



which may be easier to compute numerically. Note that





## 4 Beta

Two shape parameters

$$a, b > 0$$

$$f(x; a, b) = \frac{(a+b)}{x}$$





$$f(x_i) = x^{-1}e^{-x}$$





$$f(x;c) = c$$

## 18 Exponentiated Weibull

Two positive shape parameters  $a$  and  $c$  and  $x \in (0, \infty)$

$$\begin{aligned} f(x; a, c) &= ac[1 - \exp(-x^c)]^{a-1} \exp(-x^c) x^{c-1} \\ F(x; a, c) &= [1 - \exp(-x^c)]^a \\ G(q; a, c) &= -\log [1 - q^{1/a}]^{1/c} \end{aligned}$$

## 19 Exponential Power

One positive shape parameter  $b$ . Defined for  $x \geq 0$ .

$$\begin{aligned} f(x; b) &= ebx^{b-1} \exp(-x^b) \\ F(x; b) &= 1 - \exp(-x^b) \\ G(q; b) &= \log^{1/b}[1 - \log(1 - q)] \end{aligned}$$

## 20 Fatigue Life (Birnbaum-Sanders)

This distribution's pdf is the average of the inverse-Gaussian ( $\mu = 1$ ) and reciprocal inverse-Gaussian pdf ( $\mu = 1$ ). We follow the notation of JKB here with  $\lambda = S$ , for  $x > 0$

$$f(x; c) = \frac{1}{x+1}$$

$$f(x;c,d) = \frac{cx^{c-1}}{(1+x^c)^2}I_{(0,\infty)}(x)$$

$$F(x;c,d) = 1+x^{-c} -1$$

$$G(x;c,d) = x^{-1} -1 -x^{-1/c}$$

$$\mu = 1 -1$$

$$M(t)=\exp\frac{t}{2}(t-2c)\sqrt{1+e^{2ct}}$$

$$k=\operatorname{erf}\frac{c}{\sqrt{2}}$$

$$p=\exp\left[-\frac{c^2}{2}\right]$$

$$\mu=\frac{\sqrt{2}}{2}p+ck$$

$$\mu_2=\frac{c^2+1-\mu^2}{\sqrt{2}p^3}+\frac{2k\sqrt{2c^2+1}+2ck\sqrt{2c^2+1}}{\mu_2^2}=\frac{c\sqrt{2c^2+1}+3+6\sqrt{2c^2+1}}{\sqrt{2}c^2+2}+\frac{ck}{c^2+2}+\frac{c\sqrt{k^2-1}}{6c^2+1}\mu^2-3\mu^4-4p\mu$$

$\mu$



## 29 Generalized Pareto









## 38 HalfCauchy

If  $Z$  is Hyperbolic Secant distributed then  $e$

## 40 Half-Logistic

In the limit as  $c \rightarrow \infty$  for the generalized half-logistic we have the half-logistic defined over  $x \geq 0$ . Also, the distribution of  $|X|$  where  $X$  has logistic distribution.

$$f(x) = \frac{2e^{-x}}{(1+e^{-x})^2} = \frac{1}{2} \operatorname{sech}^2 \frac{x}{2}$$

$$F(x) = 1 - \frac{1}{1+e^x}$$



## 44 Inverse Normal (Inverse Gaussian)

## 47 Johnson SU

Defined for all  $x$  with two shape parameters  $a$  and  $b > 0$ .

$$f(x; a, b) = \frac{b}{x^2 + 1} \left( a + b \log \left( x + \sqrt{x^2 + 1} \right) \right)$$
$$F(x; a, b) = \frac{a + b \log \left( x + \sqrt{x^2 + 1} \right)}{b}$$



$$f(x) = \frac{\exp(-x)}{[1 + \exp(-x)]^2}$$

$$F(x) = \frac{1}{1 + \exp(-x)}$$

$$G(q) = -\log(1/q - 1)$$

$$\mu = \quad + \quad o(1) = 0$$

$$\mu$$

$$\begin{aligned}
 \mu &= \mu_1 \\
 \mu_2 &= \mu_2 - \mu^2 \\
 \mu_3 &= \frac{\mu_3 - 3\mu\mu_2 - \mu^3}{\mu_2^{3/2}} \\
 \mu_4 &= \frac{\mu_4 - 4\mu\mu_3 - 6\mu^2\mu_2 - \mu^4}{\mu_2^2} - 3
 \end{aligned}$$

## 54 Log Normal (Cobb-Douglass)

Has one shape parameter  $\alpha > 0$ . (Notice that the "Regress"  $A = \log S$  where  $S$  is the scale parameter and  $A$

## 56 Noncentral beta\*

Defined over  $x \in [0, 1]$  with  $a > 0$  and  $b > 0$  and  $c$

where  $U$  and  $V$  are independent and distributed as a standard normal and chi with

$$\mu = 2 \sqrt{2}$$

## 65 Pareto Second Kind (Lomax)

$c > 0$ . This is Pareto of the first kind with  $L = -1.0$  so  $x \geq 0$

$$f(x; c) = \frac{c}{(1+x)^{c+1}}$$



$$\mu = \frac{2}{4 -}$$

$$1 =$$



## 73 Reciprocal Inverse Gaussian

The pdf is found from the inverse gaussian (IG),  $f_{RIG}(x; \mu) = \frac{1}{x^2} f_{IG}(\frac{1}{x}; \mu)$  defined for  $x > 0$  as

$$f_{IG}(x; \mu) = \frac{1}{\sqrt{2\pi x^3}} \exp\left(-\frac{\mu^2}{2x} - \frac{x}{2\mu}\right)$$

$$m_n = m_d = \mu = 0$$

$$\mu_2 = \frac{\quad}{-2} > 2$$

$$_1 = 0 > 3$$

$$_2 = \frac{6}{-4} >$$

As



$\mu$

