



# Hypothesis Testing II: Two Sample *t* Tests

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## **Comparing Two Samples**

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## **Comparing Two Samples**

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- Two-Sample t-test

## Two-Sample (unpooled)

- Two samples  $X_1 = \{x_{1,1}, x_{1,2} \dots x_{1,N_1}\}$  and  $X_2 = \{x_{2,1}, x_{2,2} \dots x_{2,N_2}\}$
- Doesn't assume that variance is the same for both samples (unpooled)
- Compute mean and sample variance for sample 1  $(\bar{x_1}, s_1^2)$  and sample 2  $(\bar{x_2}, s_2^2)$

#### **Test Statistic**

T-statistic

$$T = \frac{(\overline{x}_1 - \overline{x}_2)}{\sqrt{\frac{s_1^2}{N_1} + \frac{s_2^2}{N_2}}} \tag{1}$$

Plug into t-distrubtion with

$$v = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{N_2}\right)^2}{\frac{\left(\frac{s_1^2}{N_1}\right)^2}{N_1 - 1} + \frac{\left(\frac{s_2^2}{N_2}\right)^2}{N_2 - 1}} \tag{2}$$

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- Two-tailed vs. one-tailed distinction still applies