

**\*Instructions**

Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute code, your homework should be submitted electronically on GitHub.

This problem set is due before 23:59 on Sunday December 4, 2022. No late assignments will be accepted.

**\*Question 1: Economics** In this question, use the `prestige` dataset in the `car` library. First, run the following commands:

```
install.packages(car)
library(car)
data(Prestige)
help(Prestige)
```

We would like to study whether individuals with higher levels of income have more prestigious jobs. Moreover, we would like to study whether individuals with higher levels of education have more prestigious jobs.

(a) Create a new variable **professional** by recoding the variable **type** so that professionals are coded as 1, and blue and white-collar workers as 0.

(b) Run a linear model with **prestige** as an outcome and **income**, **professional**, and the interaction of the two as predictors. Report the results.

	income	
	professional_dummy	
	income:professional_dummy	
[!htbp]	Regression Results with interaction: prestige ~ income + professional_dummy	
	Constant	
	Observations	115
	R <sup>2</sup>	
	Adjusted R <sup>2</sup>	
	Residual Std. Error	
	F Statistic	
	Note:	*p<0.05

p-value of the coefficient for professional\_dummy is smaller than 0.01, we can reject the null hypothesis that there is no effect of professional status on prestige.  
p-value of the coefficient for interaction of income and professional\_dummy is smaller than 0.01, we can reject the null hypothesis that there is no interaction effect.

(c) Write the prediction equation based on the result.

$$\hat{y} = 21.142 + 0.003x_1 + 37.781x_2 - 0.002x_1x_2$$

$x_1$  for income,  $x_2$  for professional\_dummy

(d) Interpret the coefficient for **income**.

There is a positive and statistically reliable relationship between income and prestige score. When holding the effects of

(e) Interpret the coefficient for **professional**.

There is a positive and statistically reliable relationship between professional and prestige score. When holding the effect

- (f) What is the effect of a \$1,000 increase in income on prestige score for professional occupations? In other words, we are interested in  $0.003 * 1000 - 0.002 * 1000 * 1 = 3$  [language=R, firstline=34, lastline=37] PS4.R  $\hat{y} = 1$   
 The effect of a \$1,000 increase in income on prestige score for professional occupations is an increase in prestige by 1.

- (g) What is the effect of changing one's occupations from non-professional to professional when her income is \$6,000? We are interested in  $\hat{y} = 37.781 * 1 - 0.002 * 6000 * 1$  [language=R, firstline=40, lastline=43] PS4.R  $\hat{y} = 25.781$   
 The effect of changing one's occupations from non-professional to professional when her income is \$6,000 is an increase in prestige by 25.781.

\*Question 2: Political Science Researchers are interested in learning the effect of all of those yard signs on voting p

Below is the result of a regression with two variables and a constant. The dependent variable is the proportion of t

Notes:  $R^2=0.094$ ,  $N=131$

- (a) Use the results from a linear regression to determine whether having these yard signs in a precinct affects vote share (e.  
Hypothesis:  $H_0 : B_1 = 0$  vs.  $H_a : B_1 \neq 0$   
Test-Statistics:  
 $standarderror : 0.016, t = (0.042 - 0)/0.016 = 2.625, degreeof freedom : n - 3 = 131 - 3 = 128$  [language=R, firstline=5  
P-value:  
[language=R, firstline=56, lastline=58]PS4.R  $p - value = 0.0097 < 0.05$   
Conclusion: we can reject the null hypothesis that the slope of having these yard signs in a precinct is 0.

- (b) Use the results to determine whether being next to precincts with these yard signs affects vote share (e.g., conduct a hypothesis test).  
Hypothesis:  $H_0 : B_2 = 0$  vs.  $H_a : B_2 \neq 0$   
Test-Statistics:  
 $standard\ error : 0.013, t = (0.042 - 0)/0.013 = 2.625, degree\ of\ freedom : n - 3 = 131 - 3 = 128$   
P-value:  
 $p - value = 0.0016 < 0.05$   
Conclusion: we can reject the null hypothesis that the slope of being next to precincts with yard signs is 0.

- (c) Interpret the coefficient for the constant term substantively.  
When the precinct is not assigned lawn signs or the precinct is not adjacent to lawn signs, the vote share of this precinct is 0.042.

- (d) Evaluate the model fit for this regression. What does this tell us about the importance of yard signs versus other factors?  
The  $R^2$  of the model is 9.4%, which means 9.4% of the variations are explained by the yard signs, and the rest 90.6% of the variations are explained by other factors.