Recall that

$$\underbrace{\vec{x} = \begin{bmatrix} 1 \\ 0 \end{bmatrix} t + \begin{bmatrix} 0 \\ 2 \end{bmatrix}}_{\ell_1}, \qquad \underbrace{\vec{x} = \begin{bmatrix} 1 \\ -2 \end{bmatrix} t + \begin{bmatrix} 1 \\ 3 \end{bmatrix}}_{\ell_2}.$$

- 1. Jack, you've made a mistake. The t's can be different. You need to set them different when you solve, and then you'll see Tammy is correct.
- 2.

$$\ell_1 \cap \ell_2 \neq \{\}$$

$$\iff$$

$$\begin{bmatrix} 1 \\ 0 \end{bmatrix} t + \begin{bmatrix} 0 \\ 2 \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \end{bmatrix} s + \begin{bmatrix} 1 \\ 3 \end{bmatrix} \implies t = \frac{1}{2} \quad s = \frac{3}{2}$$

So the lines intersect as Tammy said.

3. The 't' that shows up in the vector form of a line is a dummy variable. To determine if two lines written in vector form intersect, you need to replace t with a real variable. For example, you could solve

$$\begin{bmatrix} 1 \\ 0 \end{bmatrix} t + \begin{bmatrix} 0 \\ 2 \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \end{bmatrix} s + \begin{bmatrix} 1 \\ 3 \end{bmatrix}.$$