

- **Sequences and Series**

- **Tests for Convergence**

- Integral test
    - P-series
    - Upper bound practice
    - Comparison test
    - Limit comparison test
    - Ratio test(D'Alembert's Test)
    - Alternating Series Test(Leibniz's test)

- **Error Bounds**

- For alternating series
    - Absolutely/Conditionally convergence

- **Series**

- Power Series
      - Interval of convergence
      - Radius
    - Taylor Series for Function of one Variable
    - Binomial Series
    - Exponential and Logarithmic series for function
    - Trigonometric series for function

- **Operation of Series**

- Differentiation
    - Integration
    - Substitution
    - Basic operations

- **Taylor Mean Value Theorem**

- Using remainder to get homogeneous limit

- **For Competition**

- **Vectors and Matrices**

- **Vectors**

- Dot product
      - Area
      - Projection
    - Cross product
      - Area and volume
      - Operational rule
    - Cosines
    - Vector function and Derivative

- **Matrix**

- Linear equation
  - Transposition
  - Product
- **Equations of Planes**
  - Vectors in the plane and normal vector
- **Linear system**
  - Geometric meaning of the solution
  - Inverse and Adjoint matrix
  - Theorems of homogeneous and inhomogeneous
- **Differential**
  - **Partial Derivative**
    - First-order and high-order expression
    - In graph
    - Linear to plane approximation
  - **Total Differential**
    - Expression for multi-variables
    - Chain rule(parameterization and compound function)
    - Polar coordinates
    - Arc and tangent vector
  - **Gradient and Directional Derivative**
    - Expression and Orthogonality of Gradient
    - Expression of directional derivative
    - Explain the gradient (change rate/direction)
    - Using the gradient to find the tangent plane
  - **Optimization**
    - Critical point
    - Get Extreme by second partial derivative
    - Constrained optimization
    - Lagrange Function and Multipliers
    - Optimization with more than one constraints
    - Optimization with inequality constraints
  - **Non-independent Variables**
    - Constrained differentials