Python For Data Science *Cheat Sheet* SciPy - Linear Algebra

SciPy

The **SciPy** library is one of the core packages for scientific computing that provides mathematical algorithms and convenience functions built on the NumPy extension of Python.



Interacting With NumPy

Also see NumPy

```
>>> import numpy as np
>>> a = np.array([1,2,3])
>>> b = np.array([(1+5j,2j,3j), (4j,5j,6j)])
>>> c = np.array([[(1.5,2,3), (4,5,6)], [(3,2,1), (4,5,6)]])
```

Index Tricks

>>> np.mgrid[0:5,0:5]	Create a dense meshgrid
>>> np.ogrid[0:2,0:2]	Create an open meshgrid
>>> np.r_[[3,[0]*5,-1:1:10j]	Stack arrays vertically (row-wise)
>>> np.c [b,c]	Create stacked column-wise arrays

Shape Manipulation

>>> np.transpose(b)	Permute array dimensions
>>> b.flatten()	Flatten the array
>>> np.hstack((b,c))	Stack arrays horizontally (column-wise)
	Stack arrays vertically (row-wise)
>>> np.hsplit(c,2)	Split the array horizontally at the 2nd index
>>> np.vpslit(d,2)	Split the array vertically at the 2nd index

Polynomials

>>>	from numpy import polyid	
>>>	p = poly1d([3,4,5])	Create a polynomial object

Vectorizing Functions

```
>>> def myfunc(a):
    if a < 0:
        return a*2
    else:
        return a/2
>>> np.vectorize(myfunc)

Vectorize functions
```

Type Handling

>>> np.real(c)	Return the real part of the array elements
>>> np.imag(c)	Return the imaginary part of the array elements
>>> np.real_if_close(c,tol=1000)	Return a real array if complex parts close to o
>>> np.cast['f'](np.pi)	Cast object to a data type

Other Useful Functions

>>>	np.angle(b,deg=True)	Return the angle of the complex argument
>>>	g = np.linspace(0,np.pi,num=5)	Create an array of evenly spaced values
>>>	g [3:] += np.pi	(number of samples)
>>>	np.unwrap(g)	Unwrap
>>>	np.logspace(0,10,3)	Create an array of evenly spaced values (log scale)
>>>	np.select([c<4],[c*2])	Return values from a list of arrays depending on
		conditions
>>>	misc.factorial(a)	Factorial
>>>	misc.comb(10,3,exact=True)	Combine N things taken at k time
>>>	misc.central_diff_weights(3)	Weights for Np-point central derivative
>>>	misc.derivative(myfunc, 1.0)	Find the n-th derivative of a function at a point

Linear Algebra Also see NumPy

You'll use the linalg and sparse modules. Note that scipy.linalg contains and expands on numpy.linalg.

```
>>> from scipy import linalg, sparse
```

Creating Matrices

>>>	Α	=	<pre>np.matrix(np.random.random((2,2)))</pre>
>>>	В	=	np.asmatrix(b)
>>>	С	=	<pre>np.mat(np.random.random((10,5)))</pre>
>>>	D	=	np.mat([[3,4], [5,6]])

Basic Matrix Routines

Inverse

>>>	A.I
>>>	linalg.inv(A)
>>>	A.T
>>>	A.H
>>>	nn trace(A)

Norm

>>>	linalg.norm(A)
>>>	linalg.norm(A,1)
>>>	linalg.norm(A.np.inf)

Rank

>>> np.linalg.matrix_rank(C)

Determinant

>>> linalg.det(A)

Solving linear problems

>>>	linalg.solve(A,b)
>>>	E = np.mat(a).T
	linalg.lstsq(D,E)

Generalized inverse

>>>	linalg.	pinv(C)
>>>	linala	ning2(C)

Inverse

Inverse Tranpose matrix Conjugate transposition

Trace

Frobenius norm L1 norm (max column sum) L inf norm (max row sum)

Matrix rank

Determinant

(SVD)

Inverse

Norm

Solver for sparse matrices

Solver for dense matrices Solver for dense matrices Least-squares solution to linear matrix equation

Compute the pseudo-inverse of a matrix (least-squares solver)
Compute the pseudo-inverse of a matrix

Creating Sparse Matrices

ı	>>> F = np.eye(3, k=1)	Create a 2X2 identity matrix
ı	>>> G = np.mat(np.identity(2))	Create a 2x2 identity matrix
ı	>>> C[C > 0.5] = 0	
ı	>>> H = sparse.csr matrix(C)	Compressed Sparse Row matrix
ı	>>> I = sparse.csc matrix(D)	Compressed Sparse Column matrix
ı	>>> J = sparse.dok matrix(A)	Dictionary Of Keys matrix
	>>> E.todense()	Sparse matrix to full matrix
	>>> sparse.isspmatrix csc(A)	Identify sparse matrix

Sparse Matrix Routines

Inverse

	sparse.linalg.inv(I)
No	rm

Norm

>>> sparse.linalg.norm(I)
Solving linear problems

Solving linear problems >>> sparse.linalg.spsolve(H,I)

Sparse Matrix Functions

>>> sparse.linalg.expm(I) Sparse matrix exponential

Matrix Functions

Addition

>>>	nn	.add	/ A	DI
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Subtraction

>>> np.subtract(A,D)

Division

>>> np.divide(A,D)

Multiplication

```
>>> np.multiply(D,A)
>>> np.dot(A,D)
>>> np.vdot(A,D)
>>> np.inner(A,D)
>>> np.outer(A,D)
>>> np.tensordot(A,D)
>>> np.tensordot(A,D)
>>> np.kron(A,D)
```

Exponential Functions >>> linalg.expm(A)

>>>	linalg.expm2(A)
>>>	linalg.expm3(D)

Logarithm Function

>>> linalg.logm(A)

Trigonometric Tunctions

>>>	linalg.sinm(D)
>>>	linalg.cosm(D)
>>>	linalg.tanm(A)
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Hyperbolic Trigonometric Functions

```
>>> linalg.sinhm(D)
>>> linalg.coshm(D)
>>> linalg.tanhm(A)
```

Matrix Sign Function >>> np.sigm(A)

Matrix Square Root

>>> linalg.sqrtm(A)

Arbitrary Functions

Arbitrary Functions

>>> linalg.funm(A, lambda x: x*x)

Addition

Subtraction

Division

Multiplication
Dot product
Vector dot product
Inner product
Outer product
Tensor dot product
Kronecker product

Matrix exponential Matrix exponential (Taylor Series) Matrix exponential (eigenvalue

Matrix exponential (eigenvalue decomposition)

Matrix logarithm

Matrix sine Matrix cosine Matrix tangent

Hypberbolic matrix sine Hyperbolic matrix cosine Hyperbolic matrix tangent

Matrix sign function

Matrix square root

Evaluate matrix function

Decompositions

Eigenvalues and Eigenvectors >>> la, v = linalg.eig(A)

	>>>	11, 12 = 1a
	>>>	v[:,0]
	>>>	v[:,1]
	>>>	linalg.eigvals(A)

Singular Value Decomposition

>>> U,s,Vh = linalg.svd(B) >>> M,N = B.shape

>>> Sig = linalg.diagsvd(s,M,N)

LU Decomposition

>>> P,L,U = linalg.lu(C)

Solve ordinary or generalized eigenvalue problem for square matrix Unpack eigenvalues First eigenvector

First eigenvector Second eigenvector Unpack eigenvalues

Singular Value Decomposition (SVD)

Construct sigma matrix in SVD

LU Decomposition

Sparse Matrix Decompositions

	>>>	<pre>la, v = sparse.linalg.eigs(F,1)</pre>
	>>>	sparse.linalg.svds(H, 2)

Eigenvalues and eigenvectors SVD

Asking For Help

>>> help(scipy.linalg.diagsvd)
>>> np.info(np.matrix)