Using corHMM 2.0

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Introduction

The original version of corHMM contained a number of distinct functions for conducting analyses of discrete morphological characters. This included the corHMM() function for fitting a hidden rates model, which uses "hidden" states as a means of allowing transition rates in a binary character to vary across a tree. In reality, the hidden rates model falls within a general class of models, hidden Markov models (HMM), that may also be applied to multistate characters. So, whether the focal trait is binary or contains multiple states, or whether the observed states represents a set of binary and multistate characters, hidden states can be applied as a means of allowing heterogeneity in the transition model. Choosing a model specific to your question is of utmost importance in any comparative method, and in this new version of corHMM we provide users with the tools to create their own hidden Markov models.

Before delving into this further it may be worth showing a little of what is underneath the hood, so to speak. To begin, consider a single binary character with states θ and θ . If the question was to understand the asymmetry in the transition between these two states, the model, \mathbf{Q} , would be a simple θ 2x2 matrix,

$$Q = \begin{bmatrix} - & q_{0 \to 1} \\ q_{1 \to 0} & - \end{bmatrix}$$

This transition rate matrix is read as describing the transition rate from ROW to COLUMN. Thus, there are only two states, 0 and 1, and two transitions going from $0 \to 1$, and from $1 \to 0$. However, if we introduce a second binary character, the number of possible states you could observe is expanded to account for all the combination of states between two characters – that is, you could observe 00, 01, 10, or 11. To accommodate this, we need to expand our model such that it becomes a 4x4 matrix,

$$Q = \begin{bmatrix} - & q_{00 \to 01} & q_{00 \to 10} & q_{00 \to 11} \\ q_{01 \to 00} & - & q_{01 \to 10} & q_{01 \to 11} \\ q_{10 \to 00} & q_{10 \to 01} & - & q_{10 \to 11} \\ q_{11 \to 00} & q_{11 \to 01} & q_{11 \to 10} & - \end{bmatrix}$$

This model is considerably more complex, as the number of transitions in this rate matrix now goes from 2 to 12. However, with these models we often make a simplifying assumption that we do not allow for transitions in two states to occur at the same time. In other words, if a lineage is in state $\theta\theta$ it cannot immediately transition to state 11, rather, it must first transition either to state θ 1 or 10 before finally transitioning to state 11. Therefore, we can simplify the matrix by removing these "dual" transitions from the model completely,

$$Q = \begin{bmatrix} - & q_{00\to01} & q_{00\to10} & - \\ q_{01\to00} & - & - & q_{01\to11} \\ q_{10\to00} & - & - & q_{10\to11} \\ - & q_{11\to01} & q_{11\to10} & - \end{bmatrix}$$

What we just described is the popular model of Pagel (1994), which tests for correlated evolution between two binary characters. But, one thing that is not obvious: the states in the model need not be represented as combinations of binary characters. For example, the focal character may be two characters, like say, flowers that are red with and without petals, and blue flowers with and without petals. One could just code it as a single multistate character, where 1=red petals, 2=red with no petals (i.e., sepals are red), 3=blue petals, and 4=blue with no petals (i.e., sepals are blue). The model would then be,

$$Q = \begin{bmatrix} - & q_{1\rightarrow 2} & q_{1\rightarrow 3} & q_{1\rightarrow 4} \\ q_{2\rightarrow 1} & - & q_{2\rightarrow 3} & q_{2\rightarrow 4} \\ q_{3\rightarrow 1} & q_{3\rightarrow 2} & - & q_{3\rightarrow 4} \\ q_{4\rightarrow 1} & q_{4\rightarrow 2} & q_{4\rightarrow 3} & - \end{bmatrix}$$

Notice it is the same as before, but the states are transformed from binary combinations to a multistate character. As before, we may assume that transitions in two states cannot occur at the same time and remove the "dual" transitions.

$$Q = \begin{bmatrix} - & q_{1\to 2} & q_{1\to 3} & - \\ q_{2\to 1} & - & - & q_{2\to 4} \\ q_{3\to 1} & - & - & q_{3\to 4} \\ - & q_{4\to 2} & q_{4\to 3} & - \end{bmatrix}$$

Again, exactly the same.

The updated version of corHMM() now lets users transform a set of characters into a *single* multistate character. This means that two characters need not have the same number of character states – that is, one trait could have four states, and the other could be binary. We also allow any model to be expanded to accommodate an arbitrary number of hidden states. Thus, corHMM() is completely flexible and naturally contains rayDISC() and corDISC() capabilities - standalone functions in previous versions of corHMM that may have been mistaken as different "methods." As this vignette will show, they are indeed nested within a broader class of HMMs.

The vignette is comprised of three sections, where we demonstrate all new extensions as well as other new and useful features:

- Section 1 Default use of corHMM
 - 1.1: No hidden rate categores
 - 1.2: Any number of hidden rate categories
- Section 2 How to make and interpret custom models
 - 2.1: Creating and using custom rate matrices
 - * 2.1.1: One rate category
 - * 2.1.2: Any number of rate categories
 - 2.2: Some examples of "biologically informed" models
 - * 2.2.1: Ordered habitat change
 - * 2.2.2: Precursor model
 - * 2.2.3: Ontological relationship of multiple characters
- · Section 3 Estimating models when node states are fixed
 - 3.1: Fixing a single node
 - 3.2: Estimating rates under a parsimony reconstruction
 - 3.3: Fixing nodes when the model contains hidden states

Section 1: Default use of corHMM

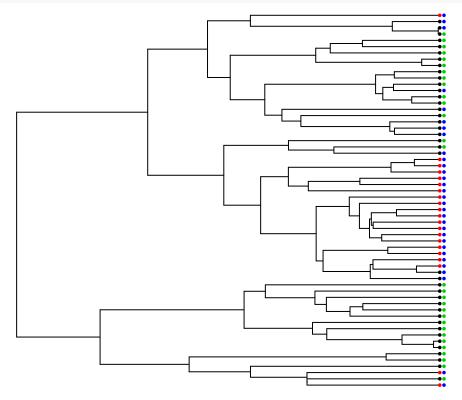
1.1: No hidden rate categories

To start, we'll use the primate dataset from Pagel and Meade (2006) that comes with corHMM:

```
set.seed(1985)
require(ape)
require(expm)
require(corHMM)
```

```
data(primates)
phy <- primates[[1]]
phy <- multi2di(phy)
data <- primates[[2]]

plot(phy, show.tip.label = FALSE)
data.sort <- data.frame(data[, 2], data[, 3], row.names = data[,1])
data.sort <- data.sort[phy$tip.label, ]
tiplabels(pch = 16, col = data.sort[,1]+1, cex = 0.5)
tiplabels(pch = 16, col = data.sort[,2]+3, cex = 0.5, offset = 0.5)</pre>
```



We have two characters each with two possible states: trait 1 is the absence (black) or presence (red) of estrus advertisement in females, and trait 2 is single male (green) or multimale (blue) mating system in primates.

The default use of corHMM() only requires that you declare your phylogeny, your dataset, and the number of rate categories (more detail about this later). We have updated corHMM() to handle different types of input data. Previously, the data could only contain two columns: [,1] a column of species names, and [,2] a column of state values. For corHMM(), the first column must be species names (as in the previous version), but there can now be any number of data columns. If your dataset does have 2 or more columns of trait information, each column is taken to describe an independently evolving character. Note that when the corHMM() call is used, the function automatically determines all the unique character combinations observed in the data set. In our primate example only 3 of the 4 possible combinations are observed, and so the model is constructed accordingly. Also, dual transitions are automatically disallowed. In other words, we expect that a species cannot go directly from estrus advertisement being absent in a single male mating system to having estrus advertisement in a multimale mating system. They must first evolve either estrus advertisement or multimale mating system.

```
Let's give this a try:
```

```
MK_3state <- corHMM(phy = phy, data = data, rate.cat = 1)</pre>
```

```
##
## Input data has more than a single column of trait information, converting...
  4 unique trait combinations found.
##
                 2
         1
                        NΑ
   "0 & 0" "0 & 1" "1 & 0" "1 & 1"
##
##
## The potential number of trait combinations is 4, but only 3 were found.
##
## State distribution in data:
## States:
           1
## Counts: 29 10 21
## Beginning thorough optimization search -- performing 0 random restarts
## Finished. Inferring ancestral states using marginal reconstruction.
MK_3state
##
##
  Fit
##
         -lnL
                   AIC
                            AICc Rate.cat ntax
##
    -41.90867 91.81735 92.54462
##
## Rates
##
              (1,R1)
                          (2,R1)
                                    (3,R1)
## (1,R1)
                  NA 0.01899828
                                        NA
## (2,R1) 0.05661669
                              NA 0.0262652
## (3,R1)
                  NA 0.01609814
                                        NA
##
## Arrived at a reliable solution
```

When you run your corHMM object you are greeted with a summary of the model. Your model fit is described by the log likelihood (lnL), Akaike information criterion (AIC), and sample size corrected Akaike information criterion (AICc). You are also given the number of rate categories (Rate.cat) and number of taxa (ntax).

The *Rates* section of the output describes transition rates between states and are organized as a matrix. Again, the *transition rate matrix* is read as the transition rate **from** ROW **to** COLUMN. For example, if you were interested in the transition rate from State 1 (i.e., absence of estrus advertisement in a single male mating system) to State 2 (i.e., absence of estrus advertisement in a multimale mating system) you would be looking at the Row 1, Column 2, entry. For a time calibrated ultrametric tree, these rates will depend on the age of your phylogeny.

You may also notice that corHMM() printed a state legend to the screen. Thus, you can obtain the exact coding for each species in an augmented dataframe provided by the corHMM() results object itself. This dataframe uses the initial user data to create columns that corresponds to how each species was represented in corHMM():

head(MK_3state\$data.legend)

```
##
                     Genus_sp T1 T2 legend
## 1
        Cercocebus_torquatus
                                   1
## 2
      Cercopithecus_aethiops
                                   1
## 3
          Cercopithecus_mona
                                0
                                   0
                                           1
## 4 Cercopithecus nictitans
                                           1
                                           2
## 5
          Colobus_angolensis
                                   1
## 6
             Colobus_guereza
```

Alternatively, a user can supply their dataset to getStateMat4Dat, which outputs a legend that is consistent with the corHMM() function. The other output is an index matrix (or rate matrix) that describes which rates

are to be estimated in corHMM(). We provide an in-depth discussion about this part of the index matrix later:

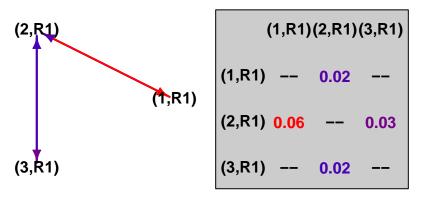
getStateMat4Dat(data)

```
## $legend
##
          1
                   2
                           NA
## "0 & 0" "0 & 1" "1 & 0" "1 & 1"
##
##
   $rate.mat
##
        (1) (2)
                 (3)
## (1)
          0
              2
                   0
## (2)
          1
              Ω
                   4
## (3)
              3
```

Finally, interpreting a Markov matrix can be difficult, especially when you're just starting out. This problem is compounded when users begin to apply the more complex Hidden Markov models (i.e. setting rate.cat > 1). To help users, we have implemented a new plotting function:

plotMKmodel(MK_3state)

Rate Category 1 (R1)



This function uses a corHMM object (which is the result of running corHMM()) or a custom rate matrix (discussed in a later section) to plot the model in two parts. On the left is a ball and stick diagram that depicts the state transitions. On the right is a simplified rate matrix that contains rounded values from the solution output of corHMM(). The colors of the arrows correspond to the magnitude of the rates.

1.2: A trait with any number of states and any number of hidden rate categories

The major difference between this version of corHMM and previous versions is allowing models of any number of states and any number of hidden rate categories (hidden rate categories will be explained in more depth in section 2). Running a hidden Markov model (HMM) only requires assigning a value greater than 1 to the rate cat input. Below, we have assigned 2 rate categories to the data from above:

```
HMM_3state <- corHMM(phy = phy, data = data, rate.cat = 2, model = "SYM")
##
## Input data has more than a single column of trait information, converting...</pre>
```

```
## 4 unique trait combinations found.
## 1 2 NA 3
## "0 & 0" "0 & 1" "1 & 0" "1 & 1"
##
```

The potential number of trait combinations is 4, but only 3 were found.

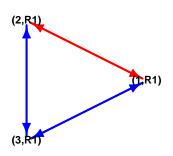
```
##
## State distribution in data:
## States:
            1
                     3
## Counts:
            29
                10
                    21
## Beginning thorough optimization search -- performing 0 random restarts
## Finished. Inferring ancestral states using marginal reconstruction.
HMM_3state
##
##
  Fit
##
         -lnL
                   AIC
                           AICc Rate.cat ntax
    -41.29805 98.5961 101.4196
##
##
## Rates
##
                 (1,R1)
                            (2,R1)
                                          (3,R1)
                                                        (1,R2)
                                                                      (2,R2)
                     NA 9.99150906 2.061154e-09 3.060740e-02
##
  (1,R1)
                                                                          NA
   (2,R1) 9.991509e+00
                                   1.332035e-02
                                                            NA 3.060740e-02
                                NA
   (3,R1) 2.061154e-09 0.01332035
                                              NA
                                                            NA
                                                                          NA
   (1,R2) 1.143431e-02
                                NA
                                              NA
                                                            NA
                                                               2.061154e-09
   (2,R2)
                     NA 0.01143431
                                              NA 2.061154e-09
##
                                                                          NA
##
   (3,R2)
                     NA
                                NA 1.143431e-02 4.807380e-03 1.352960e-02
##
               (3,R2)
## (1,R1)
                   NA
  (2,R1)
                   NΑ
  (3,R1) 0.03060740
   (1,R2) 0.00480738
## (2,R2) 0.01352960
## (3,R2)
                   NA
##
## Arrived at a reliable solution
```

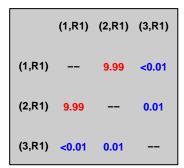
Models with more states take longer to estimate because of the expansion of the state space and the number of transition rates connecting them. Hidden rate models further expand the state space. For example, adding a second rate category went from 4 transition rates to 14. In section 1.1 we left our parameters unconstrained. We estimated all transisions as independent and allowed for transitions from all states to any other state. However, we can constrain a model in corHMM in two different ways. The easiest way is to set the model to either "SYM" or "ER". This is what we've done for the HMM_3state model above. By setting model = "SYM", we have forced the transition rates between any two states to be equal. In comparison, model = "ER" constrains all transition rates between states to be the same. Finally, model = "ARD" (the default) allows all transition rates to be independently estimated. Although "ER" and "SYM are common restrictions, it is often more useful to manually restrict your model to match a biological hypothesis (which is described in the next section).

Interpreting the estimated rate matrix for this hidden Markov model is intimidating. But, the same principles of interpreting the transition rate matrices apply – that is, you still read rates from row to column. However, there is the added complexity of transitions among the different rate categories (as represented by R1 and R2). plotMkmodel() will plot the underlying structure of model in discrete parts. In the following example, the first 2 panels show how observed states transition within each rate category, and the last panel shows transitions among the different rate classes:

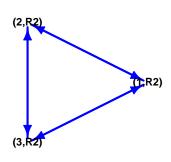
```
plotMKmodel(HMM_3state)
```

Rate Category 1 (R1)



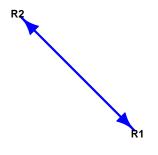


Rate Category 2 (R2)



	(1,R2)	(2,R2)	(3,R2)
(1,R2)		<0.01	<0.01
(2,R2)	<0.01		0.01
(3,R2)	<0.01	0.01	

Rate Category Transitions



	R1	R2
R1		0.03
R2	0.01	

Section 2: How to make and interpret custom models

2.1: Creating and using custom rate matrices

2.1.1: One rate category

A custom rate matrix allows you to specify explicit hypotheses. For example, such an approach allows users to test whether traits evolve in a certain order, testing for different rates of character evolution in different clades, or testing for the presence of hidden precursors before a state can evolve.

At its core, the purpose of a rate matrix (i.e., rate.mat) is to indicate to corHMM which parameters are being estimated. It specifies to corHMM() which rates in the matrix are being estimated and if any of them are expected to be identical. Let's start by using the getStateMat4Dat() function to get a generic rate.mat object:

```
LegendAndRateMat <- getStateMat4Dat(data)
RateMat <- LegendAndRateMat$rate.mat
RateMat
```

```
## (1) (2) (3)
## (1) 0 2 0
## (2) 1 0 4
## (3) 0 3 0
```

The numbers in this matrix are not rates, they are used to index the unique parameters to be estimated by corHMM(). Each distinct number is a parameter to be estimated independently from all others. Let's manually create the symmetric model we used in secion 1.2. In the symmetric model we want transitions to a state to be the same as from that state. This means that $(1) \rightarrow (2) \& (2) \rightarrow (1)$ are equal AND that $(3) \rightarrow (2)$ and $(2) \rightarrow (3)$ are equal. In other words, based on the rate.mat above, we want parameters 1 & 2 to be equal and we want parameters 3 & 4 to be equal as shown below:

```
pars2equal <- list(c(1,2), c(3,4))
StateMatA_constrained <- equateStateMatPars(RateMat, pars2equal)
StateMatA_constrained</pre>
```

```
## (1) (2) (3)
## (1) 0 1 0
## (2) 1 0 2
## (3) 0 2 0
```

To manually create a symmetric model, users may use the equateStateMatPars() function, in which the first argument is the rate matrix being modified (i.e., rate.mat object) and second argument is list of the parameters to be equated. One thing to note is that you must have the appropriate number of rate categories since a user rate matrix is not duplicated or changed by corHMM(). Thus, this custom model can only be used if we set rate.cat=1 since that is the appropriate number of rate categories. We can now provide this customized rate.mat to corHMM():

```
MK_3state_customSYM <- corHMM(phy = phy, data = data, rate.cat = 1, rate.mat = StateMatA_constrained)
```

```
##
## Input data has more than a single column of trait information, converting...
## 4 unique trait combinations found.
## 1 2 NA 3
## "0 & 0" "0 & 1" "1 & 0" "1 & 1"
##
## The potential number of trait combinations is 4, but only 3 were found.
##
```

```
## State distribution in data:
## States: 1
                2
## Counts: 29 10 21
## Beginning thorough optimization search -- performing 0 random restarts
## Finished. Inferring ancestral states using marginal reconstruction.
MK_3state_customSYM
##
## Fit
##
         -1nI.
                   ATC
                           AICc Rate.cat ntax
##
    -44.36715 92.73429 92.94482
                                        1
##
## Rates
##
              (1,R1)
                         (2,R1)
                                     (3,R1)
## (1,R1)
                  NA 0.02568899
                             NA 0.01969411
## (2,R1) 0.02568899
## (3,R1)
                  NA 0.01969411
##
## Arrived at a reliable solution
```

2.1.2: Any number of rate categories

If you wanted to add hidden rate categories, you need to know (1) you need to know the dynamics within each rate category, and (2) transitions among the different rate classes. We begin by constructing two within rate category rate.mat objects (R1 and R2). In R1, we assume a drift-like hypothesis where all transition rates are equal. In R2, we assume that the combination of estrus advertisement and multimale mating systems are not lost once they evolve:

```
RateCat1 <- getStateMat4Dat(data)$rate.mat # R1
RateCat1 <- equateStateMatPars(RateCat1, c(1:4))</pre>
RateCat1
        (1) (2) (3)
##
   (1)
## (2)
                  1
          1
              0
## (3)
RateCat2 <- getStateMat4Dat(data)$rate.mat # R2
RateCat2 <- dropStateMatPars(RateCat2, 3)</pre>
RateCat2
        (1) (2) (3)
## (1)
              2
                  0
         0
## (2)
          1
              0
                  3
          0
                  0
## (3)
              Λ
```

With respect to transitions *among* the different rate classes, we have implemented a separate matrix generator, getRateCatMat(). By default, this function will assume that all transitions among the specified number of rate classes occur independently. In our example, we will generate a matrix that specifies how transitions between R1 and R2 occur. Note that R1 and R2 could represent a biologically-relevant, but unmeasured factor, such as, say, temperate or tropical environments, island or mainland, presence or absence of a third trait. Basically, it is everything and anything that can influence the evolution of your observed characters.

For illustrative purposes, we will specify that the transition rate from R1 to R2 is the same as the rate from R2 to R1:

```
RateClassMat <- getRateCatMat(2) #
RateClassMat <- equateStateMatPars(RateClassMat, c(1,2))
RateClassMat
## R1 R2
## R1 0 1
## R2 1 0</pre>
```

We now group all of our rate classes together in a list. The first element of the list corresponds to R1, the second to R2, etc.

```
StateMats <- list(RateCat1, RateCat2)
StateMats</pre>
```

```
## [[1]]
##
        (1)
            (2)
                  (3)
##
   (1)
          0
               1
                    0
##
   (2)
                    1
## (3)
          0
                    0
##
## [[2]]
##
        (1) (2)
                  (3)
##
          0
               2
                    0
   (1)
##
   (2)
          1
                    3
                    0
##
   (3)
               0
```

Rate Category 1 (R1)

We now have all the components necessary to create the full model using the getFullMat()function. This function requires that the first input be a list of the within rate class matrices and the second argument be the among rate class matrices:

```
FullMat <- getFullMat(StateMats, RateClassMat)
FullMat</pre>
```

```
(1,R1) (2,R1) (3,R1) (1,R2) (2,R2) (3,R2)
##
## (1,R1)
                                           5
                                                   0
                 0
                          1
                                   0
## (2,R1)
                  1
                          0
                                   1
                                           0
                                                   5
                                                            0
## (3,R1)
                  0
                                   0
                                           0
                                                   0
                                                            5
                          1
## (1,R2)
                  5
                          0
                                   0
                                           0
                                                   3
                                                            0
## (2,R2)
                                   0
                                           2
                                                            4
                  0
                          5
                                                   0
## (3,R2)
                          0
                                   5
                                           0
```

Even though we created this larger index matrix from individuals components, we may not be sure it's exactly what we want. We can use plotMkmodel() to take a look at the model setup before running the analysis:

```
plotMKmodel(pp = FullMat, rate.cat = 2, display = "row", text.scale = 0.7)
```

Rate Category 2 (R2)

(2,R1) (1,R1) (2,R1) (3,R1) (2,R2) (1,R2) (2,R2) (3,R2) (1,R2) (2,R2) (3,R2) (1,R2) (2,R2) (3,R2) (1,R2) (2,R2) (2,R2) (2,R2) (3,R2) (2,R2) (2

Since this is the model we intended on making, we can run corHMM() with our custom matrix:

```
HMM_3state_custom <- corHMM(phy = phy, data = data, rate.cat = 2, rate.mat = FullMat, node.states = "no.
```

Rate Category Transitions

```
##
## Input data has more than a single column of trait information, converting...
## 4 unique trait combinations found.
##
                  2
          1
                          NA
## "0 & 0" "0 & 1" "1 & 0" "1 & 1"
##
## The potential number of trait combinations is 4, but only 3 were found.
##
## State distribution in data:
## States: 1
## Counts: 29 10 21
## Beginning thorough optimization search -- performing 0 random restarts
HMM_3state_custom
##
## Fit
##
          -lnL
                     AIC
                              AICc Rate.cat ntax
##
    -41.49312 92.98624 94.09735
                                           2
                                                60
##
## Rates
               (1,R1)
                            (2,R1)
                                        (3,R1)
                                                    (1,R2)
                                                                   (2,R2)
##
                    NA 0.04521237
                                            NA 0.03984679
## (1,R1)
                                                                       NA
## (2,R1) 0.04521237
                                NA 0.04521237
                                                         NA 3.984679e-02
## (3,R1)
                    NA 0.04521237
                                            NA
                                                         NA
                                                                       NA
## (1,R2) 0.03984679
                                NA
                                            NA
                                                         NA 2.061154e-09
                    NA 0.03984679
                                            NA 0.08572475
## (2,R2)
                                                                       NA
                                NA 0.03984679
## (3,R2)
                   NA
                                                         NA
                                                                       NA
                  (3,R2)
##
## (1,R1)
                      NA
## (2,R1)
## (3,R1) 3.984679e-02
## (1,R2)
                      NA
## (2,R2) 2.061154e-09
## (3,R2)
                      NA
##
## Arrived at a reliable solution
We may plot the resulting parameter estimates as before:
plotMKmodel(HMM_3state_custom, display = "row", text.scale = 0.7)
      Rate Category 1 (R1)
                                          Rate Category 2 (R2)
                                                                            Rate Category Transitions
                  (1,R1) (2,R1) (3,R1)
                                                      (1,R2) (2,R2) (3,R2)
                                                                                            R1
                                                                                                 R2
                                                                                                 0.04
               (2,R1) 0.05
                                                   (2,R2)
               (3.R1)
                                                   (3.R2)
                                                                                       R2
                                                                                            0.04
```

2.2: Biological examples

2.2.1: Ordered habitat change

(1)

0

2

A lot of these new capabilities in corHMM were inspired by our current project examining the ancestral habitat during primary endosymbiosis. In our model, we have three possible habitats: marine, freshwater, and terrestrial. Our very large phylogeny of green plants contains many species with a diverse range of life histories. For example, cyanobacteria can move freely between all of these states, whereas some species may move between terrestrial and marine through freshwater. Some species may even move freely between aquatic states, but once they become terrestrial they are stuck there. In this section we will demonstrate how to create a custom hidden Markov model which satisfies all of these requirements.

To do this we will use a simulated a dataset that contains these 3 states:

```
load("simulatedData.Rsave")
head(MFT dat)
##
                     d
      sp
## 1
           Freshwater
      s7
## 2 s14
               Marine
## 3 s16
               Marine
## 4 s17 Terrestrial
## 5 s18 Terrestrial
## 6 s21
               Marine
summary(as.factor(MFT_dat[,2])) # how many of each state do we have?
##
    Freshwater
                      Marine Terrestrial
##
                          14
As before, start off by getting a legend and rate matrix from this dataset:
MFT_LegendAndRate <- getStateMat4Dat(MFT_dat)</pre>
MFT_LegendAndRate
## $legend
##
                1
                                2
                                               3
##
    "Freshwater"
                        "Marine" "Terrestrial"
##
##
   $rate.mat
##
       (1) (2)
                (3)
##
   (1)
          0
              3
## (2)
          1
              0
                  6
## (3)
          2
                   0
```

Here, freshwater habitat will be State 1, marine habitat will be State 2,and terrestrial habitat will be State 3. Now, we need to create 3 different rate classes that are consistent with our hypotheses of how habitat changes occurs. We'll say that rate class R1 is one in which lineages cannot leave a terrestrial habitat, rate class R2 will allow lineages to transition between marine and terrestrial *only* through freshwater, and rate class R3 will be unrestricted movement between the habitats.

For R1 we need terrestrial to be an absorbing state, meaning once terrestriality evolves it is not lost. Since 1 = freshwater, 2 = marine, and 3 = terrestrial, that means removing from (3) to (1) and from (3) to (2).

```
MFT_R1 <- dropStateMatPars(MFT_LegendAndRate$rate.mat, c(2,4))
MFT_R1
## (1) (2) (3)</pre>
```

```
## (2) 1 0 4
## (3) 0 0 0
```

For R2, we need to disallow transitions between terrestrial and marine. We disallow the positions (1,3) and (3,1) in the rate matrix. In this case, any lineage can move into freshwater and move out of freshwater, but they are not allowed to transition directly between terrestrial and marine habitats:

```
MFT_R2 <- dropStateMatPars(MFT_LegendAndRate$rate.mat, c(4,6))
MFT_R2</pre>
```

```
## (1) (2) (3)
## (1) 0 3 4
## (2) 1 0 0
## (3) 2 0 0
```

For R3, we allow all possible transitions to occur, which is the default matrix provided by getStateMat4Dat:

```
MFT_R3 <- MFT_LegendAndRate$rate.mat
MFT_R3</pre>
```

```
## (1) (2) (3)
## (1) 0 3 5
## (2) 1 0 6
## (3) 2 4 0
```

Let's put all these matrices in a list,

```
MFT_ObsStateClasses <- list(MFT_R1, MFT_R2, MFT_R3)</pre>
```

Since we only have 100 species in this example, let's constrain our parameters a bit further and state that transitions between rate classes occur at the same rate:

```
MFT_RateClassMat <- getRateCatMat(3) # we have 3 rate classes
MFT_RateClassMat <- equateStateMatPars(MFT_RateClassMat, 1:6)
```

Next, we put it all together into a corHMM compatible rate.mat:

```
MFT_FullMat <- getFullMat(MFT_ObsStateClasses, MFT_RateClassMat)
MFT_FullMat</pre>
```

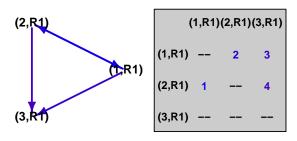
```
##
            (1,R1) (2,R1) (3,R1) (1,R2) (2,R2) (3,R2) (1,R3) (2,R3) (3,R3)
## (1,R1)
                  0
                           2
                                   3
                                           15
                                                    0
                                                             0
                                                                     15
                                                                              0
                                                                                       0
## (2,R1)
                  1
                           0
                                   4
                                            0
                                                   15
                                                             0
                                                                      0
                                                                             15
                                                                                       0
## (3,R1)
                  0
                           0
                                   0
                                            0
                                                    0
                                                            15
                                                                      0
                                                                              0
                                                                                      15
                           0
                                   0
                                            0
                                                    7
                                                                              0
## (1,R2)
                 15
                                                             8
                                                                     15
                                                                                       0
                         15
## (2,R2)
                  0
                                   0
                                            5
                                                    0
                                                             0
                                                                      0
                                                                             15
                                                                                       0
## (3,R2)
                  0
                           0
                                  15
                                            6
                                                    0
                                                             0
                                                                      0
                                                                              0
                                                                                      15
                           0
                                   0
                                           15
                                                             0
## (1,R3)
                 15
                                                    0
                                                                      0
                                                                             11
                                                                                      13
## (2,R3)
                  0
                         15
                                   0
                                            0
                                                   15
                                                             0
                                                                      9
                                                                              0
                                                                                      14
                  0
                           0
                                  15
                                            0
                                                    0
                                                            15
                                                                     10
                                                                             12
                                                                                       0
## (3,R3)
```

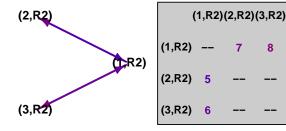
That's kind of difficult to interpret, so let's plot it out and see if it's what we wanted:

```
plotMKmodel(pp = MFT_FullMat, rate.cat = 3, display = "square", text.scale = 0.9)
```

Rate Category 1 (R1)

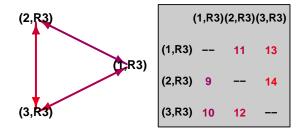
Rate Category 2 (R2)

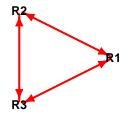




Rate Category 3 (R3)

Rate Category Transitions





	R1	R2	R3
R1		15	15
R2	15		15
R3	15	15	

To run this model, we would only need to specify 1) the data, 2) the phylogeny, 3) this matrix, and 4) that this matrix has 3 rate categories:

MFT_res.corHMM <- corHMM(phy = phy, data = MFT_dat, rate.cat = 3, rate.mat = MFT_FullMat, node.states =

- ## State distribution in data:
- ## States: ?
- ## Counts: 60
- ## Beginning thorough optimization search -- performing 0 random restarts
- ## Warning in log(root.p): NaNs produced

```
## Warning in log(root.p): NaNs produced
```

```
MFT res.corHMM
##
## Fit
##
            -lnL AIC
                          AICc Rate.cat ntax
##
    -3.27518e-09 30 40.90909
##
## Rates
##
              (1,R1)
                           (2,R1)
                                         (3,R1) (1,R2)
                                                               (2,R2)
## (1,R1)
                  NA 2.061457e-09 2.061154e-09
                                                    100
                                                                   NA
## (2,R1)
           99.77544
                                NA 1.705693e-08
                                                     NA 1.000000e+02
## (3,R1)
                  NA
                                NA
                                             NA
                                                     NA
                                                                   NA
## (1,R2) 100.00000
                                NA
                                             NA
                                                     NA 2.063446e-09
## (2,R2)
                  NA 1.000000e+02
                                             NA
                                                    100
                                                                   NA
## (3,R2)
                  NA
                                NA 1.000000e+02
                                                    100
                                                                   NA
## (1,R3) 100.00000
                                NA
                                             NA
                                                    100
                                                                   NA
## (2,R3)
                  NA 1.000000e+02
                                             NA
                                                     NA 1.000000e+02
## (3,R3)
                                NA 1.000000e+02
                  NA
                                                     NA
                                                                   NA
##
                 (3,R2)
                           (1,R3)
                                         (2,R3)
                                                        (3,R3)
                     NA 100.00000
## (1,R1)
                                             NA
                                                           NA
## (2,R1)
                                NA 1.000000e+02
                     NA
                                                           NA
## (3,R1) 1.000000e+02
                                NA
                                             NA 1.000000e+02
## (1,R2) 2.061174e-09 100.00000
                                             NA
                                                           NA
## (2,R2)
                                NA 1.000000e+02
                     NA
                                                           NA
## (3,R2)
                     NA
                                NA
                                             NA 1.000000e+02
## (1,R3)
                     NA
                                NA 2.061154e-09 2.061787e-09
## (2,R3)
                     NA 100.00000
                                             NA 3.446674e-04
## (3,R3) 1.000000e+02
                         99.96077 1.664310e-02
## Arrived at a reliable solution
```

Warning in log(root.p): NaNs produced

2.2.2: The precursor model

The precursor model of Marazzi et al. (2012) marks the beginning of HMMs being used in a phylogenetic comparative context. Marazzi et al. (2012) were interested in locating putative evolutionary precursors of plant extrafloral nectaries (EFNs). Specifically, there were 2 states, presence (1) or absence (0) of EFNs, but that only species with an unobserved, hidden "precursor" trait could gain EFNs. Here we show how you could design the canonical precursor model in corHMM using custom rate matrices.

We will start by loading a simulated dataset of presence and absence of extrafloral nectaries a randomly generated birth-death tree:

```
phy <- read.tree("randomBD.tree")
load("simulatedData.Rsave")
head(Precur_Dat)

## sp d
## s7 s7 0
## s14 s14 0
## s16 s16 0
## s17 s17 0
## s18 s18 1</pre>
```

```
## s21 s21 0
```

Next, generate an observed states only matrix using the input single binary trait data set:

```
Precur_LegendAndMat <- getStateMat4Dat(Precur_Dat)
Precur_LegendAndMat</pre>
```

```
## $legend

## 1 2

## "0" "1"

## $rate.mat

## (1) (2)

## (1) 0 2

## (2) 1 0
```

Based on the legend, the absence of EFNs will be State 1 and the presence of EFNs will be State 2. For a precursor model the transitions between the two observed states, 1 and 2, are modulated by a third, hidden trait, which we will call a precursor. The precursor is represented by being in State 1 (lacking EFNs), but being in the "precursor rate class" (R2 in this case). In other words, if we observe that a species lacks EFN's, we do not know if they also have the precursor (i.e., 1, R2) or not (i.e., 1,R1). We do know, however, that under a precursor model that if we observe EFN, they must always also have the precursor trait, and so the presence of EFNs is always (2,R2). So, we will use rate class R2 as a direct measurement of transitioning between presence and absence of EFNs.

The first rate class, R1, will represent character changes in the absence of the precursor, which is not possible without first gaining the "precursor". So, we will generate the default matrix, then drop all possible transitions from this matrix:

```
Precur_R1 <- Precur_LegendAndMat$rate.mat
Precur_R1 <- dropStateMatPars(Precur_R1, c(1,2))
Precur_R1
## (1) (2)
## (1) 0 0</pre>
```

The second rate class, R2, will represent how our character changes in the presence of the precursor. In this rate class, we expect that species can either gain or lose EFNs at the same rate:

```
Precur_R2 <- Precur_LegendAndMat$rate.mat
Precur_R2 <- equateStateMatPars(Precur_R2, c(1,2))
Precur_R2</pre>
```

```
## (1) (2)
## (1) 0 1
## (2) 1 0
```

(2)

Finally, we set up a matrix for that governs the transitions among the rate classes:

```
RateClassMat <- getRateCatMat(2) #
RateClassMat <- equateStateMatPars(RateClassMat, c(1,2))
RateClassMat
```

```
## R1 R2
## R1 0 1
## R2 1 0
```

Putting them rate classes together we almost get the right model, but we need to remove one extra transition rate between that connects rate class R1 and R2 in the presence of EFNs, because, again, the precursor

model assumes that EFNs can *only* be gained in rate class 1.

```
Precur_FullMat <- getFullMat(list(Precur_R1, Precur_R2), RateClassMat)
Precur_FullMat[c(4,2), c(2,4)] <- 0
Precur_FullMat</pre>
```

```
##
           (1,R1) (2,R1) (1,R2) (2,R2)
## (1,R1)
                 0
                                 2
## (2,R1)
                 0
                         0
                                 0
                                         0
## (1,R2)
                 2
                         0
                                 0
                                         1
                         0
                                         0
## (2,R2)
```

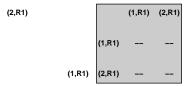
If you're unsure that the model is correct, you can plot the index matrix:

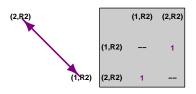
```
plotMKmodel(Precur_FullMat, 2, display = "row", text.scale = 0.7)
```

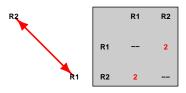
Rate Category 1 (R1)

Rate Category 2 (R2)

Rate Category Transitions







Since the model looks correct, we can run corHMM() making sure to specify that we have 2 rate categories (or rate classes or hidden states - it's all the same).

Precur_res.corHMM <- corHMM(phy = phy, data = Precur_Dat, rate.cat = 2, rate.mat = Precur_FullMat)</pre>

```
## State distribution in data:
```

States: 1 2 ## Counts: 57 43

Beginning thorough optimization search -- performing 0 random restarts

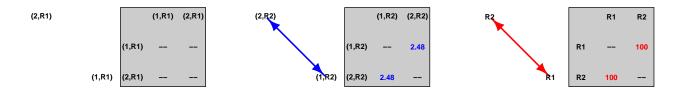
Finished. Inferring ancestral states using marginal reconstruction.

Precur_res.corHMM

```
##
## Fit
##
        -lnL
                   AIC
                            AICc Rate.cat ntax
    -65.9401 135.8802 136.0039
##
                                        2 100
##
## Rates
##
             (1,R1) (2,R1)
                               (1,R2)
                                         (2,R2)
                        NA 99.997653
## (1,R1)
                 NA
                                             NA
## (2,R1)
                 NA
                        NA
                                             NA
                                   NA
## (1,R2) 99.99765
                        NA
                                   NA 2.480293
## (2,R2)
                 NA
                        NA
                            2.480293
                                             NA
##
## Arrived at a reliable solution
```

```
plotMKmodel(Precur_res.corHMM, display = "row", text.scale = 0.7)
```

Rate Category 1 (R1) Rate Category 2 (R2) Rate Category Transitions



2.2.3: Ontological relationship of multiple characters

Lets say we had a dataset with multiple characters: 1) presence or absence of limbs, 2) presence or absence of fingers, 3) corporeal or incorporeal form. It could look something like this:

```
data(primates)
phy <- primates[[1]]
phy <- multi2di(phy)
data <- primates[[2]]
Limbs <- c("Limbs", "noLimbs")[data[,2]+1]
Fings <- vector("numeric", length(phy$tip.label))
Fings[which(Limbs == "Limbs")] <- round(runif(length(which(Limbs == "Limbs")), 0, 1))
Corpo <- rep("corporeal", length(phy$tip.label))
Ont_Dat <- data.frame(sp = phy$tip.label, limbs = Limbs, fings = Fings, corp = Corpo)
head(Ont_Dat)</pre>
```

```
##
                              limbs fings
                                                corp
## 1
              Homo_sapiens noLimbs
                                         0 corporeal
## 2
              Pan_paniscus
                              Limbs
                                         1 corporeal
## 3
           Pan_troglodytes
                              Limbs
                                         0 corporeal
## 4
           Gorilla_gorilla
                              Limbs
                                         1 corporeal
## 5
            Pongo_pygmaeus
                              Limbs
                                         0 corporeal
## 6 Pongo_pygmaeus_abelii
                              Limbs
                                         1 corporeal
```

Previously, the user would have had to convert this dataset into a format that could be read by the rayDISC() function. This task previously involved taking all possible unique combinations and creating a multistate character, but this version of corHMM() will internally do this for you:

```
Ont_LegendAndMat <- getStateMat4Dat(Ont_Dat)
Ont_LegendAndMat</pre>
```

```
## $legend
##
                             1
                                                          2
##
     "Limbs & 0 & corporeal"
                                  "Limbs & 1 & corporeal"
##
   "noLimbs & 0 & corporeal" "noLimbs & 1 & corporeal"
##
##
## $rate.mat
        (1) (2) (3)
##
                  4
##
   (1)
         0
              3
                  0
   (2)
         1
              0
##
   (3)
         2
                  0
```

Even though there were 3 binary characters (meaning 8 possible states), only 3 combinations were actually observed. This is because all of the species were corporeal and thus the incorporeal form didn't factor into

the matrix structure. The next thing to notice is that one of the potential states (No Limbs, Yes Fingers) is not present in the dataset and thus not included in the model. In addition, the transition from 3 (No Limbs, No Fingers) to 2 (Yes Limbs, Yes Fingers) is not allowed because it is impossible to have fingers without having limbs. Finally, all dual transitions have been removed.

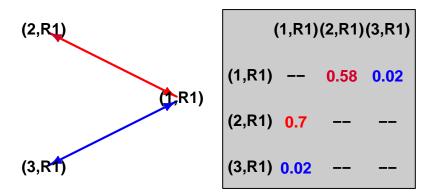
```
Ont_res.corHMM <- corHMM(phy = phy, data = Ont_Dat, rate.cat = 1, rate.mat = Ont_LegendAndMat$rate.mat,</pre>
```

```
##
## Input data has more than a single column of trait information, converting...
  4 unique trait combinations found.
##
##
     "Limbs & 0 & corporeal"
                               "Limbs & 1 & corporeal"
##
   "noLimbs & 0 & corporeal" "noLimbs & 1 & corporeal"
##
##
  The potential number of trait combinations is 4, but only 3 were found.
##
##
## State distribution in data:
## States:
            1
                2
## Counts: 21 18 21
## Beginning thorough optimization search -- performing 0 random restarts
```

Plotting the results provides an overview of the rate classes amongst states.

plotMKmodel(Ont_res.corHMM)

Rate Category 1 (R1)



Note that hidden states can be added to this model easily by following the examples above.

Section 3: Estimating models when node states are fixed

3.1: Fixing a single node

We also added the ability to fix any or all nodes in the input phylogeny while estimating a model. This new feature was inspired by a request from Scott Edwards, who was interested in whether the range of rates of flight gain and loss will result in the highest probability of a volant ancestor to flightless lineages. He ran a series of ancestral state reconstructions under a range of rates of gain and loss of flight. These ancestral state reconstructions focused on a single ancestor at a time (since each ancestor will have a slightly different

set of parameters) and recorded the probability of a volant ancestor. These analyses are included in the supplemental of Sackton et al. (2019).

In this updated version of corHMM, a user can fix anywhere from a single node in a tree to an entire reconstruction from, say parsimony, and estimate the transitions rate. One can even obtain the likelihood of a reconstruction based on a fixed set of rates. To demonstrate, let's start by running a simple analysis of a binary character, but fixing the state of a single node in the the primate tree. Specifically, we are going to fix the most recent common ancestor (MRCA) of Gorilla gorilla and Homo sapiens as exhibiting estrus advertisement (i.e., State 1). The first step is to determine the the indices for each state:

```
data(primates)
phy <- primates[[1]]
phy <- multi2di(phy)
data <- primates[[2]]
getStateMat4Dat(data[,c(1,2)])

## $legend
## 1 2</pre>
```

```
## 1 2
## "0" "1"
##
## $rate.mat
## (1) (2)
## (1) 0 2
## (2) 1 0
```

Here, index 2 represents the presence of estrus advertisement in the model. The next step is to create a vector of node states. We start by generating a string of NA of length equal to the number of nodes plus the number of tips in the tree. The NA simply tells corHMM() to ignore as these are nodes that are not fixed. We then have to determine which node is the MRCA of *Gorilla gorilla* and *Homo sapiens*:

```
label.vector <- rep(NA, Ntip(phy) + Nnode(phy))
homo_gorilla <- getMRCA(phy,tip=c("Homo_sapiens", "Gorilla_gorilla"))
homo_gorilla</pre>
```

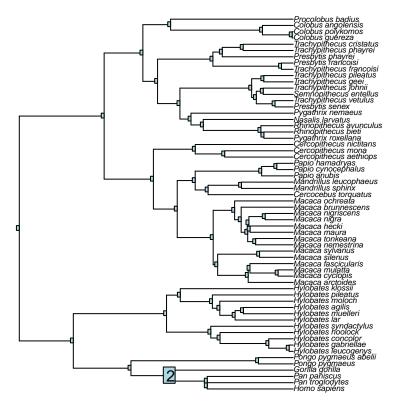
```
## [1] 64
```

The node number should be 64. To set the state of the node, simply replace the NA with the state of interest in the label.vector, in this case with a 2, in the 64th element. To set the node labels, we will clip off the first 60 elements, as these represent the states of the tips, which we set differently:

```
label.vector[homo_gorilla] <- 2
phy$node.label <- label.vector[-c(1:Ntip(phy))]</pre>
```

Plotting the tree allows users to visually check whether the right node was fixed:

```
plot(phy, cex=.5)
nodelabels(phy$node.label)
```



From here simply input the tree object in corHMM() as normal, but the option fix.nodes needs to be set to TRUE:

```
## State distribution in data:
## States: 1 2
## Counts: 39 21
## Beginning thorough optimization search -- performing 0 random restarts
## Finished. Inferring ancestral states using marginal reconstruction.
```

We can then compare the fit of this model with another model where the same node is fixed to lacking estrus advertisement:

```
label.vector[homo_gorilla] <- 1</pre>
phy$node.label <- label.vector[-c(1:Ntip(phy))]</pre>
fix.node64.noestrus <- corHMM(phy, data[,c(1,2)], model="ER", rate.cat=1, fixed.nodes=TRUE)
## State distribution in data:
## States: 1
## Counts: 39 21
## Beginning thorough optimization search -- performing 0 random restarts
## Finished. Inferring ancestral states using marginal reconstruction.
fix.node64.noestrus
##
## Fit
##
         -lnL
                   AIC
                            AICc Rate.cat ntax
    -22.22758 46.45517 46.52414
##
##
## Rates
```

(1,R1)

(1,R1)

(2,R1)

NA 0.008339521

```
## (2,R1) 0.008339521 NA
##
## Arrived at a reliable solution
```

This comparison shows that the model where the MRCA of Gorilla gorilla and Homo sapiens is assumed to have exhibited estrus advertisement requires higher rates, and produces a substantially worse likelihood, than the model that assumes the MRCA lacked estrus advertisement.

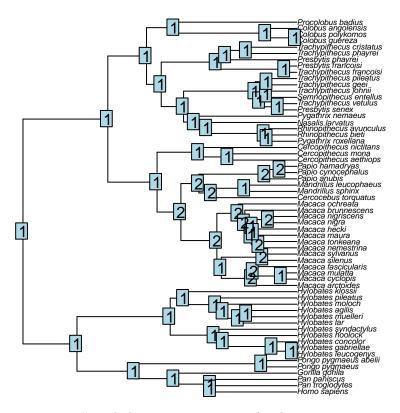
3.2: Estimating rates under a parsimony reconstruction

It is also possible to estimate transition rates where all nodes are fixed in the tree. For example, what if one wanted to examine the fit of a model where all nodes are fixed to according to a maximum parsimony reconstruction. Here we will use phangorn for these purposes. However, with phangorn there is the burden of dealing with their unique phyDat format. To deal with this, we implemented a function, ConvertPhangornReconstructions() that will convert the phyDat formatted output into something we can modify and input into corHMM(). Specifically, we can take the mpr.recon object from phangorn and convert the output as a vector and add them as node states in the phylogeny:

```
library(phangorn)
data.sort <- data.frame(data[,2], row.names=data[,1])
data.sort <- data.sort[phy$tip.label,]
dat<-as.matrix(data.sort)
rownames(dat) <- phy$tip.label
dat<-phyDat(dat,type="USER", levels=c("0","1"))
mpr.recon <- ancestral.pars(phy, dat, type = c("MPR"))
mpr.recon.converted <- ConvertPhangornReconstructions(mpr.recon)
phy$node.label <- mpr.recon.converted[(Ntip(phy)+1):length(mpr.recon.converted)]</pre>
```

Plotting the tree shows the parsimony reconstruction:

```
plot(phy, cex=.5)
nodelabels(phy$node.label)
```



Next, input the tree into corHMM() and obtain a rate estimate for this reconstruction:

```
fixed.parsimony.recon <- corHMM(phy, data[,c(1,2)], model="ER", rate.cat=1, fixed.nodes=TRUE)

## State distribution in data:

## States: 1 2

## Counts: 39 21

## Beginning thorough optimization search -- performing 0 random restarts

## Finished. Inferring ancestral states using marginal reconstruction.

fixed.parsimony.recon</pre>
##
```

```
## Fit
##
         -lnL
                    AIC
                            AICc Rate.cat ntax
##
    -54.94063 111.8813 111.9502
##
## Rates
##
               (1,R1)
                          (2,R1)
## (1,R1)
                  NA 0.02978916
##
  (2,R1) 0.02978916
## Arrived at a reliable solution
```

Interestingly, the parsimony reconstruction suggests a lot more change than if we estimated the states from the model itself.

3.3: Fixing nodes when the model contains hidden states

Finally, if the model contains hidden states, the user needs to fix the state of the node based on the observed state only. Remember, since we cannot actually observe hidden states, we must treat the state of the node as

ambiguous across all possible rate classes like we would a tip. Let's run a quick example where we fix the MRCA of *Gorilla gorilla* and *Homo sapiens* as lacking estrus advertisement:

```
label.vector <- rep(NA, Ntip(phy) + Nnode(phy))
homo_gorilla <- getMRCA(phy,tip=c("Homo_sapiens", "Gorilla_gorilla"))
label.vector[homo_gorilla] <- 1
phy$node.label <- label.vector[-c(1:Ntip(phy))]
fix.node64.noestrus <- corHMM(phy, data[,c(1,2)], model="ARD", rate.cat=2, fixed.nodes=TRUE)

## State distribution in data:
## States: 1 2
## Counts: 39 21
## Beginning thorough optimization search -- performing 0 random restarts
## Finished. Inferring ancestral states using marginal reconstruction.</pre>
```

Now, if we print out the line corresponding to our fixed node,

```
fix.node64.noestrus$states[homo_gorilla-Ntip(phy),]
```

```
## (1,R1) (2,R1) (1,R2) (2,R2)
## 0.8751289 0.0000000 0.1248711 0.0000000
```

there should be some uncertainty as to whether the absence of estrus advertisement is in R1 or R2. The total probability, however, of the node being in observed state 1 should sum to 1:

```
sum(fix.node64.noestrus$states[homo_gorilla-Ntip(phy),])
```

[1] 1

References

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