

MATH 217 Linear Algebra and Differential Equations  
FINAL EXAM

1. Find the general solution of the following Bernoulli equation:  
 $y' - \frac{2y}{x} = 2x\sqrt{y}.$
2. Find an integrating factor and solve the given equation:  
 $2(\cos^2 y \cdot \cos 2y - x) dy - \sin 2y dx = 0.$
3. Solve the following differential equations using the method of variation of parameters:  
 $xy'' - y' = x^3.$
4. Solve the following differential equations using the method of undetermined coefficients:  
 $y'' + y = 4 \sin x.$
5. Solve the following Cauchy-Euler equation using the substitution  $x = e^t$  :  
 $x^2 y'' + 3xy' + y = 0.$