

INTERVALOS DE CONFIANZA FINAL

Time

$$x_1, x_2 \stackrel{i.i.d.}{\sim} U\left(\theta - \frac{1}{2}, \theta + \frac{1}{2}\right)$$

$$\theta \in \mathbb{R}$$

$$X = (x_1, x_2)$$

Time $m = \min\{x_1, x_2\}$

$V = (m, M)$ $M = \max\{x_1, x_2\}$

$$Pr(m \leq \theta \leq M)$$

$$= Pr(x_1 < \theta < x_2) + Pr(x_2 < \theta < x_1)$$

$$\begin{aligned} & \cancel{Pr(x_1 < \theta)} \cancel{Pr(\theta < x_2)} + \\ & \cancel{Pr(x_2 < \theta)} \cancel{Pr(\theta < x_1)} \end{aligned}$$

$$\gamma = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$$

$$I(X) = (m, M)$$

$$\Rightarrow Pr(\theta \in I(X)) = \frac{1}{2}$$

$$Pr\left(M - \frac{1}{2} \leq \theta \leq m + \frac{1}{2}\right) = 1$$

OBS

$$y \sim \begin{cases} m = y_1 \\ M = y_2 \end{cases}$$

$$\tilde{I}(x) = (m, M)$$

$$Pr(\theta \in \tilde{I}(x)) = \frac{1}{2}$$

$$y_2 - y_1 > \frac{1}{2} \Rightarrow y_1 < y_2 - \frac{1}{2}$$

$$\Rightarrow m < \theta < M$$

$$Pr(\theta \in \tilde{I}(y)) = 1$$

HIPÓTESIS

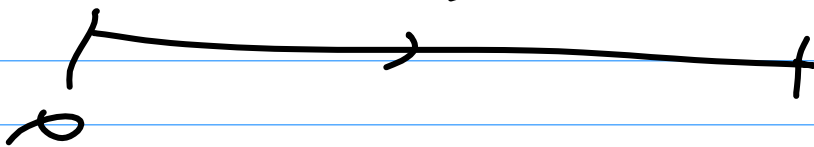
CONJUNTO X

PART. GAO

$$\tilde{X} = \{X_i : X_i \cap X_j = \emptyset, \forall i, j$$

$$\bigcup_{i=1}^n X_i = X \}$$

$$[0, 1]$$



$$(0, \frac{1}{2}), [\frac{1}{2}, 1]$$

Δ

\emptyset

$$\beta \in (-\infty, \infty)$$

$$\begin{cases} H_0 : \beta \leq 0 \\ H_1 : \beta > 0 \end{cases}$$

$$\beta > 0$$

$$\beta = \epsilon > 0$$

$$\beta = 0.001 \quad (0.0009, 0.003)$$

DE
9.1

$$C = n\sigma^2$$

ICs e
TESTES

$$X_1, \dots, X_n \sim F(\theta)$$

n PARAMETRE

$$\mu \in (0, \infty)$$

$$X_1, \dots, X_n \sim N(\underline{\mu}, \underbrace{\sigma^2}_{\text{COVARIANCE}})$$

$$\left\{ \begin{array}{l} H_0: \mu \geq \tau \\ H_1: \mu < \tau \end{array} \right.$$

$$I(X) = (A(X), B(X))$$

$$\Pr(\mu \in I(X)) \geq \gamma$$

$$\sigma^2 \in \text{COVARIANCE}$$

$$\frac{\bar{X}_n - \mu}{\sqrt{\frac{\sigma^2}{n}}} \sim N(0, 1)$$

$$z = \Phi^{-1}\left(\frac{1+\gamma}{2}\right)$$

$$A(X) = \overline{X_n} - \frac{Z}{\sqrt{\frac{\sigma^2}{n}}}$$

$$B(X) = \overline{X_n} + \frac{Z}{\sqrt{\frac{\sigma^2}{n}}}$$

→ COMPONENTES FIJOS.

$$\underline{X} = \underline{x}$$

$$Z \in I(\underline{x})$$

$$Pr(\mu \in \Lambda_0) =$$

$$Pr(Z \in I(\underline{x})) = \delta$$

HIPÓTESIS SIMPLES

$$\boxed{\mu = 7} \quad \text{???}$$

HIPÓTESIS COMPOSTA

$$\mu \in (a, b), \quad b > a$$

$$(a, b) \subset (-\infty, \infty)$$

$$H_0: \mu \neq 7$$

$$\in (0, 7) \cup (7, \infty)$$

$$H_1: \mu = 7$$

$$\text{SHARP} \quad -\infty < a < b < \infty$$

$$H_1: \mu \in (a, b)$$

EXAMPLE 1

$$H_0: \mu \in (a, b)$$

$$-\infty < a < b < \infty$$

• COMPOSITE
• BILATERAL

$$H_1: \mu \notin (a, b)$$

$$\mu \in (-\infty, a] \cup [b, \infty)$$

$\uparrow \qquad \qquad \uparrow$

EXAMPLE 2

$$H_0: \mu = \mu_0$$

• SIMPLE
• BILATERAL

$$H_1: \mu \neq \mu_0$$

$$\mu \in (-\infty, \mu_0) \cup (\mu_0, \infty)$$

$$\theta \in [0, \infty)$$

$$H_0: \theta = 0$$

$$H_1: \theta \in (0, \infty)$$