Notebook - Maratona de Programação

Cabo HDMI, VGA, USB

Contents

1 String

1.1 String hash

Complexity: O(n) preprocessing, O(1) query
Computes the hash of arbitrary substrings of a given string s.

```cpp
// TITLE: String hash
// COMPLEXITY: O(n) preprocessing, O(1) query
// DESCRIPTION: Computes the hash of arbitrary substrings of a given string s.

bool isprime(int x)
{
    if (x < 2)
        return false;
    for (int i = 2; i * i <= x; i++)
    {
        if (x % i == 0)
            return false;
    }
    return true;
}

struct hashs
{
    string s;
    int m1, m2, n, p;
    vector<int> p1, p2, sum1, sum2;

    hashs(string s) : s(s), n(s.size()), p1(n + 1), p2(n + 1), sum1(n + 1), sum2(n + 1)
    {
        srand(time(0));
        p = 31;
        m1 = rand() / 10 + 1e9; // 1000253887;
        m2 = rand() / 10 + 1e9; // 1000546873;
        while (!isprime(m1))
            m1++;
        while (!isprime(m2))
            m2++;

        p1[0] = p2[0] = 1;
        loop(i, 1, n + 1)
        {
            p1[i] = (p * p1[i - 1]) % m1;
            p2[i] = (p * p2[i - 1]) % m2;
        }

        sum1[0] = sum2[0] = 0;
        loop(i, 1, n + 1)
        {
            sum1[i] = (sum1[i - 1] * p) % m1 + s[i - 1];
            sum2[i] = (sum2[i - 1] * p) % m2 + s[i - 1];
            sum1[i] %= m1;
            sum2[i] %= m2;
        }
    }

    // hash do intervalo [l, r)
    int gethash(int l, int r)
    {
        int c1 = m1 - (sum1[l] * p1[r - l]) % m1;
        int c2 = m2 - (sum2[l] * p2[r - l]) % m2;
        int h1 = (sum1[r] + c1) % m1;
        int h2 = (sum2[r] + c2) % m2;
        return (h1 << 30) ^ h2;
    }
};
```

1.2 Z function

Complexity: Z function complexity
z function

```cpp
// TITLE: Z function
// COMPLEXITY: Z function complexity
// DESCRIPTION: z function

void z_function(string& s)
{
    return;
}
```

2 Segtree

2.1 Standard SegTree

Complexity: O(log(n)) query and update
Sum segment tree with point update.

```cpp
// TITLE: Standard SegTree
// COMPLEXITY: O(log(n)) query and update
// DESCRIPTION: Sum segment tree with point update.

using type = int;

type iden = 0;
vector<type> seg;
int segsize;

type func(type a, type b)
{
    return a + b;
}

// query do intervalo [l, r)
type query(int l, int r, int no = 0, int lx = 0, int rx = segsize)
{
    // l lx rx r
    if (r <= lx or rx <= l)
        return iden;
    if (l <= lx and rx <= r)
        return seg[no];

    int mid = lx + (rx - lx) / 2;
    return func(query(l, r, 2 * no + 1, lx, mid),
                query(l, r, 2 * no + 2, mid, rx));
}

void update(int dest, type val, int no = 0, int lx = 0, int rx = segsize)
{
    if (dest < lx or dest >= rx)
        return;
    if (rx - lx == 1)
    {
        seg[no] = val;
        return;
    }

    int mid = lx + (rx - lx) / 2;
    update(dest, val, 2 * no + 1, lx, mid);
    update(dest, val, 2 * no + 2, mid, rx);
    seg[no] = func(seg[2 * no + 1], seg[2 * no + 2]);
}

signed main()
{
    ios_base::sync_with_stdio(0);
```

```
    cin.tie(0);
    cout.tie(0);
    int n;
    cin >> n;
    segsize = n;
    if (__builtin_popcount(n) != 1)
    {
        segsize = 1 + (int)log2(segsize);
        segsize = 1 << segsize;
    }
    seg.assign(2 * segsize - 1, iden);

    loop(i, 0, n)
    {
        int x;
        cin >> x;
        update(i, x);
    }
}
```

3 Set

3.1 Ordered Set

Complexity: O(log(n))

```
// TITLE: Ordered Set
// COMPLEXITY: O(log(n))
// DESCRIPION: Set but you can look witch elements is in position (k)

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

#define ordered_set tree<int, null_type,less<int>, rb_tree_tag,tree_order_statistics_node_update>

int32_t main() {
    ordered_set o_set;

    o_set.insert(5);
    o_set.insert(1);
    o_set.insert(2);
    // o_set = {1, 2, 5}
    5 == *(o_set.find_by_order(2));
    2 == o_set.order_of_key(4); // {1, 2}
}
```

3.2 Multiset

Complexity: O(log(n))
Same as set but you can have multiple elements with same values

```
// TITLE: Multiset
// COMPLEXITY: O(log(n))
// DESCRIPTION: Same as set but you can have multiple elements with same values

int main() {
  multiset<int> set1;
}
```

3.3 Set

Complexity: Insertion Log(n)
Keeps elements sorted, remove duplicates, upper_bound, lower_bound, find, count

```
// TITLE: Set
// COMPLEXITY: Insertion Log(n)
// Description: Keeps elements sorted, remove duplicates, upper_bound, lower_bound, find, count

int main() {
  set<int> set1;

  set1.insert(1);        // O(log(n))
  set1.erase(1);         // O(log(n))

  set1.upper_bound(1);   // O(log(n))
  set1.lower_bound(1);   // O(log(n))
  set1.find(1);          // O(log(n))
  set1.count(1);         // O(log(n))

  set1.size();           // O(1)
  set1.empty();          // O(1)

  set1.clear()           // O(1)
  return 0;
}
```

4 Graph

4.1 Topological Sort

Complexity: O(N + M), N: Vertices, M: Arestas
Retorna no do grapho em ordem topologica, se a quantidade de nos retornada nao for igual a quantidade de nos e impossivel

```
// TITLE: Topological Sort
// COMPLEXITY: O(N + M), N: Vertices, M: Arestas
// DESCRIPTION: Retorna no do grapho em ordem topologica, se a quantidade de nos retornada nao for igual a quantidade de nos e impossivel

typedef vector<vector<int>> Adj_List;
typedef vector<int> Indegree_List; // How many nodes depend on him
typedef vector<int> Order_List;    // The order in which the nodes appears

Order_List kahn(Adj_List adj, Indegree_List indegree)
{
    queue<int> q;
    // priority_queue<int> q; // If you want in lexicografic order
    for (int i = 0; i < indegree.size(); i++) {
        if (indegree[i] == 0)
            q.push(i);
    }
    vector<int> order;

    while (not q.empty()) {
        auto a = q.front();
        q.pop();

        order.push_back(a);
        for (auto b: adj[a]) {
            indegree[b]--;
            if (indegree[b] == 0)
                q.push(b);
        }
```

```
    }
    return order;
}

int32_t main()
{

    Order_List = kahn(adj, indegree);
    if (Order_List.size() != N) {
        cout << "IMPOSSIBLE" << endl;
    }
    return 0;
}
```

4.2 Dinic

Complexity: O(V*V*E), Bipartite is O(sqrt(V) E)
Dinic is a strongly polynomial maximum flow algorithm, doesnt depend on capacity values good for matching

```
// TITLE: Dinic
// COMPLEXITY: O(V*V*E), Bipartite is O(sqrt(V) E)
// DESCRIPTION: Dinic is a strongly polynomial maximum flow algorithm, doesnt depend on capacity values good for matching

const int oo = 0x3f3f3f3f3f3f3f3f;
// Edge structure
struct Edge
{
    int from, to;
    int flow, capacity;

    Edge(int from_, int to_, int flow_, int capacity_)
        : from(from_), to(to_), flow(flow_), capacity(capacity_)
    {}
};

struct Dinic
{
    vector<vector<int>> graph;
    vector<Edge> edges;
    vector<int> level;
    int size;

    Dinic(int n)
    {
        graph.resize(n);
        level.resize(n);
        size = n;
        edges.clear();
    }

    void add_edge(int from, int to, int capacity)
    {
        edges.emplace_back(from, to, 0, capacity);
        graph[from].push_back(edges.size() - 1);

        edges.emplace_back(to, from, 0, 0);
        graph[to].push_back(edges.size() - 1);
    }

    int get_max_flow(int source, int sink)
    {
        int max_flow = 0;
        vector<int> next(size);
        while(bfs(source, sink)) {
            next.assign(size, 0);
            for (int f = dfs(source, sink, next, oo); f != 0; f = dfs(source, sink, next, oo)) {
                max_flow += f;
            }
        }
        return max_flow;
    }

    bool bfs(int source, int sink)
    {
        level.assign(size, -1);
        queue<int> q;
        q.push(source);
        level[source] = 0;

        while(!q.empty()) {
            int a = q.front();
            q.pop();

            for (int & b: graph[a]) {
                auto edge = edges[b];
                int cap = edge.capacity - edge.flow;
                if (cap > 0 && level[edge.to] == -1) {
                    level[edge.to] = level[a] + 1;
                    q.push(edge.to);
                }
            }
        }
        return level[sink] != -1;
    }

    int dfs(int curr, int sink, vector<int> & next, int flow)
    {
        if (curr == sink) return flow;
        int num_edges = graph[curr].size();

        for (; next[curr] < num_edges; next[curr]++) {
            int b = graph[curr][next[curr]];
            auto & edge = edges[b];
            auto & rev_edge = edges[b^1];

            int cap = edge.capacity - edge.flow;
            if (cap > 0 && (level[curr] + 1 == level[edge.to])) {
                int bottle_neck = dfs(edge.to, sink, next, min(flow, cap));
                if (bottle_neck > 0) {
                    edge.flow += bottle_neck;
                    rev_edge.flow -= bottle_neck;
                    return bottle_neck;
                }
            }
        }
        return 0;
    }
};

// Example on how to use
void solve()
{
    int n, m;
    cin >> n >> m;
    int N = n + m + 2;

    int source = N - 2;
    int sink = N - 1;

    Dinic flow(N);

    for (int i = 0; i < n; i++) {
```

```
        int q; cin >> q;
        while(q--) {
            int b; cin >> b;
            flow.add_edge(i, n + b - 1, 1);
        }
    }
    for (int i =0; i < n; i++) {
        flow.add_edge(source, i, 1);
    }
    for (int i =0; i < m; i++) {
        flow.add_edge(i + n, sink, 1);
    }

    cout << m - flow.get_max_flow(source, sink) << endl;

    // Getting participant edges
    for (auto & edge: flow.edges) {
        if (edge.capacity == 0) continue; // This means is a reverse edge
        if (edge.from == source || edge.to == source) continue;
        if (edge.from == sink   || edge.to == sink) continue;
        if (edge.flow == 0) continue; // Is not participant

        cout << edge.from + 1 << " " << edge.to -n + 1 << endl;
    }
}
```

4.3 Bellman Ford

Complexity: O(n * m) | n = |nodes|, m = |edges|
Finds shortest paths from a starting node to all nodes of the graph. The node can have negative cycle and belman-ford will detected

```
// TITLE: Bellman Ford
// COMPLEXITY: O(n * m) | n = |nodes|, m = |edges|
// DESCRIPTION: Finds shortest paths from a starting node to all nodes of the graph. The node can have negative cycle and belman-ford will detected

// a and b vertices, c cost
// [{a, b, c}, {a, b, c}]
vector<tuple<int, int, int>> edges;
int N;

void bellman_ford(int x){
    for (int i = 0; i < N; i++){
        dist[i] = oo;
    }
    dist[x] = 0;

    for (int i = 0; i < N - 1; i++){
        for (auto [a, b, c]: edges){
            if (dist[a] == oo) continue;
            dist[b]= min(dist[b], dist[a] + w);
        }
    }
}
// return true if has cycle
bool check_negative_cycle(int x){
    for (int i = 0; i < N; i++){
        dist[i] = oo;
    }
    dist[x] = 0;

    for (int i = 0; i < N - 1; i++){
        for (auto [a, b, c]: edges){
            if (dist[a] == oo) continue;
            dist[b]= min(dist[b], dist[a] + w);
        }
    }

    for (auto [a, b, c]: edges){
        if (dist[a] == oo) continue;
        if (dist[a] + w < dist[b]){
            return true;
        };
    }
    return false;
}
```