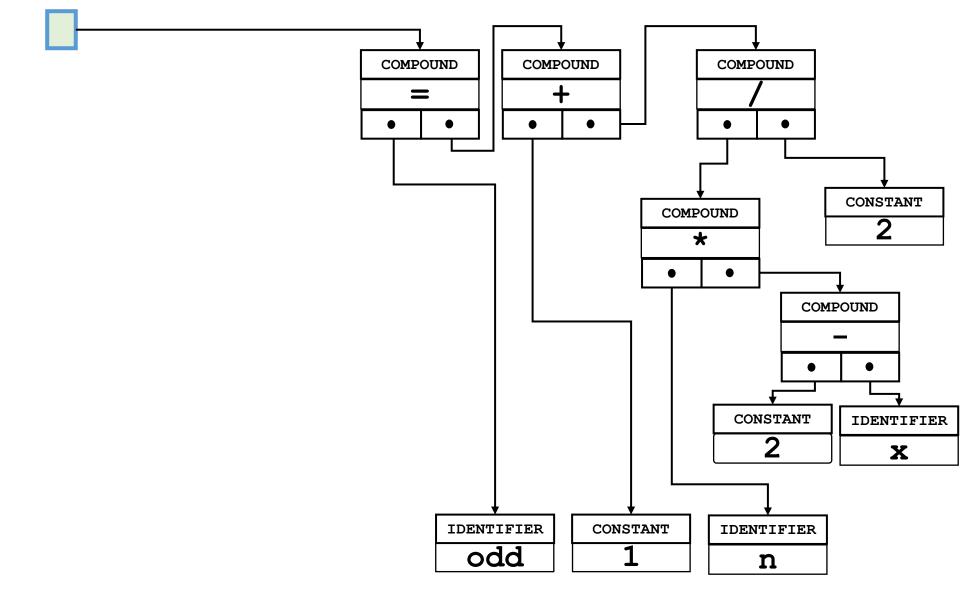
$$Odd = 1 + n * (2 - x) / 2$$



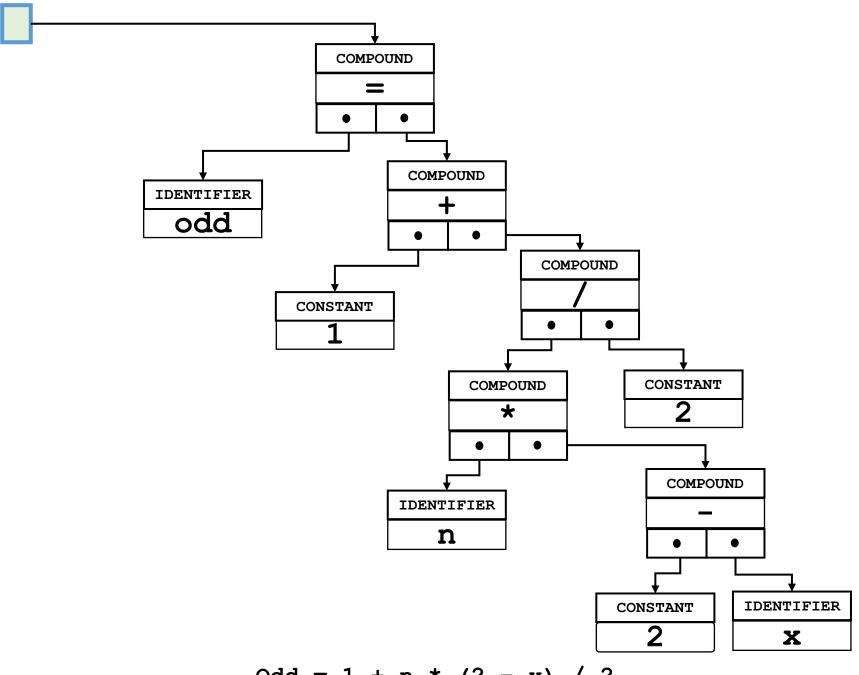
$$Odd = 1 + n * (2 - x) / 2$$



$$Odd = 1 + n * (2 - x) / 2$$



$$Odd = 1 + n * (2 - x) / 2$$



Odd = 1 + n * (2 - x) / 2

```
/*
 * File: exp.h
 * This interface defines a class hierarchy for arithmetic expressions.
 */
#ifndef exp h
#define exp_h
#include <string>
#include "map.h"
#include "tokenscanner.h"
/* Forward reference */
class EvaluationContext;
/*
 * Type: ExpressionType
 * This enumerated type is used to differentiate the three different
 * expression types: CONSTANT, IDENTIFIER, and COMPOUND.
 */
enum ExpressionType { CONSTANT, IDENTIFIER, COMPOUND };
```

```
/*
 * Class: Expression
 * This class is used to represent a node in an expression tree.
 * Expression itself is an abstract class. Every Expression object
 * is therefore created using one of the three concrete subclasses:
 * ConstantExp, IdentifierExp, or CompoundExp.
 */
class Expression {
public:
   Expression();
   virtual ~Expression();
   virtual int eval(EvaluationContext & context) = 0;
   virtual std::string toString() = 0;
   virtual ExpressionType type() = 0;
/* Getter methods for convenience */
   virtual int getConstantValue();
   virtual std::string getIdentifierName();
   virtual std::string getOperator();
   virtual Expression *getLHS();
   virtual Expression *getRHS();
};
```

```
/*
 * Class: ConstantExp
 * This subclass represents a constant integer expression.
 */
class ConstantExp: public Expression {
public:
   ConstantExp(int val);
   virtual int eval(EvaluationContext & context);
   virtual std::string toString();
   virtual ExpressionType type();
   virtual int getConstantValue();
private:
   int value;
};
```

```
/*
 * Class: IdentifierExp
 * This subclass represents a expression corresponding to a variable.
 */
class IdentifierExp: public Expression {
public:
   IdentifierExp(string name);
   virtual int eval(EvaluationContext & context);
   virtual std::string toString();
   virtual ExpressionType type();
   virtual string getIdentifierName();
private:
   std::string name;
};
```

```
/*
 * Class: CompoundExp
 * This subclass represents a compound expression.
 */
class CompoundExp: public Expression {
public:
   CompoundExp(string op, Expression *lhs, Expression *rhs);
   virtual ~CompoundExp();
   virtual int eval(EvaluationContext & context);
   virtual std::string toString();
   virtual ExpressionType type();
   virtual std::string getOperator();
   virtual Expression *getLHS();
   virtual Expression *getRHS();
private:
   std::string op;
   Expression *lhs, *rhs;
};
```

```
/*
 * Class: EvaluationContext
 * This class encapsulates the information that the evaluator needs to
 * know in order to evaluate an expression.
 */
class EvaluationContext {
public:
   void setValue(std::string var, int value);
   int getValue(std::string var);
   bool isDefined(std::string var);
private:
   Map<std::string,int> symbolTable;
};
#endif
```

Selecting Fields from Subtypes

• The Expression class exports several methods that allow clients to select fields from one of the concrete subtypes:

```
virtual int getConstantValue();
virtual std::string getIdentifierName();
virtual std::string getOperator();
virtual Expression *getLHS();
virtual Expression *getRHS();
```

- The implementation of these methods in the Expression class always generates an error. Each subclass overrides that implementation with code that returns the appropriate instance variable.
- These methods exist primarily for the convenience of the client. A more conventional strategy would be to have each subclass export only the getters that apply to that subtype. Adopting this strategy, however, forces clients to include explicit type casting, which quickly gets rather tedious.

Code for the eval Method

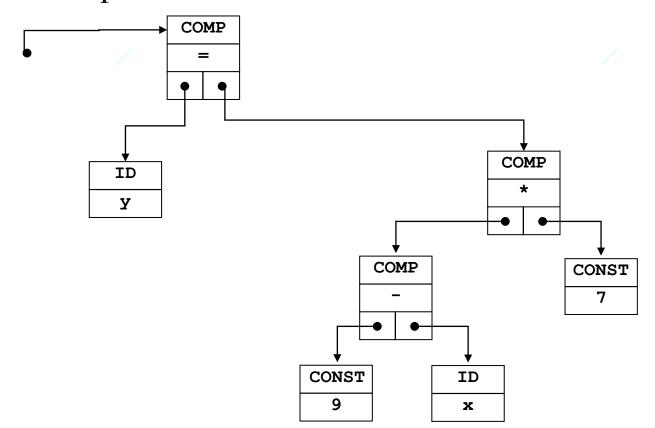
```
int ConstantExp::eval(EvaluationContext & context) {
   return value:
int IdentifierExp::eval(EvaluationContext & context) {
   if (!context.isDefined(name)) error(name + " is undefined");
   return context.getValue(name);
int CompoundExp::eval(EvaluationContext & context) {
   int right = rhs->eval(context);
   if (op == "=") {
      context.setValue(lhs->getIdentifierName(), right);
      return right;
   int left = lhs->eval(context);
   if (op == "+") return left + right;
   if (op == "-") return left - right;
   if (op == "*") return left * right;
   if (op == "/") {
      if (right == 0) error("Division by 0");
      return left / right;
   }
   error("Illegal operator in expression");
   return 0;
```

Exercise: Evaluating an Expression

• Trace through the steps involved in evaluating the expression

$$y = (9 - x) * 7$$

in a context in which **x** has the value 3. The representation of this expression looks like this:



To: BASIC Development Group

From: Bill Gates

Subject: C++ reimplementation

Date: April 1, 1981

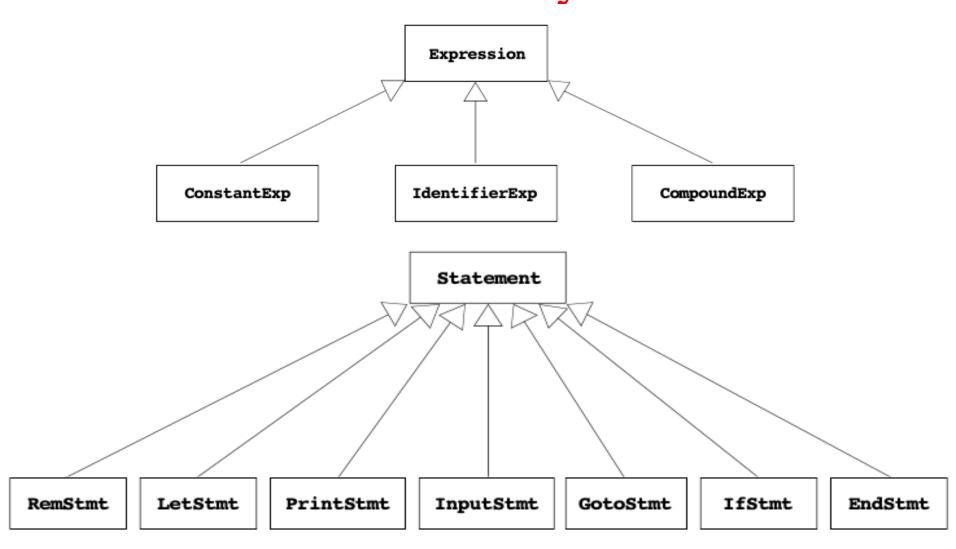
This guy from Bell Labs, Bjarne Stroustroup, just sent me a parser program written in a new language he's calling C++. His parser is much simpler than ours but still seems quite efficient. The code is much easier to read as well.

I think it's time to move away from assembly language for our version of BASIC, and C++ may be just the right tool.

Please get going on this project as soon as possible.

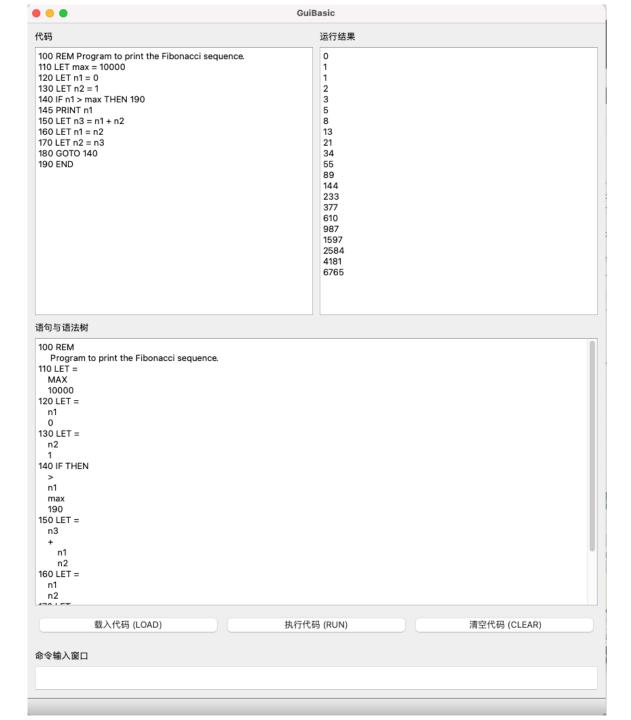
Bill Dates

The Expression/Statement Class Hierarchy

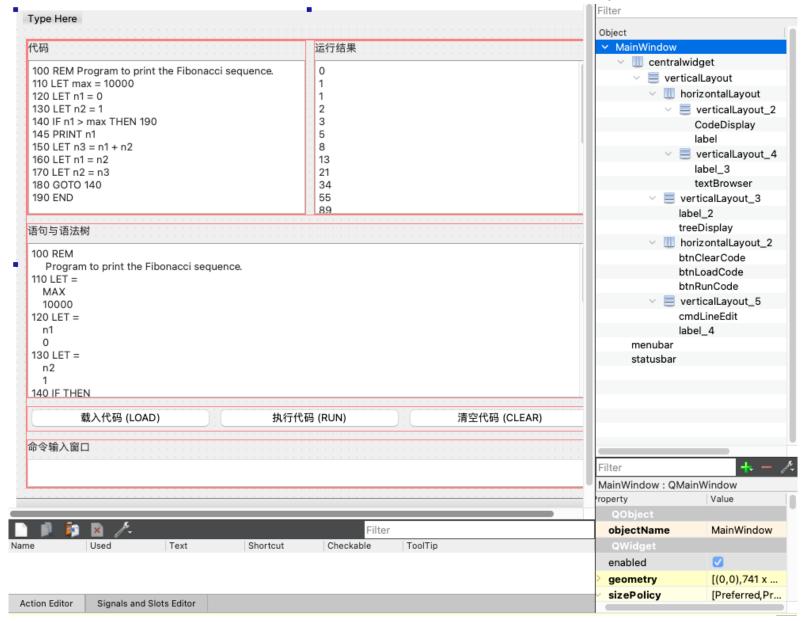


Recommended Files

| main.cpp | Main file of the project |
|---------------------|---|
| mainwindow.h/cpp/ui | Main Window (and UI) |
| program.h/cpp | Declare/implement a stored program |
| statement.h/cpp | Declare/implement statements |
| exp.h/cpp | Declare/implement expressions |
| parser.h/cpp | Parse a given expression |
| tokenizer.h/cpp | Convert strings to a list of tokens |
| evalstate.h/cpp | A space storing all variables during evaluation |



Recommended UI Layout



多□段提交

| □□程序保存、加□、□□、□示等 □□Let、Print等□句 □□Expression 的 parsing 和 evaluate (此□□□□整的程序□构,□表+□法□) □目的其他部分(最□提交) | 1. | 画 GUI 界面,□□交互(如□取用□□入) |
|---|----|--|
| 4. □ □ Expression 的 parsing 和 evaluate (此□□□□ 整的程序□构,□表+□法□) | 2. | □□程序保存、加□、□□、□示等 |
| 整的程序□构,□表+□法□) | 3. | □ Let、Print 等□ 句 |
| | 4. | □ □ Expression 的 parsing 和 evaluate(此□□□有完 |
| 5. □目的其他部分(最□提交) | | 登的程序□构,□表+□法□ |
| | 5. | □目的其他部分(最□提交) |

□ 交/未提交 每次 -2