



Universidade Federal de Pernambuco  
Centro de Informática

# **Automatic Speaker Verification Using Adapted Gaussian Mixture Models**

Final Term Paper

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March 3, 2015



# Declaration

This paper is a presentation of my research work, as partial fulfillment of the requirement for the degree in Computer Engineering. Wherever contributions of others are involved, every effort is made to indicate this clearly, with due reference to the literature, and acknowledgement of collaborative research and discussions.

The work was done under the guidance of Prof. Dr. Tsang Ing Ren, at Centro de Informática, Universidade Federal de Pernambuco, Brazil.

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Eduardo Martins Barros de Albuquerque Tenório

In my capacity as supervisor of the candidate's paper, I certify that the above statements are true to the best of my knowledge.

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Prof. Dr. Tsang Ing Ren

March 3, 2015



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*Live long and prosper*

Vulcan salute





# **Abstract**

TODO escrever o abstract após terminar tudo (após a conclusão).



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# 1. Introduction

The increasing popularity and the intensive use of computational systems in the everyday of modern life create the need for easier and less invasive forms of user recognition. While entering a hard-to-memorize password in a terminal and identifying a person by placing a human finger to listen to telephone calls are the status quo for respectively authentication and identification, voice biometrics presents itself as a continuing improvement alternative. Passwords can be forgotten and people are biased and unable to be massively trained, but the unique characteristics of a person's voice combined with an automatic speaker recognizer outperform any "manual" attempt.

Speech is the most natural way humans have to communicate, being incredibly complex and with numerous specific details related to its producer, *Bimbot et al.* [1]. Therefore, it is expected an increasing use of vocal interfaces to perform actions such as computer login, voice search (e.g., Apple Siri, Google Now and Samsung S Voice) and identification of speakers in a conversation and its content. At present, fingerprint biometrics is adopted in several solutions (e.g., ATMs, *Wang & Wu* [2]), authentication through facial recognition comes as built-in software for average computers and iris scan was adopted for a short time by United Kingdom's and permanently by United Arab Emirates' border controls, *Sasse* [3], *Raisi & Khouri* [4]. These examples indicate a near future where biometrics are common, with people talking to the computer and receiving concise answers, and cash withdrawals allowed via a combination of speaker verification, correctly dictated captcha and other techniques.

Current commercial products based on voice technology (e.g., Dragon NaturallySpeaking, KIVOX and VeriSpeak) are usually intended to perform either **speech recognition** (*what* is being said) or **speaker recognition** (*who* is speaking). Voice search applications are designed to determine the content of a speech, usually with no concern about who the speaker is or if there is more than one, while computer login and telephone fraud prevention supplement a memorized personal identification code with speaker verification, *Reynolds* [5], not interested on the message spoken. Few applications perform both processes, such as automatic speaker labeling of recorded meetings, that transcribes what each person is saying. To achieve this goal, numerous voice processing techniques have become known in industry and academy, such as Natural Language Processing (NLP), Hidden Markov Models (HMMs) and Gaussian Mixture Models (GMMs). Although all of these are interesting state-of-the-art techniques, this paper covers a subarea of speaker recognition and only a small subset will be unraveled.

## 1.1 Speaker Recognition

As stated in *Reynolds & Campbell* [6], speaker recognition may be divided in two subareas. The first is **speaker identification**, aimed to determine the identity of a speaker

from a non-unitary set of known speakers. This task is also named speaker identification in **closed set**. In the second, **speaker verification**, the goal is to determine if a speaker is who he or she claims to be, not an imposter. As the set of imposters is unknown, this is an **open set** problem. An intermediate task is **open set identification**, when an “unmatched class” is added in order to categorize all unknown speakers.

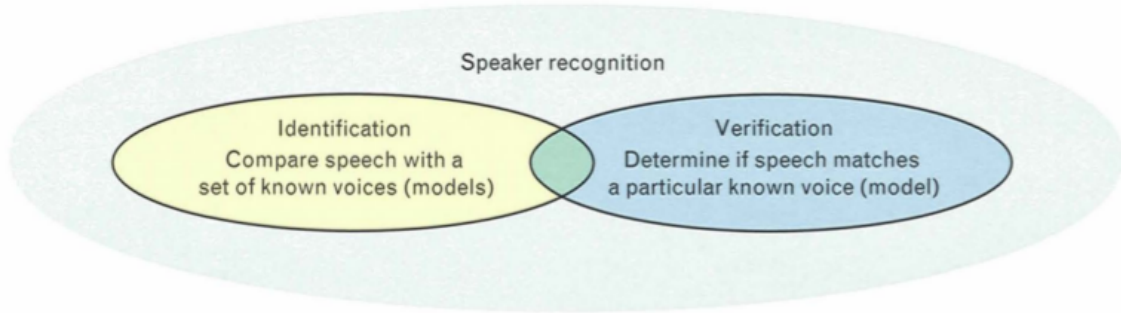


Figure 1.1: Speaker identification and speaker verification are different, but not entirely, *Reynolds* [5].

The text inputted may have constraints, such as type (e.g., digits and letters), number of words used (e.g., one word or sentences) and etc. In **text-dependent** systems the content of the speech is relevant to the evaluation, and the testing texts must belong to the training set, *Hébert* [7]. A change in the training inputs demands a complete new training section. **Text-independent** systems have no restrictions to the message in both sets, with the non-textual characteristics of the user’s voice (e.g., pitch and accent) being the important aspects to the evaluator. These characteristics are present in different sentences, use of foreign languages and even gibberish. Between the extremes in constraints falls the **vocabulary-dependent system**, which restricts the speech to come from a limited vocabulary (e.g., digits such as “two” or “one-two-three”), *Reynolds* [5].

## 1.2 Why Gaussian Mixture Models?

The focus of this paper is on **text-independent speaker verification**, and as independence of the spoken context is a key characteristic of the problem, the most appropriate approach is to consider the training data as a stochastic variable. The best suited distribution to represent random data is the gaussian (or normal), leading to the choice of GMMs to model an Automatic Speaker Verifier (ASV).

The verification system is constructed using an Universal Background Model-Gaussian Mixture Model (UBM-GMM) to represent all speakers as a single background and a GMM (named Speaker-GMM) or an adaptation of the UBM-GMM (named Adapt-GMM-UBM) through Bayesian Adaptation, *Brown, Lee and Spohrer* [8], both described in details in Chapter 4. Finally, a likelihood ratio test is used to evaluate a speech signal and decide if it belongs or not to the claimed speaker (see Chapter 2).

## 1.3 Objectives

This study is aimed to implement an ASV and analyze the following:

- False detection and false rejection rates using a DET curve, *Martin et al.* [9].

- Accuracy for different sizes of mixture and features.
- Comparison between Speaker-GMM and Adapt-GMM-UBM verifications.

### 1.4 Document Structure

Chapter 2 contains basic information about speaker verification systems, as well as its basic architecture. The feature extraction process is explained in Chapter 3, from the reasons for its use to the chosen technique (Mel-Frequency Cepstral Coefficient, MFCC). In Chapter 4 the theories of GMM, UBM-GMM and Adapt-GMM-UBM are presented. Experiments are described in Chapter 5, as well as its results. Finally, Chapter 6 concludes the study. Furthermore, important contents are presented in the appendices. Appendix A shows the results and curves for Speaker-GMM verification and Appendix B for Adapt-GMM-UBM.





## 2. Speaker Verification Systems

The process of speaker verification lies on the field of pattern classification, with the speaker's utterance (a speech signal) as input for a classifier. The usage of this type of system is to determine if a claimed identity is true (user is classified as “enrolled”) or false (user is classified as “imposter”).

Differently from the speaker identification process, where the inputted speech is tested for all enrolled speakers and identified as the one with the highest score, in speaker verification only one speaker (the claimed identity) is tested. In order to perform a better comparison, a test against a model representing the other speakers is executed and the resulted score is compared with the score from the previous test, delivering a more reliable process.

### 2.1 Utterance

An utterance is a piece of speech produced by a speaker. It may be a word, a statement or any vocal sound. The terms *utterance* and *speech signal* sometimes are used interchangeably, but from herenow speech signal will be defined as an utterance recorded, digitalized and ready to be processed. An example is shown in Fig. 2.1.

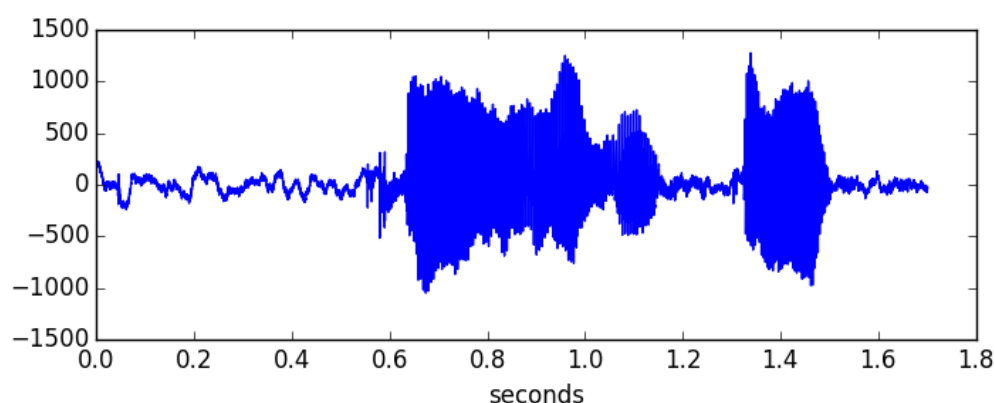


Figure 2.1: Speech signal from utterance “karen livescu”, *Woo, Park & Hazen* [10].

### 2.2 Features

The raw speech signal is unfit for use by an ASV. For a correct processing, the unique features from the speaker's vocal tract are extracted, what reduces the number of variables the system needs to deal with (leading to a simpler implementation) and performs a better evaluation (prevents the curse of dimensionality). Due to the stationary properties of the

speech signal when analyzed in a short period of time, it is divided in overlapping frames of small and predefined length, to avoid “loss of significance”, *Davis & Mermelstein* [11], *Rabiner & Schafer* [12]. This extraction is executed by the MFCC algorithm, explained in details in Chapter 3.

## 2.3 Speaker Verification

If a speaker  $\mathcal{S}$  claims to be a particular user  $\mathcal{S}_i$  from  $\mathcal{S}$  (set of enrolled users), the strength of this claim resides on how similar the features  $\mathbf{X}$ , extracted from a speech signal  $\mathbf{Y}$  spoken by  $\mathcal{S}$ , are to the features from  $\mathcal{S}_i$  “memorized” by the system. Then a simple equation

$$p(\mathbf{X}|\mathcal{S}_i) \begin{cases} \geq \alpha, & \text{accept } \mathcal{S}, \\ < \alpha, & \text{reject } \mathcal{S}, \end{cases} \quad (2.1)$$

should be enough (considering all speakers equally probable). However, a subset of enrolled speakers may have vocal similarities or the features  $\mathbf{X}$  may be common to all enrolled users, leading to a misclassification of an imposter as a registered speaker (a false detection). To reduce the error rate the system must decide not only if a speech signal came from the claimed speaker, but also if it came from a set composed of all other enrolled speakers and compare the likelihoods.

### 2.3.1 Likelihood Ratio Test

Given the vector of features  $\mathbf{X}$ , and assuming it was produced by only one speaker, the detection<sup>1</sup> task can be restated as a basic test between two hypotheses, *Reynolds* [13]:

$H_0$ :  $\mathbf{X}$  is from the claimed speaker  $\mathcal{S}_i$ ;

$H_1$ :  $\mathbf{X}$  is not from the claimed speaker  $\mathcal{S}_i$ .

The optimum test to decide which hypothesis is valid is the **likelihood ratio test** between both likelihoods  $p(\mathbf{X}|H_0)$  and  $p(\mathbf{X}|H_1)$ , *Reynolds, Quatieri & Dunn* [14],

$$\frac{p(\mathbf{X}|H_0)}{p(\mathbf{X}|H_1)} \begin{cases} \geq \theta, & \text{accept } H_0, \\ < \theta, & \text{reject } H_0, \end{cases} \quad (2.2)$$

where the decision threshold for accepting or rejecting  $H_0$  is  $\theta$  (a low  $\theta$  generates a more permissive system, while a high  $\theta$ , a more restrictive). Applying the logarithm, the behavior of the likelihood ratio is maintained and Eq. 2.2 is replaced by the log-likelihood ratio

$$\Lambda(\mathbf{X}) = \log p(\mathbf{X}|H_0) - \log p(\mathbf{X}|H_1). \quad (2.3)$$

### 2.3.2 Training

Once the features are extracted from the speech signal, they are used to train the models  $\lambda_{hyp}$  and  $\lambda_{\overline{hyp}}$  for  $H_0$  and  $H_1$ , respectively. A high-level demonstration of the training of  $\lambda_{hyp}$  (mathematical representation of  $\mathcal{S}_i$ ) is shown in Fig. 2.2:

<sup>1</sup>the terms verification and detection are used interchangeably

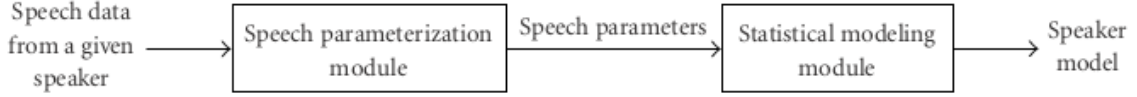


Figure 2.2: The statistical model of  $\mathcal{S}$  is created from the speech signal  $\mathbf{Y}$ , *Bimbot et. al.* [1].

Due to  $\lambda_{hyp}$  be a model of  $\mathcal{S}_i$ , the features used for training (i.e., estimate  $p(\mathbf{X}|\lambda_{hyp})$ ) are extracted from speech signals produced by  $\mathcal{S}_i$ . The model  $\lambda_{\overline{hyp}}$ , however, is not well-defined. It should be composed of the features extracted from speech signals from all other speakers except  $\mathcal{S}_i$ , but creating a single  $\lambda_{\overline{hyp}}$  for each speaker is complicated and with no expressive gain. Instead, what is normally done is use all speakers to generate a background model  $\lambda_{bkg}$ , *Reynolds* [15], in which the weight of each  $\mathcal{S}_i$  is minimized.

### 2.3.3 Test

As seen in Eq. 2.2, the decision process is based on a function *Score*. Replacing each  $H_j$  for its corresponding model, the likelihood of a  $\lambda_j$  given  $\mathbf{X}$  can be written as

$$p(\mathbf{X}|\lambda_j) = \prod_{t=1}^T p(\mathbf{x}_t|\lambda_j). \quad (2.4)$$

Using the logarithm function, Eq. 2.4 becomes

$$\log p(\mathbf{X}|\lambda_j) = \frac{1}{T} \sum_{t=1}^T \log p(\mathbf{x}_t|\lambda_j), \quad (2.5)$$

where the term  $\frac{1}{T}$  is used to normalize the log-likelihood to the duration of the speech signal. That said, the likelihood ratio given by Eq. 2.3 becomes

$$\Lambda(\mathbf{X}) = \log p(\mathbf{X}|\lambda_{hyp}) - \log p(\mathbf{X}|\lambda_{bkg}), \quad (2.6)$$

and the speaker is accepted if  $\Lambda(\mathbf{X}) \geq \log \theta$ , for an arbitrary value of  $\theta$ .



### 3. Feature Extraction

As an acoustic wave propagated through space over time, the speech signal is not appropriate to be evaluated by an ASV. In order to deliver decent outcomes, a good parametric representation must be provided. This task is performed by the feature extraction process, which transforms a speech signal into a sequence of characterized measurements, i.e. features. The selected representation compress the speech data by eliminating information not pertinent to the phonetic analysis and enhancing those aspects of the signal that contribute significantly to the detection of phonetic differences, *Davis & Mermelstein* [11]. According to *Wolf* [16], the ideal features should:

- occur naturally and frequently in normal speech;
- be easily measurable;
- vary highly among speakers and be very consistent for each speaker;
- not change over time nor be affected by the speaker's health;
- be robust to reasonable background noise and to transmission characteristics;
- be difficult to be artificially produced;
- not be easily modifiable by the speaker.

Features may be categorized based on vocal tract or behavioral aspects, divided in (1) short-time spectral, (2) spectro-temporal, (3) prosodic and (4) high level, *Pinheiro* [17]. Short-time spectral features are usually calculated using millisecond length windows and describe the voice spectral envelope, composed of supralaryngeal properties of the vocal tract, e.g. timbre. Spectro-temporal and prosodic occur over time (e.g., rhythm and intonation), and high level features occur during the conversation (e.g., accent).

The parametric representations evaluated in *Davis & Mermelstein* [11] may be divided into those based on the Fourier spectrum, such as Mel-Frequency Cepstrum Coefficients (MFCC) and Linear Frequency Cepstrum Coefficients (LFCC), and those based on the Linear Prediction Spectrum, such as Linear Prediction Coefficients (LPC), Reflection Coefficients (RC) and Linear Prediction Cepstrum Coefficients (LPCC). The better evaluated representation was the MFCC, with minimum and maximum accuracy of 90.2% and 99.4%, respectively, leading to its choice as the parametric representation in this work.

#### 3.1 Mel-Frequency Cepstral Coefficient

MFCC is a highly used parametric representation in the area of voice processing, due to its similarity with the way the human ear operates. Despite the fact the ear is divided in three sections, i.e. outer, middle and inner ears, only the last is mimicked. The mechanical pressure waves produced by the triad hammer-anvil-stirrup are received by the cochlea

(Fig. 3.1), a spiral-shaped cavity with a set of inner hair cells attached to a membrane (the basilar membrane) and filled with a liquid. This structure converts motion to neural activity through a non-uniform spectral analysis, *Rabiner & Schafer* [12], and passes it to the pattern recognizer in the brain.



Figure 3.1: Cochlea divided by frequency regions, *ScienceBlogs* [18].

A key factor in the perception of speech and other sounds is **loudness**, a quality related to the physical property of the sound pressure level. Loudness is quantified by relating the actual sound pressure level of a pure tone (in dB relative to a standard reference level) to the perceived loudness of the same tone (in a unit called phons) over the range of human hearing (20 Hz–20 kHz), *Rabiner & Schafer* [12]. As shown in Fig. 3.2, a 100 Hz tone at 60 dB is equal in loudness to a 1000 Hz tone at 50 dB, both having the **loudness level** of 50 phons (by convention).

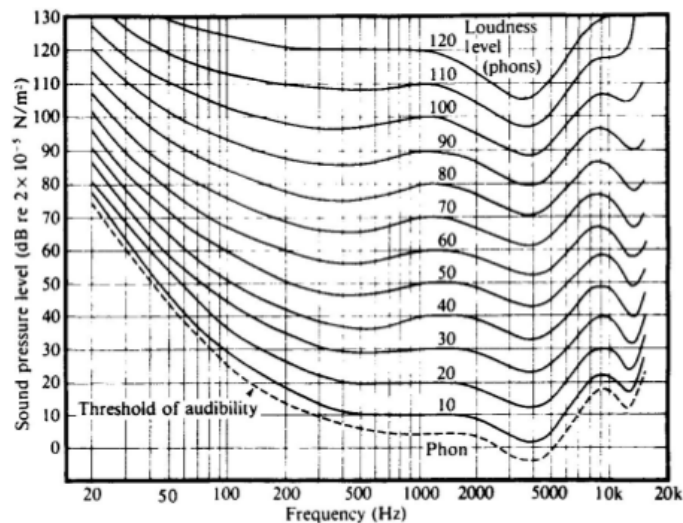


Figure 3.2: Loudness level for human hearing, *Fletcher & Munson* [19].

#### 3.1.1 The Mel Scale

The mel scale is the result of an experiment conducted by *Stevens, Volkman and Newman* [20] intended to measure the perception of a pitch and construct a scale based on it. Each observer was asked to listen to two tones, one in the fixed frequencies 125, 200, 300, 400, 700, 1000, 2000, 5000, 8000 and 12000 Hz, and the other free to have its frequency varied by the observer for each fixed frequency of the first tone. An interval of 2 seconds separated both tones. The observers were instructed to say in which frequency the second tone was “half the loudness” of the first. A geometric mean was taken from the observers’ answers and a measure of 1000 mels was assigned to the frequency of 1000 Hz, 500 mels to the frequency sounding half as high (as determined by Fig. 1 in *Stevens et. al.* [20]) and so on.

Decades after the scale be defined, *O’Shaughnessy* [21] presented an equation to convert frequencies in Hertz to frequencies in mels.

$$f_{mel} = 2595 \log_{10} \left( 1 + \frac{f}{700} \right) \quad (3.1)$$

Being logarithmic, the growth of a mel-frequency curve is slow when Eq. 3.1 is applied to a linear growth of the frequency in Hertz. Sometimes the mel conversion is used only for frequencies higher than 1000 Hz, while in lower,  $f_{mel}$  and  $f_{Hz}$  share the same value. In this work all conversions will use Eq. 3.1, as shown by Fig. 3.3.

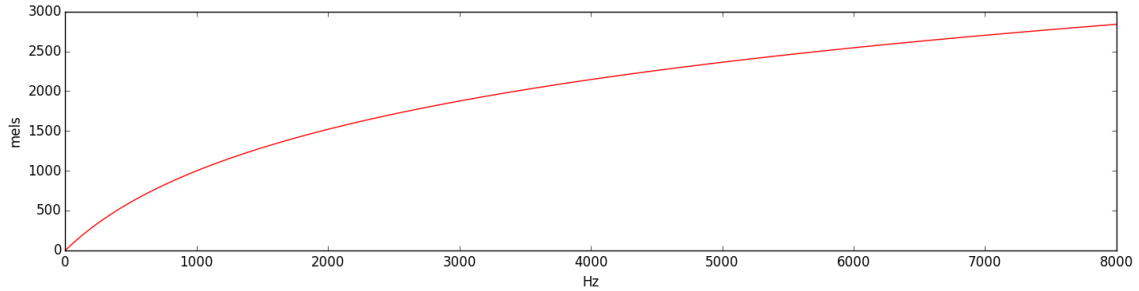


Figure 3.3: The logarithm curve of the mel scale.

#### 3.1.2 Extraction Process

In an ASV the feature extraction module receives a raw speech signal and returns a vector of cepstral features in mel scale (see Fig. 3.4). The number of features in each frame is defined at the moment of extraction (e.g., 6, 13 or 19), but the user has the option to append time variations of the MFCCs (i.e., delta coefficients) in order to improve the representation.

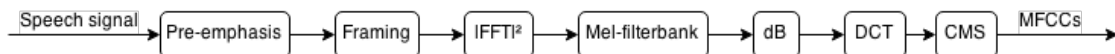


Figure 3.4: Modular representation of the MFCC extraction.

As the human voice is concentrated in the lower frequencies (see Fig. 3.5), the higher ones are enhanced to improve the classification. A first order Finite Impulse Response (FIR) filter is used

$$s_{emph}[n] = s[n] - a \cdot s[n - 1], \quad (3.2)$$

with values of  $a$  usually in the interval  $[0.95, 0.98]$ , *Bimbot et. al.* [1]. This is an optional stage of the MFCC extraction process.

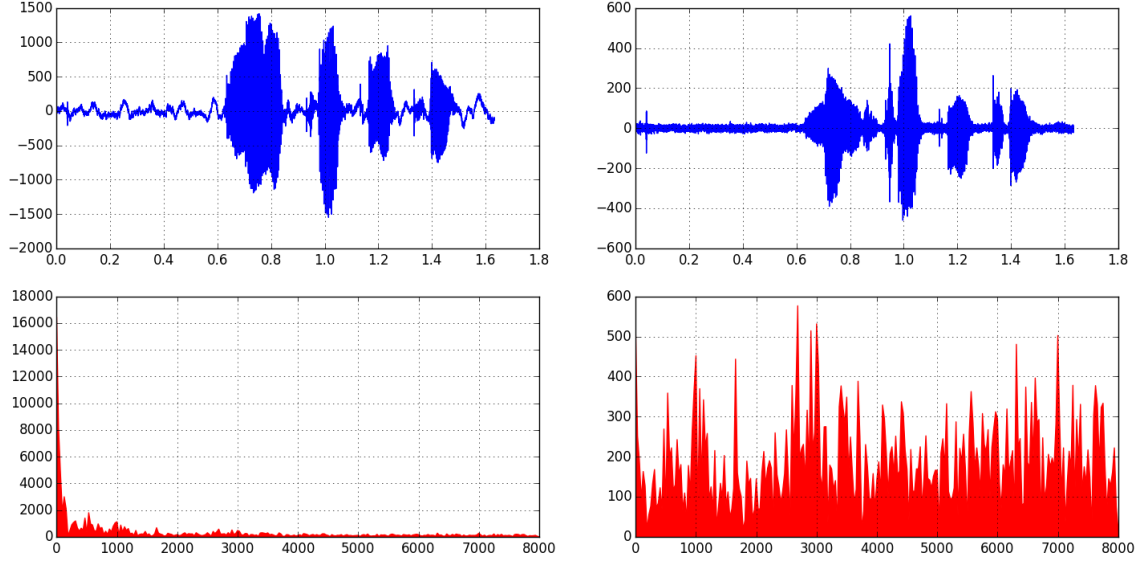


Figure 3.5: Raw (left) and pre-emphasized (right) speech signal, with respective spectral magnitudes (at bottom in red).

The first mandatory stage of the feature process is the division of the input signal in overlapping frames, by the application of a sliding window (commonly Hamming, to taper the signal on the ends and reduce the side effects, *Bimbot et. al.* [1]). The window has a width in the order of milliseconds (to perform a short-time analysis) and a shift that must be shorter than the width, or the frames will not be overlapped. Usual values for the window's width are between 20 and 40, and for the shift, 10.



Figure 3.6: 51° and 52° frames. Notice the initial and final samples of each figure.



### 3. FEATURE EXTRACTION

For each frame the Fast Fourier Transform (FFT) is calculated, with number of points greater than the width of the window (usually 512). Finally, the modulus of the FFT is calculated and the power spectrum is obtained. Due to its symmetry, only half of the points are kept.

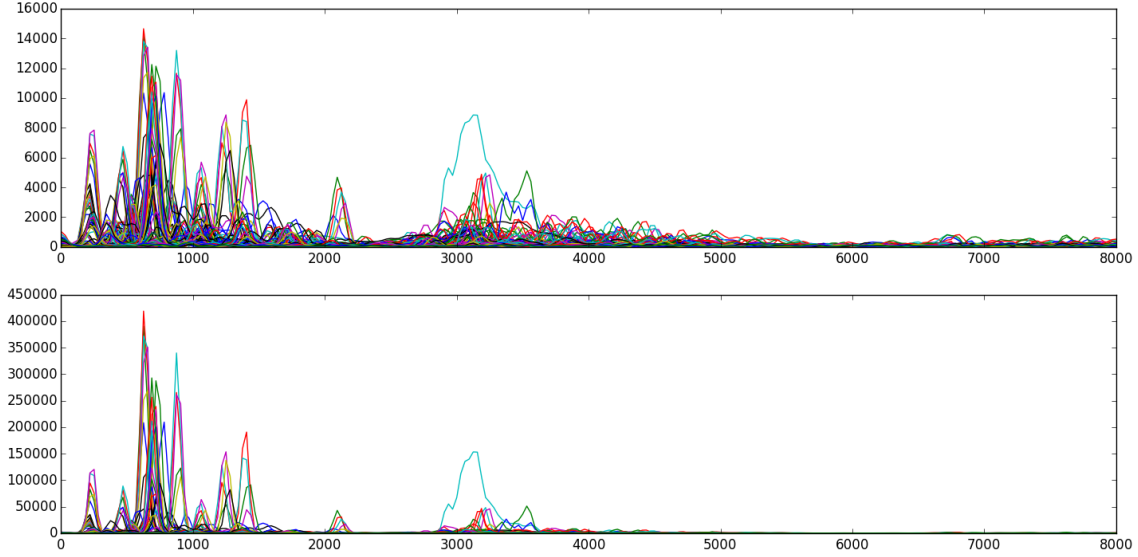


Figure 3.7:  $|FFT|$  (top) and  $|FFT|^2$  (bottom)

To get the envelope (and to reduce the size of spectral coefficients), the spectrum is multiplied by a filterbank in the mel scale. As seen in Fig. 3.8, the width of the filters enlarge when the frequency increases (these frequencies bands have the same width in mels). This is an approximation of the filtering process executed by the cochlea (see Fig. 3.1), and is done this way due to the higher accuracy of human hearing in lower frequencies than in higher ones. The result of the filtering is the energy in each sample of the frame (see Fig. 3.9 (left)).

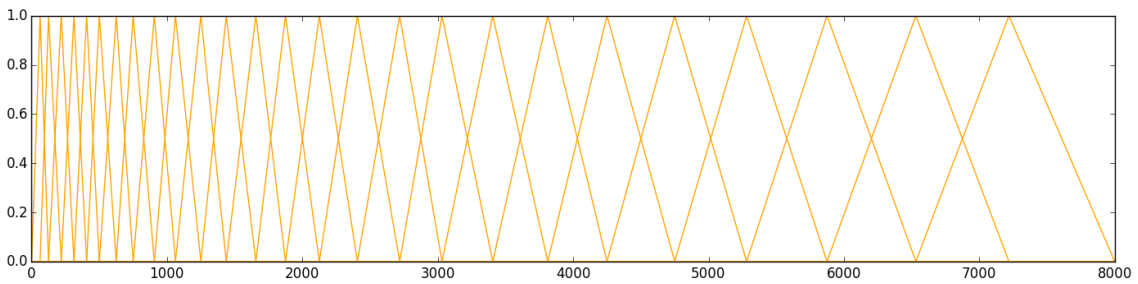


Figure 3.8: Filter bank with 22 filters.

The spectral coefficients are then converted to dB by the application of the function  $20 \log(\cdot)$  to each sample of each frame, reducing the differences between energy values.

Until now the features are in the mel scale, but are not yet “cepstral”. The last necessary stage is to apply a Discrete Cosine Transform (DCT) to the spectral coefficients in order to yield the cepstral coefficients:

$$c_n = \sum_{k=1}^K S_k \cdot \cos \left[ n \left( k - \frac{1}{2} \right) \frac{\pi}{K} \right], \quad n = 1, 2, \dots, L, \quad (3.3)$$

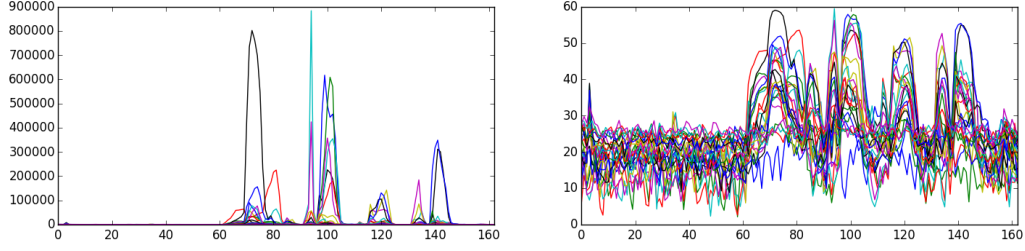


Figure 3.9: Spectral coefficients after the filterbank (left) and after the log conversion (right).

where  $K$  is the number of spectral coefficients,  $S_k$  is a spectral coefficient, and  $L$  is the number of cepstral coefficients to calculate ( $L \leq K$ ). The application of a lifter (a cepstral filter) is usual after the computation of the DCT, to smooth the coefficients. After this stage, the MFCCs are extracted.

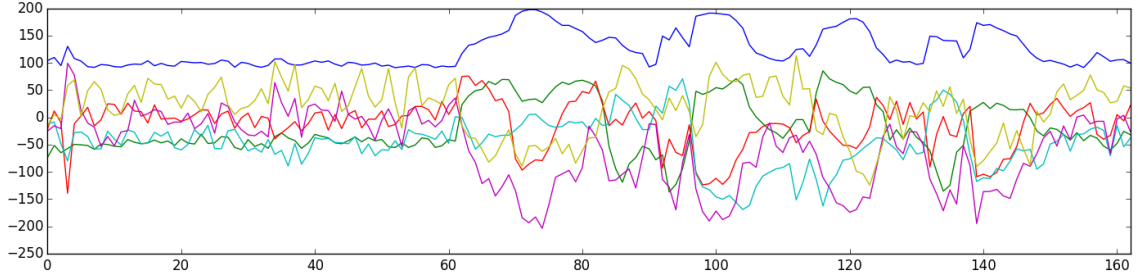


Figure 3.10: 6 MFCCs for each frame.

In Fig. 3.10, the blue line represents the first feature, and as it is obvious, its values over time are much higher than the values of the others. To correct this discrepancy, the feature is changed by the summed energy of each frame, bringing it closer to the others (see Fig. 3.11).

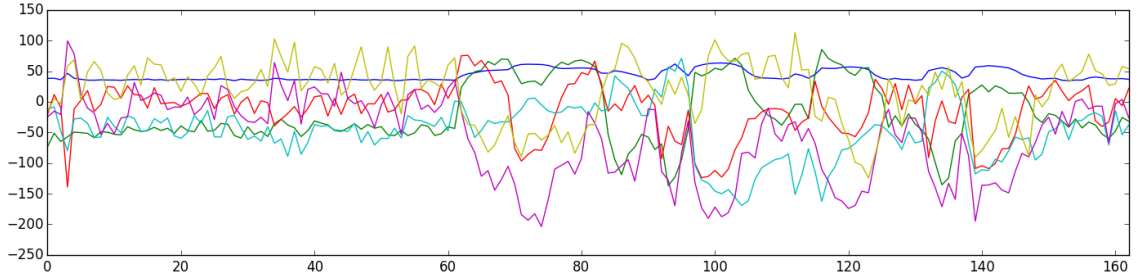


Figure 3.11: First feature changed by the summed energy of each frame.

Even an utterance recorded in a quiet environment still suffers with the side effects of any noise captured during the recording, what may degrade the performance. For speeches recorded in regular places (e.g., a living room or a park), the environment robustness is a need. Cepstral Means Subtraction,

$$c_n = c_n - \frac{1}{T} \sum_{t=1}^T c_{n,t}, \quad (3.4)$$

reduces the disturbing channel effect before the ASV be trained, delivering a cleaner signal to the models, *Westphal* [22].

### 3. FEATURE EXTRACTION

In order to improve the speech parameters, the differences in time of each coefficient may be added as new features. In a vector with 6 features per frame, the velocity and acceleration of each coefficient may be added, providing 12 more features to the parametrization, all of them related to the ones previously extracted. These new features are the **deltas** of the MFCCs, given by

$$d_t = \frac{\sum_{n=1}^N n(c_{t+n} - c_{t-n})}{2 \sum_{n=1}^N n^2}. \quad (3.5)$$

where  $N$  (by default 2) determines how far from the frame  $t$  the calculation is taken. Fig. 3.13 shows the MFCCs from Fig. 3.12 improved by the addition of deltas of first and second orders.

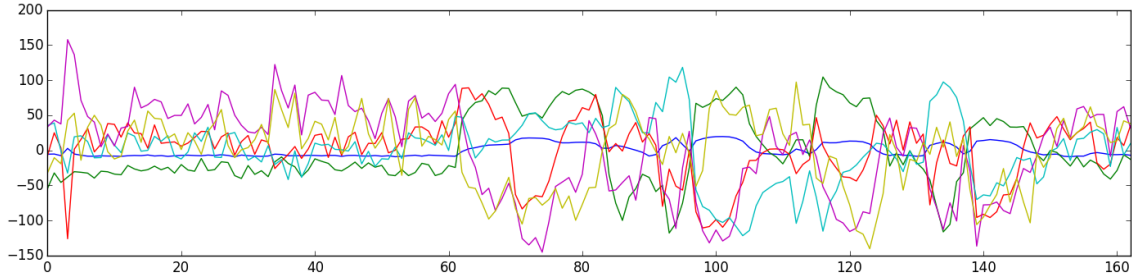


Figure 3.12: CMS applied to the MFCCs from Fig. 3.11.

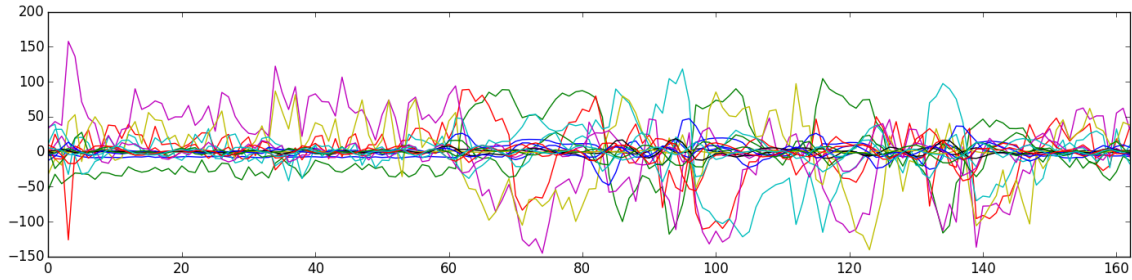


Figure 3.13: MFCCs from Fig. 3.12 with deltas of order 1 and 2 added.

Eq. 3.5 may be used to calculate deltas of any order, just as the acceleration (second order) is derived from the velocity (first order). However, as seen in Fig. 3.13, each order of delta delivers lower coefficients, providing a more marginal gain with the increase in order.



## 4. Gaussian Mixture Models

Chapter 2 briefly discussed the use of models  $\lambda_{hyp}$  and  $\lambda_{bkg}$  for a claimed speaker and for a background composed of all enrolled speakers, respectively, to perform a verification process. As the features from the speech signal (see Chapter 3) have unknown values until the moment of extraction, it is reasonable to model the ASV to accept random values.

For all sorts of probability distributions, the gaussian (or normal) is the one that best describes the behavior of a random variable of unknown distribution, due to the central limit theorem. Its equation for a  $D$ -dimensional space is

$$p(\mathbf{x}) = p(\mathbf{x}, \boldsymbol{\mu}, \boldsymbol{\Sigma}) = \frac{1}{(2\pi)^{D/2} |\boldsymbol{\Sigma}|^{1/2}} e^{-\frac{1}{2}(\mathbf{x}-\boldsymbol{\mu})' \boldsymbol{\Sigma}^{-1} (\mathbf{x}-\boldsymbol{\mu})}, \quad (4.1)$$

where  $\mathbf{x}$  is a  $D$ -dimensional input vector,  $\boldsymbol{\mu}$  the  $D$ -dimensional vector of means,  $\boldsymbol{\Sigma}$  the  $D \times D$  matrix of covariances,  $|\boldsymbol{\Sigma}|$  the determinant of  $\boldsymbol{\Sigma}$ , and  $(\mathbf{x} - \boldsymbol{\mu})'$  the transposed of the column-matrix  $(\mathbf{x} - \boldsymbol{\mu})$ .

### 4.1 Definition

A weighted sum of  $p(\mathbf{x})$ 's is used to model the speaker verification system, trying to estimate the composition that best represents the training data. This weighted sum is named Gaussian Mixture Model (GMM), first used for speaker recognition in *Reynolds* [23], and is given by

$$p(\mathbf{x}|\lambda) = \sum_{i=1}^M w_i p_i(\mathbf{x}), \quad (4.2)$$

where  $M$  is the size of the distribution used,  $\sum_{i=1}^M w_i = 1$ , and  $\lambda = \{w_i, \boldsymbol{\mu}_i, \boldsymbol{\Sigma}_i\}$  is the model representation, for  $i = 1, \dots, M$ . Applying Eq. 4.1 to Eq. 4.2, the likelihood for the GMM is

$$p(\mathbf{x}|\lambda) = \sum_{i=1}^M w_i \frac{1}{(2\pi)^{D/2} |\boldsymbol{\Sigma}_i|^{1/2}} e^{-\frac{1}{2}(\mathbf{x}-\boldsymbol{\mu}_i)' \boldsymbol{\Sigma}_i^{-1} (\mathbf{x}-\boldsymbol{\mu}_i)}. \quad (4.3)$$

The idea behind use a GMM as a model for a speaker  $\mathcal{S}$  is to achieve a  $\lambda$  that maximizes the likelihood when applied to features  $\mathbf{X}$  extracted from a speech signal produced by  $\mathcal{S}$ . This value is found by a Maximum Likelihood Estimation (MLE) algorithm. For a sequence of  $T$  training vectors  $\mathbf{X} = \{\mathbf{x}_1, \dots, \mathbf{x}_T\}$ , the GMM likelihood can be written as

$$p(\mathbf{x}|\lambda) = \prod_{t=1}^T P(\mathbf{x}_t|\lambda). \quad (4.4)$$

Unfortunately, this expression is a nonlinear function of the parameters  $\lambda$  and direct maximization is not possible, *Reynolds* [24], leading to estimate  $p(\mathbf{x}|\lambda)$  iteratively using the Expectation-Maximization (EM) algorithm.

## 4.2 Expectation-Maximization

The idea of the EM algorithm is to estimate a new model  $\lambda^{(j+1)}$  from a previous model  $\lambda^{(j)}$ , such that  $p(\mathbf{x}|\lambda^{(j+1)}) \geq p(\mathbf{x}|\lambda^{(j)})$ , approximating the GMM to the training data at each iteration, until some convergence threshold is reached. The algorithm is composed of 2 steps, an expectation of the *a posteriori* probabilities for each distribution  $i$ , and a maximization step, when the parameters  $w_i$ ,  $\mu_i$  and  $\Sigma_i$  are updated. The following description of the steps uses a  $\lambda$  with diagonal<sup>1</sup>  $\Sigma_i$  (i.e., change the  $D \times D$  matrix  $\Sigma_i$  for a  $D$ -dimensional vector  $\sigma_i$  of variances).

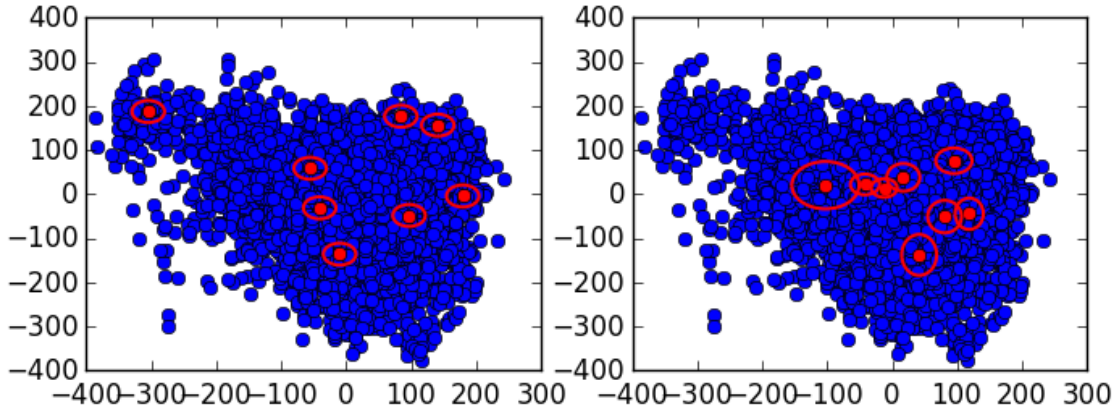


Figure 4.1: Features before (left), with random means and equal variances, and after (right) the EM algorithm. Only the first deviation is shown.

### E-Step

The expectation step consists of estimate the *a posteriori* probabilities for each distribution  $i$  and each feature vector  $\mathbf{x}_t$ ,

$$P(i|\mathbf{x}_t, \lambda) = \frac{w_i p_i(\mathbf{x}_t)}{\sum_{k=1}^M w_k p_k(\mathbf{x}_t)}. \quad (4.5)$$

### M-Step

In the maximization step the model is updated by recalculation of the parameters  $w_i$ ,  $\mu_i$  and  $\Sigma_i$ , and the algorithm guarantees that each new  $\lambda^{(j+1)}$  represents the training data better than the previous ones. From *Reynolds* [24], the updates of  $w_i$ ,  $\mu_i$  and  $\Sigma_i$  are given by the equations below.

<sup>1</sup>As stated in *Reynolds et. al.* [14], diagonal covariance matrix GMMs outperform and are more computationally efficient than full covariance matrix GMMs. Also, the density modeling of an  $M$ th order full covariance matrix GMM can equally well be achieved using a larger order diagonal covariance.

**Weights:**

$$\bar{w}_i = \frac{1}{T} \sum_{t=1}^T P(i|\mathbf{x}_t, \lambda), \quad (4.6)$$

**Means:**

$$\bar{\mu}_i = \frac{1}{T} \frac{\sum_{t=1}^T P(i|\mathbf{x}_t, \lambda) \mathbf{x}_t}{\sum_{t=1}^T P(i|\mathbf{x}_t, \lambda)}, \quad (4.7)$$

**Variances:**

$$\bar{\sigma}_i = \frac{1}{T} \frac{\sum_{t=1}^T P(i|\mathbf{x}_t, \lambda) \mathbf{x}_t^2}{\sum_{t=1}^T P(i|\mathbf{x}_t, \lambda)} - \bar{\mu}_i^2. \quad (4.8)$$

This algorithm trains the GMMs used in the ASV shown in Section 2.3 and previously described in Section 4.1. Fig. 4.1 shows the mixture before and after the training.

### 4.3 Universal Background Model

An Universal Background Model-Gaussian Mixture Model (UBM-GMM), shortened to UBM, is a GMM composed of features from all enrolled speakers. The idea is to generate a model where common characteristics presented in the corpus are well represented. This done, a speech composed of parts of speeches from enrolled speakers is more difficultly misclassified.

There are many configurations for an UBM, but, as it is possible to see in *Reynolds et al.* [14], male and female speakers present distinct vocal traits and are better represented when trained separately (also, female voices are more similar to each other than males, leading to more distinct male configurations). The  $M$ th order UBM is created merging trained male and female models, both of order  $M/2$  (see Fig. 4.2).

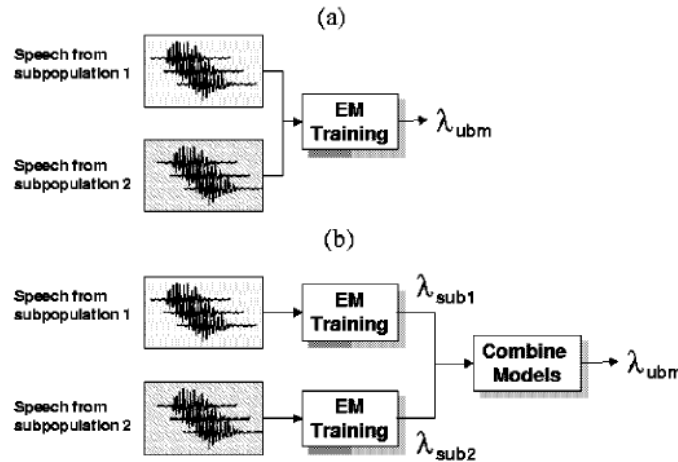


Figure 4.2: UBM with gender trained (a) together and (b) separately and combined. *Reynolds et al.* [14]

## 4.4 Adapted Gaussian Mixture Model

TODO colocar algo aqui

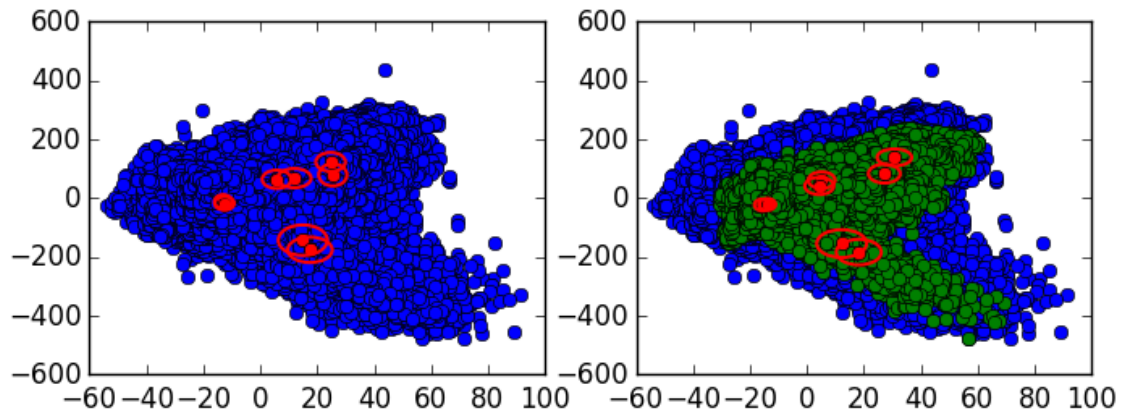


Figure 4.3: UBM trained (left) and weights, means and variances adapted for a female speaker (right). The blue dots are the background features and the green the speaker's.



## 5. Experiments

The ASR was implemented in its entirety using the programming language Python (version 3.4) and the frameworks NumPy (version 1.8.1) and SciPy (version 0.14.0), meaning the feature extraction, the GMM and UBM models, and the identification and verification classifiers. All codes and data are stored in the public repository <https://github.com/embatbr/tg>, as well as this document and secondary resources.

The database used for this work is the **MIT Mobile Device Speaker Verification Corpus (MIT-MDSCV)**, Woo *et. al.* [10]. Two different sets of models were trained. The first was a single speaker GMM for each enrolled speaker, using the utterances relative to the speaker presented in the dataset *enroll\_1*. The trainings took 2-12 seconds each, by the EM algorithm. The second set was of UBMs, also using the utterances from the dataset *enroll\_1*. Two types of UBMs were created: an unisex and a divided by gender, both described in Section 4.3 from chapter Chapter 4. The unisex UBM took 3-6 minutes of training, while the divided by gender took 7-10 minutes. Both sets of models were created and trained for 32, 64 and 128 distributions, 6, 13 and 19 cepstral coefficients and 0, 1 and 2 orders of delta.

Three experiments were conducted: identification, verification using unisex trained UBMs and verification using gender trained UBMs.

### 5.1 Identification

The identification is performed by the application of Eq. ?? to vectors of features  $\mathbf{X}$  extracted from speech signals in *enroll\_2* and models  $\lambda_j$  stored in the directory *bases/gmms*. The set of enrolled speakers is composed of all 26 males and 22 females. Each speaker in *enroll\_2* has 54 recorded utterances, with all tested and the percentage of correct identification calculated. TABELA ERRADA!

Model Order	#Coeffs.	#Deltas		
		0	1	2
$M = 32$	6	29.55	40.28	51.74
	13	57.68	69.60	74.77
	19	71.76	81.52	84.53
$M = 64$	6	29.55	40.28	51.74
	13	57.68	69.60	74.77
	19	71.76	81.52	84.53
$M = 128$	6	29.55	40.28	51.74
	13	57.68	69.60	74.77
	19	71.76	81.52	84.53

Table 5.1: Average correct identification of speakers.

The values shown in Table 5.1 are the mean of the success rates for every speaker in the given configuration.

## **5.2 Verification**

### **5.2.1 Unisex**

### **5.2.2 Gender**

## **6. Conclusion**

TODO escrever a conclusão após terminar tudo (antes do abstract)



## **A. Results for Speaker-GMM**

Appendix with results for the traditional verification technique



## **B. Results for Adapt-GMM-UBM**

Appendix with results for the technique Adapt-GMM-UBM





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