

# C. 8 .Message Authentication and Hash Functions

- message authentication is concerned with:
  - protecting the integrity of a message
  - validating identity of originator
  - non-repudiation of origin (dispute resolution)
- will consider the security requirements
- then three alternative functions used:
  - message encryption
  - message authentication code (MAC)
  - hash function

# Security Requirements

- disclosure
- traffic analysis
- masquerade
- content modification
- sequence modification
- timing modification
- source repudiation
- destination repudiation

# Message Encryption

- message encryption by itself also provides a measure of authentication
- if symmetric encryption is used then:
  - receiver know sender must have created it
  - since only sender and receiver know key used
  - know content cannot of been altered
  - if message has suitable structure, redundancy or a checksum to detect any changes

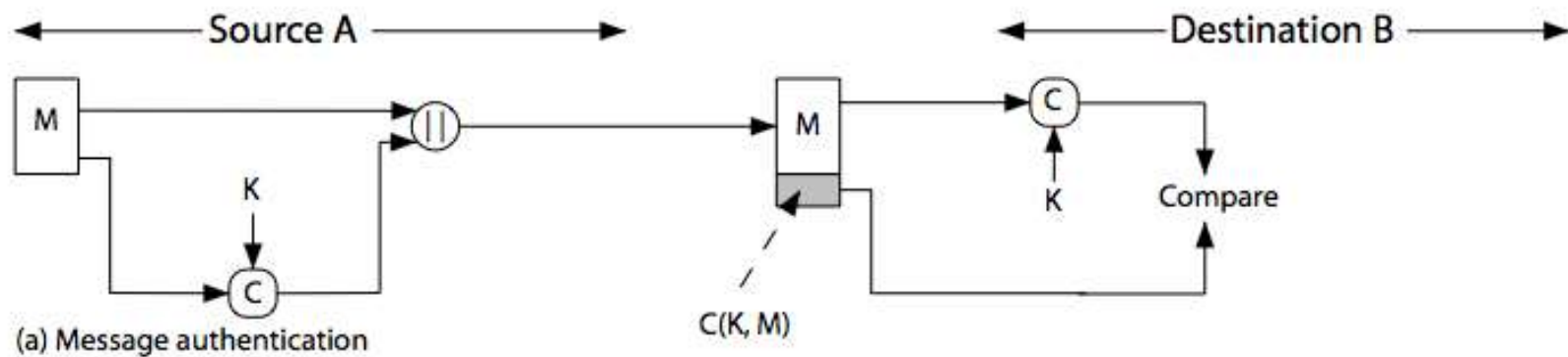
# Message Encryption

- if public-key encryption is used:
  - encryption provides no confidence of sender
  - since anyone potentially knows public-key
  - however if
    - sender **signs** message using their private-key
    - then encrypts with recipients public key
    - have both secrecy and authentication
  - again need to recognize corrupted messages
  - but at cost of two public-key uses on message

# Message Authentication Code (MAC)

- generated by an algorithm that creates a small fixed-sized block
  - depending on both message and some key
  - like encryption though need not be reversible
- appended to message as a **signature**
- receiver performs same computation on message and checks it matches the MAC
- provides assurance that message is unaltered and comes from sender

# Message Authentication Code



# Message Authentication Codes

- as shown the MAC provides authentication
- can also use encryption for secrecy
  - generally use separate keys for each
  - can compute MAC either before or after encryption
  - is generally regarded as better done before
- why use a MAC?
  - sometimes only authentication is needed
  - sometimes need authentication to persist longer than the encryption (eg. archival use)
- note that a MAC is not a digital signature

# MAC Properties

- a MAC is a cryptographic checksum

$$\text{MAC} = C_K(M)$$

- condenses a variable-length message  $M$
  - using a secret key  $K$
  - to a fixed-sized authenticator
- is a many-to-one function
  - potentially many messages have same MAC
  - but finding these needs to be very difficult



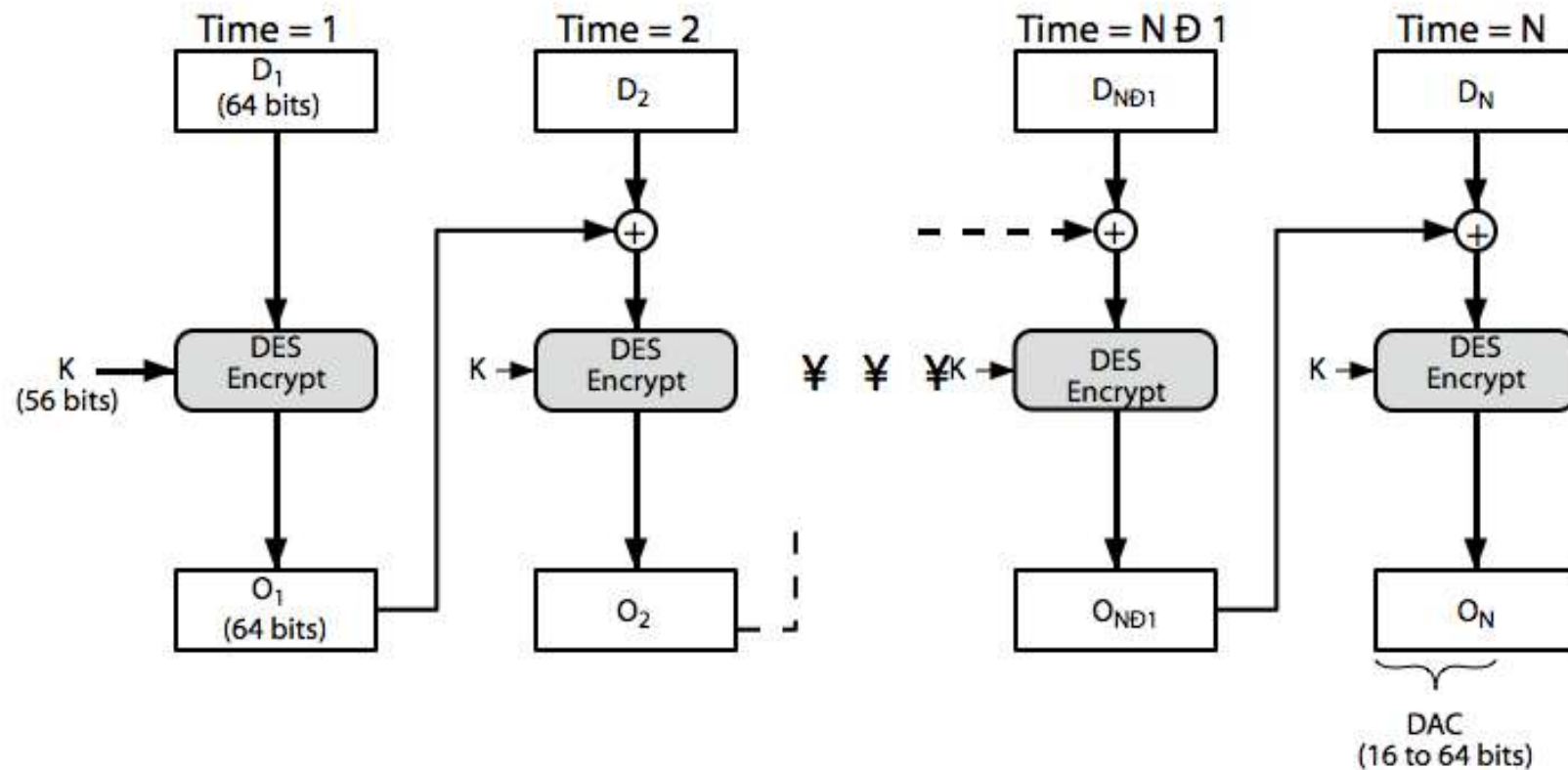
# Requirements for MACs

- taking into account the types of attacks
- need the MAC to satisfy the following:
  1. knowing a message and MAC, is infeasible to find another message with same MAC
  2. MACs should be uniformly distributed
  3. MAC should depend equally on all bits of the message

# Using Symmetric Ciphers for MACs

- can use any block cipher chaining mode and use final block as a MAC
- **Data Authentication Algorithm (DAA)** is a widely used MAC based on DES-CBC
  - using IV=0 and zero-pad of final block
  - encrypt message using DES in CBC mode
  - and send just the final block as the MAC
    - or the leftmost M bits ( $16 \leq M \leq 64$ ) of final block
- but final MAC is now too small for security

# Data Authentication Algorithm



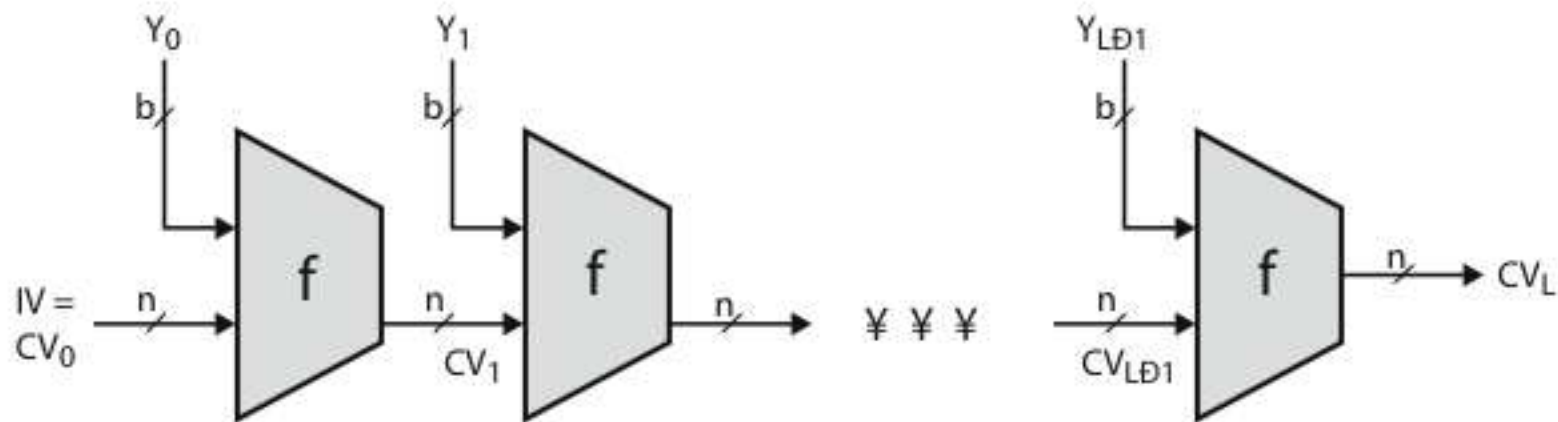
# Hash Functions

- condenses arbitrary message to fixed size

$$h = H(M)$$

- usually assume that the hash function is public and not keyed
  - cf. MAC which is keyed
- hash used to detect changes to message
- can use in various ways with message
- most often to create a digital signature

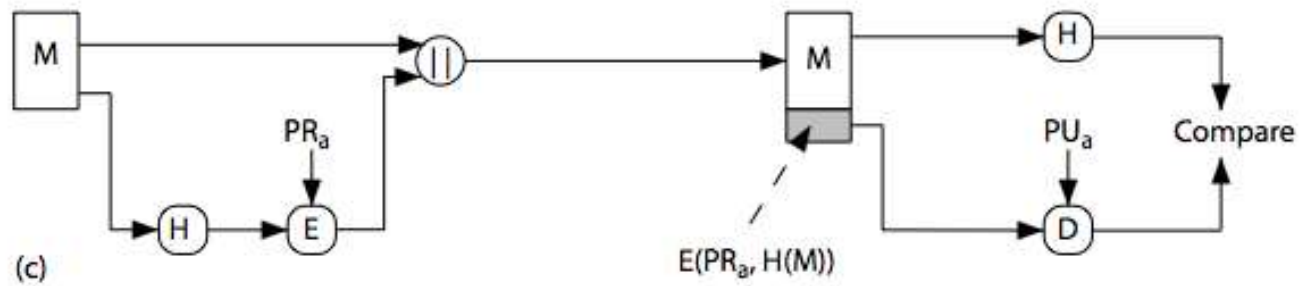
# General structure of Hash Functions



$IV$  = Initial value  
 $CV_i$  = chaining variable  
 $Y_i$  =  $i$ th input block  
 $f$  = compression algorithm

$L$  = number of input blocks  
 $n$  = length of hash code  
 $b$  = length of input block

# Hash Functions & Digital Signatures



# Requirements for Hash Functions

1. can be applied to any sized message  $M$
2. produces fixed-length output  $h$
3. is easy to compute  $h=H(M)$  for any message  $M$
4. given  $h$  is infeasible to find  $x$  s.t.  $H(x)=h$ 
  - one-way property
5. given  $x$  is infeasible to find  $y$  s.t.  $H(y)=H(x)$ 
  - weak collision resistance
6. is infeasible to find any  $x, y$  s.t.  $H(y)=H(x)$ 
  - strong collision resistance

# Simple Hash Functions

- are several proposals for simple functions
- based on XOR of message blocks
- not secure since can manipulate any message and either not change hash or change hash also
- need a stronger cryptographic function (next chapter)



# Birthday Attacks

- might think a 64-bit hash is secure
- but by **Birthday Paradox** is not
- **birthday attack** works thus:
  - opponent generates  $2^{m/2}$  variations of a valid message all with essentially the same meaning
  - opponent also generates  $2^{m/2}$  variations of a desired fraudulent message
  - two sets of messages are compared to find pair with same hash (probability  $> 0.5$  by birthday paradox)
  - have user sign the valid message, then substitute the forgery which will have a valid signature
- conclusion is that need to use larger MAC/hash

# Block Ciphers as Hash Functions

- can use block ciphers as hash functions
  - using  $H_0=0$  and zero-pad of final block
  - compute:  $H_i = E_{M_i} [H_{i-1}]$
  - and use final block as the hash value
  - similar to CBC but without a key
- resulting hash is too small (64-bit)
  - both due to direct birthday attack
  - and to “meet-in-the-middle” attack
- other variants also susceptible to attack

# Hash Functions & MAC Security

- like block ciphers have:
- **brute-force** attacks exploiting
  - strong collision resistance hash have cost  $2^{m/2}$ 
    - have proposal for h/w MD5 cracker
    - 128-bit hash looks vulnerable, 160-bits better
  - MACs with known message-MAC pairs
    - can either attack key space (cf key search) or MAC
    - at least 128-bit MAC is needed for security

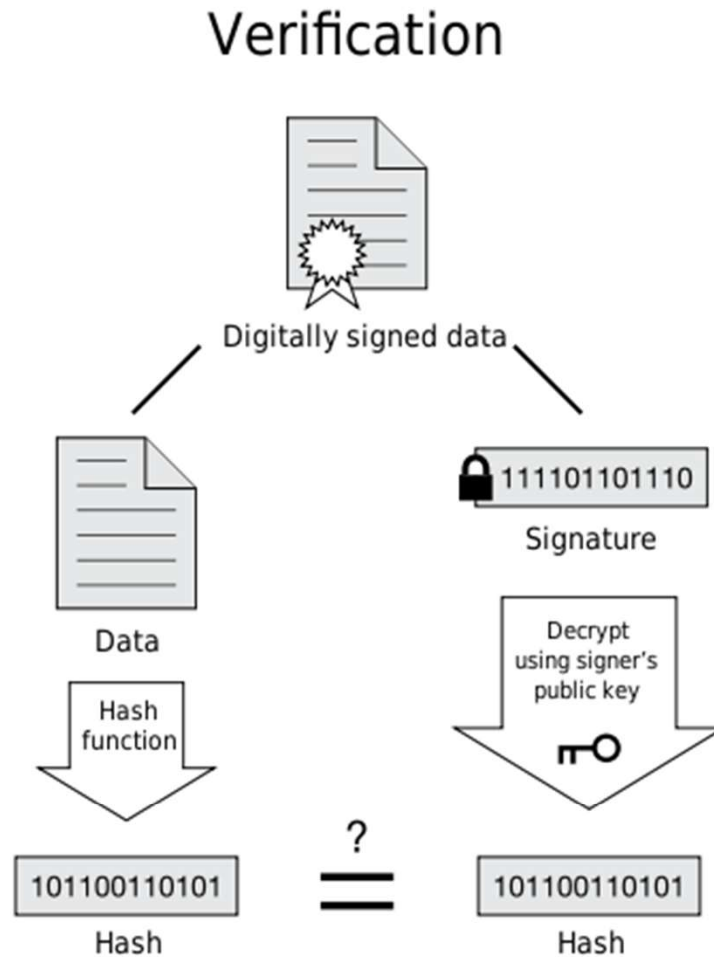
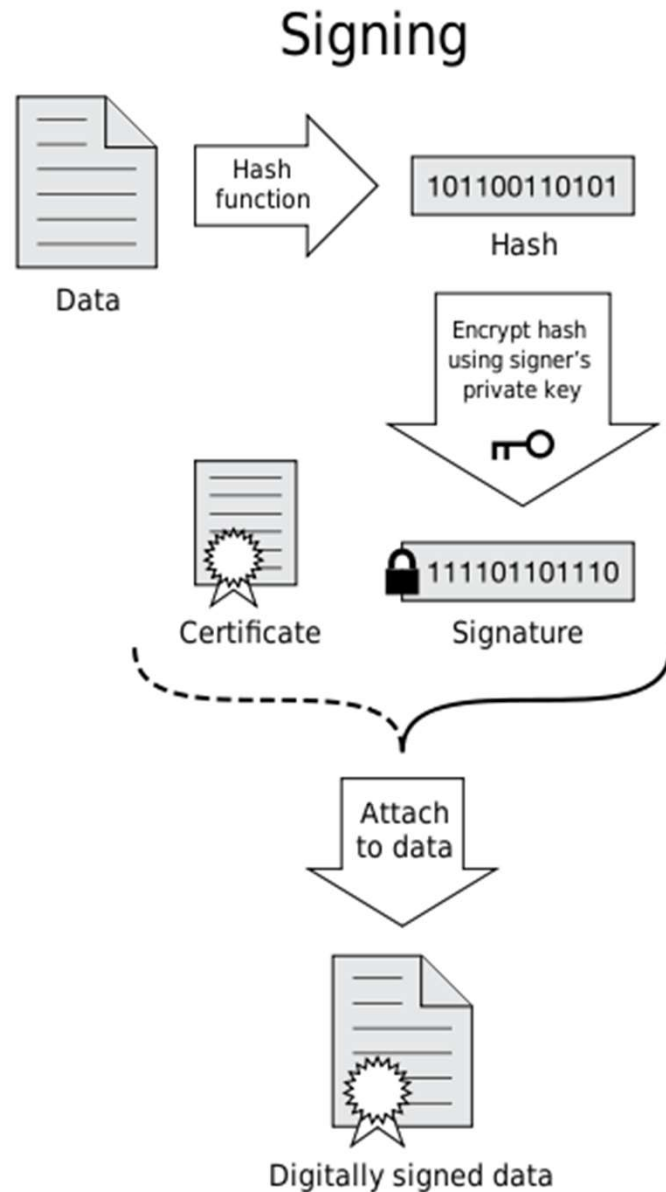
# Hash Functions & MAC Security

- **cryptanalytic attacks** exploit structure
  - like block ciphers want brute-force attacks to be the best alternative
- have a number of analytic attacks on iterated hash functions
  - $CV_i = f[CV_{i-1}, M_i]; H(M) = CV_N$
  - typically focus on collisions in function  $f$
  - like block ciphers is often composed of rounds
  - attacks exploit properties of round functions

# Digital Signatures

- have looked at message authentication
  - but does not address issues of lack of trust
- digital signatures provide the ability to:
  - verify author, date & time of signature
  - authenticate message contents
  - be verified by third parties to resolve disputes
- hence include authentication function with additional capabilities

# Digital Signatures



If the hashes are equal, the signature is valid.

# Digital Signature Properties

- must depend on the message signed
- must use information unique to sender
  - to prevent both forgery and denial
- must be relatively easy to produce
- must be relatively easy to recognize & verify
- be computationally infeasible to forge
  - with new message for existing digital signature
  - with fraudulent digital signature for given message
- be practical save digital signature in storage

# Direct Digital Signatures

- involve only sender & receiver
- assumed receiver has sender's public-key
- digital signature made by sender signing entire message or hash with private-key
- can encrypt using receivers public-key
- important that sign first then encrypt message & signature
- security depends on sender's private-key



# Arbitrated Digital Signatures

- involves use of arbiter A
  - validates any signed message
  - then dated and sent to recipient
- requires suitable level of trust in arbiter
- can be implemented with either private or public-key algorithms
- arbiter may or may not see message

# Authentication Protocols

- used to convince parties of each others identity and to exchange session keys
- may be one-way or mutual
- key issues are
  - confidentiality – to protect session keys
  - timeliness – to prevent replay attacks
- published protocols are often found to have flaws and need to be modified

# Replay Attacks

- where a valid signed message is copied and later resent
  - simple replay
  - repetition that can be logged
  - repetition that cannot be detected
  - backward replay without modification
- countermeasures include
  - use of sequence numbers (generally impractical)
  - timestamps (needs synchronized clocks)
  - challenge/response (using unique nonce)

# Using Symmetric Encryption

- as discussed previously can use a two-level hierarchy of keys
- usually with a trusted Key Distribution Center (KDC)
  - each party shares own master key with KDC
  - KDC generates session keys used for connections between parties
  - master keys used to distribute these to them

# Needham-Schroeder Protocol

- original third-party key distribution protocol
- for session between A B mediated by KDC
- protocol overview is:
  1. A->KDC:  $ID_A || ID_B || N_1$
  2. KDC -> A:  $E_{K_a}[K_s || ID_B || N_1 || E_{K_b}[K_s || ID_A]]$
  3. A -> B:  $E_{K_b}[K_s || ID_A]$
  4. B -> A:  $E_{K_s}[N_2]$
  5. A -> B:  $E_{K_s}[f(N_2)]$

# Needham-Schroeder Protocol

- used to securely distribute a new session key for communications between A & B
- but is vulnerable to a replay attack if an old session key has been compromised
  - then message 3 can be resent convincing B that is communicating with A
- modifications to address this require:
  - timestamps (Denning 81)
  - using an extra nonce (Neuman 93)

# Using Public-Key Encryption

- have a range of approaches based on the use of public-key encryption
- need to ensure have correct public keys for other parties
- using a central Authentication Server (AS)
- various protocols exist using timestamps or nonces

# Denning AS Protocol

- Denning 81 presented the following:
  1.  $A \rightarrow AS: ID_A || ID_B$
  2.  $AS \rightarrow A: E_{PRas}[ID_A || PU_a || T] || E_{PRas}[ID_B || PU_b || T]$
  3.  $A \rightarrow B: E_{PRas}[ID_A || PU_a || T] || E_{PRas}[ID_B || PU_b || T] || E_{Pub}[E_{PRa}[K_s || T]]$
- note session key is chosen by A, hence AS need not be trusted to protect it
- timestamps prevent replay but require synchronized clocks



# One-Way Authentication

- required when sender & receiver are not in communications at same time (eg. email)
- have header in clear so can be delivered by email system
- may want contents of body protected & sender authenticated

# Using Symmetric Encryption

- can refine use of KDC but can't have final exchange of nonces, vis:
  1. A → KDC:  $ID_A || ID_B || N_1$
  2. KDC → A:  $E_{K_a}[K_s || ID_B || N_1 || E_{K_b}[K_s || ID_A]]$
  3. A → B:  $E_{K_b}[K_s || ID_A] || E_{K_s}[M]$
- does not protect against replays
  - could rely on timestamp in message, though email delays make this problematic

# Public-Key Approaches

- have seen some public-key approaches
- if confidentiality is major concern, can use:  
A->B:  $E_{P_{Ub}}[K_s] || E_{K_s}[M]$   
– has encrypted session key, encrypted message
- if authentication needed use a digital signature with a digital certificate:  
A->B:  $M || E_{P_{Ra}}[H(M)] || E_{P_{Ra_s}}[T || ID_A || PU_a]$   
– with message, signature, certificate

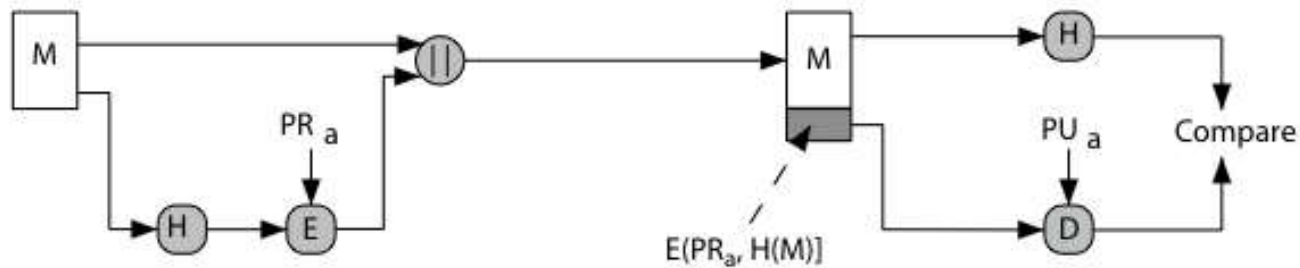
# Digital Signature Standard (DSS)

- US Govt approved signature scheme
- designed by NIST & NSA in early 90's
- published as FIPS-186 in 1991
- revised in 1993, 1996 & then 2000
- uses the SHA hash algorithm
- DSS is the standard, DSA is the algorithm
- FIPS 186-2 (2000) includes alternative RSA & elliptic curve signature variants

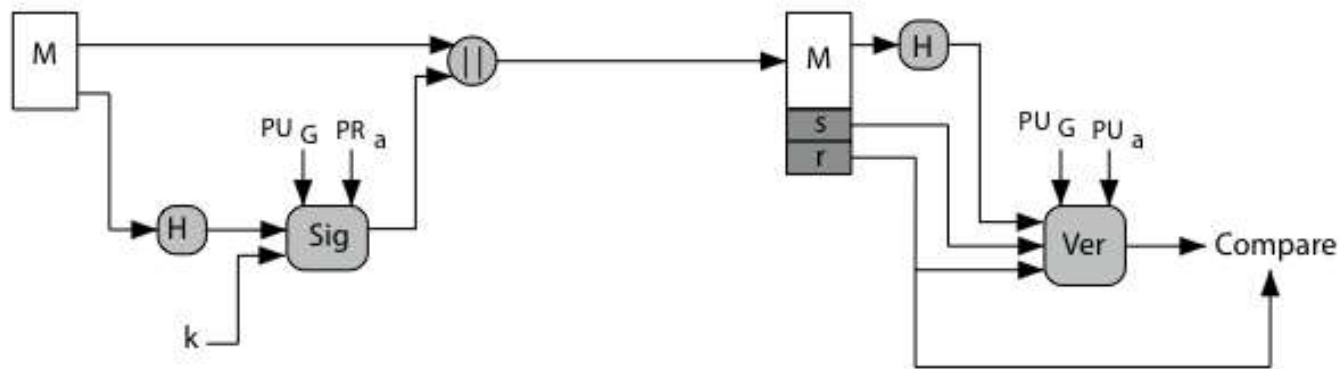
# Digital Signature Algorithm (DSA)

- creates a 320 bit signature
- with 512-1024 bit security
- smaller and faster than RSA
- a digital signature scheme only
- security depends on difficulty of computing discrete logarithms
- variant of ElGamal & Schnorr schemes

# Digital Signature Algorithm (DSA)



(a) RSA Approach



(b) DSS Approach

# DSA Key Generation

- have shared global public key values  $(p, q, g)$ :
  - choose  $q$ , a 160 bit
  - choose a large prime  $2^{L-1} < p < 2^L$ 
    - where  $L = 512$  to  $1024$  bits and is a multiple of 64
    - and  $q$  is a prime factor of  $(p-1)$
  - choose  $g = h^{(p-1)/q}$ 
    - where  $h < p-1$ ,  $h^{(p-1)/q} \pmod{p} > 1$
- users choose private & compute public key:
  - choose  $x < q$
  - compute  $y = g^x \pmod{p}$

# DSA Signature Creation

- to **sign** a message  $M$  the sender:
  - generates a random signature key  $k$ ,  $k < q$
  - nb.  $k$  must be random, be destroyed after use, and never be reused
- then computes signature pair:
$$r = (g^k \pmod p) \pmod q$$
$$s = (k^{-1} \cdot H(M) + x \cdot r) \pmod q$$
- sends signature  $(r, s)$  with message  $M$



# DSA Signature Verification

- having received  $M$  & signature  $(r, s)$
- to **verify** a signature, recipient computes:  
$$w = s^{-1} \pmod{q}$$
$$u1 = (H(M) \cdot w) \pmod{q}$$
$$u2 = (r \cdot w) \pmod{q}$$
$$v = (g^{u1} \cdot y^{u2} \pmod{p}) \pmod{q}$$
- if  $v=r$  then signature is verified