

# DATABASES DESIGN & RELATIONAL ALGEBRA

## DataBase Foundations

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# Outline

- 1 Basic Concepts ✓
- 2 Normalization *// old times*
- 3 Relational Algebra



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# Databases Design Foundations

- In the context of **databases**, the **design** of a database is the process of producing a **detailed data model** of a database.
- This **data model** contains all the needed **logical and physical design choices** and **physical storage parameters** needed to generate a design in a **data definition language**, which can then be used to create a database.
- A **fully attributed data model** contains detailed attributes for **each entity**.
- Relational Data Models** avoid **redundancy** and **inconsistency** by ensuring that data is **normalized**.



# Set Theory in Databases

Entity  $\leftrightarrow$  Object

- The **set theory** is a branch of **mathematical logic** that studies sets, which are **collections of objects**.
- The **set theory** is applied in **databases** to define the **relational model** and the **relational algebra**.
- The **relational model** is a **mathematical model** of data for large shared **data banks** and it has a **solid theoretical foundation**.
- The **relational algebra** is a **procedural query language**, which takes relations as **input** and produces relations as **output**.

DB

c1	c2	c3	c4

row = entity spe.

list of rows

Backend

Class:

C1: order

C2: --

C3: --

list of objects

Data

SQL



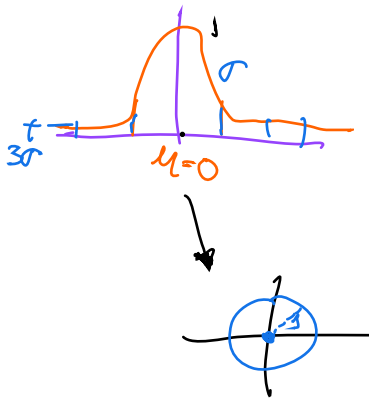
# Outline

## 1 Basic Concepts

*standardize*

## 2 Normalization

## 3 Relational Algebra

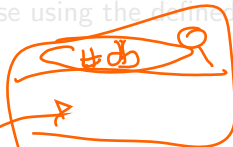
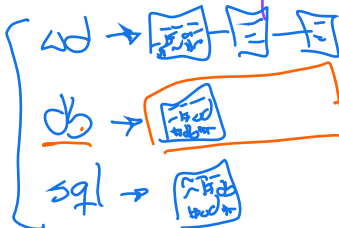


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# Normalization in Databases

- **Normalization** is the process of **organizing** the **columns** (attributes) and **tables** (relations) of a relational database to **minimize data redundancy**.
- **Normalization** involves **decomposing** a table into **smaller tables** and defining **relationships** between them.
- The objective is to **isolate data** so that **additions, deletions, and modifications** of a field can be made in just **one table** and then **propagated** through the rest of the database using the defined relationships.





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# Ontologies

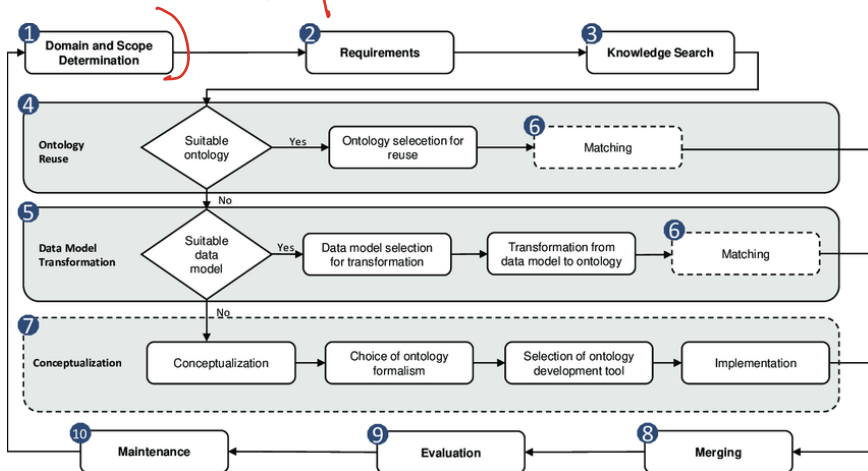
→ experts systems

- An **ontology** is a formal naming and definition of the types, properties, and interrelationships of the entities that really or fundamentally exist for a particular domain of discourse.
- **Ontologies** are used in databases to define the schema of the database.
- The schema of a database is a formal definition of the structure of the database: the types of data that are stored, the relationships between the data, and the constraints on the data.



# Ontology Workflow

30 steps



# Normal Levels

- ① **First normal form (1NF):** The table is a two-dimensional table with rows and columns. Each column contains atomic values, and there are no repeating groups or arrays.
- ② **Second normal form (2NF):** The table is in first normal form and all the non-key attributes are fully functionally dependent on the primary key.
- ③ **Third normal form (3NF):** The table is in second normal form and all the non-key attributes are non-transitively dependent on the primary key.
- ④ **Fourth normal form (4NF):** The table is in third normal form and there are no multi-valued dependencies.



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# What is relational algebra?

db transactions

- The **relational algebra** is a **procedural query language**, which takes **relations** as **input** and produces relations as **output**.
- The **relational algebra** is a **set of operations** that can be performed on a **relation**. Also, it is used to define the **relational model**, which is a **mathematical model** of data for large shared data banks.
- Let's take a look at the **basic operations** of the **relational algebra**. First, remember next table called **Students**:

ID	Name	Lastname	Address	Phone	Age
1	John	Doe	123 Fake St	555-1234	25
2	Jane	Smith	456 Elm St	555-5678	30
3	Mike	Johnson	789 Evergreen St	555-9012	35

Steps: 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 25. 26. 27. 28. 29. 30. 31. 32. 33. 34. 35. 36. 37. 38. 39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51. 52. 53. 54. 55. 56. 57. 58. 59. 60. 61. 62. 63. 64. 65. 66. 67. 68. 69. 70. 71. 72. 73. 74. 75. 76. 77. 78. 79. 80. 81. 82. 83. 84. 85. 86. 87. 88. 89. 90. 91. 92. 93. 94. 95. 96. 97. 98. 99. 100.



# Select Operation

if

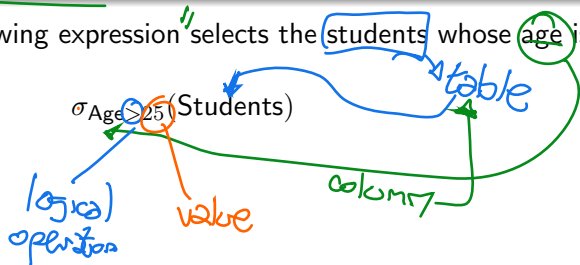
 $\{ col > < open\_logx \text{ value} \}$ 
 $>, <, >=, <=, =, !=$ 

## Definition

 $Relation \Rightarrow Table \rightarrow Entity$ 

**Select:**  $\sigma_{condition}(R)$  is a unary operation that returns the rows (subset) of  $R$  that satisfy the condition.

For example, the following expression "selects the students whose age is greater than 25":



ID	Name	Lastname	Address	Phone	Age
2	Jane	Smith	456 Elm St.	555-9878	30
3	Mike	Johnson	789 Gorgeen St.	555-9012	35



# Project Operation

## Definition

**Project:**  $\pi_{\text{column\_list}}(R)$ , is a unary operation that returns the columns (subset) of  $R$  that are specified in the column list.

For example, the following expression projects the name and lastname of the students:

$\pi_{\text{Name, Lastname}}(\text{Students})$

STUDENTS

Name	lastname
John	Doe
Jane	Smith
Mike	Johnson

student returns name  
age > 31

$\pi_{\text{name}}(\sigma_{\text{age} > 31}(\text{STUDENTS}))$

Name
Mike





# Union Operation

## Definition

**Union:**  $R \cup S$ , is a binary operation that returns the rows that are in  $R$  or in  $S$ .

For example, the following expression returns the students whose age is greater than 25 or whose lastname is Johnson:

$$\sigma_{\text{Age} > 25}(\text{Students}) \cup \sigma_{\text{Lastname} = \text{Johnson}}(\text{Students})$$

ID	...	...	...
2			
3			

ID	...	...	...
3			

ID	...	...	...
2			
3			

ID	...	...	...
2			
3			

$$\sigma_{\text{Age} > 25}(\text{Students}) \cup \sigma_{\text{Lastname} = \text{Johnson}}(\text{Students}) \rightarrow$$



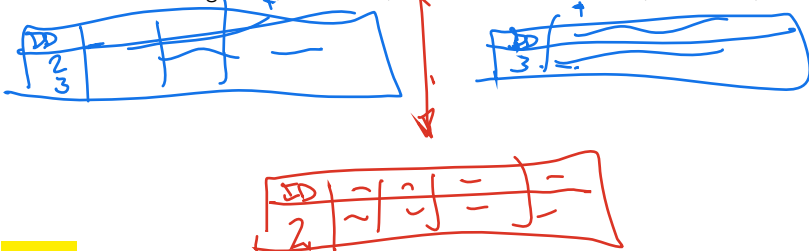
# Set Different Operation

## Definition

**Set Different:**  $R - S$  is a binary operation that returns the rows that are in  $R$  but not in  $S$ .

For example, the following expression returns the students whose age is greater than 25 but not whose lastname is Johnson:

$\sigma_{\text{Age} > 25}(\text{Students}) - \sigma_{\text{Lastname} = \text{Johnson}}(\text{Students})$



# Cartesian Product Operation

## Definition

**Cartesian Product:**  $R \times S$  is a binary operation that returns the Cartesian product of  $R$  and  $S$ . A formal definition is:

$$R \times S = \{r \cup s \mid r \in R \wedge s \in S\}$$

For example, the following expression returns the Cartesian product of the students and the courses:

Students

ID	name
1	ana
2	bob

Courses

ID	name
1	ana
2	bob

Students  $\times$  Courses

ID	name	ID	name
1	ana	1	ana
1	ana	2	bob
2	bob	1	ana
2	bob	2	bob



# Rename Operation

## Definition

**Rename**:  $\rho_{\text{new\_name}}(R)$ , is a unary operation that returns the relation  $R$  with the name  $R$  changed to  $\text{new\_name}$ .

For example, the following expression returns the students relation with the name changed to **People**:

$\rho_{\text{People}}(\text{Students})$

*relation*

<i>ID</i>	<i>name</i>	<i>last</i>	<i>Address</i>	<i>Phone</i>	<i>Age</i>
1					
2					
3					



# Exercises

- 1 Select the **students** whose **age** is **greater** than 25 and whose **lastname** is **Johnson**.
- 2 Project the **name** and **lastname** of the **students** whose **age** is **greater** than 25.
- 3 Select the **students** whose **age** is **greater** than 25 and whose **lastname** is **Johnson**, and **project** the **name** and **lastname** of the **students**, and **rename** the relation to **People**.



# Exercises

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# Thanks!

## Questions?



Repo: <https://github.com/EngAndres/ud-public/tree/main/courses/databases-foundations>

