

**MAT 137**  
**Tutorial #5— Computation of derivatives**  
**October 31–November 1, 2016**

1. Compute the derivative of the following functions:

(a)  $f(x) = \frac{x^2 + 2}{x^2 - 2}$

(b)  $f(x) = x^3 \tan(2x + 1)$

(c)  $f(x) = \sqrt{\frac{x+1}{x-1}}$

(d)  $f(x) = \sin^2 x + \sin x^2 + \sin(2x) + \sin^2 x^2$

(e)  $f(x) = \frac{1 + x \sin x}{x + \cos x}$

(f)  $f(x) = \sqrt{x + \sqrt{x + \sqrt{x}}}$

Check your answers:

(a)  $f'(2) = -4$

(b)  $f'(1) = 3 \tan 3 + 2 \sec^2 3$

(c)  $f'(2) = \frac{-1}{\sqrt{3}}, \quad f'(-2) = \frac{-1}{3\sqrt{3}},$   
 $f'(0)$  undefined.

(d)  $f'(2) = \sin 4 + 6 \cos 4 + 4 \sin 8$

(e)  $f'\left(\frac{\pi}{2}\right) = \frac{2}{\pi}$

(f)  $f'(1) = \frac{3 + 4\sqrt{2}}{8\sqrt{2}\sqrt{1 + \sqrt{2}}}$

2. Find a polynomial which has positive derivative when  $1 < x < 2$ , and negative derivative when  $x < 1$  or  $2 < x$ .
3. Find a function which has a vertical tangent line at  $x = 1$ , positive derivative when  $x < 1$ , and negative derivative when  $x > 1$ .
4. Find a polynomial that has the same tangent line at the points with  $x$ -coordinate 0 and the point with  $x$ -coordinate 2, but a different tangent line at the point with  $x$ -coordinate 1.

*Note:* “The same tangent line” does not mean merely the same derivative; it means more than that.