### Unit 3 Lecture 4: Lasso regression

#### October 19, 2021

In this R demo, we will learn about the glmnet and glmnetUtils packages and how to run a cross-validated lasso and elastic net regressions using the cv.glmnet() and cva.glmnet() functions, respectively.

Let's load the  ${\tt glmnetUtils}$  package:

```
library(glmnetUtils)
```

Let's also source a file called plot\_glmnet with some helper functions.

```
source("../../functions/plot_glmnet.R")
```

We will apply lasso regression to study the effect of 97 socioeconomic factors on violent crimes per capita based on data from 90 communities in Florida:

```
crime_data = read_csv("../../data/CrimeData_FL.csv")
crime_data
```

```
## # A tibble: 90 x 98
##
      population household.size race.pctblack race.pctwhite race.pctasian
##
           <dbl>
                           <dbl>
                                         <dbl>
                                                        <dbl>
                                                                      <dbl>
##
   1
           16023
                            2.63
                                         13.8
                                                         83.9
                                                                       1.42
##
    2
           29721
                            2.34
                                          3.52
                                                         95.1
                                                                       1.03
    3
                                                         97.4
##
           10205
                            2.46
                                          1.06
                                                                       1.04
##
   4
          124773
                            2.47
                                         29.1
                                                         68.2
                                                                       1.75
                                                         67.2
##
   5
           13024
                            2.25
                                         31.3
                                                                       0.5
##
   6
          280015
                            2.44
                                         25.0
                                                         70.9
                                                                       1.35
##
    7
           79443
                            2.94
                                          3.48
                                                         93.1
                                                                       2.12
##
   8
           16444
                            2.57
                                          5.38
                                                                       1.96
                                                         91.2
##
   9
           46194
                            2.28
                                         20.1
                                                         77.7
                                                                       0.63
## 10
           14044
                            2.17
                                          0.48
                                                         98.3
                                                                       0.58
## # ... with 80 more rows, and 93 more variables: race.pcthisp <dbl>,
       age.pct12to21 <dbl>, age.pct12to29 <dbl>, age.pct16to24 <dbl>,
       age.pct65up <dbl>, pct.urban <dbl>, med.income <dbl>, pct.wage.inc <dbl>,
## #
## #
       pct.farmself.inc <dbl>, pct.inv.inc <dbl>, pct.socsec.inc <dbl>,
## #
       pct.pubasst.inc <dbl>, pct.retire <dbl>, med.family.inc <dbl>,
## #
       percap.inc <dbl>, white.percap <dbl>, black.percap <dbl>,
       indian.percap <dbl>, asian.percap <dbl>, hisp.percap <dbl>, ...
```

Let's split the data into training and testing, as usual:

```
set.seed(471)
train_samples = sample(1:nrow(crime_data), 0.8*nrow(crime_data))
crime_data_train = crime_data %>% filter(row_number() %in% train_samples)
crime_data_test = crime_data %>% filter(!(row_number() %in% train_samples))
```

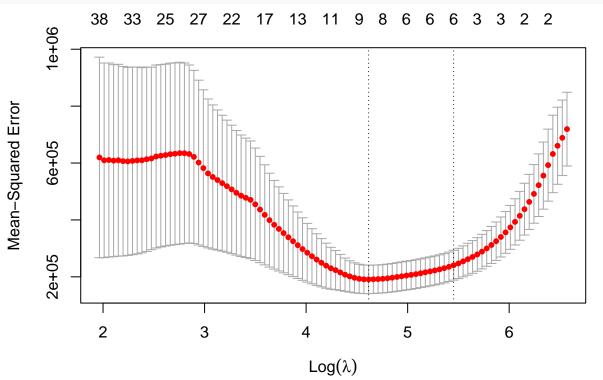
## Running a cross-validated lasso regression

We call cv.glmnet on crime\_data\_train:

### Inspecting the results

The glmnet package has a very nice plot function to produce the CV plot:

plot(lasso\_fit)



The lasso\_fit object has several fields with information about the fit:

```
# lambda sequence
head(lasso_fit$lambda)

## [1] 713.0629 680.6531 649.7163 620.1857 591.9973 565.0901

# number of nonzero coefficients
head(lasso_fit$nzero)

## so s1 s2 s3 s4 s5
## 0 1 1 2 2 2

# CV estimates
head(lasso_fit$cvm)

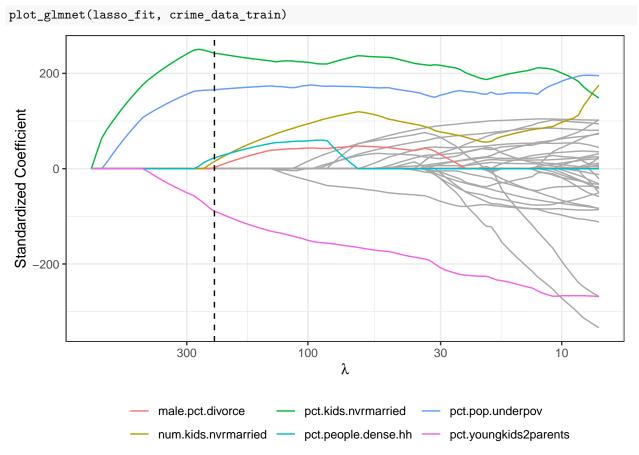
## [1] 719195.4 688634.8 660698.6 631908.0 592507.2 555672.5

# CV standard errors
head(lasso_fit$cvsd)
```

## [1] 129486.1 132612.6 135495.0 136165.2 126567.6 117928.5

```
# lambda achieving minimum CV error
lasso_fit$lambda.min
## [1] 101.0748
# lambda based on one-standard-error rule
lasso_fit$lambda.1se
## [1] 233.4959
To get the fitted coefficients at the selected value of lambda:
coef(lasso_fit, s = "lambda.1se") %>% head()
## 6 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                  1138.536
## population
## household.size
## race.pctblack
## race.pctwhite
## race.pctasian
coef(lasso_fit, s = "lambda.min") %>% head()
## 6 x 1 sparse Matrix of class "dgCMatrix"
                         s1
## (Intercept)
                  7695.849
## population
## household.size
## race.pctblack
## race.pctwhite
## race.pctasian
Note that these coefficient vectors are sparse. We can get a list of the nonzero coefficients as follows:
coef(lasso_fit, s = "lambda.1se") %>%
  as.matrix() %>%
  as.data.frame() %>%
  rownames_to_column() %>%
  as_tibble() %>%
  rename(Feature = rowname, Coefficient = s1) %>%
  filter(Coefficient != 0, Feature != "(Intercept)") %>%
  arrange(desc(abs(Coefficient)))
## # A tibble: 6 x 2
##
     Feature
                            Coefficient
##
     <chr>>
                                   <dbl>
## 1 pct.kids.nvrmarried
                               72.7
## 2 pct.pop.underpov
                               22.7
## 3 pct.youngkids2parents
                               -7.27
## 4 pct.people.dense.hh
                                5.38
## 5 male.pct.divorce
                                0.912
## 6 num.kids.nvrmarried
                                0.00301
```

To visualize the fitted coefficients as a function of lambda, we can make a plot of the coefficients like we saw in class. To do this, we can use the plot\_glmnet function, which by default shows a dashed line at the lambda value chosen using the one-standard-error rule:



By default, plot\_glmnet annotates the features with nonzero coefficients. To interpret these coefficient estimates, recall that they are for the *standardized* features.

## Making predictions

```
To make predictions on the test data, we can use the predict function (which we've seen before):
```

# Elastic net regression

Next, let's run an elastic net regression. We can do this via the cva.glmnet() function:

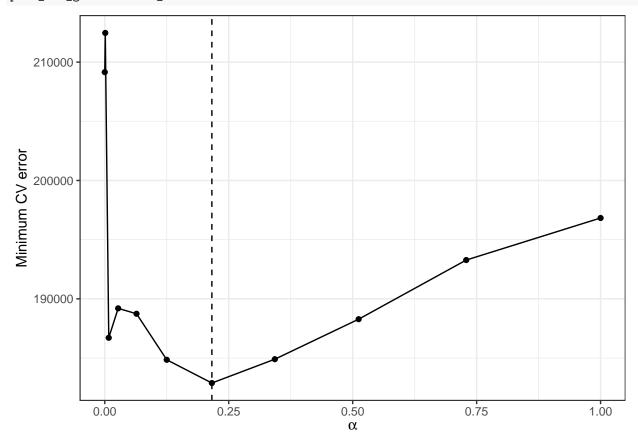
The following are the values of alpha that were used:

```
elnet_fit$alpha
```

```
## [1] 0.000 0.001 0.008 0.027 0.064 0.125 0.216 0.343 0.512 0.729 1.000
```

We can plot the minimum CV error for each value of alpha using the helper function plot\_cva\_glmnet() from plot\_glmnet.R:

```
plot_cva_glmnet(elnet_fit)
```



We can then extract the cv.glmnet fit object based on the optimal alpha using extract\_best\_elnet from plot\_glmnet.R:

```
elnet_fit_best = extract_best_elnet(elnet_fit)
```

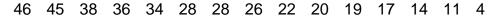
The elnet\_fit\_best object is a usual glmnet fit object, with an additional field called alpha specifying which value of alpha was used:

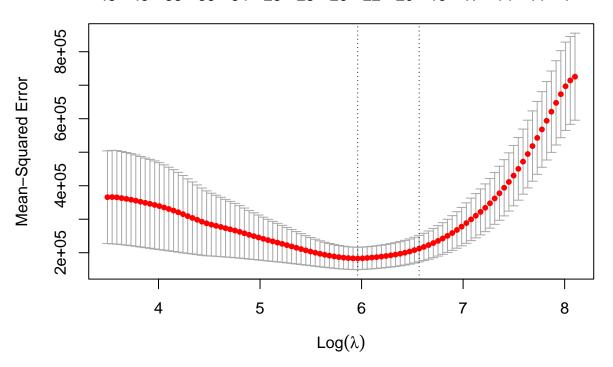
```
elnet_fit_best$alpha
```

## [1] 0.216

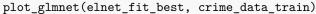
We can make a CV plot to select lambda as usual:

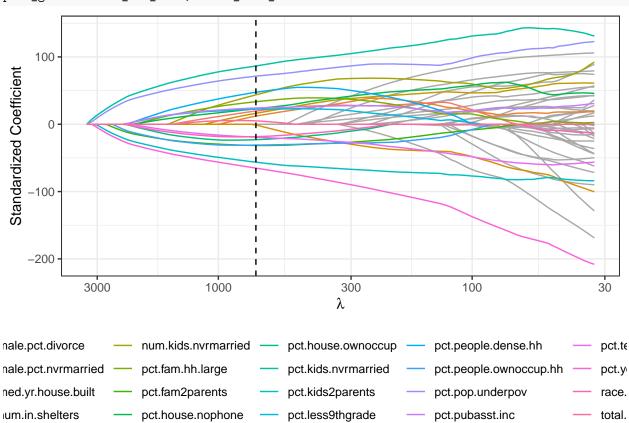
```
plot(elnet_fit_best)
```



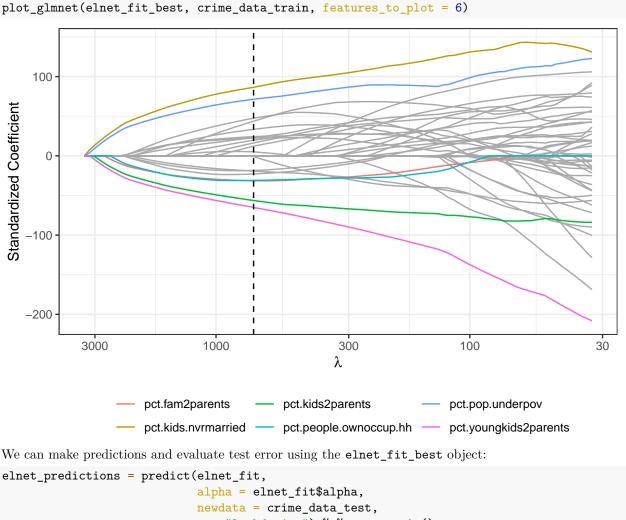


And we can make a trace plot for this optimal value of alpha:





This is too many features to highlight, so let's choose a smaller number:



## [1] 170.5095

## Ridge logistic regression

We can also run a lasso-penalized logistic regression. Let's try it out on a binarized version of the crime data:

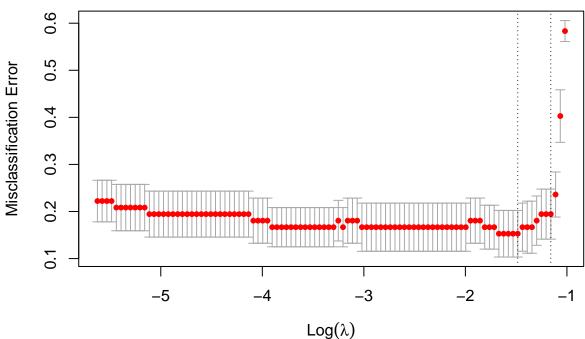
```
as.numeric(violentcrimes.perpop > median(violentcrimes.perpop)))
```

To run the logistic lasso regression, we call cv.glmnet as before, adding the argument family = binomial to specify that we want to do a logistic regression and the argument type.measure = "class: to specify that we want to use the misclassification error during cross-validation.

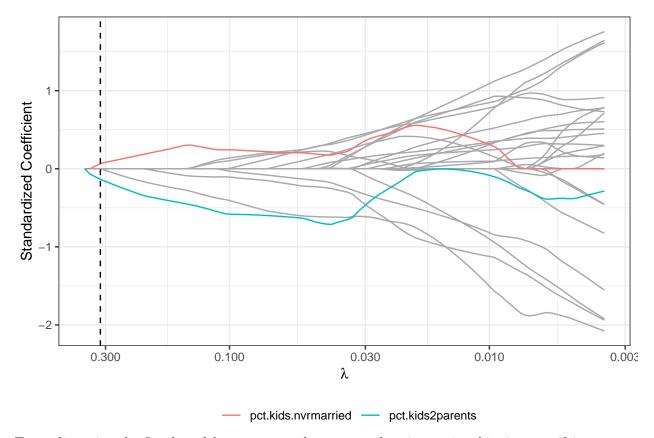
We can then take a look at the CV plot and the trace plot as before:

plot(lasso\_fit)





plot\_glmnet(lasso\_fit, crime\_data\_binary\_train)



To predict using the fitted model, we can use the predict function again, this time specifying type = "response" to get the predictions on the probability scale (as opposed to the log-odds scale).

**##** [1] 0.5750745 0.5179763 0.4617836 0.4392386 0.4409267 0.4460029

We can threshold the probabilities to get binary predictions as we did with regular logistic regression.