

MAT 137
Tutorial #6– Inverse trigonometric functions
November 14–15, 2016

Recall that the following two functions

$$\begin{array}{ll} y = \sin x, & \frac{-\pi}{2} \leq x \leq \frac{\pi}{2} \\ x = \arcsin y, & -1 \leq y \leq 1 \end{array}$$

are inverses of each other. This implies:

$$\begin{array}{ll} \sin(\arcsin u) = u & \text{for all } -1 \leq u \leq 1, \\ \arcsin(\sin u) = u & \text{for all } \frac{-\pi}{2} \leq u \leq \frac{\pi}{2}. \end{array}$$

If you get confused, it may help to write similar expressions for all six trigonometric functions, and to draw their graphs.

1. Compute:

- (a) $\arccos(\cos 2)$
- (b) $\arctan(\tan 2)$
- (c) $\arcsin(\sin 2)$

Warning: The three questions all have different answers.

2. Sketch the graph of the following functions.

- (a) $f(x) = \sin(\arcsin x)$
- (b) $f(x) = \arcsin(\sin x)$
- (c) $f(x) = \tan(\arctan x)$
- (d) $f(x) = \arctan(\tan x)$

Warning: The four graphs are all different.

3. Find formulas for the following expressions, using rational functions and roots (if necessary). Write the values of x for which is formula is valid.

- (a) $\arccos(\sin x) =$
- (b) $\sec(\arccos x) =$
- (c) $\sin(\arccos x) =$
- (d) $\sin(\arctan x) =$
- (e) $\cot(\operatorname{arcsec} x) =$