

**MAT 137**  
**Tutorial #18– Convergence Tests**  
**March 20-21, 2017**

Determine which ones of the following series are absolutely convergent, conditionally convergent, or divergent.

1.  $\sum_{n=1}^{\infty} \frac{e^{1-1/n}}{3 + \sin n}$

2.  $\sum_{n=1}^{\infty} \frac{1}{n}$

3.  $\sum_{n=1}^{\infty} \frac{(-1)^n}{n}$

4.  $\sum_{n=1}^{\infty} \frac{1}{n^2}$

5.  $\sum_{n=1}^{\infty} \frac{(-1)^n}{n^2 + 6}$

6.  $\sum_{n=1}^{\infty} \frac{n^2}{\sqrt{n^5 + 4n + 11}}$

7.  $\sum_{n=1}^{\infty} (-1)^n \sin \frac{1}{n}$

8.  $\sum_{n=1}^{\infty} (-1)^n n \sin \frac{1}{n}$

9.  $\sum_{n=1}^{\infty} \frac{(n+3)2^n}{n!}$

10.  $\sum_{n=1}^{\infty} \frac{n!(2n)!}{(3n)!}$

11.  $\sum_{n=1}^{\infty} \frac{1}{n^n}$

12.  $\sum_{n=1}^{\infty} \frac{2 \cdot 4 \cdot 6 \cdot \dots \cdot (2n)}{1 \cdot 3 \cdot 5 \cdot \dots \cdot (2n-1)} \cdot \frac{\pi^{n+1}}{e^{2n-1}}$

13.  $\sum_{n=1}^{\infty} \frac{\sin n}{n^2}$

14.  $\sum_{n=1}^{\infty} \frac{n!}{10^{4n}}$

15.  $\frac{1}{2} + \frac{2}{3^2} - \frac{4}{4^3} + \frac{8}{5^4} + \frac{16}{6^5} - \frac{32}{7^6} + \dots$

16.  $\sum_{n=2}^{\infty} \frac{\cos(n\pi)}{\ln n}$

17.  $\sum_{n=2}^{\infty} \frac{1}{n (\ln n)^2}$

18.  $\sum_{n=2}^{\infty} \frac{1}{\ln n}$

19.  $\sum_{n=2}^{\infty} \frac{\ln n}{n^{1.1}}$

20.  $\sum_{n=2}^{\infty} \frac{1}{(\ln n)^3}$