$$L$$
 D
 f
 S

$$\frac{L}{f} = \frac{l}{s} \Rightarrow s = \frac{l}{L}$$

$$L$$
 = side of area to acquire

l = side of sensor

d = lens effective diametre

D = lens-object distance

f = lens focal length

$$\frac{f}{d} = \# = \text{lens aperture}$$

$$\frac{l}{L} = \text{de-magnification}$$

$$\frac{L}{D} = \frac{l}{(f+s)} = \frac{l}{(f+\frac{l}{L}f)} \Rightarrow \text{ the distance needed to acquire } L \text{ an area with a side } L \text{ is } D = (\frac{L}{l}+1) f$$

The fraction of photons that are collected is

$$\epsilon = \frac{\pi (d/2)^2}{4\pi D^2} = \frac{d^2}{[4f((L/l)+1)]^2} = \frac{1}{[4\#((L/l)+1)]^2}$$