

7.12.2021

Seminar 10 – LR(0) parsing

Ex.: Given the grammar $G = (\{S, A\}, \{a, b, c\}, \{S \rightarrow aA, A \rightarrow bA \mid c\}, S)$, parse the sequence $w = abbc$ using an LR(0) parser.

$S' \rightarrow S$

(1) $S \rightarrow aA$

(2) $A \rightarrow bA$

(3) $A \rightarrow c$

LR(0) item $[A \rightarrow \alpha. \beta]$

$[A \rightarrow \alpha. B\beta], [B \rightarrow. \gamma]$

I. Compute canonical collection of states #VA: David T.

$s_0 = \text{closure}(\{[S' \rightarrow. S]\}) = \{[S' \rightarrow. S], [S \rightarrow. aA]\}$

$s_1 = \text{goto}(s_0, S) = \text{closure}(\{[S' \rightarrow S.]\}) = \{[S' \rightarrow S.]\}$

$\text{goto}(s_0, A) = \emptyset = \text{goto}(s_0, b) = \text{goto}(s_0, c)$

$s_2 = \text{goto}(s_0, a) = \text{closure}(\{[S \rightarrow a.A]\}) = \{[S \rightarrow a.A], [A \rightarrow. bA], [A \rightarrow. c]\}$

$s_3 = \text{goto}(s_2, A) = \text{closure}(\{[S \rightarrow aA.]\}) = \{[S \rightarrow aA.]\}$

$s_4 = \text{goto}(s_2, b) = \text{closure}(\{[A \rightarrow b.A]\}) = \{[A \rightarrow b.A], [A \rightarrow. bA], [A \rightarrow. c]\}$

$s_5 = \text{goto}(s_2, c) = \text{closure}(\{[A \rightarrow c.]\}) = \{[A \rightarrow c.]\}$

$s_6 = \text{goto}(s_4, A) = \text{closure}(\{[A \rightarrow bA.]\}) = \{[A \rightarrow bA.]\}$

$\text{goto}(s_4, b) = \text{closure}(\{[A \rightarrow b.A]\}) = s_4$

$\text{goto}(s_4, c) = \text{closure}(\{[A \rightarrow c.]\}) = s_5$

$C = \{s_0, s_1, s_2, s_3, s_4, s_5, s_6\}$

II. Build LR(0) parsing table #VA: Andrada T.

| GOTO | | | | | | |
|------|---------|---|---|---|---|---|
| | ACTION | S | A | a | b | c |
| 0 | shift | 1 | | 2 | | |
| 1 | accept | | | | | |
| 2 | shift | | 3 | | 4 | 5 |
| 3 | reduce1 | | | | | |
| 4 | shift | | 6 | | 4 | 5 |
| 5 | reduce3 | | | | | |
| 6 | reduce2 | | | | | |

III. Parse the sequence #VA: Andrada T.

| Work stack | Input stack | Output band |
|-------------|-------------|-------------|
| \$0 | abbc\$ | € |
| \$0a2 | bbc\$ | € |
| \$0a2b4 | bc\$ | € |
| \$0a2b4b4 | c\$ | € |
| \$0a2b4b4c5 | \$ | € |
| \$0a2b4b4A6 | \$ | 3 |
| \$0a2b4A6 | \$ | 23 |
| \$0a2A3 | \$ | 223 |
| \$0S1 | \$ | 1223 |
| acc | \$ | 1223 |

$S \Rightarrow aA \Rightarrow abA \Rightarrow abbA \Rightarrow abbc$ (! Rightmost derivation)