

Lista de exercicios - Circuitos lógicos e digitais

ALUNO: CAIO HENRIQUE DE OLIVEIRA

1) CONVERTA PARA O SISTEMA DECIMAL

a) $100110 = 38_{10}$

32	16	8	4	2	1
1	0	0	1	1	0

b) $011110 = 30_{10}$

32	16	8	4	2	1
0	1	1	1	1	0

c) $111011 = 59_{10}$

32	16	8	4	2	1
1	1	1	0	1	1

d) $1010000 = 80_{10}$

64	32	16	8	4	2	1
1	0	1	0	0	0	0

e) $11000101 = 197_{10}$

128	64	32	16	8	4	2	1
1	1	0	0	0	1	0	1

f) $11010110 = 214_{10}$

128	64	32	16	8	4	2	1
1	1	0	1	0	1	1	0

g) $011001100110101 = 13109_{10}$

16384	8192	4096	2048	1024	512	256	128	64	32	16	8	4	2	1
0	1	1	0	0	1	1	0	0	1	1	0	1	0	1

SOMANDO, TEMOS

2) CONVERTA PARA O SISTEMA BINÁRIO:

a) $78 = 1001110_2$

64	32	16	8	4	2	1
1	0	0	1	1	1	0

b) $102 = 1100110_2$

64	32	16	8	4	2	1
1	1	0	0	1	1	0

c) $215 = 11010111_2$

128	64	32	16	8	4	2	1
1	1	0	1	0	1	1	1

d) $404 = 110010100_2$

256	128	64	32	16	8	4	2	1
1	1	0	0	1	0	1	0	0

e) $808 = 1100101000_2$

512	256	128	64	32	16	8	4	2	1
1	1	0	0	1	0	1	0	0	0

f) $5429 = 1010100110101_2$

4096	2048	1024	512	256	128	64	32	16	8	4	2	1
1	0	1	0	1	0	0	1	1	0	1	0	1

$16383 = 1111111111111_2$

8192	4096	2048	1024	512	256	128	64	32	16	8	4	2	1
1	1	1	1	1	1	1	1	1	1	1	1	1	1

3-

A) $512 \rightarrow \log_2(512) = 9$
 número de Bits necessários = 9

B) $12 \rightarrow \log_2(12) \approx 3,6$
 número de Bits necessários = 4

C) $2 \rightarrow \log_2(2) = 1$
 número de Bits necessários = 1

D) $17 \rightarrow \log_2(17) \approx 4,08$
 número de Bits necessários = 5

E) $33 \rightarrow \log_2(33) \approx 5,04$
 número de Bits necessários = 6

F) $43 \rightarrow \log_2(43) \approx 5,42$
 número de Bits necessários = 6

G) $7 \rightarrow \log_2(7) \approx 2,8$
 número de Bits necessários = 3

4) A) $479_{16} = (4 \times 16^2) + (7 \times 16^1) + (9 \times 16^0)$
 $= (4 \times 256) + (7 \times 16) + (9 \times 1)$
 $= 1145_{10}$

B) $4AB_{16} = (4 \times 16^2) + (10 \times 16^1) + (11 \times 16^0)$
 $= (4 \times 256) + (10 \times 16) + (11 \times 1)$
 $= 1195_{10}$

C) $BDE_{16} = (11 \times 16^2) + (13 \times 16^1) + (14 \times 16^0)$
 $= (11 \times 256) + (13 \times 16) + (14 \times 1)$
 $= 3038_{10}$

D) $F0CA_{16} = (15 \times 16^3) + (0 \times 16^2) + (12 \times 16^1) + (10 \times 16^0)$
 $= (15 \times 4096) + (0) + (12 \times 16) + (10)$
 $= 61642_{10}$

E) $2D3F_{16} = (2 \times 16^3) + (13 \times 16^2) + (3 \times 16^1) + (15 \times 16^0)$
 $= (2 \times 4096) + (13 \times 256) + (3 \times 16) + (15 \times 1)$
 $= 11583_{10}$

5

(A) $486_{10} = 1E6_{16}$

$$\begin{array}{r} 486 \overline{) 16} \\ 16 \overline{) 30} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \\ 16 \overline{) 14} \end{array}$$

6

(B) $2000_{10} = 7D0_{16}$

$$\begin{array}{r} 2000 \overline{) 16} \\ 16 \overline{) 128} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \\ 16 \overline{) 112} \end{array}$$

7

(C) $4096_{10} = 1000_{16}$

$$\begin{array}{r} 4096 \overline{) 16} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \\ 16 \overline{) 256} \end{array}$$

8

(D) $5555_{10} = 15B3_{16}$

$$\begin{array}{r} 5555 \overline{) 16} \\ 16 \overline{) 347} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \\ 16 \overline{) 336} \end{array}$$

9

(E) $35479_{10} = 8A97_{16}$

$$\begin{array}{r} 35479 \overline{) 16} \\ 16 \overline{) 2217} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \\ 16 \overline{) 2208} \end{array}$$

10

(A) $84_{16} \rightarrow 8 = 1000, 4 = 0100$
 $84_{16} = 10000100_2$

11

(B) $7F_{16} \rightarrow 7 = 0111, F = 1111$
 $7F_{16} = 01111111_2$

12

(C) $3B8C_{16} \rightarrow 3 = 0011, B = 1011, 8 = 1000, C = 1100$
 $3B8C_{16} = 0011101110001100_2$

13

(D) $47FD_{16} \rightarrow 4 = 0100, 7 = 0111, F = 1111, D = 1101$
 $47FD_{16} = 0100011111111101_2$

14

(E) $FACD_{16} \rightarrow F = 1111, A = 1001, C = 1100, D = 1101$
 $FACD_{16} = 1111100111001101_2$

(*) a) $10011_2 = \underbrace{0001}_1 + \underbrace{0011}_3$
 $10011_2 = 13_{16}$

b) $1110011100_2 = \underbrace{0011}_3 + \underbrace{1001}_9 + \underbrace{1100}_C$
 $1110011100_2 = 39C_{16}$

c) $1001100110011_2 = \underbrace{1001}_9 + \underbrace{1001}_9 + \underbrace{0011}_3$
 $1001100110011_2 = 993_{16}$

d) $11111011110010_2 = \underbrace{0011}_3 + \underbrace{1110}_E + \underbrace{1111}_F + \underbrace{0010}_2$
 $11111011110010_2 = 3EF2_{16}$

e) $1000000000100010_2 = \underbrace{0100}_4 + \underbrace{0000}_0 + \underbrace{0001}_1 + \underbrace{0001}_1 + \underbrace{0000}_0$
 $1000000000100010_2 = 40110_{16}$



8) a) $1000_2 + 1001_2 = \begin{array}{r} 1000 \\ + 1001 \\ \hline 10001 \end{array}$

b) $10001_2 + 11110_2 = \begin{array}{r} 10001 \\ + 11110 \\ \hline 101111 \end{array}$

c) $101_2 + 100101_2 = \begin{array}{r} 101 \\ + 100101 \\ \hline 101010 \end{array}$

d) $1110_2 + 1001011_2 + 11101_2 = \begin{array}{r} 111 \\ + 1001011 \\ \hline 1011001 \end{array} + \begin{array}{r} 111 \\ + 1011001 \\ \hline 1110110_2 \end{array}$

e) $110101_2 + 1011001_2 + 1111110_2 = \begin{array}{r} 110101 \\ + 1011001 \\ \hline 1001110 \end{array} + \begin{array}{r} 111111 \\ + 10001110 \\ \hline 100001100_2 \end{array}$

9 a) $01110100_2 \xrightarrow{\text{invertido}} 10001011_2$

b) $11000010_2 \xrightarrow{\text{invertido}} 00111101_2$

10 a) $-1011_2 \xrightarrow{+1} 01011_2 \xrightarrow{\text{invertido}} 10100_2 + 1 = 10101_2$

b) $-10001_2 \xrightarrow{+1} 010001_2 \xrightarrow{\text{invertido}} 101110_2 + 1 = 101111_2$

c) $-1011101_2 \xrightarrow{\text{invertido}} 0100010_2 + 1 = 0100011_2$

d) $-11010100_2 \xrightarrow{\text{invertido}} 00101011_2 + 1 = 00101100_2$

e) $-01010011_2 \xrightarrow{\text{invertido}} 10101100_2 + 1 = 10101101_2$

11 $10110111_2 \rightarrow \text{INVERTENDO OS BITS}$

↓ negative

$10110111_2 \rightarrow 01001000_2 + 1 = 01001001_2$

CONVERTENDO p/ decimal

128	64	32	16	8	4	2	1
0	1	0	0	1	0	0	1

$= 73_{10}$

∴ O número original é negativo,

logo $\rightarrow -73_{10}$

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(12) (A) $101101_2 - 100111_2$

8 bits \downarrow \downarrow 8 bits \downarrow

00101101 00010011

$$\begin{array}{r} 100101101 \\ + 11101101 \\ \hline 100011010 \end{array}$$

DESCARTANDO O BIT À ESQUERDA TEMOS:

$00011010_2 = (26)_{10}$

(B) $10000110_2 - 110011_2$

JÁ TEM 8 bits \uparrow

$00110011_2 \xrightarrow{\text{INVERTENDO}} 11001100 + 1 = 11001101$

$$\begin{array}{r} 10000110 \\ + 11001101 \\ \hline 1011010011_2 \end{array}$$

DESCARTANDO TEMOS:

$01010011_2 = (83)_{10}$

(C) $111100_2 - 11101011_2$

8 bits \downarrow

00111100

$\hookrightarrow \text{INVERTENDO} \rightarrow 00101000 + 1 = 00101001$

$$\begin{array}{r} 00111100 \\ + 00101001 \\ \hline 01010001_2 = \end{array}$$

$(81)_{10}$

(D) $-10010011 + 11011010_2$

$\hookrightarrow \text{INVERTENDO} \rightarrow 01101100 + 1 = 01101101$

$$\begin{array}{r} 01101101 \\ + 11011010 \\ \hline 101000111_2 \end{array}$$

DESCARTANDO O BIT À ESQUERDA

$(71)_{10}$

(E) $-10011101 - 1000101_2$

8 bits \downarrow

$01000101 \xrightarrow{\text{INVERTENDO}} 10111010 + 1 = 10111011_2$

$\hookrightarrow \text{INVERTENDO} \rightarrow 01100010 + 1 = 01100011_2$

$$\begin{array}{r} 10111011 \\ + 01100011 \\ \hline 100011110 \end{array}$$

DESCARTANDO

$00011110_2 = (30)_{10}$

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(13) $44_{16} - 3E_{16}$

$44_{16} = 01000100_2$

$3E_{16} = 00111110_2 \rightarrow \text{invertido} \rightarrow 11000001 \oplus 1 = 11000010_2$

$$\begin{array}{r} 01000100 \\ + 11000010 \\ \hline \end{array}$$

00000110

DESCARTANDO, Temos $00000110_2 = (6)_{10}$

(B) $A9_{16} - E0_{16}$

$A9_{16} = 10101001_2$

$E0_{16} = 11100000_2$

$$\begin{array}{r} 10101001 \\ + 00100000 \\ \hline \end{array}$$

11001001_2

negativo

$\hookrightarrow \text{invertido} \rightarrow 00011111 \oplus 1 = 00100000_2$

$\hookrightarrow \text{invertido} \rightarrow 00101110 \oplus 1 = 00101111_2$

$(-55)_{10}$

55₁₀, como o número é negativo,

(C) $-BC_{16} + FC_{16}$

$BC_{16} = 10111100$

$-BC = 01000100$

$FC_{16} = 11111000_2$

$\hookrightarrow \text{invertido} \rightarrow 01000100 \oplus 1 = 01000101_2$

$$\begin{array}{r} 01000101 \\ + 11111000 \\ \hline \end{array}$$

001000010_2

DESCARTANDO, Temos $01000000_2 = (64)_{10}$

(D) $-22_{16} - 1D_{16}$

$\hookrightarrow \text{complemento de 2} \rightarrow 22 = 00100010 \rightarrow \text{invertido} \rightarrow 11011101_2 + 1$

$-22 = 11011101_2$

$1D = 00011101_2 \rightarrow \text{complemento de 2} \rightarrow 11100010 + 1 = 11100011_2$

$\hookrightarrow \text{complemento de 2} = 00111101_2 + 1 =$

00111111

$(-63)_{10}$

$$\begin{array}{r} 11011101 \\ + 11100011 \\ \hline \end{array}$$

11000001_2

$\hookrightarrow \text{DESCARTANDO} \text{ Temos } 11000001_2 \rightarrow \text{negativo}$