

This is false. Consider, in fact, one of the examples from the text, with two men and two women.

m prefers w to w' .

m' prefers w' to w .

w prefers m' to m .

w' prefers m to m' .

Note that there are no pairs at all where each ranks the other first, so clearly no such pair can show up in a stable matching.