#### FUNDAÇÃO GETULIO VARGAS SCHOOL OF APPLIED MATHEMATICS

CAIO F. LINS PEIXOTO

# LINEAR INVERSE PROBLEMS AND NONPARAMETRIC REGRESSION METHODS IN INSTRUMENTAL VARIABLE ESTIMATION

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Bachelor's dissertation presented to the School of Applied Mathematics (FGV/EMAp) to obtain the Bachelor's degree in Applied Mathematics.

Area of Study: Linear Inverse Problems, Kernel Methods, Machine Learning, Nonparametric Statistics, Instrumental Variable Regression.

Advisor: Yuri F. Saporito

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Thanks, ...

#### **Abstract**

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### 1 Introduction

Remember to cite every person (NEWEY; POWELL, 2003).

## 2 Application in Econometrics: Instrumental Variable Regression

In this chapter, we turn our attention back to the main application being considered in this thesis: instrumental variable regression. We start by formally characterizing the type of problem this econometric approach was developed to solve, and then present one of the most well-known and employed estimation procedures for conducting it: two—Is it? stages least squares (2SLS). Nextly, we show how an IV regression problem can be formulated as a linear inverse problem and discuss the seminal nonparametric method of Newey and Powell (NEWEY; POWELL, 2003), followed by a more recent nonparametric approach called Kernel Instrumental Variable (KIV) (SINGH; SAHANI; GRETTON, 2019). We finish with an in-depth analysis of our method, pointing out its relationship to other methods, as well as its strengths and weaknesses.

#### 2.1 The Method of Instrumental Variables

### 3 Conclusion

#### References

NEWEY, Whitney K.; POWELL, James L. Instrumental Variable Estimation of Nonparametric Models. **Econometrica**, v. 71, n. 5, p. 1565–1578, 2003. DOI: http://dx.doi.org/10.1111/1468-0262.00459.

SINGH, Rahul; SAHANI, Maneesh; GRETTON, Arthur. Kernel Instrumental Variable Regression. In\_\_\_\_\_\_. **Advances in Neural Information Processing Systems**.

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