

Notebook - Maratona de Programação

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Geometria 1 1 typedef long long 11; 3 bool ge(const ll& a, const ll& b) { return a >= b; } Linear Transformation 4 bool le(const ll& a, const ll& b) { return a <= b; } 5 bool eq(const ll& a, const ll& b) { return a == b; } $_1$ // Apply linear transformation (p -> q) to r. 6 bool gt(const ll& a, const ll& b) { return a > b; } point linear_transformation(point p0, point p1, point 7 bool lt(const ll& a, const ll& b) { return a < b; } q0, point q1, point r) { 8 int sgn(const ll& a) { return a >= 0 ? a ? 1 : 0 : point dp = p1-p0, dq = q1-q0, $num((dp^dq)$, (dp^dq) return q0 + point((r-p0)^(num), (r-p0)*(num))/(dp $_{10}$ struct pt { *dp); 11 x, y; 5 } pt() { } 12 pt(11 _x, 11 _y) : x(_x), y(_y) { } 13 Inside Polygon pt operator - (const pt& p) const { 14 return pt(x - p.x, y - p.y); 15 1 // Convex O(logn) 16 11 cross(const pt& p) const { 3 bool insideT(point a, point b, point c, point e){ return x * p.y - y * p.x; int x = ccw(a, b, e); 19 11 cross(const pt& a, const pt& b) const { int y = ccw(b, c, e); 20 return (a - *this).cross(b - *this); int z = ccw(c, a, e); 21 return !((x==1 or y==1 or z==1) and (x==-1 or y22 11 dot(const pt& p) const { ==-1 or z==-1)):**return** x * p.x + y * p.y; 24 25 11 dot(const pt& a, const pt& b) const { 10 bool inside(vp &p, point e){ // ccw 26 return (a - *this).dot(b - *this); 27 int 1=2, r=(int)p.size()-1; 28 while(1<r){ 12 11 sqrLength() const { int mid = (1+r)/2; 29 30 return this -> dot(*this); 14 if(ccw(p[0], p[mid], e) == 1) 1 = m i d + 1; 3.1 15 3.2 bool operator == (const pt& p) const { else{ 16 r=mid; 33 return eq(x, p.x) && eq(y, p.y); } 34 35 }; } 19 20 // if(r==(int)p.size()-1 and ccw(p[0], p[r], e) 37 const pt inf_pt = pt(1e18, 1e18); 21 ==0) return false; 38 39 struct QuadEdge { // if(r==2 and ccw(p[0], p[1], e)==0) return40 pt origin; false: // if(ccw(p[r], p[r-1], e) == 0) return false; QuadEdge* rot = nullptr; 41 QuadEdge* onext = nullptr; 42 return insideT(p[0], p[r-1], p[r], e); 24 43 bool used = false; 25 } QuadEdge* rev() const { 44 26 45 return rot->rot; 27 28 // Any O(n) 46 QuadEdge* lnext() const { return rot ->rev() ->onext ->rot; 30 int inside(vp &p, point pp){ 48 // 1 - inside / 0 - boundary / -1 - outside 49 3.1 50 QuadEdge* oprev() const { 32 int n = p.size(); return rot -> onext -> rot; for(int i=0;i<n;i++){</pre> 51 33 int j = (i+1) %n;52 34 pt dest() const { if(line({p[i], p[j]}).inside_seg(pp)) 5.3 5.4 return rev() -> origin; return 0: 36 55 37 56 }; int inter = 0; 57 for (int i = 0; i < n; i++) {</pre> 39 58 QuadEdge* make_edge(pt from, pt to) { int j = (i+1)%n;QuadEdge* e1 = new QuadEdge; if($p[i].x \le pp.x$ and $pp.x \le p[j].x$ and $ccw(p^{59}$ 41 QuadEdge* e2 = new QuadEdge; [i], p[j], pp)==1) QuadEdge* e3 = new QuadEdge; inter++; // up 6.1 42 else if($p[j].x \le pp.x$ and $pp.x \le p[i].x$ and 62 QuadEdge* e4 = new QuadEdge; 43 e1->origin = from; ccw(p[i], p[j], pp) == -1) 63 inter++; // down e2->origin = to; 44 e3->origin = e4->origin = inf_pt; 65

1.3 Delaunay

if(inter%2==0) return -1; // outside

else return 1; // inside

46

49 }

66

67

68

69

70

71

7.2

e1 - > rot = e3:

e2 - > rot = e4;

 $e3 \rightarrow rot = e2;$

e4 - > rot = e1;

e1 -> onext = e1:

 $e2 \rightarrow onext = e2$:

e3 - > onext = e4;

```
137 #endif
       e4 -  onext = e3:
7.3
74
       return e1;
                                                            138 }
75 }
                                                            139
                                                            140 pair < QuadEdge*, QuadEdge*> build_tr(int 1, int r,
void splice(QuadEdge* a, QuadEdge* b) {
                                                                   vector <pt>& p) {
       swap(a->onext->rot->onext, b->onext->rot->onext);141
                                                                   if (r - 1 + 1 == 2) {
78
       swap(a->onext, b->onext);
                                                                       QuadEdge* res = make_edge(p[1], p[r]);
79
                                                           142
80 }
                                                                       return make_pair(res, res->rev());
                                                           143
81
                                                           144
82 void delete_edge(QuadEdge* e) {
                                                                   if (r - 1 + 1 == 3) {
                                                            145
       splice(e, e->oprev());
                                                                       QuadEdge *a = make_edge(p[1], p[1 + 1]), *b =
83
                                                            146
84
       splice(e->rev(), e->rev()->oprev());
                                                                    make_edge(p[l + 1], p[r]);
       delete e->rev()->rot;
                                                                       splice(a->rev(), b);
85
                                                            147
       delete e->rev();
                                                                       int sg = sgn(p[1].cross(p[1 + 1], p[r]));
86
                                                            148
                                                                       if (sg == 0)
87
       delete e->rot;
                                                            149
       delete e;
                                                                            return make_pair(a, b->rev());
88
89 }
                                                                       QuadEdge* c = connect(b, a);
                                                                       if (sg == 1)
90
                                                                            return make_pair(a, b->rev());
91 QuadEdge* connect(QuadEdge* a, QuadEdge* b) {
       QuadEdge* e = make_edge(a->dest(), b->origin);
92
                                                            154
                                                                       else
       splice(e, a->lnext());
                                                                           return make_pair(c->rev(), c);
93
                                                                   }
       splice(e->rev(), b);
94
       return e:
                                                                   int mid = (1 + r) / 2;
9.5
96 }
                                                                   QuadEdge *ldo, *ldi, *rdo, *rdi;
                                                            158
                                                                   tie(ldo, ldi) = build_tr(l, mid, p);
97
98 bool left_of(pt p, QuadEdge* e) {
                                                                   tie(rdi, rdo) = build_tr(mid + 1, r, p);
                                                                   while (true) {
99
       return gt(p.cross(e->origin, e->dest()), 0);
100 }
                                                                       if (left_of(rdi->origin, ldi)) {
                                                                            ldi = ldi->lnext();
102 bool right_of(pt p, QuadEdge* e) {
                                                                            continue:
                                                            164
       return lt(p.cross(e->origin, e->dest()), 0);
103
104 }
                                                                       if (right_of(ldi->origin, rdi)) {
                                                                           rdi = rdi->rev()->onext;
106 template <class T>
                                                            168
                                                                            continue;
_{\rm 107} T det3(T a1, T a2, T a3, T b1, T b2, T b3, T c1, T c2 _{\rm 169}
                                                                       }
       , T c3) {
       return a1 * (b2 * c3 - c2 * b3) - a2 * (b1 * c3 -171
108
                                                                   QuadEdge* basel = connect(rdi->rev(), ldi);
               a3 * (b1 * c2 - c1 * b2);
                                                                   auto valid = [&basel](QuadEdge* e) { return
109
                                                            173
                                                                   right_of(e->dest(), basel); };
110 }
                                                                   if (ldi->origin == ldo->origin)
112 bool in_circle(pt a, pt b, pt c, pt d) {
                                                                       ldo = basel->rev();
_{\rm 113} // If there is <code>__int128</code>, calculate directly.
                                                                   if (rdi->origin == rdo->origin)
114 // Otherwise, calculate angles.
                                                                       rdo = basel;
#if defined(__LP64__) || defined(_WIN64)
                                                            178
                                                                   while (true) {
       \__int128 det = -det3 < \__int128 > (b.x, b.y, b.
                                                           179
                                                                       QuadEdge* lcand = basel->rev()->onext;
116
                                                                       if (valid(lcand)) {
       sqrLength(), c.x, c.y,
                                                            180
                                         c.sqrLength(), d.x181
                                                                            while (in_circle(basel->dest(), basel->
       , d.y, d.sqrLength());
                                                                   origin, lcand->dest(),
       det += det3<__int128>(a.x, a.y, a.sqrLength(), c.182
                                                                                              lcand -> onext -> dest())) {
118
                                                                                QuadEdge* t = lcand->onext;
       x, c.y, c.sqrLength(), d.x,
                                                                                delete_edge(lcand);
                              d.y, d.sqrLength());
119
                                                           184
       det -= det3<__int128>(a.x, a.y, a.sqrLength(), b.185
                                                                                lcand = t;
       x, b.y, b.sqrLength(), d.x,
                                                           186
                               d.y, d.sqrLength());
                                                           187
                                                                       QuadEdge* rcand = basel->oprev();
       det += det3<__int128>(a.x, a.y, a.sqrLength(), b.188
       x, b.y, b.sqrLength(), c.x,
                                                                       if (valid(rcand)) {
                                                           189
                               c.y, c.sqrLength());
                                                                            while (in_circle(basel->dest(), basel->
123
                                                                   origin, rcand->dest(),
124
       return det > 0:
                                                                                              rcand -> oprev() -> dest()))
125 #else
       auto ang = [](pt 1, pt mid, pt r) {
126
           11 x = mid.dot(1, r);
                                                                                QuadEdge* t = rcand->oprev();
           11 y = mid.cross(1, r);
                                                                                delete_edge(rcand);
128
           long double res = atan2((long double)x, (long194
                                                                                rcand = t;
        double)y);
130
           return res:
                                                                       if (!valid(lcand) && !valid(rcand))
       long double kek = ang(a, b, c) + ang(c, d, a) -
                                                                            break:
                                                           198
       ang(b, c, d) - ang(d, a, b);
                                                                       if (!valid(lcand) ||
       if (kek > 1e-8)
                                                                            (valid(rcand) && in_circle(lcand->dest(),
                                                            200
           return true:
                                                                    lcand ->origin ,
134
                                                            201
                                                                                                         rcand->origin,
136
            return false;
                                                                    rcand -> dest())))
```

```
basel = connect(rcand, basel->rev());
                                                                if(a.x>0 and a.y>=0) return 0;
202
203
           else
                                                                  if(a.x<=0 and a.y>0) return 1;
                                                                  if(a.x<0 and a.y<=0) return 2;
               basel = connect(basel->rev(), lcand->rev 5
204
       ());
                                                                  return 3;
       }
                                                            7 }
       return make_pair(ldo, rdo);
206
                                                            9 bool comp(point a, point b) { // ccw
207 }
                                                                 int qa = quadrants(a);
208
                                                            1.0
209 vector<tuple<pt, pt, pt>> delaunay(vector<pt> p) {
                                                                  int qb = quadrants(b);
                                                           11
                                                                  if(qa == qb) return (a ^ b) > 0;
       sort(p.begin(), p.end(), [](const pt& a, const pt 12
                                                                  else return qa < qb;</pre>
       & b) {
                                                           13
           return lt(a.x, b.x) || (eq(a.x, b.x) && lt(a.14)
       y, b.y));
                                                            _{16} // only vectors in range [x+0, x+180)
       });
212
       auto res = build_tr(0, (int)p.size() - 1, p);
213
                                                           17 bool comp(point a, point b){
       QuadEdge* e = res.first;
                                                                  return (a ^ b) > 0; // ccw
214
                                                           18
                                                                  // return (a ^ b) < 0; // cw
215
       vector < QuadEdge*> edges = {e};
                                                            19
       while (lt(e->onext->dest().cross(e->dest(), e->
                                                           20 }
216
       origin), 0))
                                                              1.6 Minkowski Sum
217
           e = e->onext;
       auto add = [&p, &e, &edges]() {
218
           QuadEdge* curr = e;
219
                                                            vp mk(const vp &a,const vp &b){
           do {
220
                                                                  int i = 0, j = 0;
               curr->used = true;
221
                                                                  for(int k = 0; k < (int)a.size(); k++)if(a[k] < a[i</pre>
               p.push_back(curr->origin);
222
                                                                  ٦)
                edges.push_back(curr->rev());
223
                                                                       i = k:
                                                            4
                curr = curr->lnext();
224
                                                                  for(int k = 0; k < (int)b.size(); k++)if(b[k] < b[j</pre>
                                                            5
           } while (curr != e);
225
                                                                  1)
       };
226
                                                                      j = k;
       add();
                                                            7
228
       p.clear();
                                                            8
                                                                  vp c;
       int kek = 0;
229
                                                                  c.reserve(a.size() + b.size());
                                                            9
       while (kek < (int)edges.size()) {</pre>
                                                                  for(int k = 0; k < int(a.size()+b.size()); k++){</pre>
                                                           10
231
           if (!(e = edges[kek++])->used)
                                                                       point pt{a[i] + b[j]};
               add();
232
                                                                       if((int)c.size() >= 2 and !ccw(c[c.size()-2],
233
                                                                   c.back(), pt))
       vector < tuple < pt , pt , pt >> ans;
234
                                                                          c.pop_back();
       for (int i = 0; i < (int)p.size(); i += 3) {</pre>
235
                                                                       c.pb(pt);
                                                           14
           ans.push_back(make_tuple(p[i], p[i + 1], p[i
236
                                                                      int q = i+1, w = j+1;
       + 21)):
                                                                      if(q == int(a.size())) q = 0;
                                                            16
                                                            17
                                                                       if(w == int(b.size())) w = 0;
238
       return ans;
                                                                      if(ccw(c.back(), a[i]+b[w], a[q]+b[j]) < 0) i
                                                            18
239 }
                                                                   = q;
                                                           19
                                                                       else j = w;
   1.4 Convex Hull
                                                           20
                                                           21
 vp convex_hull(vp P)
                                                                  if(!ccw(c[0], c[(int)c.size()-1], c[(int)c.size()
                                                           22
 3
       sort(P.begin(), P.end());
                                                           2.3
                                                                       c.pop_back();
       vp L, U;
                                                                  if(!ccw(c.back(), c[0], c[1])){
 4
                                                           24
       for(auto p: P){
                                                                       c[0]=c.back();
                                                           25
           while(L.size()>=2 and ccw(L.end()[-2], L.back 26
                                                                       c.pop_back();
       (), p)!=1)
                                                           27
              L.pop_back();
                                                           28
                                                                  c.shrink_to_fit();
           L.pb(p);
                                                           2.9
 9
                                                           30
                                                                  return c;
       reverse(P.begin(), P.end());
                                                           31 }
 10
       for(auto p: P){
           while (U.size() \ge 2 \text{ and } ccw(U.end()[-2], U.back } 1.7
                                                                    Tetrahedron Distance3d
 12
       (), p)!=1)
               U.pop_back();
 13
                                                            1 bool nulo(point a){
           U.pb(p);
14
                                                                  return (eq(a.x, 0) and eq(a.y, 0) and eq(a.z, 0))
       }
       L.pop_back();
16
                                                            3 }
       L.insert(L.end(), U.begin(), U.end()-1);
 17
18
       return L;
                                                            5 ld misto(point p1, point p2, point p3){
 19 }
                                                            6
                                                                  return (p1^p2)*p3;
                                                            7 }
   1.5 Sort By Angle
                                                            9 ld dist_pt_face(point p, vp v){
 int quadrants(point a)
                                                                 assert(v.size()==3);
                                                           10
```

```
point v1 = v[1]-v[0];
                                                                           point n2 = v2^n;
                                                            7.8
13
       point v2 = v[2] - v[0];
                                                            79
                                                                            point o1o2 = 12[0]-11[0];
                                                                            1d escalar = (o1o2*n2)/(v1*n2);
       point n = (v1^v2);
14
                                                            80
                                                            8.1
                                                                            if(escalar < 0 or escalar > 1) ok = false;
       for(int i=0;i<3;i++){
                                                                            swap(11,12);
           point va = p-v[i];
                                                                            swap(v1,v2);
17
                                                            83
           point vb = v[(i+1)%3]-v[i];
           point ve = vb^n;
                                                                       if(ok) ans = min(ans,dist_line(11,12));
19
                                                            8.5
           ld d = ve*v[i];
20
                                                            86
           //se ponto coplanar com um dos lados do
                                                            87
      prisma (va^vb eh nulo),
                                                                   return ans;
                                                            88
          //ele esta dentro do prisma (poderia
                                                            89 }
       desconsiderar pois distancia
                                                            90
                                                            91 ld ver(vector<vp> &vet){
          //vai ser a msm da distancia do ponto ao
                                                                   ld ans = LLINF;
       segmento)
                                                            92
           if (! nulo(va^vb) and (v[(i+2)%3]*ve>d) ^ (p*ve 93)
                                                                   // vertice - face
24
      >d)) return LLINF;
                                                            94
                                                                   for(int k=0; k<2; k++)
                                                                       for(int pt=0;pt<4;pt++)</pre>
25
                                                            9.5
                                                                           for (int i=0; i<4; i++) {
       //se ponto for coplanar ao triangulo (e dentro do 97
27
                                                                                vp v;
       triangulo)
                                                                                for(int j=0;j<4;j++){
                                                            98
       //vai retornar zero corretamente
                                                                                    if(i!=j) v.pb(vet[!k][j]);
                                                            99
       return fabs(misto(p-v[0],v1,v2)/norm(n));
29
                                                           100
30 }
                                                                                ans = min(ans, dist_pt_face(vet[k][pt
                                                                   ], v));
3.1
32 ld dist_pt_seg(point p, vp li){
       return norm((li[1]-li[0])^(p-li[0]))/norm(li[1]-103
33
      li[0]);
                                                                   // edge - edge
                                                           104
34 }
                                                                   for(int i1=0;i1<4;i1++)</pre>
                                                           105
                                                                       for(int j1=0;j1<i1;j1++)</pre>
3.5
                                                           106
36 ld dist_line(vp l1, vp l2){
                                                                            for(int i2=0;i2<4;i2++)
       point n = (11[1]-11[0])^(12[1]-12[0]);
                                                                                for(int j2=0; j2<i2; j2++)</pre>
3.7
                                                           108
       if(nulo(n)) //retas paralelas - dist ponto a reta109
                                                                                    ans = min(ans, dist_seg({vet[0][
38
                                                                   i1], vet[0][j1]},
           return dist_pt_seg(12[0],11);
                                                                                                              {vet[1][
40
       point o1o2 = 12[0]-11[0];
                                                                   i2], vet[1][j2]}));
41
       return fabs((o1o2*n)/norm(n)):
42
43 }
                                                           112
                                                                   return ans;
44 // retas paralelas e intersecao nao nula
                                                           113 }
45 ld dist_seg(vp l1, vp l2){
                                                              1.8
                                                                    Numintersectionline
46
       assert(12.size() == 2);
47
       assert(11.size()==2);
48
                                                            int main()
49
                                                            2 {
       //pontos extremos do segmento
50
                                                                   int lim = 1e6:
51
       ld ans = LLINF;
                                                                   Segtree st(lim+100);
                                                             4
       for(int i=0;i<2;i++)
52
                                                                   int n, m, y, x, 1, r;
           for(int j=0;j<2;j++)
                                                                   cin >> n >> m;
               ans = min(ans, norm(l1[i]-l2[j]));
54
                                                                   int open=-1, close=INF; // open -> check -> close
       //verificando distancia de ponto extremo com
56
                                                                   vector< pair<int, pii> > sweep;
                                                            9
      ponto interno dos segs
       for(int t=0;t<2;t++){
57
                                                                   11 \text{ ans} = 0:
                                                            11
           for(int i=0;i<2;i++){</pre>
58
                                                                   for(int i=0;i<n;i++){ // horizontal</pre>
               bool c=true;
59
                                                                       cin >> y >> 1 >> r;
                                                            1.3
               for(int k=0;k<2;k++){
60
                                                            1.4
                                                                       sweep.pb({1, {open, y}});
                   point va = 11[i]-12[k];
61
                                                                       sweep.pb({r, {close, y}});
                                                            15
                    point vb = 12[!k]-12[k];
                                                            16
                    ld ang = atan2(norm((vb^va)), vb*va); 17
63
                                                                   for(int i=0;i<m;i++){ // vertical</pre>
                    if(ang>PI/2) c = false;
64
                                                                       cin >> x >> 1 >> r;
                                                            18
               }
6.5
                                                                       sweep.pb({x, {1, r}});
                                                            19
               if(c)
                    ans = min(ans, dist_pt_seg(l1[i], 12)); 21
                                                                   sort(sweep.begin(), sweep.end());
           }
68
           swap(11,12);
                                                                   // set < int > on;
                                                            23
      }
70
                                                                   for(auto s: sweep){
71
                                                            25
                                                                       if(s.ss.ff == open) {
       //ponto interno com ponto interno dos segmentos
72
                                                                           st.update(s.ss.ss, 1);
       point v1 = 11[1]-11[0], v2 = 12[1]-12[0];
73
                                                                            // on.insert(s.ss.ss);
                                                            27
       point n = v1^v2;
74
                                                            28
       if(!nulo(n)){
75
                                                                       else if(s.ss.ff==close){
           bool ok = true;
                                                                           st.update(s.ss.ss, -1);
                                                            3.0
77
           for(int t=0;t<2;t++){
                                                                           // on.erase(s.ss.ss);
                                                            31
```

```
}
                                                          25 }
32
33
           else{
              ans += st.query(s.ss.ff, s.ss.ss);
34
                                                            1.11 Mindistpair
              // auto it1 = on.lower_bound(s.ss.ff);
               // auto it2 = on.upper_bound(s.ss.ss);
                                                           1 11 MinDistPair(vp &vet){
               // for(auto it = it1; it!=it2; it++){
37
                                                                int n = vet.size();
               //
                      intersection -> (s.ff, it);
                                                                 sort(vet.begin(), vet.end());
               // }
39
                                                                 set <point > s;
          }
40
      }
41
                                                                 ll best_dist = LLINF;
42
                                                                 int j = 0;
43
      cout << ans << endl;
                                                                 for(int i=0;i<n;i++){</pre>
44
                                                                     11 d = ceil(sqrt(best_dist));
45
                                                                     while (j < n \text{ and } vet[i].x-vet[j].x >= d){
                                                          10
46
      return 0;
                                                          11
                                                                         s.erase(point(vet[j].y, vet[j].x));
                                                          12
                                                                         j++:
                                                                     }
                                                          13
  1.9 Polygon Diameter
                                                          14
                                                                     auto it1 = s.lower_bound({vet[i].y - d, vet[i
                                                          15
double diameter(const vector<point> &p) {
                                                                 ].x});
      vector < point > h = convexHull(p);
                                                                     auto it2 = s.upper_bound({vet[i].y + d, vet[i
                                                          16
      int m = h.size();
                                                                 ].x});
      if (m == 1)
                                                          17
          return 0;
                                                                     for(auto it=it1; it!=it2; it++){
                                                          18
      if (m == 2)
                                                                         11 dx = vet[i].x - it->y;
                                                          19
          return dist(h[0], h[1]);
                                                          20
                                                                         11 dy = vet[i].y - it->x;
      int k = 1;
                                                                         if(best_dist > dx*dx + dy*dy){
      while (area(h[m - 1], h[0], h[(k + 1) % m]) >
                                                                             best_dist = dx*dx + dy*dy;
      area(h[m - 1], h[0], h[k]))
                                                                             // vet[i] e inv(it)
          ++k;
                                                                         }
10
                                                          24
      double res = 0;
                                                          25
      for (int i = 0, j = k; i \le k && j \le m; i++) {
12
          res = max(res, dist(h[i], h[j]));
                                                                     s.insert(point(vet[i].y, vet[i].x));
13
          while (j < m && area(h[i], h[(i + 1) % m], h _{28}
      [(j + 1) \% m]) > area(h[i], h[(i + 1) \% m], h[j]) 29
                                                                 return best dist:
      ) {
               res = max(res, dist(h[i], h[(j + 1) % m])
      );
                                                            1.12
                                                                    Rotating Callipers
16
               ++j;
          }
                                                           1 int N;
19
      return res;
                                                           3 int sum(int i, int x){
20 }
                                                                if(i+x>N-1) return (i+x-N);
                                                           4
                                                                 return i+x;
  1.10 Polygon Cut Length
                                                          6 }
1 // Polygon Cut length
                                                          8 ld rotating_callipers(vp &vet){
2 ld solve(vp &p, point a, point b){ // ccw
                                                                 N = vet.size();
                                                                 ld ans = 0;
      int n = p.size();
                                                          10
      1d ans = 0;
                                                                 11
                                                                 for(int i=0;i<N;i++){ // p1</pre>
      for (int i = 0; i < n; i + +) {</pre>
                                                                     int p2 = sum(i, 1); // p2
                                                          13
          int j = (i+1) % n;
                                                                     int p4 = sum(i, 3); // p4
                                                          14
                                                                     for(int j=sum(i, 2); j!=i; j=sum(j, 1)){ // p3
                                                          15
q
           int signi = ccw(a, b, p[i]);
                                                          16
                                                                         if(j==p2) p2 = sum(p2, 1);
                                                                         while(sum(p2, 1)!=j and areaT(vet[p2],
           int signj = ccw(a, b, p[j]);
10
                                                          17
                                                                 vet[i], vet[j]) < areaT(vet[sum(p2, 1)], vet[i],</pre>
           if(signi == 0 and signj == 0){
                                                                 vet[j]))
              if((b-a) * (p[j]-p[i]) > 0){
13
                                                          18
                                                                             p2 = sum(p2, 1);
                   ans += param(a, b, p[j]);
                                                                         while (sum(p4, 1)!=i and areaT(vet[p4],
14
                   ans -= param(a, b, p[i]);
                                                                 vet[i], vet[j]) < areaT(vet[sum(p4, 1)], vet[i],</pre>
15
                                                                 vet[j]))
16
          }else if(signi <= 0 and signj > 0){
                                                                             p4 = sum(p4, 1);
              ans -= param(a, b, inter_line({a, b}, {p[21]})
18
                                                                         ans = max(ans, area(vet[i], vet[p2], vet[
      i], p[j]})[0]);
19
          }else if(signi > 0 and signj <= 0){</pre>
                                                                 j], vet[p4]));
20
               ans += param(a, b, inter_line({a, b}, {p[23]
                                                                     }
      i], p[j]})[0]);
21
                                                          2.5
                                                                 return ans;
                                                          26
                                                          27 }
23
```

return abs(ans * norm(b-a));

24

1.13 Half Plane Intersect

```
1 // Half plane intersect O(n3)
vp half_plane_intersect(vector<line> &v){
      vp ret;
       int n = v.size();
      for(int i=0; i<n; i++){</pre>
          for(int j=i+1; j<n; j++){
               point crs = inter(v[i], v[j]);
               if(crs.x == INF) continue;
               bool bad = 0;
               for(int k=0; k<n; k++)</pre>
1.0
                   if(v[k].eval(crs) < -EPS){</pre>
                        bad = 1;
13
                        break;
1.5
               if(!bad) ret.push_back(crs);
           }
18
       return ret;
19
20 }
```

$1.14 \quad 2d$

```
point p1((a1*b1), abs((a1^b1)));
                                                          63
                                                                 point p2((a2*b2), abs((a2^b2)));
1 #define vp vector<point>
                                                          64
                                                                 return (p1^p2) <= 0;
                                                          65
                                                          66 }
3 // typedef ll cod;
4 // bool eq(cod a, cod b) { return (a==b); }
                                                          6.7
                                                          68 ld area(vp &p){ // (points sorted)
5 typedef ld cod;
                                                              ld ret = 0;
6 bool eq(cod a, cod b){ return abs(a - b) <= EPS; }</pre>
                                                          69
                                                                 for(int i=2;i<(int)p.size();i++)</pre>
                                                          7.0
8 struct point{
                                                          7.1
                                                                    ret += (p[i]-p[0])^(p[i-1]-p[0]);
                                                                 return abs(ret/2);
      cod x, y;
                                                          72
                                                          73 }
      int id;
1.0
                                                          74 ld areaT(point &a, point &b, point &c){
      point(cod x=0, cod y=0): x(x), y(y){}
11
                                                                 return abs((b-a)^(c-a))/2.0;
                                                          7.5
12
      point operator+(const point &o) const{ return {x+76 }
13
      o.x, y+o.y}; }
      point operator-(const point &o) const{ return {x-78 point center(vp &A){
14
      o.x, y-o.y}; }
                                                               point c = point();
                                                                int len = A.size();
      point operator*(cod t) const{ return {x*t, y*t}; 80
1.5
                                                          8.1
                                                                for(int i=0;i<len;i++)</pre>
      point operator/(cod t) const{ return {x/t, y/t}; 82
                                                                 return c/len;
      cod operator*(const point &o) const{ return x * o 84 }
      .x + y * o.y; }
      cod operator^(const point &o) const{ return x * 0 86 point forca_mod(point p, ld m){
                                                         87 ld cm = norm(p);
      .y - y * o.x; }
                                                          88
                                                                if(cm<EPS) return point();</pre>
      bool operator<(const point &o) const{</pre>
19
                                                                return point(p.x*m/cm,p.y*m/cm);
          return (eq(x, o.x) ? y < o.y : x < o.x);
                                                          89
                                                         90 }
21
      bool operator == (const point &o) const{
                                                          9.1
                                                          92 ld param(point a, point b, point v){
          return eq(x, o.x) and eq(y, o.y);
23
                                                                 // v = t*(b-a) + a // return t;
                                                          93
24
                                                                 // assert(line(a, b).inside_seg(v));
                                                          94
25
                                                          95
                                                                 return ((v-a) * (b-a)) / ((b-a) * (b-a));
26 };
                                                          96 }
28 ld norm(point a){ // Modulo
                                                          97
                                                          98 bool simetric(vector<point> &a){ //ordered
29
      return sqrt(a*a);
                                                          99
                                                               int n = a.size();
30 }
                                                                c = center(a);
                                                         100
                                                                if(n&1) return false;
32 int ccw(point a, point b, point e){ //-1=dir; 0=
      collinear; 1=esq;
cod tmp = (b-a) ^ (e-a); // from a to b
                                                         102
                                                                 for(int i=0;i<n/2;i++)
                                                                     if(!collinear(a[i], a[i+n/2], c))
                                                         103
                                                         104
                                                                        return false;
      return (tmp > EPS) - (tmp < -EPS);</pre>
34
35 }
                                                         105
                                                                 return true;
                                                         106
37 bool nulo(point a){
                                                         107
                                                         108 point mirror(point m1, point m2, point p){
     return (eq(a.x, 0) and eq(a.y, 0));
                                                         109
                                                               // mirror point p around segment m1m2
                                                                 point seg = m2-m1;
                                                         110
40 point rotccw(point p, ld a){
```

// a = PI*a/180; // graus

47 ld proj(point a, point b){ // a sobre b

50 ld angle(point a, point b){ // em radianos

ld ang = a*b / norm(a) / norm(b);

return a*b/norm(b);

return atan2(v.x, v.y);

ld aux = angle(a,b)*180/PI;

return ((a^b) <=0 ? aux:360-aux);

b2){ // ang(a1,b1) <= ang(a2,b2)

+p.x*sin(a)));

54 ld angle_vec(point v){

(a in front of b)

return point((p.x*cos(a)-p.y*sin(a)), (p.y*cos(a)

44 point rot90cw(point a) { return point(a.y, -a.x); };

45 point rot90ccw(point a) { return point(-a.y, a.x); };

return acos(max(min(ang, (ld)1), (ld)-1));

// return 180/PI*atan2(v.x, v.y); // graus

58 ld order_angle(point a, point b){ // from a to b ccw

62 bool angle_less(point a1, point b1, point a2, point

4.1

43 }

48

49 }

51

52

55 56

59

60

61 }

57 }

53 }

```
1d t0 = ((p-m1)*seg) / (seg*seg);
                                                                     return {}:
                                                          181
       point ort = m1 + seg*t0;
                                                          182
                                                                 return ans;
       point pm = ort-(p-ort);
                                                          183
113
       return pm;
                                                          184
114
115 }
                                                          185 ld dist_seg(point p, point a, point b){ // point -
116
                                                                 if(((p-a)*(b-a)) < EPS) return norm(p-a);
118 ///////////
                                                                 if(((p-b)*(a-b)) < EPS) return norm(p-b);
                                                          187
                                                                 return abs((p-a)^(b-a))/norm(b-a);
119 // Line //
                                                          188
120 ///////////
                                                          189 }
                                                          190
                                                          191 ld dist_line(point p, line l){ // point - line
122
   struct line{
                                                                 return abs(l.eval(p))/sqrt(l.a*l.a + l.b*l.b);
123
       point p1, p2;
                                                          192
       cod a, b, c; // ax+by+c = 0;
                                                          193
124
       // y-y1 = ((y2-y1)/(x2-x1))(x-x1)
                                                          194
       line(point p1=0, point p2=0): p1(p1), p2(p2){
                                                          195 line bisector(point a, point b){
126
           a = p1.y - p2.y;
b = p2.x - p1.x;
127
                                                                 point d = (b-a)*2;
                                                                 return line(d.x, d.y, a*a - b*b);
128
                                                          197
           c = p1 ^p2;
                                                          198 }
130
                                                          199
                                                          200 line perpendicular(line 1, point p){ // passes
           if(a < 0){
131
               a *= -1;
                                                                 through p
               b *= -1;
                                                                 return line(1.b, -1.a, -1.b*p.x + 1.a*p.y);
                                                          201
               c *= -1;
                                                          202 }
134
           }
                                                          203
136
                                                          204
       line(cod a=0, cod b=0, cod c=0): a(a), b(b), c(c)205 //////////
137
                                                          206 // Circle //
           // isso aqui eh um lixo mas quebra um galho 208
139
       kkkkkk
                                                          209 struct circle{
           if(b==0){}
                                                                 point c; cod r;
140
                                                          210
               p1 = point(1, -c/a);
                                                                 circle() : c(0, 0), r(0){}
                                                          211
141
               p2 = point(0, -c/a);
                                                          212
                                                                 circle(const point o) : c(o), r(0){}
                                                                 circle(const point a, const point b){
           }else{
                                                          213
143
               p1 = point(1, (-c-a*1)/b);
                                                                      c = (a+b)/2;
144
                                                          214
                                                                     r = norm(a-c);
               p2 = point(0, -c/b);
145
                                                          215
           }
                                                          216
146
       }
                                                                 circle(const point a, const point b, const point
147
                                                          217
148
149
       cod eval(point p){
                                                                     c = inter_line(bisector(a, b), bisector(b, cc
                                                                 ));
           return a*p.x+b*p.y+c;
                                                          219
                                                                     r = norm(a-c);
       bool inside(point p){
                                                          220
           return eq(eval(p), 0);
                                                          221
                                                                 bool inside(const point &a) const{
                                                          222
                                                                      return norm(a - c) <= r + EPS;
154
       point normal(){
                                                          223
           return point(a, b);
                                                          224 };
                                                          225
158
                                                          226 pair < point , point > tangent_points(circle cr, point p)
       bool inside_seg(point p){
159
                                                                 1d d1 = norm(p-cr.c), theta = asin(cr.r/d1);
           return (
160
                                                          227
               ((p1-p) ^ (p2-p)) == 0 and
                                                                 point p1 = rotccw(cr.c-p, -theta);
                                                          228
               ((p1-p) * (p2-p)) <= 0
                                                                 point p2 = rotccw(cr.c-p, theta);
                                                          229
           ):
                                                                 assert(d1 >= cr.r);
       }
                                                                 p1 = p1 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
164
                                                                 p2 = p2 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
                                                          232
166 }:
                                                                 return {p1, p2};
                                                          233
167
                                                          234 }
     be careful with precision error
168 //
                                                          235
169 vp inter_line(line l1, line l2){
                                                          236
       ld det = l1.a*l2.b - l1.b*l2.a;
                                                          237 circle incircle(point p1, point p2, point p3){
170
       if(det==0) return {};
                                                          238
                                                                 1d m1 = norm(p2-p3);
                                                                 1d m2 = norm(p1-p3);
       1d x = (11.b*12.c - 11.c*12.b)/det;
                                                          239
172
       1d y = (11.c*12.a - 11.a*12.c)/det;
173
                                                          240
                                                                 1d m3 = norm(p1-p2);
                                                                 point c = (p1*m1 + p2*m2 + p3*m3)*(1/(m1+m2+m3));
       return {point(x, y)};
174
                                                          241
175 }
                                                          242
                                                                 1d s = 0.5*(m1+m2+m3);
176
                                                          243
                                                                 1d r = sqrt(s*(s-m1)*(s-m2)*(s-m3)) / s;
177 // segments not collinear
                                                                 return circle(c, r);
                                                          244
                                                          245 }
178 vp inter_seg(line l1, line l2){
       vp ans = inter_line(l1, l2);
179
                                                          246
       if(ans.empty() or !11.inside_seg(ans[0]) or !12.247 circle circumcircle(point a, point b, point c) {
       inside_seg(ans[0]))
                                                          248
                                                                 circle ans;
```

```
1 // typedef int cod;
       point u = point((b-a).y, -(b-a).x);
249
250
       point v = point((c-a).y, -(c-a).x);
                                                            2 // bool eq(cod a, cod b){ return (a==b); }
       point n = (c-b)*0.5;
       1d t = (u^n)/(v^u);
                                                            4 #define vp vector <point >
       ans.c = ((a+c)*0.5) + (v*t);
                                                            5 typedef ld cod;
                                                            6 bool eq(cod a, cod b){ return fabs(a - b) <= EPS; }</pre>
       ans.r = norm(ans.c-a);
254
255
       return ans;
256
                                                            8 struct point
257
258 vp inter_circle_line(circle C, line L){
                                                                  cod x, y, z;
       point ab = L.p2 - L.p1, p = L.p1 + ab * ((C.c-L._{11})
                                                                  point(cod x=0, cod y=0, cod z=0): x(x), y(y), z(z)
259
       p1)*(ab) / (ab*ab));
        ld \ s \ = \ (L.p2-L.p1) \ \hat{} \ (C.c-L.p1) \ , \ h2 \ = \ C.r*C.r \ - \ s*s_{12} 
       / (ab*ab);
                                                                  point operator+(const point &o) const{
                                                           13
       if (h2 < -EPS) return {};</pre>
261
                                                           14
                                                                      return {x+o.x, y+o.y, z+o.z};
       if (eq(h2, 0)) return {p};
262
                                                           15
       point h = (ab/norm(ab)) * sqrt(h2);
263
                                                           16
                                                                  point operator - (const point &o) const{
       return {p - h, p + h};
264
                                                                      return \{x-o.x, y-o.y, z-o.z\};
265
                                                                  point operator*(cod t) const{
266
                                                           19
267 vp inter_circle(circle C1, circle C2){
                                                                      return {x*t, y*t, z*t};
                                                           20
       if(C1.c == C2.c) { assert(C1.r != C2.r); return
                                                           21
       {}: }
                                                                  point operator/(cod t) const{
                                                           22
       point vec = C2.c - C1.c;
                                                                     return {x/t, y/t, z/t};
       bool operator == (const point &o) const{
       1d p = (d2 + C1.r*C1.r - C2.r*C2.r)/(d2*2), h2 = 26
                                                                      return eq(x, o.x) and eq(y, o.y) and eq(z, o.
       C1.r*C1.r - p*p*d2;
                                                                  z):
       if (sum*sum < d2 or dif*dif > d2) return {};
       point mid = C1.c + vec*p, per = point(-vec.y, vec 28
                                                                  cod operator*(const point &o) const{ // dot
       .x) * sqrt(max((1d)0, h2) / d2);
                                                                      return x*o.x + y*o.y + z*o.z;
                                                           29
       if(eq(per.x, 0) and eq(per.y, 0)) return {mid};
274
                                                           30
       return {mid + per, mid - per};
                                                                  point operator^(const point &o) const{ // cross
275
                                                           3.1
276
                                                                      return point(y*o.z - z*o.y,
                                                                                    z*o.x - x*o.z,
277
                                                           33
_{278} // minimum circle cover O(n) amortizado
                                                                                    x*o.y - y*o.x);
279 circle min_circle_cover(vector<point> v){
                                                           3.5
       random_shuffle(v.begin(), v.end());
                                                           36 }:
280
       circle ans;
281
                                                           37
       int n = v.size();
                                                           38 ld dist(point a, point b){
282
       for(int i=0;i<n;i++) if(!ans.inside(v[i])){</pre>
283
                                                           39
                                                                 return sqrt((a-b)*(a-b));
                                                           40 }
284
           ans = circle(v[i]);
           for(int j=0;j<i;j++) if(!ans.inside(v[j])){</pre>
                                                           41 bool nulo(point a){
285
286
               ans = circle(v[i], v[j]);
                                                           42
                                                                 return (eq(a.x, 0) and eq(a.y, 0) and eq(a.z, 0))
               for(int k=0;k<j;k++) if(!ans.inside(v[k])</pre>
287
       ) {
                    ans = circle(v[i], v[j], v[k]);
288
               }
                                                           45 ld norm(point a){ // Modulo
           }
                                                           46
                                                                 return sqrt(a*a);
291
                                                           47 }
       return ans;
                                                           48 ld proj(point a, point b){ // a sobre b
292
293 }
                                                                 return (a*b)/norm(b);
                                                           49
                                                           50 }
   1.15 Intersect Polygon
                                                           _{\mbox{\scriptsize 51}} ld angle(point a, point b){ // em radianos
                                                                  return acos((a*b) / norm(a) / norm(b));
                                                           52
                                                           53 }
 1 bool intersect(vector<point> A, vector<point> B) //
                                                           54
       Ordered ccw
                                                           55 cod triple(point a, point b, point c){
 2 {
                                                                  return (a * (b^c)); // Area do paralelepipedo
                                                           56
       for(auto a: A)
                                                           57 }
           if(inside(B, a))
                                                           5.8
               return true:
                                                           59 point normilize(point a){
       for(auto b: B)
                                                                  return a/norm(a);
                                                           60
           if(inside(A, b))
                                                           61 }
               return true;
                                                           62
                                                           63 struct plane{
       if(inside(B, center(A)))
                                                                 cod a, b, c, d;
                                                           64
           return true;
                                                           65
                                                                  point p1, p2, p3;
                                                                  {\tt plane(point\ p1=0,\ point\ p2=0,\ point\ p3=0):\ p1(p1)}
                                                           66
13
       return false;
                                                                  , p2(p2), p3(p3){
14 }
                                                                      point aux = (p1-p3)^(p2-p3);
                                                           67
                                                                      a = aux.x; b = aux.y; c = aux.z;
                                                           68
   1.16 3d
                                                           69
                                                                      d = -a*p1.x - b*p1.y - c*p1.z;
```

```
int n:
7.0
                                                               3.8
       plane(point p, point normal){
                                                               39
                                                                       map < int , int > parent;
           normal = normilize(normal);
                                                                       map < int , vi > comp;
                                                               40
            a = normal.x; b = normal.y; c = normal.z;
                                                               41
            d = -(p*normal);
                                                                       int find(int v) {
                                                                           if(v==parent[v])
7.5
                                                               43
       // ax+by+cz+d = 0;
                                                                           return parent[v]=find(parent[v]);
                                                               45
      cod eval(point &p){
78
                                                               46
           return a*p.x + b*p.y + c*p.z + d;
79
                                                               47
                                                                       void join(int a, int b) {
80
                                                               48
81 };
                                                                           a = find(a);
                                                                           b = find(b);
                                                               5.0
83 cod dist(plane pl, point p){
                                                                           if(a!=b) {
                                                               51
       \textcolor{return}{\textbf{return}} \hspace{0.2cm} \texttt{fabs(pl.a*p.x} \hspace{0.2cm} + \hspace{0.2cm} \texttt{pl.b*p.y} \hspace{0.2cm} + \hspace{0.2cm} \texttt{pl.c*p.z} \hspace{0.2cm} + \hspace{0.2cm} \texttt{pl.d} \hspace{0.2cm} _{52}
                                                                                if((int)comp[a].size()<(int)comp[b].size</pre>
       ) / sqrt(pl.a*pl.a + pl.b*pl.b + pl.c*pl.c);
85 }
                                                                                     swap(a, b);
86
                                                               5.4
                                                                                for(auto v: comp[b])
87 point rotate(point v, point k, ld theta){
                                                                                    comp[a].pb(v);
      // Rotaciona o vetor v theta graus em torno do
                                                               56
       eixo k
                                                               5.7
                                                                                comp[b].clear();
       // theta *= PI/180; // graus
                                                               58
                                                                                parent[b]=a;
       return (
                                                               59
9.0
           v*cos(theta)) +
                                                               60
            ((k^v)*sin(theta)) +
                                                               6.1
92
            (k*(k*v))*(1-cos(theta)
                                                               62 };
93
       );
94
95 }
                                                               64 int trie[MAX][2];
                                                               65 set < int > idx[MAX];
        Algoritmos
                                                               66 int finish [MAX];
                                                               67 int nxt = 1;
                                                               68
  2.1 Mst Xor
                                                               69 void add(int s){
                                                               70
                                                                     int node = 0;
                                                                       for(int i=30; i>=0; i--){
                                                               7.1
1 // omg why just 2 seconds
                                                                           bool c = (s & (1<<i));
2 #include <bits/stdc++.h>
                                                               72
                                                                           if(trie[node][c] == 0)
3 // #define int long long
                                                               7.3
4 #define ff first
                                                               74
                                                                               node = trie[node][c] = nxt++;
                                                               75
5 #define ss second
                                                                                node = trie[node][c];
                                                               76
6 #define ll long long
7 #define ld long double
                                                               7.7
                                                                           finish[node]++;
8 #define pb push_back
                                                               78
                                                               79 }
9 #define eb emplace_back
10 #define pii pair<int, int>
                                                               80
                                                               81 void remove(int s){
#define pll pair<11, 11>
                                                               82
                                                                      int node = 0;
12 #define ti tuple < int, int, int>
                                                                       for(int i=30;i>=0;i--){
13 #define vi vector<int>
                                                               83
14 #define vl vector<ll>
                                                                           bool c = (s & (1 << i));
                                                                           node = trie[node][c];
15 #define vii vector<pii>
16 #define sws ios_base::sync_with_stdio(false);cin.tie(86
                                                                           finish[node]--;
      NULL); cout.tie(NULL);
                                                               88 }
17 #define endl '\n'
18 #define teto(a, b) (((a)+(b)-1)/(b))
                                                               90 int min_xor(int s){
19 #define all(x) x.begin(), x.end()
20 #define forn(i, n) for(int i = 0; i < (int)n; i++)</pre>
                                                               91
                                                                       int node = 0;
                                                                      int ans = 0;
^{21} #define forne(i, a, b) for(int i = a; i <= b; i++)
                                                               92
22 #define dbg(msg, var) cerr << msg << " " << var <<
                                                                       for(int i=30; i>=0; i--){
                                                               93
                                                                           bool c = (s & (1<<i));
                                                               94
       endl:
                                                                           if(finish[trie[node][c]] != 0)
                                                               95
                                                               96
                                                                               node = trie[node][c];
24 using namespace std;
                                                               97
                                                                           elsef
                                                               98
                                                                               ans ^= 1 << i;
26 const int MAX = 6e6+10;
27 \text{ const } 11 \text{ MOD} = 1e9+7;
                                                               99
                                                                                node = trie[node][!c];
                                                              100
28 const int INF = 0x3f3f3f3f;
29 const 11 LLINF = 0x3f3f3f3f3f3f3f3f3f;
30 const ld EPS = 1e-6;
                                                              102
                                                                       return ans:
                                                              103
31 const ld PI = acos(-1);
                                                              104
                                                              105
33 // End Template //
                                                               106 int32_t main()
                                                              107 { sws:
35 const int N = 2e5+10;
```

37 struct DSU {

int n;

```
cin >> n:
110
                                                              1.0
       vi x(n);
       for(int i=0;i<n;i++)</pre>
                                                                     int merge(int a, int b){
112
                                                              12
           cin >> x[i];
                                                              13
                                                                         return max(a, b);
113
       sort(x.begin(), x.end());
115
                                                              15
       x.erase(unique(x.begin(), x.end()), x.end());
                                                                     void build(){
                                                              16
       n = x.size();
                                                                         for(int i=n-1; i>0; i--)
                                                              1.7
                                                                              t[i] = merge(t[i << 1], t[i << 1|1]);
118
                                                              18
       DSU dsu;
119
                                                              19
                                                              20
       11 \text{ mstsum} = 0;
                                                              21
                                                                     int query(int 1, int r){
                                                                         int resl = -INF, resr = -INF;
                                                              22
                                                                         for(l+=n, r+=n+1; l<r; l>>=1, r>>=1){
       vi pais;
                                                              23
       for(int i=0;i<n;i++){</pre>
124
                                                              24
                                                                              if(1&1) resl = merge(resl, t[1++]);
            add(x[i]);
                                                                              if(r\&1) resr = merge(t[--r], resr);
125
                                                              25
            dsu.parent[x[i]] = x[i];
                                                              26
            dsu.comp[x[i]].pb(x[i]);
                                                              27
                                                                         return merge(resl, resr);
            pais.pb(x[i]);
129
                                                              29
                                                                     void update(int p, int value){
                                                              30
131
       while ((int) pais.size()!=1){
                                                              31
            vector<ti> edges;
                                                                         for(t[p]=max(t[p], value); p >>= 1;)
                                                             3.2
132
            for(auto p: pais){
                                                                              t[p] = merge(t[p << 1], t[p << 1|1]);
                                                             33
                vi &nodes = dsu.comp[p];
134
                                                             3.4
                                                             35 };
135
                for(auto u: nodes) remove(u);
136
                                                             36
                                                             37 struct point{
137
                // query
                                                             38
                                                                     int x, y, z, id;
                ti ed = {LLINF, 0, 0};
                                                                     bool left:
139
                                                              3.9
                for(auto u: nodes){
                                                                     point(int x=0, int y=0, int z=0): x(x), y(y), z(z)
140
                                                              40
                    int xr = min_xor(u);
141
                                                                     ) {
                     ed = min(ed, {xr, u, xr^u});
                                                                         left = false;
                                                              41
142
                }
                                                              42
                edges.pb(ed);
                                                                     bool operator < (point &o) {</pre>
144
                                                              43
                                                                         if(x != o.x) return x < o.x;</pre>
                // add back
                                                                         if(y != o.y) return y > o.y;
146
                                                              45
147
                for(auto u: nodes) add(u);
                                                              46
                                                                         return z < o.z;
            }
                                                              47
                                                              48 };
149
            for(auto [xr, u, v]: edges){
                if(dsu.find(u)!=dsu.find(v)){
                                                              5.0
                                                              51 void cdq(int 1, int r, vector<point> &a, vi &dp){
                     // u, v -> mst
                     // cout << "mst = " << u << " " << v 52
                                                                     if(l==r) return;
        << endl;
                                                              53
                     mstsum += xr;
                                                                     int mid = (1+r) / 2;
                                                              54
                     dsu.join(u, v);
                                                              5.5
                }
                                                                     cdq(1, mid, a, dp);
            }
                                                              5.7
            vi pais2;
                                                              58
                                                                     // compress z
158
                                                                     set < int > uz; map < int, int > idz;
159
            for(auto p: pais)
                                                              59
                if(p==dsu.find(p))
                                                                     for(int i=1;i<=r;i++) uz.insert(a[i].z);
160
                                                              60
                    pais2.pb(p);
                                                                     int id = 0;
                                                              61
                                                                     for(auto z: uz) idz[z] = id++;
            swap(pais, pais2);
                                                              62
                                                              63
163
164
                                                              64
                                                                     vector < point > tmp;
       cout << mstsum << endl;</pre>
                                                                     for(int i=1;i<=r;i++){</pre>
                                                              65
                                                              66
                                                                         tmp pb(a[i]);
166
                                                                         tmp.back().x = 0;
167
                                                              67
                                                                         tmp.back().z = idz[tmp.back().z];
168
       return 0;
                                                              68
169 }
                                                                         if(i<=mid)
                                                              6.9
                                                              70
                                                                              tmp.back().left = true;
   2.2 Cdq
                                                              7.1
                                                                     }
                                                              72
                                                              73
                                                                     Segtree st(id);
 1 // LIS 3D problem
                                                              74
                                                              75
                                                                     sort(tmp.rbegin(), tmp.rend());
 3 struct Segtree{
                                                              76
       vi t;
                                                                     for(auto t: tmp){
       int n;
                                                                         if(t.left){
                                                              78
                                                                             st.update(t.z, dp[t.id]);
       Segtree(int n){
                                                              79
                                                              80
                                                                         }else{
           this -> n = n;
            t.assign(2*n, 0);
                                                              81
                                                                              dp[t.id] = max(dp[t.id], st.query(0, t.z)
```

```
-1)+1);
                                                                   1d m1 = (2*1 + r) / 3;
                                                             5
82
           }
                                                             6
                                                                   1d m2 = (1 + 2*r) / 3;
                                                                   if(check(m1) > check(m2))
83
84
                                                                       1 = m1;
       cdq(mid+1, r, a, dp);
                                                            9
86 }
                                                                       r = m2;
                                                            10
                                                            11 }
89 int32_t main()
                                                                    Misc
                                                               3
90 {sws;
91
                                                                    Rand
92
       int n; cin >> n;
                                                               3.1
93
       vector < point > vet(n);
94
                                                             1 mt19937 rng(chrono::steady_clock::now().
       for(int i=0;i<n;i++){</pre>
95
                                                                   time_since_epoch().count()); // mt19937_64
            cin >> vet[i].x >> vet[i].y >> vet[i].z;
96
                                                             uniform_int_distribution<int> distribution(1,n);
97
98
                                                            4 num = distribution(rng); // num no range [1, n]
       sort(vet.begin(), vet.end());
                                                             5 shuffle(vec.begin(), vec.end(), rng); // shuffle
100
       for (int i = 0; i < n; i++)</pre>
                                                            7 using ull = unsigned long long;
           vet[i].id = i;
102
                                                             8 ull mix(ull o){
                                                                  o+=0 x9e3779b97f4a7c15;
       vi dp(n, 1);
                                                                   o=(o^(o>>30))*0xbf58476d1ce4e5b9;
                                                                   o=(o^(o>>27))*0x94d049bb133111eb;
       cdq(0, n-1, vet, dp);
106
                                                            12
                                                                   return o^(o>>31);
                                                            13 }
       int ans = 0;
108
                                                            14 ull hash(pii a) {return mix(a.first ^ mix(a.second))
       for(int i=0;i<n;i++)</pre>
109
           ans = max(ans, dp[i]);
110
                                                              3.2 Bitwise
       cout << ans << endl;</pre>
113
114
                                                             1 // Bitwise
       return 0:
115
                                                                  #pragma GCC target("popcnt")
116 }
                                                                   unsigned char a = 5, b = 9; // a = (00000101), b
                                                             3
                                                                   = (00001001)
   2.3 Histogram Rectangle
                                                                   AND -
                                                                                       // The result is 00000001
                                                                                   a&b
                                                             5
                                                                   (1)
 1 ll bestRectangle(vi hist){
                                                                   OR -
                                                                                         // The result is 00001101
                                                                                   alb
                                                             6
       int n = hist.size();
                                                                   (13)
       stack<11> s;
                                                                                   a^b
                                                                                         // The result is 00001100
                                                                   XOR -
       s.push(-1);
                                                                   (12)
       11 ans = hist[0];
                                                                                   ~a
                                                                   NOT -
                                                                                         // The result is 11111010
       vl left_smaller(n, -1), right_smaller(n, n);
                                                                   (250)
       for(int i=0;i<n;i++){</pre>
                                                                                   b <<1 // The result is 00010010
                                                                   Left shift -
           while(!s.empty() and s.top()!=-1 and hist[s.
                                                                   (18)
       top()]>hist[i]){
                                                                   Right shift - b >> 1 // The result is 00000100
               right_smaller[s.top()] = i;
                s.pop();
 10
           }
                                                                   // Exchange two int variables
            if(i>0 and hist[i] == hist[i-1])
12
                                                            13
               left_smaller[i] = left_smaller[i-1];
                                                                       a^=b;
                                                            14
 14
            else
                                                                       b^=a;
                                                            1.5
 1.5
               left_smaller[i] = s.top();
                                                                       a^=b;
                                                            16
 16
            s.push(i);
                                                            17
17
                                                                   // Even or Odd
                                                            18
       for(int j=0;j<n;j++){</pre>
19
                                                                       (x & 1)? printf("Odd"): printf("Even");
                                                            20
           ll area = hist[j]*(right_smaller[j]-
20
                                                            21
       left_smaller[j]-1);
                                                                   // Turn on the j-th bit
                                                            22
           ans = max(ans, area);
                                                            23
22
                                                                       int S = 34; //(100010)
                                                            24
       return ans;
23
                                                                       int j = 3;
                                                            2.5
24 }
                                                                       S = S | (1 << j);
                                                            27
         Ternary Search
                                                            28
                                                            29
                                                                   // Turn off the j-th bit
 1 // Ternary
                                                            3.0
 _{2} ld l = _{-1}e4, r = 1e4;
                                                                       int S = 42; //(101010)
                                                            31
```

33

3 int iter = 100;

4 while(iter - -) {

int j = 1;

```
S &= ~(1<<j)
                                                         8 #define mp make_pair
3.4
35
          S == 40 //(101000)
                                                         10 const 11 MOD = 998'244'353;
36
                                                         11 const int MAX = 2e5 + 5;
      // Check the j-th element
                                                           3.4 Ordered Set
39
          int S = 42; //(101010)
          int j = 3;
                                                         1 #include <bits/extc++.h>
4.1
                                                         using namespace __gnu_pbds; // or pb_ds;
42
          T = S & (1 << j); // T = 0
                                                        3 template < typename T, typename B = null_type >
                                                         4 using ordered_set = tree<T, B, less<T>, rb_tree_tag,
44
      // Least significant bit (lsb)
                                                               tree_order_statistics_node_update>;
46
          int lsb(int x){ return x&-x; }
                                                           4 Math
      // Exchange o j-th element
49
                                                           4.1 Randommod
50
          S ^= (1<<i)
5.1
                                                        int randommod() {
      // Position of the first bit on
                                                              auto primo = [](int num) {
                                                        2
53
                                                                  for(int i = 2; i*i <= num; i++) {
                                                         3
54
          T = (S & (-S))
                                                                       if(num%i == 0) return false;
55
                                                         4
          T -> 4 bit ligado //(1000)
56
                                                         5
                                                                   return true;
                                                         6
      // Most significant digit of N
                                                               };
5.8
                                                         7
                                                               uniform_int_distribution <int> distribution
59
                                                         8
          double K = log10(N);
                                                               (100000007, 1500000000);
60
                                                               int num = distribution(rng);
          K = K - floor(K);
61
                                                         9
          int X = pow(10, K);
                                                               while(!primo(num)) num++;
                                                         10
                                                               return num;
63
      // Number of digits in N
                                                         12 }
64
6.5
                                                          4.2 Division Trick
          X =floor(log10(N)) + 1;
66
      // Power of two
                                                         1 for(int l = 1, r; l <= n; l = r + 1) {</pre>
68
                                                              r = n / (n / 1);
          bool isPowerOfTwo(int x){ return x && (!(x&(x 3
                                                               // n / i has the same value for l <= i <= r \,
7.0
      -1))); }
                                                         4 }
7.1
                                                           4.3 Inverso Mult
      // Turn off the first bit 1
72
73
          m = m & (m-1);
7.4
                                                         1 // gcd(a, m) = 1 para existir solucao
      // Built-in functions
                                                         \frac{1}{2} // ax + my = 1, ou a*x = 1 (mod m)
7.6
                                                         3 ll inv(ll a, ll m) { // com gcd
          // Number of bits 1
                                                         4
                                                             11 x, y;
          __builtin_popcount()
                                                         5
                                                               gcd(a, m, x, y);
          __builtin_popcountl1()
                                                               return (((x % m) +m) %m);
7.9
                                                         6
                                                         7 }
          // Number of leading zeros
8.1
          __builtin_clz()
                                                        9 ll inv(ll a, ll phim) { // com phi(m), se m for primo
          __builtin_clzl1()
                                                                entao phi(m) = p-1
83
                                                               ll e = phim - 1;
84
                                                         10
          // Number of trailing zeros
                                                               return fexp(a, e);
          __builtin_ctz()
                                                        12 }
86
87
          __builtin_ctzl1()
                                                           4.4 Crt
88
      // floor(log2(x))
89
90
                                                         1 tuple < 11, 11, 11 > ext_gcd(11 a, 11 b) {
          int flog2(int x) { return 32-1-_builtin_clz(x 2 if (!a) return {b, 0, 1};
91
                                                        3
                                                               auto [g, x, y] = ext_gcd(b\%a, a);
92
                                                         4
                                                               return \{g, y - b/a*x, x\};
          int flog211(11 x){ return 64-1-
                                                         5 }
      __builtin_clzll(x); }
                                                         7 struct crt {
  3.3 Template
                                                              11 a, m;
                                                         8
#include <bits/stdc++.h>
                                                               crt() : a(0), m(1) {}
                                                         10
                                                               crt(ll a_, ll m_) : a(a_), m(m_) {}
2 using namespace std;
                                                         11
                                                               crt operator * (crt C) {
                                                         12
                                                                   auto [g, x, y] = ext_gcd(m, C.m);
4 using ll = long long;
                                                         1.3
                                                                   if ((a - C.a) % g) a = -1;
5 using ii = pair<int, int>;
                                                         14
6 using vi = vector < int >;
                                                                   if (a == -1 or C.a == -1) return crt(-1, 0);
                                                         1.5
7 #define pb emplace_back
                                                                   11 lcm = m/g*C.m;
                                                         16
```

```
ll ans = a + (x*(C.a-a)/g \% (C.m/g))*m;
                                                               11 x = 0, y = 0, t = 30, prd = 2, x0 = 1, q;
1.7
                                                        3.8
18
          return crt((ans % lcm + lcm) % lcm, lcm);
                                                        39
                                                               while (t % 40 != 0 or gcd(prd, n) == 1) {
                                                                   if (x==y) x = ++x0, y = f(x);
19
                                                        40
20 };
                                                                   q = mul(prd, abs(x-y), n);
                                                         41
                                                                   if (q != 0) prd = q;
                                                         42
                                                                   x = f(x), y = f(f(y)), t++;
  4.5 Gaussxor
                                                        43
                                                         44
                                                               return gcd(prd, n);
                                                        4.5
1 struct Gauss {
                                                        46 }
      array<11, LOG_MAX> vet;
                                                        47
      int size;
                                                        48 vector<ll> fact(ll n) {
      Gauss() : size(0) {
                                                        49
                                                               if (n == 1) return {};
          fill(vet.begin(), vet.end(), 0);
                                                               if (prime(n)) return {n};
                                                        50
                                                        51
                                                             11 d = rho(n);
      Gauss(vector<1l> vals) : size(0) {
                                                               vector<11> 1 = fact(d), r = fact(n / d);
                                                        52
          fill(vet.begin(), vet.end(), 0);
                                                        53
                                                               1.insert(l.end(), r.begin(), r.end());
          for(ll val : vals) add(val);
9
                                                        54
                                                               return 1;
                                                        55 }
      bool add(ll val) {
          for(int i = LOG_MAX-1; i >= 0; i--) if(val &
12
                                                           4.7 Fast Exponentiaion
      (1LL << i)) {
              if(vet[i] == 0) {
13
                                                         1 ll fexp(ll b, ll e, ll mod) {
14
                  vet[i] = val;
                                                               ll res = 1;
                  size++;
15
                                                               b \% = mod;
                                                         3
                  return true;
                                                               while(e){
1.7
                                                                  if(e & 1LL)
18
              val ^= vet[i];
                                                         5
                                                                      res = (res * b) % mod;
          }
                                                         6
19
                                                                   e = e >> 1LL;
          return false;
20
                                                                   b = (b * b) \% mod;
                                                         8
                                                               }
                                                         9
22 }:
                                                         10
                                                               return res;
                                                         11 }
  4.6 Pollard Rho
                                                                Linear Diophantine Equation
1 ll mul(ll a, ll b, ll m) {
      11 \text{ ret} = a*b - (11)((1d)1/m*a*b+0.5)*m;
                                                         1 // Linear Diophantine Equation
      return ret < 0 ? ret+m : ret;</pre>
                                                         2 int gcd(int a, int b, int &x, int &y)
4 }
                                                               if (a == 0)
                                                         4
6 ll pow(ll a, ll b, ll m) {
      ll ans = 1;
                                                                   x = 0; y = 1;
      for (; b > 0; b /= 211, a = mul(a, a, m)) {
                                                                   return b;
          if (b % 211 == 1)
9
              ans = mul(ans, a, m);
1.0
                                                               int x1, y1;
                                                         9
11
      }
                                                               int d = gcd(b%a, a, x1, y1);
12
      return ans;
                                                               x = y1 - (b / a) * x1;
13 }
                                                         12
                                                               y = x1;
14
                                                        13
                                                               return d;
15 bool prime(ll n) {
                                                        14 }
      if (n < 2) return 0;
17
      if (n <= 3) return 1;
                                                         16 bool find_any_solution(int a, int b, int c, int &x0,
      if (n % 2 == 0) return 0;
                                                               int &y0, int &g)
19
                                                         17 {
      ll r = \__builtin\_ctzll(n - 1), d = n >> r;
20
                                                               g = gcd(abs(a), abs(b), x0, y0);
                                                        18
      for (int a : {2, 325, 9375, 28178, 450775,
                                                               if (c % g)
                                                        19
      9780504, 795265022}) {
                                                                  return false;
                                                        2.0
          11 x = pow(a, d, n);
          if (x == 1 or x == n - 1 or a % n == 0)
23
                                                               x0 *= c / g;
                                                        22
      continue;
                                                               y0 *= c / g;
                                                        23
24
                                                               if (a < 0) x0 = -x0;
                                                        24
          for (int j = 0; j < r - 1; j++) {
25
                                                               if (b < 0) y0 = -y0;
                                                        25
26
              x = mul(x, x, n);
                                                        26
                                                               return true;
              if (x == n - 1) break;
                                                        27 }
          }
          if (x != n - 1) return 0;
29
                                                        29 // All solutions
30
                                                        31
      return 1;
32 }
                                                           4.9 Miller Habin
34 ll rho(ll n) {
      if (n == 1 or prime(n)) return n;
```

auto f = [n](11 x) {return mul(x, x, n) + 1;};

36

37

1 ll mul(ll a, ll b, ll m) {

return (a*b-ll(a*(long double)b/m+0.5)*m+m)%m;

```
3 }
                                                           29
                                                           30
                                                                  for(int len = 2; len <= n; len <<= 1){</pre>
                                                                      ld ang = 2 * PI / len * (invert ? -1 : 1);
5 ll expo(ll a, ll b, ll m) {
                                                           3.1
      if (!b) return 1;
                                                           32
                                                                      num wlen(cos(ang), sin(ang));
      ll ans = expo(mul(a, a, m), b/2, m);
                                                                       for(int i=0;i<n;i+=len){</pre>
      return b%2 ? mul(a, ans, m) : ans;
                                                                           num w(1);
                                                           34
9 }
                                                                           for (int j=0;j<len/2;j++){</pre>
                                                                               num u = a[i+j], v = a[i+j+len/2] * w;
1.0
                                                           3.6
                                                                               a[i+j] = u + v;
11 bool prime(ll n) {
                                                           37
                                                                               a[i+j+len/2] = u - v;
      if (n < 2) return 0;
                                                           38
      if (n <= 3) return 1;
                                                                               w = w * wlen;
13
                                                           39
14
      if (n % 2 == 0) return 0;
                                                           40
                                                                           }
                                                                      }
1.5
                                                           41
      11 d = n - 1;
                                                           42
16
                                                                  if(invert)
1.7
      int r = 0;
                                                           43
      while (d % 2 == 0) {
                                                                    for(num &x: a)
18
                                                           44
19
          r++;
                                                           45
                                                                        x = x/n;
           d /= 2;
20
                                                           46
                                                           47 }
22
                                                           48
      // com esses primos, o teste funciona garantido
                                                           49 vl multiply(vi const& a, vi const& b){
      para n <= 2^64
                                                                  vector < num > fa(a.begin(), a.end());
                                                           50
      // funciona para n <= 3*10^24 com os primos ate
                                                                  vector < num > fb(b.begin(), b.end());
24
                                                           5.1
      41
                                                                  int n = 1;
      for (int i : {2, 325, 9375, 28178, 450775,
                                                                  while(n < int(a.size() + b.size()) )</pre>
25
                                                           5.3
      9780504, 795265022}) {
                                                                      n <<= 1;
                                                           54
          if (i >= n) break;
                                                           55
                                                                  fa.resize(n);
           11 x = expo(i, d, n);
                                                                  fb.resize(n);
                                                           56
           if (x == 1 \text{ or } x == n - 1) continue;
                                                           57
                                                                  fft(fa, false);
                                                                  fft(fb, false);
29
                                                           5.8
           bool deu = 1;
                                                           59
                                                                  for(int i=0;i<n;i++)
30
           for (int j = 0; j < r - 1; j++) {
                                                                      fa[i] = fa[i]*fb[i];
3.1
                                                           60
               x = mul(x, x, n);
                                                           61
                                                                  fft(fa, true);
32
               if (x == n - 1) {
                                                           62
                                                                  vl result(n);
                   deu = 0;
                                                                  for(int i=0;i<n;i++)</pre>
                                                           63
34
                                                                       result[i] = round(fa[i].a);
                   break:
                                                           64
                                                                  while(result.back() == 0) result.pop_back();
               }
36
                                                           6.5
                                                           66
                                                                  return result;
                                                           67 }
           if (deu) return 0;
3.9
                                                              4.11 Fft Tourist
40
      return 1;
41 }
                                                            1 struct num{
  4.10 Fft Simple
                                                                 ld x, y;
                                                           2
                                                            3
                                                                  num() { x = y = 0; }
                                                                  num(1d x, 1d y) : x(x), y(y) {}
1 struct num{
                                                            4
      ld a {0.0}, b {0.0};
                                                            5 };
      num(){}
      num(ld na) : a{na}{}
                                                            7 inline num operator+(num a, num b) { return num(a.x +
      num(ld na, ld nb) : a{na}, b{nb} {}
                                                                   b.x, a.y + b.y); }
      const num operator+(const num &c) const{
                                                            8 inline num operator-(num a, num b) { return num(a.x -
          return num(a + c.a, b + c.b);
                                                                   b.x, a.y - b.y); }
                                                            9 inline num operator*(num a, num b) { return num(a.x *
      const num operator-(const num &c) const{
                                                                   b.x - a.y * b.y, a.x * b.y + a.y * b.x); }
          return num(a - c.a, b - c.b);
                                                           inline num conj(num a) { return num(a.x, -a.y); }
1.0
                                                           11
       const num operator*(const num &c) const{
                                                           12 int base = 1;
12
          return num(a*c.a - b*c.b, a*c.b + b*c.a);
                                                           13 vector < num > roots = {{0, 0}, {1, 0}};
13
                                                           14 \text{ vi rev} = \{0, 1\};
14
1.5
       const num operator/(const int &c) const{
                                                           15
16
          return num(a/c, b/c);
                                                           16 void ensure_base(int nbase){
                                                                 if(nbase <= base)</pre>
17
                                                           17
18 };
                                                                      return;
                                                           1.8
void fft(vector<num> &a, bool invert){
                                                                  rev.resize(1 << nbase);</pre>
                                                           2.0
```

22

23

24

25

26

27

nbase - 1));

roots.resize(1 << nbase):

while(base < nbase){</pre>

for(int i = 0; i < (1 << nbase); i++)</pre>

rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (

ld angle = 2*PI / (1 << (base + 1));</pre>

int n = a.size();

j^=bit;

if(i<j)

for(int $i=1, j=0; i < n; i++){$

for(; j&bit; bit>>=1)

swap(a[i], a[j]);

int bit = n >> 1;

j^=bit;

21

22

23

25

27

28

```
for(int i = 1 << (base - 1); i < (1 << base); 96
                                                                   ensure base(nbase):
28
        i++){
                                                            97
                                                                   int sz = 1 << nbase;</pre>
                                                                   if(sz > (int) fa.size())
               roots[i << 1] = roots[i];
                                                            9.8
               ld angle_i = angle * (2 * i + 1 - (1 <<</pre>
                                                            99
                                                                       fa.resize(sz);
       base));
                                                                   for(int i=0;i<(int)a.size();i++){</pre>
               roots[(i << 1) + 1] = num(cos(angle_i),
31
                                                                        int x = (a[i] % m + m) % m;
       sin(angle_i));
                                                                        fa[i] = num(x & ((1 << 15) - 1), x >> 15);
32
           }
           base++;
33
                                                           104
                                                                   fill(fa.begin() + a.size(), fa.begin() + sz, num
34
35 }
                                                                   {0, 0});
                                                                   fft(fa, sz);
                                                                   if(sz > (int) fb.size())
37 void fft(vector<num> &a, int n = -1){
      if(n == -1)
                                                                       fb.resize(sz);
                                                           108
          n = a.size();
39
                                                           109
                                                                   if(eq)
                                                                        copy(fa.begin(), fa.begin() + sz, fb.begin())
40
                                                           110
41
       assert((n & (n-1)) == 0);
       int zeros = __builtin_ctz(n);
42
       ensure_base(zeros);
                                                                       for(int i = 0; i < (int) b.size(); i++){</pre>
       int shift = base - zeros;
                                                                           int x = (b[i] % m + m) % m;
44
                                                           113
       for(int i = 0; i < n; i++)</pre>
                                                                            fb[i] = num(x & ((1 << 15) - 1), x >> 15)
                                                           114
45
           if(i < (rev[i] >> shift))
46
               swap(a[i], a[rev[i] >> shift]);
47
                                                                       fill(fb.begin() + b.size(), fb.begin() + sz,
                                                                   num {0, 0});
       for(int k = 1; k < n; k <<= 1)
49
           for(int i = 0; i < n; i += 2 * k)
                                                                        fft(fb, sz);
50
               for(int j = 0; j < k; j++){
51
                                                            118
                   num z = a[i+j+k] * roots[j+k];
                                                                   1d ratio = 0.25 / sz;
                                                           119
                    a[i+j+k] = a[i+j] - z;
                                                                   num r2(0, -1);
                                                           120
                    a[i+j] = a[i+j] + z;
                                                                   num r3(ratio, 0);
5.4
55
                                                                   num r4(0, -ratio);
56 }
                                                           123
                                                                   num r5(0, 1);
                                                                   for(int i=0;i<=(sz >> 1);i++) {
                                                           124
58 vector < num > fa, fb;
                                                                       int j = (sz - i) & (sz - 1);
59 vi multiply(vi &a, vi &b){
                                                                       num a1 = (fa[i] + conj(fa[j]));
                                                           126
       int need = a.size() + b.size() - 1;
                                                                       num a2 = (fa[i] - conj(fa[j])) * r2;
       int nbase = 0;
                                                                       num b1 = (fb[i] + conj(fb[j])) * r3;
6.1
                                                           128
                                                                       num b2 = (fb[i] - conj(fb[j])) * r4;
       while((1 << nbase) < need) nbase++;</pre>
                                                           129
62
       ensure_base(nbase);
                                                                        if(i != j){
63
                                                           130
                                                                            num c1 = (fa[j] + conj(fa[i]));
       int sz = 1 << nbase;</pre>
                                                           131
64
65
       if(sz > (int) fa.size())
                                                                            num c2 = (fa[j] - conj(fa[i])) * r2;
          fa.resize(sz);
                                                                            num d1 = (fb[j] + conj(fb[i])) * r3;
66
                                                                            num d2 = (fb[j] - conj(fb[i])) * r4;
67
                                                            134
       for(int i = 0; i < sz; i++){</pre>
                                                           135
                                                                            fa[i] = c1 * d1 + c2 * d2 * r5;
68
           int x = (i < (int) a.size() ? a[i] : 0);</pre>
                                                                            fb[i] = c1 * d2 + c2 * d1;
69
                                                           136
           int y = (i < (int) b.size() ? b[i] : 0);</pre>
                                                           137
70
           fa[i] = num(x, y);
                                                                        fa[j] = a1 * b1 + a2 * b2 * r5;
                                                           138
                                                                        fb[j] = a1 * b2 + a2 * b1;
       fft(fa, sz);
73
                                                           140
74
       num r(0, -0.25 / sz);
                                                                   fft(fa, sz);
                                                            141
       for(int i = 0; i <= (sz >> 1); i++){
                                                                   fft(fb, sz);
7.5
                                                            142
          int j = (sz - i) & (sz - 1);
                                                                   vi res(need);
76
                                                           143
           num z = (fa[j] * fa[j] - conj(fa[i] * fa[i]))_{144}
                                                                   for(int i=0;i<need;i++){</pre>
        * r;
                                                                       ll aa = round(fa[i].x);
                                                           145
           if(i != j) {
                                                                        11 bb = round(fb[i].x);
7.8
                                                            146
                                                                       11 cc = round(fa[i].y);
               fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[147])
                                                                       res[i] = (aa + ((bb \% m) << 15) + ((cc \% m)
       j])) * r;
           }
                                                                   << 30)) % m;
80
81
           fa[i] = z;
                                                           149
                                                           150
                                                                   return res;
82
83
      fft(fa, sz);
                                                           151
       vi res(need);
                                                           152
84
       for(int i = 0; i < need; i++)</pre>
           res[i] = round(fa[i].x):
86
                                                           154
                                                           156 int main()
88
       return res:
89 }
                                                           157 {sws;
90
                                                           158
                                                                   //FFT
91
                                                           159
                                                                   vi fx{1, 2, 3}; // 1+2x+3x^2
92 vi multiply_mod(vi &a, vi &b, int m, int eq = 0){
      int need = a.size() + b.size() - 1;
                                                                   vi gx{4, 5}; // 4+5x
93
       int nbase = 0;
                                                            162
                                                                   vi res;
       while((1 << nbase) < need) nbase++;</pre>
95
                                                           163
```

```
res = multiply(fx,gx); //4 + 13x + 22x^2 + 15x^3 4.14 Raiz Primitiva
164
166
       return 0:
                                                           1 ll fexp(ll b, ll e, ll mod) {
                                                                 if(e == 0) return 1LL;
168 }
                                                                 11 \text{ res} = fexp(b, e/2LL, mod);
                                                           3
                                                                 res = (res*res)%mod;
  4.12 Matrix Exponentiation
                                                                 if(e%21.1.)
                                                           5
                                                                     res = (res*b)%mod;
 1 struct Matrix {
                                                                 return res%mod:
       vector < vl > m;
                                                           9 }
       int r, c;
                                                          10
                                                          11 vl fatorar(ll n) { // fatora em primos
       Matrix(vector < vl > mat) {
                                                          12
                                                                 vl fat;
          m = mat;
                                                                 for(int i = 2; i*i <= n; i++) {
                                                          13
           r = mat.size();
                                                                     if(n\%i == 0) {
           c = mat[0].size();
                                                          14
                                                                         fat pb(i);
                                                          1.5
                                                                          while (n\%i == 0)
1.0
                                                                             n /= i;
       Matrix(int row, int col, bool ident=false) {
                                                          17
12
           r = row; c = col;
                                                          18
                                                                 }
           m = vector < vl > (r, vl(c, 0));
                                                          19
13
                                                                 return fat;
14
           if(ident) {
                                                          2.0
                                                          21 }
              for(int i = 0; i < min(r, c); i++) {
15
                   m[i][i] = 1;
                                                          22
                                                          23 // O(log(n) ^ 2)
               }
1.7
                                                          24 bool raiz_prim(ll a, ll mod, ll phi, vl fat) {
18
           }
                                                                 if(__gcd(a, mod) != 1 or fexp(a, phi/2, mod) ==
                                                          25
19
                                                                 1) // phi de euler sempre eh PAR
20
                                                                     return false;
       Matrix operator*(const Matrix &o) const {
                                                          26
          assert(c == o.r); // garantir que da pra
                                                          27
22
                                                                 for(auto f : fat) {
                                                          28
       multiplicar
                                                                     if(fexp(a, phi/f, mod) == 1)
                                                          29
          vector<vl> res(r, vl(o.c, 0));
                                                          30
                                                                         return false;
24
           for(int i = 0; i < r; i++) {
                                                          31
               for(int k = 0; k < c; k++) {
26
                   for(int j = 0; j < o.c; j++) {</pre>
                                                          33
                                                                 return true:
                       res[i][j] = (res[i][j] + m[i][k]*34 }
28
       o.m[k][j]) % MOD;
                                                          _{36} // mods com raizes primitivas: 2, 4, p^k, 2*p^k, p eh
29
                   }
                                                                  primo impar, k inteiro --- O(n log^2(n))
               }
3.0
                                                          37 ll achar_raiz(ll mod, ll phi) {
           }
                                                                 if(mod == 2) return 1;
32
           return Matrix(res);
                                                          3.9
                                                                 vl fat, elementos;
                                                                 fat = fatorar(phi);
       }
                                                          40
34
35 }:
                                                          41
                                                                 for(11 i = 2; i <= mod-1; i++) {
                                                          42
37 Matrix fexp(Matrix b, int e, int n) {
                                                                     if(raiz_prim(i, mod, phi, fat))
                                                                         return i;
      if(e == 0) return Matrix(n, n, true); //
                                                          44
       identidade
                                                          45
       Matrix res = fexp(b, e/2, n);
                                                          46
39
                                                                 return -1; // retorna -1 se nao existe
       res = (res * res);
                                                          47
40
                                                          48 }
       if(e\%2) res = (res * b);
41
                                                          49
                                                          50 vl todas_raizes(ll mod, ll phi, ll raiz) {
43
       return res;
                                                                 vl raizes;
                                                          51
                                                                 if(raiz == -1) return raizes;
                                                          52
  4.13 Mulmod
                                                          53
                                                                 ll r = raiz;
                                                                 for(ll i = 1; i <= phi-1; i++) {
                                                          54
                                                          55
                                                                     if(__gcd(i, phi) == 1) {
 1 ll mulmod(ll a, ll b) {
                                                          5.6
                                                                          raizes.pb(r);
       if(a == 0) {
                                                          5.7
          return OLL;
                                                          58
                                                                     r = (r * raiz) \% mod;
                                                          59
       if(a\%2 == 0) {
                                                          60
           11 \text{ val} = \text{mulmod}(a/2, b);
                                                                 return raizes:
                                                          61
           return (val + val) % MOD;
                                                          62 }
                                                                     Bigmod
                                                             4.15
           ll val = mulmod((a-1)/2, b);
           val = (val + val) % MOD;
           return (val + b) % MOD;
                                                           1 ll mod(string a, ll p) {
       }
                                                              11 \text{ res} = 0, b = 1;
13
14 }
                                                                 reverse(all(a));
```

```
60 //calculate p*q mod f
      for(auto c : a) {
                                                               61 inline void mull(ll*p,ll*q)
           11 tmp = (((11)c-'0')*b) % p;
                                                               62 {
           res = (res + tmp) % p;
                                                               63
                                                                       for(int i=0;i<m+m;++i) t_[i]=0;</pre>
                                                                       for(int i=0;i<m;++i) if(p[i])</pre>
                                                               64
           b = (b * 10) \% p;
                                                                           for(int j=0;j<m;++j)</pre>
9
                                                               6.5
                                                                                t_[i+j]=(t_[i+j]+p[i]*q[j])%MOD;
                                                                       for(int i=m+m-1;i>=m;--i) if(t_[i])
                                                               6.7
       return res;
                                                                           //miuns t_[i]x^{i-m}(x^m-\sum_{j=0}^{m-1}x^{j})
12
                                                               68
13 }
                                                                       m-j-1}h_j)
                                                                           for(int j=m-1; ~j; --j)
                                                               69
  4.16 Berlekamp Massey
                                                               70
                                                                                t_{[i-j-1]}=(t_{[i-j-1]}+t_{[i]}*h_{[j]})%MOD;
                                                                       for(int i=0;i<m;++i) p[i]=t_[i];</pre>
                                                               72 }
2 #define SZ 233333
                                                               73 inline ll calc(ll K)
                                                               74 {
                                                                       for(int i=m; ~i; --i)
                                                               75
4 ll qp(ll a, ll b)
                                                                           s[i]=t[i]=0;
                                                               7.6
                                                               7.7
                                                                       //init
       11 x=1; a\%=MOD;
                                                                       s[0]=1; if(m!=1) t[1]=1; else t[0]=h[0];
       while(b)
                                                               78
                                                               79
                                                                       //binary-exponentiation
                                                               80
                                                                       while(K)
           if (b&1) x=x*a\%MOD;
9
                                                               8.1
           a = a * a % MOD; b >> = 1;
10
                                                                           if(K&1) mull(s,t);
       }
                                                               82
11
                                                                           mull(t,t); K>>=1;
                                                               83
       return x;
12
                                                               84
13 }
                                                                       11 su = 0;
14 namespace linear_seq {
                                                               85
                                                                       for(int i=0;i<m;++i) su=(su+s[i]*a[i])%MOD;</pre>
                                                               86
                                                               87
                                                                       return (su%MOD+MOD)%MOD;
16 inline vector < int > BM (vector < int > x)
                                                               88 }
       //ls: (shortest) relation sequence (after filling 89 inline int work(vector<int> x,ll n)
        zeroes) so far
                                                               90 -
                                                                       if(n<int(x.size())) return x[n];</pre>
                                                               91
       //\,\mathrm{cur}: current relation sequence
       vector < int > ls, cur;
                                                               92
                                                                       vector < int > v = BM(x); m = v.size(); if(!m) return 0;
2.0
                                                                       for(int i=0;i<m;++i) h[i]=v[i],a[i]=x[i];</pre>
                                                               93
       //lf: the position of ls (t')
                                                                       return calc(n);
       //ldt: delta of ls (v')
                                                               94
22
                                                               95 }
       int lf = 0, ldt = 0;
       for(int i=0;i<int(x.size());++i)</pre>
                                                               96
24
                                                               97 }
25
                                                               98 using linear_seq::work;
           11 t=0;
           //evaluate at position i
27
                                                                4.17 Totient
           for(int j = 0; j < int(cur.size()); ++j)</pre>
                t=(t+x[i-j-1]*(l1)cur[j])%MOD;
29
            \textbf{if((t-x[i])\%MOD==0)} \quad \textbf{continue;} \quad //\texttt{good} \quad \texttt{so} \quad \texttt{far} \quad \texttt{i} \quad // \quad \texttt{phi(p^k)} = (p^k-1) \cdot (p-1) \quad \texttt{com} \quad \texttt{p} \quad \texttt{primo} 
3.0
                                                               2 // O(sqrt(m))
31
           //first non-zero position
           if(!cur.size())
                                                                3 ll phi(ll m){
32
33
                                                                       11 res = m;
                                                                       for(11 d=2; d*d<=m; d++) {</pre>
                cur.resize(i+1):
3.4
                                                                5
                                                                           if(m % d == 0){
3.5
                lf = i; ldt = (t - x [i]) % MOD;
                                                                                res = (res/d)*(d-1);
                continue;
36
           }
                                                                                while (m\%d == 0)
37
           //cur=cur-c/ldt*(x[i]-t)
                                                                                     m /= d;
           11 k=-(x[i]-t)*qp(1dt,MOD-2)%MOD/*1/1dt*/;
                                                                           }
39
                                                               10
           vector<int> c(i-lf-1); //add zeroes in front 11
           c.pb(k);
                                                                       if(m > 1)
4.1
                                                               12
42
           for(int j=0;j<int(ls.size());++j)</pre>
                                                               1.3
                                                                           res /= m;
                c.pb(-ls[j]*k%MOD);
                                                                           res *= (m-1);
43
           if(c.size() < cur.size()) c.resize(cur.size()); 15</pre>
44
           for(int j = 0; j < int(cur.size()); ++ j)</pre>
                                                                       return res;
46
               c[j]=(c[j]+cur[j])%MOD;
                                                               17 }
            //if cur is better than ls, change ls to cur 18
47
           if(i-lf+(int)ls.size()>=(int)cur.size())
                                                               19 // modificacao do crivo, O(n*log(log(n)))
               ls = cur , lf = i , ldt = (t - x [i]) % MOD;
                                                               20 vl phi_to_n(ll n){
49
            cur=c;
50
                                                              21
                                                                      vector < bool > isprime(n+1, true);
                                                                       vl tot(n+1);
5.1
                                                               22
       for(int i=0;i<int(cur.size());++i)</pre>
                                                                       tot[0] = 0; tot[1] = 1;
                                                               23
                                                                       for(ll i=1;i<=n; i++){
5.3
          cur[i]=(cur[i]%MOD+MOD)%MOD;
                                                               24
54
       return cur;
                                                               25
                                                                           tot[i] = i;
55 }
                                                               26
56 int m; //length of recurrence
                                                               2.7
57 //a: first terms
                                                                       for(11 p=2;p<=n;p++){
                                                               28
58 //h: relation
                                                                         if(isprime[p]){
                                                               29
59 11 a[SZ],h[SZ],t_[SZ],s[SZ],t[SZ];
                                                                                tot[p] = p-1;
                                                               30
```

```
for(11 i=p+p;i<=n;i+=p){</pre>
                                                                       mu[j] -= mu[i];
                                                         7
3.1
                  isprime[i] = false;
                                                         8
                   tot[i] = (tot[i]/p)*(p-1);
33
                                                               return mu;
                                                        10 }
34
          }
      }
36
                                                                Grafos
                                                           5
37
      return tot;
38 }
                                                           5.1
                                                                 Ford
  4.18 Kitamasa
                                                         1 const int N = 2000010;
using poly = vector<mint>; // mint = int mod P with
                                                         s struct Ford {
      operators +, - and *
get rid of the annoying "hey a.size() is
                                                                  int to, f, c;
      unsigned" warning
4 poly pmul(const poly& a, const poly& b) {
                                                               int vis[N]:
      poly c(len(a) + len(b) - 1, 0);
                                                               vector < int > adj[N];
      for (int i = 0; i < len(a); i++)
                                                        10
                                                               vector < Edge > edges;
          for (int j = 0; j < len(b); j++)</pre>
                                                               int cur = 0;
              c[i+j] = c[i+j] + a[i] * b[j];
                                                        12
                                                               void addEdge(int a, int b, int cap, int rcap) {
9
      return c;
                                                        13
10 }
                                                         14
                                                                   Edge e;
                                                                   e.to = b; e.c = cap; e.f = 0;
11
                                                         1.5
12 // only works if b.back() == 1
                                                         16
                                                                   edges.pb(e);
13 poly pmod(const poly& a, const poly& b) {
                                                                   adj[a].pb(cur++);
                                                         17
      poly c(a.begin(), a.end());
      for (int i = len(c) - 1; i >= len(b) - 1; i --) { 19
                                                                   e = Edge();
          int k = i - (len(b) - 1); // index of the
                                                                   e.to = a; e.c = rcap; e.f = 0;
16
                                                        20
      quotient term
                                                         21
                                                                   edges.pb(e);
          for (int j = 0; j < len(b); j++)
                                                        22
                                                                   adj[b].pb(cur++);
              c[j+k] = c[j+k] - c[i] * b[j];
18
                                                        23
                                                        24
                                                               int dfs(int s, int t, int f, int tempo) {
      c.resize(len(b) - 1);
20
                                                        25
                                                                   if(s == t)
21
      return c;
                                                        26
22 }
                                                        27
                                                                       return f;
                                                                   vis[s] = tempo;
23
                                                        28
24 poly ppwr(poly x, ll e, poly f) {
      poly ans = { 1 };
                                                                   for(int e : adj[s]) {
                                                        3.0
2.5
      for (; e > 0; e /= 2) {
                                                                       if(vis[edges[e].to] < tempo and (edges[e</pre>
                                                               ].c - edges[e].f) > 0) {
          if (e & 1) ans = pmod(pmul(ans, x), f);
27
          x = pmod(pmul(x, x), f);
                                                                           if(int a = dfs(edges[e].to, t, min(f,
                                                                edges[e].c-edges[e].f) , tempo)) {
29
                                                                                edges[e].f += a;
30
      return ans;
                                                        33
31 }
                                                                                edges[e^1].f -= a;
                                                         34
                                                                                return a;
                                                        3.5
33 // values = { A0, A1, ..., An }. recurrence = C0 \times A0 36
                                                                           }
      + C1 × A1 + ... + Cn × An generates A\{n+1\}
                                                      37
                                                                       }
34 mint kitamasa(const poly& values, const poly&
                                                                   }
                                                        38
      recurrence, ll n) {
                                                        39
                                                                   return 0;
      poly f(len(recurrence) + 1);
35
                                                        40
      f.back() = 1;
      for (int i = 0; i < len(recurrence); i++)</pre>
                                                               int flow(int s, int t) {
3.7
                                                        42
          f[i] = mint(0) - recurrence[i];
                                                                   int mflow = 0, tempo = 1;
38
                                                         43
39
                                                                   while(int a = dfs(s, t, INF, tempo)) {
      auto d = ppwr(poly{0, 1}, n, f); // x^N \mod f(x) 45
                                                                       mflow += a;
40
41
                                                                       tempo++;
      mint ans = 0;
                                                                   }
42
                                                         47
      for (int i = 0; i < len(values); i++)</pre>
43
                                                         48
                                                                   return mflow;
          ans = ans + d[i] * values[i];
                                                         49
44
45
      return ans:
                                                         50 };
46 }
                                                           5.2 2sat
  4.19 Mobius
                                                         vector < int > g[MAX], gt[MAX], S; int vis[MAX], cor[MAX
1 vi mobius(int n) {
                                                              ];
      // g(n) = sum{f(d)} \Rightarrow f(n) = sum{mu(d)*g(n/d)}
      vi mu(n+1);
                                                         3 int val(int n, bool tvalue) {
      mu[1] = 1; mu[0] = 0;
                                                               if(tvalue) return 2*n;
      for(int i = 1; i <= n; i++)
                                                               return 2*n +1;
5
          for(int j = i + i; j <= n; j += i)
                                                         6 }
```

```
vector <T> u. v:
8 void dfs(int u) {
                                                                   vector < int > p, way;
      vis[u] = 1; for(int v : g[u]) if(!vis[v]) dfs(v); 6
                                                                   T inf;
9
       S.push_back(u);
1.0
11 }
                                                                   hungarian(int n_, int m_) : n(n_), m(m_), u(m+1),
                                                                   v(m+1), p(m+1), way(m+1) {
12
void dfst(int u, int e) {
                                                                       a = vector < vector < T >> (n, vector < T > (m));
                                                                       inf = numeric_limits <T>::max();
       cor[u] = e;
1.4
                                                            1.0
       for(int v : gt[u]) if(!cor[v]) dfst(v, e);
15
                                                            11
16 }
                                                                   pair <T, vector <int>> assignment() {
                                                                       for (int i = 1; i <= n; i++) {
17
                                                            13
                                                                           p[0] = i;
18 void kosaraju(int n) {
                                                            14
      for(int i = 0; i <= n; i++) if(!vis[i]) dfs(i);</pre>
                                                                           int j0 = 0;
19
                                                            15
       for(int i = 0; i <= n; i++) for(int j : g[i])</pre>
                                                                           vector < T > minv(m+1, inf);
                                                                           vector < int > used (m+1, 0);
21
           gt[j].push_back(i);
                                                            17
       int e = 0; reverse(S.begin(), S.end());
                                                                           do {
22
                                                            18
23
       for(int u : S) if(!cor[u]) dfst(u, ++e);
                                                                               used[j0] = true;
24 }
                                                                               int i0 = p[j0], j1 = -1;
                                                            2.0
                                                                               T delta = inf;
_{26} // antes de chamar essa funcao, colocar as arestas do _{22}
                                                                                for (int j = 1; j \le m; j++) if (!
       grafo
                                                                   used[j]) {
                                                                                    T cur = a[i0-1][j-1] - u[i0] - v[
27 bool solve(int n, vi &res) {
      kosaraju(2*n); // MAX > 2*N
                                                                   i];
28
                                                                                    if (cur < minv[j]) minv[j] = cur,</pre>
       vi r;
                                                                   way[j] = j0;
3.0
       forn(i, n) {
                                                                                    if (minv[j] < delta) delta = minv</pre>
3.1
           int t = val(i, true), f = val(i, false);
32
                                                                   [j], j1 = j;
           if(cor[t] == cor[f]) {
33
               return false;
                                                                                for (int j = 0; j \le m; j++)
                                                            27
           }
                                                                                    if (used[j]) u[p[j]] += delta, v[
3.5
                                                            28
36
           else {
                                                                   j] -= delta;
               if(cor[t] > cor[f])
                                                                                    else minv[j] -= delta;
3.7
                                                            29
                  r.pb(1);
                                                                                j0 = j1;
38
                                                            30
                                                            31
                                                                           } while (p[j0] != 0);
                   r pb(0);
                                                                           do {
40
                                                            32
                                                                                int j1 = way[j0];
41
                                                            33
                                                                               p[j0] = p[j1];
       }
42
                                                            3.4
43
       swap(r, res);
                                                            35
                                                                               j0 = j1;
                                                                           } while (j0);
       return true;
44
                                                            36
45
                                                            37
                                                            38
                                                                       vector < int > ans(m);
  5.3 Kahn
                                                                       for (int j = 1; j \le n; j++) ans[p[j]-1] = j
                                                            3.9
                                                            40
                                                                       return make_pair(-v[0], ans);
vi g[MAX];
                                                            41
1 int in[MAX], cor[MAX];
                                                            42 };
3 void kahn(int n) {
      int label = 1:
                                                                    Dfs Tree
                                                              5.5
       priority_queue <int, vector <int>, greater <int>> pq
       ; // trocar por queue para O(n)
                                                            int desce[MAX], sobe[MAX], vis[MAX], h[MAX];
       for(int i = 1; i <= n; i++) {
                                                            1 int backedges[MAX], pai[MAX];
           if(in[i] == 0) {
               pq.push(i);
                                                            4 // backedges[u] = backedges que comecam embaixo de (
                                                                  ou =) u e sobem pra cima de u; backedges[u] == 0
      }
1.0
                                                                   => u eh ponte
                                                            5 void dfs(int u, int p) {
       while(pq.size()) {
12
                                                                  if(vis[u]) return;
          int u = pq.top(); pq.pop();
13
                                                                   pai[u] = p;
           cor[u] = label++;
14
                                                                   h[u] = h[p]+1;
           for(auto prox : g[u]) {
15
                                                            9
                                                                   vis[u] = 1;
16
               in[prox] --;
                                                            10
               if(in[prox] == 0) {
                                                            11
                                                                   for(auto v : g[u]) {
                   pq.push(prox);
1.8
                                                                       if(p == v or vis[v]) continue;
                                                            12
               }
19
                                                            13
                                                                       dfs(v, u);
           }
20
                                                                       backedges[u] += backedges[v];
                                                            14
       }
21
                                                            15
22 }
                                                            16
                                                                   for(auto v : g[u]) {
                                                                       if(h[v] > h[u]+1)
                                                            17
  5.4 Hungarian
                                                                           desce[u]++;
                                                                       else if(h[v] < h[u]-1)
                                                            1.9
1 template < typename T> struct hungarian {
                                                                           sobe[u]++;
                                                            20
      int n, m;
                                                            21
      vector < vector < T >> a;
                                                                   backedges[u] += sobe[u] - desce[u];
                                                            22
```

```
23
                                                          5.9
                                                          60 const int LOG = 22;
  5.6 Lca
                                                          61 vector < vector < int >> g(N);
                                                          62 int t, n;
1 template < typename T > struct rmq {
                                                          63 vector < int > in(N), height(N);
                                                          64 vector<vector<int>> up(LOG, vector<int>(N));
      vector<T> v;
                                                          65 void dfs(int u, int h=0, int p=-1) {
      int n; static const int b = 30;
                                                                up[0][u] = p;
                                                          66
      vector < int > mask , t;
                                                                 in[u] = t++;
                                                          67
                                                                 height[u] = h;
      int op(int x, int y) { return v[x] < v[y] ? x : y 68
                                                                 for (auto v: g[u]) if (v != p) dfs(v, h+1, u);
                                                          69
                                                          70 }
      int msb(int x) { return __builtin_clz(1) -
      __builtin_clz(x); }
                                                          72 void blift() {
      rmq() {}
      rmq(const vector<T>& v_) : v(v_), n(v.size()),
                                                          73
                                                                up[0][0] = 0;
                                                          74
                                                                 for (int i=1;i<LOG;i++) {</pre>
      mask(n), t(n) {
          for (int i = 0, at = 0; i < n; mask[i++] = at 75
                                                                      for (int j=0;j<n;j++) {
10
                                                                          up[i][j] = up[i-1][up[i-1][j]];
       |= 1) {
                                                          7.6
               at = (at << 1) &((1 << b) -1);
                                                          78
               while (at and op(i, i-msb(at&-at)) == i)
                                                          79 }
      at ^= at&-at;
          }
13
          for (int i = 0; i < n/b; i++) t[i] = b*i+b-1-81 int lca(int u, int v) {
14
                                                                 if (u == v) return u;
      msb(mask[b*i+b-1]);
                                                                 if (in[u] < in[v]) swap(u, v);</pre>
          for (int j = 1; (1<<j) <= n/b; j++) for (int 83
                                                                 for (int i=LOG-1;i>=0;i--) {
      i = 0; i+(1 << j) <= n/b; i++)
                                                          84
                                                                      int u2 = up[i][u];
              t[n/b*j+i] = op(t[n/b*(j-1)+i], t[n/b*(j-85)]
16
                                                                      if (in[u2] > in[v])
       -1)+i+(1<<(j-1))]);
                                                                          u = u2:
17
      int small(int r, int sz = b) { return r-msb(mask[88])
                                                                 return up[0][u];
                                                          89
      r]&((1 << sz) -1)); }
                                                           90 }
      T query(int 1, int r) {
19
                                                          91
          if (r-l+1 <= b) return small(r, r-l+1);</pre>
20
           int ans = op(small(l+b-1), small(r));
                                                          92 t = 0;
                                                          93 dfs(0):
           int x = 1/b+1, y = r/b-1;
           if (x <= y) {
                                                          94 blift();
23
24
               int j = msb(y-x+1);
                                                             5.7 Hld Aresta
               ans = op(ans, op(t[n/b*j+x], t[n/b*j+y
25
       -(1<<j)+1]));
          }
                                                           vector<vector<pair<int, int>>> g(MAX, vector<pair<int</pre>
27
          return ans;
                                                                 ,int>>());
                                                           vi in(MAX), inv(MAX), sz(MAX);
29 };
                                                           3 vi peso(MAX), pai(MAX);
                                                           4 vi head(MAX), tail(MAX), h(MAX);
3.0
31 namespace lca {
      vector < int > g[MAX];
                                                           6 int tin;
32
33
      int v[2*MAX], pos[MAX], dep[2*MAX];
      int t:
                                                           s void dfs(int u, int p=-1, int depth=0){
3.4
3.5
      rmq < int > RMQ;
                                                           9
                                                                sz[u] = 1; h[u] = depth;
                                                           10
                                                                 for(auto &i: g[u]) if(i.ff != p){
36
      void dfs(int i, int d = 0, int p = -1) {
                                                                     auto [v, w] = i;
37
          v[t] = i, pos[i] = t, dep[t++] = d;
                                                                      dfs(v, u, depth+1);
                                                           12
          for (int j : g[i]) if (j != p) {
                                                                      pai[v] = u; sz[u] += sz[v]; peso[v] = w;
39
                                                          13
               dfs(j, d+1, i);
                                                                     if (sz[v] > sz[g[u][0].ff] or g[u][0].ff == p
40
                                                           14
               v[t] = i, dep[t++] = d;
                                                                 ) swap(i, g[u][0]);
41
42
                                                          15
      }
                                                           16 }
43
      void build(int n, int root) {
                                                           void build_hld(int u, int p = -1) {
44
           t = 0;
                                                                 v[in[u] = tin++] = peso[u]; tail[u] = u;
46
           dfs(root);
                                                           19
                                                                 inv[tin-1] = u;
                                                                 for(auto &i: g[u]) if(i.ff != p) {
          RMQ = rmq < int > (vector < int > (dep, dep + 2*n - 1)); 20
47
48
                                                           21
                                                                     int v = i.ff;
                                                                      head[v] = (i == g[u][0] ? head[u] : v);
      int lca(int a, int b) {
49
                                                           22
50
          a = pos[a], b = pos[b];
                                                                      build_hld(v, u);
          return v[RMQ.query(min(a, b), max(a, b))];
5.1
                                                          24
                                                                 if(g[u].size() > 1) tail[u] = tail[g[u][0].ff];
52
                                                           25
53
      int dist(int a, int b) {
                                                          26 }
          return dep[pos[a]] + dep[pos[b]] - 2*dep[pos[27 void init_hld(int root = 0) {
54
      lca(a, b)]];
                                                                 dfs(root);
                                                           28
                                                                 tin = 0:
5.5
                                                           29
56 }
                                                                 build_hld(root);
                                                                 build();
                                                          31
58 // binary lift
                                                          32 }
```

```
33 void reset(){
                                                          28
34
      g.assign(MAX, vector<pair<int,int>>());
                                                          29
                                                                      return ans;
      in.assign(MAX, 0), sz.assign(MAX, 0);
3.5
                                                          3.0
36
      peso.assign(MAX, 0), pai.assign(MAX, 0);
                                                          3.1
      head.assign(MAX, 0); tail.assign(MAX, 0);
                                                          32
                                                                 void addEdge(int from, int to, T cap, T cost) {
                                                                     edges[from].push_back(list.size());
      h.assign(MAX, 0); inv.assign(MAX, 0);
38
                                                          33
                                                                      list.push_back(Edge(to, cap, cost));
                                                                      edges[to].push_back(list.size());
      t.assign(4*MAX, 0); v.assign(MAX, 0);
40
                                                          3.5
      lazy.assign(4*MAX, 0);
                                                                      list.push_back(Edge(from, 0, -cost));
41
                                                          36
42 }
                                                                 }
                                                          37
43 ll query_path(int a, int b) {
                                                          38 private:
      if (a == b) return 0;
                                                          3.9
      if(in[a] < in[b]) swap(a, b);</pre>
45
                                                          40
                                                                 std::vector<std::vector<int>> edges;
                                                                 std::vector<Edge> list;
46
                                                          41
      if(head[a] == head[b]) return query(in[b]+1, in[a 42
                                                                 std::vector<int> from;
47
                                                                 std::vector<T> dist, pot;
                                                          43
      return merge(query(in[head[a]], in[a]),
                                                          44
                                                                 std::vector<bool> visit;
       query_path(pai[head[a]], b));
                                                          4.5
                                                                 /*bool dij(int src, int sink) {
50 void update_path(int a, int b, int x) {
                                                                     T INF = std::numeric_limits < T > :: max();
                                                          47
      if (a == b) return;
                                                                      dist.assign(n, INF);
51
                                                          48
      if(in[a] < in[b]) swap(a, b);</pre>
                                                                      from.assign(n, -1);
52
                                                          49
                                                                     visit.assign(n, false);
53
                                                          5.0
      if(head[a] == head[b]) return (void)update(in[b
                                                                     dist[src] = 0;
      ]+1, in[a], x);
                                                                      for(int i = 0; i < n; i++) {
                                                          52
      update(in[head[a]], in[a], x); update_path(pai[
                                                                          int best = -1;
                                                          5.3
                                                                          for (int j = 0; j < n; j++) {
      head[a]], b, x);
                                                          5.4
                                                                              if(visit[j]) continue;
56
                                                          55
57 ll query_subtree(int a) {
                                                                              if(best == -1 || dist[best] > dist[j
                                                          56
                                                                 ]) best = j;
      if(sz[a] == 1) return 0;
5.8
      return query(in[a]+1, in[a]+sz[a]-1);
59
60 }
                                                                          if(dist[best] >= INF) break;
                                                          5.8
61 void update_subtree(int a, int x) {
                                                                          visit[best] = true;
                                                          5.9
      if(sz[a] == 1) return;
                                                          60
                                                                          for(auto e : edges[best]) {
                                                                              auto ed = list[e];
      update(in[a]+1, in[a]+sz[a]-1, x);
63
                                                          61
64 }
                                                                              if(ed.cap == 0) continue;
                                                                              T toDist = dist[best] + ed.cost + pot
65 int lca(int a, int b) {
      if(in[a] < in[b]) swap(a, b);</pre>
66
                                                                 [best] - pot[ed.to];
       return head[a] == head[b] ? b : lca(pai[head[a]], 64
                                                                              assert(toDist >= dist[best]);
                                                                              if(toDist < dist[ed.to]) {</pre>
                                                          6.5
68 }
                                                           66
                                                                                  dist[ed.to] = toDist;
                                                                                  from[ed.to] = e;
                                                          6.7
  5.8 Mcmf
                                                          68
                                                          6.0
                                                                          }
                                                                     }
                                                           70
1 template <class T = int>
                                                                      return dist[sink] < INF;</pre>
2 class MCMF {
g public:
       struct Edge {
                                                                 std::pair<T, T> augment(int src, int sink) {
           Edge(int a, T b, T c) : to(a), cap(b), cost(c^{74})
                                                                      std::pair<T, T> flow = {list[from[sink]].cap,
      ) {}
           int to;
6
                                                                     for(int v = sink; v != src; v = list[from[v
           T cap, cost;
                                                                 ]^1].to) {
      }:
                                                                          flow.first = std::min(flow.first, list[
      MCMF(int size) {
                                                                 from[v]].cap);
1.0
                                                                          flow.second += list[from[v]].cost;
                                                          7.8
          n = size;
                                                          79
           edges.resize(n);
12
                                                                      for(int v = sink; v != src; v = list[from[v
          pot.assign(n, 0);
                                                          80
13
                                                                 l^1l.to) {
           dist.resize(n);
                                                                          list[from[v]].cap -= flow.first;
                                                          81
1.5
          visit.assign(n, false);
                                                                          list[from[v]^1].cap += flow.first;
                                                          82
16
                                                                      }
                                                          83
                                                                      return flow;
      std::pair<T, T> mcmf(int src, int sink) {
                                                          84
1.8
19
           std::pair<T, T> ans(0, 0);
                                                          85
           if(!SPFA(src, sink)) return ans;
20
                                                                 std::queue < int > q;
                                                          87
21
           fixPot():
                                                                 bool SPFA(int src, int sink) {
          // can use dijkstra to speed up depending on ^{88}\,
22
                                                                      T INF = std::numeric_limits<T>::max();
      the graph
                                                                      dist.assign(n, INF);
                                                          90
           while(SPFA(src, sink)) {
               auto flow = augment(src, sink);
                                                                      from.assign(n, -1);
                                                          91
24
                                                                      q.push(src);
               ans.first += flow.first;
                                                          92
                                                                      dist[src] = 0;
               ans.second += flow.first * flow.second;
                                                          93
26
                                                           94
                                                                      while(!q.empty()) {
               fixPot();
27
```

```
int on = q.front();
                                                          12 void scc(int u, int c){
9.5
               q.pop();
                                                          vis[u] = 1; comp[u] = c;
               visit[on] = false;
                                                                 for(auto v: gi[u]) if(!vis[v]) scc(v, c);
97
                                                          14
               for(auto e : edges[on]) {
                                                          15 }
98
                    auto ed = list[e];
                   if(ed.cap == 0) continue;
                                                          17 void kosaraju(){
100
                   T toDist = dist[on] + ed.cost + pot[ 18
                                                                 for(int i=0;i<n;i++) vis[i] = 0;</pre>
       on] - pot[ed.to];
                                                                 for(int i=0;i<n;i++) if(!vis[i]) dfs(i);</pre>
                                                          19
                   if(toDist < dist[ed.to]) {</pre>
                                                                 for(int i=0; i<n; i++) vis[i] = 0;
                                                          20
                       dist[ed.to] = toDist;
                                                         21
                                                                 while(S.size()){
103
                        from[ed.to] = e;
                                                                     int u = S.top();
                                                          22
104
                        if(!visit[ed.to]) {
                                                          23
                                                                     S.pop();
                            visit[ed.to] = true;
106
                                                          24
                                                                     if(!vis[u]) scc(u, u);
                            q.push(ed.to);
                                                          25
                       }
108
                                                          26 }
                   }
                                                             5.11 Dinic
               }
           }
           return dist[sink] < INF;</pre>
                                                           1 const int N = 300;
       }
113
114
                                                           3 struct Dinic {
       void fixPot() {
115
                                                                struct Edge {
                                                           4
           T INF = std::numeric_limits <T>::max();
116
                                                                     int from, to; ll flow, cap;
           for(int i = 0; i < n; i++) {
               if(dist[i] < INF) pot[i] += dist[i];</pre>
118
                                                                 vector < Edge > edge;
119
       }
120
                                                                 vector < int > g[N];
                                                           g
121 };
                                                                 int ne = 0;
                                                           10
                                                                 int lvl[N], vis[N], pass;
                                                          11
  5.9 Centroid
                                                          12
                                                                 int qu[N], px[N], qt;
                                                          13
                                                                 ll run(int s, int sink, ll minE) {
                                                          14
 int sz[MAX];
                                                                     if(s == sink) return minE;
                                                          15
 2 bool erased[MAX];
                                                          16
 3 vi grafo[MAX];
                                                                     11 \text{ ans} = 0;
                                                          1.8
 5 void dfs(int u, int p=-1){
                                                                     for(; px[s] < (int)g[s].size(); px[s]++) {</pre>
                                                          19
      sz[u] = 1;
                                                          2.0
                                                                          int e = g[s][ px[s] ];
       for(int v: grafo[u]) if(v!=p and !erased[v]){
                                                                          auto &v = edge[e], &rev = edge[e^1];
                                                          21
           dfs(v, u);
                                                                          if(lvl[v.to] != lvl[s]+1 || v.flow >= v.
                                                          22
           sz[u] += sz[v];
 9
                                                                 cap)
10
                                                                              continue;
                                                                                                  // v.cap - v.flow
11 }
                                                                  < lim
                                                                          11 tmp = run(v.to, sink,min(minE, v.cap-v
int centroid(int u, int p=-1, int size=-1){
                                                                  .flow));
       if(size == -1) size = sz[u];
14
                                                                          v.flow += tmp, rev.flow -= tmp;
                                                          25
       for(int v: grafo[u])
15
                                                          26
                                                                          ans += tmp, minE -= tmp;
          if(v!=p and !erased[v] and sz[v]>size/2)
16
                                                                          if(minE == 0) break:
                                                          2.7
               return centroid(v, u, size);
                                                          28
1.8
       return u:
                                                          29
                                                                     return ans;
19 }
                                                          30
20
                                                                 bool bfs(int source, int sink) {
                                                          31
21 pii centroids(int u=1){ // idx 1
                                                                     qt = 0;
                                                          32
                                                                     qu[qt++] = source;
                                                          33
       int c1=centroid(u), c2=c1;
2.3
                                                                     lvl[source] = 1;
                                                          3.4
       for(int v: grafo[c1]) if(2*sz[v]==sz[u]) c2=v;
24
                                                                     vis[source] = ++pass;
                                                          3.5
       return {c1, c2};
25
                                                                     for(int i = 0; i < qt; i++) {
                                                          36
26 }
                                                                         int u = qu[i];
                                                          37
                                                                         px[u] = 0;
   5.10 Kosaraju
                                                                          if(u == sink) return true;
                                                          3.9
                                                                          for(auto& ed : g[u]) {
                                                                              auto v = edge[ed];
 1 int n;
                                                          41
 vi g[MAX], gi[MAX]; // grafo invertido
                                                                              if(v.flow >= v.cap || vis[v.to] ==
                                                          42
 3 int vis[MAX], comp[MAX]; // componente conexo de cada
                                                                 pass)
                                                                                  vertice
                                                          43
                                                                              vis[v.to] = pass;
 4 stack<int> S;
                                                                              lvl[v.to] = lvl[u]+1;
                                                          45
 6 void dfs(int u){
                                                                              qu[qt++] = v.to;
                                                          46
                                                                          }
       vis[u] = 1;
                                                          47
       for(auto v: g[u]) if(!vis[v]) dfs(v);
                                                                     }
                                                          48
       S.push(u);
                                                                     return false;
                                                           49
10 }
                                                          5.0
                                                                 11 flow(int source, int sink) {
                                                          51
```

```
reset_flow();
52
53
           11 \text{ ans} = 0;
                                                                  if(head[a] == head[b]) return query(in[b], in[a])
           //for(lim = (1LL << 62); lim >= 1; lim /= 2)
5.4
           while(bfs(source, sink))
                                                                  return merge(query(in[head[a]], in[a]),
               ans += run(source, sink, LLINF);
                                                                  query_path(pai[head[a]], b));
           return ans:
                                                           47 }
57
                                                           48 void update_path(int a, int b, int x) {
      void addEdge(int u, int v, ll c, ll rc) {
                                                                  if(in[a] < in[b]) swap(a, b);</pre>
59
                                                           49
           Edge e = \{u, v, 0, c\};
60
                                                           50
           edge.pb(e);
                                                                  if(head[a] == head[b]) return (void)update(in[b],
61
                                                           51
           g[u].push_back(ne++);
                                                                   in[a], x):
62
63
                                                                  update(in[head[a]], in[a], x); update_path(pai[
           e = {v, u, 0, rc};
64
                                                                  head[a]], b, x);
                                                           53 }
           edge.pb(e);
65
66
           g[v].push_back(ne++);
                                                           54 ll query_subtree(int a) {
                                                                  return query(in[a], in[a]+sz[a]-1);
67
                                                           55
68
      void reset_flow() {
                                                           56 }
          for(int i = 0; i < ne; i++)
                                                           57 void update_subtree(int a, int x) {
69
                                                                  update(in[a], in[a]+sz[a]-1, x);
               edge[i].flow = 0;
                                                           58
                                                           59 }
           memset(lvl, 0, sizeof(lvl));
           memset(vis, 0, sizeof(vis));
                                                           60 int lca(int a, int b) {
72
           memset(qu, 0, sizeof(qu));
                                                                  if(in[a] < in[b]) swap(a, b);</pre>
73
                                                           61
7.4
           memset(px, 0, sizeof(px));
                                                           62
                                                                  return head[a] == head[b] ? b : lca(pai[head[a]],
           qt = 0; pass = 0;
                                                           63 }
7.6
77 };
```

5

12

1.7

20

21

22

2.3

24

25

27

28

3.1

32

3.3

34

35

36

38

3.9

5.12 Hld Vertice

```
1 // Use it together with recursive_segtree
vector < vi > g(MAX, vi());
3 vi in(MAX), inv(MAX), sz(MAX);
4 vi peso(MAX), pai(MAX);
5 vi head(MAX), tail(MAX), h(MAX);
7 int tin;
9 void dfs(int u, int p=-1, int depth=0){
      sz[u] = 1; h[u] = depth;
      for(auto &v: g[u]) if(v != p){
          dfs(v, u, depth+1);
12
          pai[v] = u; sz[u] += sz[v];
          if (sz[v] > sz[g[u][0]] or g[u][0] == p) swap 11
14
      (v, g[u][0]);
15
16 }
void build_hld(int u, int p = -1) {
      v[in[u] = tin++] = peso[u]; tail[u] = u;
1.8
19
      inv[tin-1] = u;
      for(auto &v: g[u]) if(v != p) {
20
21
          head[v] = (v == g[u][0] ? head[u] : v);
           build_hld(v, u);
22
23
      if(g[u].size() > 1) tail[u] = tail[g[u][0]];
24
25
26 void init_hld(int root = 0) {
27
      dfs(root);
      tin = 0;
28
      build_hld(root);
30
      build();
31 }
32 void reset(){
      g.assign(MAX, vi());
3.3
      in.assign(MAX, 0), sz.assign(MAX, 0);
      {\tt peso.assign(MAX, 0), pai.assign(MAX, 0);}
3.5
      head.assign(MAX, 0); tail.assign(MAX, 0);
3.7
      h.assign(MAX, 0); inv.assign(MAX, 0);
38
      t.assign(4*MAX, 0); v.assign(MAX, 0);
39
      lazy.assign(4*MAX, 0);
40
41 }
42 ll query_path(int a, int b) {
      if(in[a] < in[b]) swap(a, b);</pre>
```

6 Numeric

Lagrange Interpolation 6.1

```
1 // Lagrange's interpolation O(n^2)
2 ld interpolate(vii d, ld x){
      1d y = 0;
       int n = d.size();
       for(int i=0;i<n;i++){</pre>
           ld yi = d[i].ss;
           for(int j=0;j<n;j++)</pre>
               if(j!=i)
                   yi = yi*(x - d[j].ff)/(ld)(d[i].ff - d
       [i].ff):
           y += yi;
       return y;
14 }
16 // O(n)
18 template < typename T = mint >
19 struct Lagrange {
       vector < T > y, den, l, r;
       int n:
       Lagrange(const vector < T > & _y) : y(_y), n(_y.size
       ()) {
           den.resize(n, 0);
           1.resize(n, 0); r.resize(n, 0);
           for (int i = 0; i < n; i++) {</pre>
                den[i] = ifac[i] * ifac[n - 1 - i];
                if ((n - 1 - i) % 2 == 1) den[i] = -den[i
       ];
       }
       T eval(T x) {
           1[0] = 1;
           for (int i = 1; i < n; i++)</pre>
               l[i] = l[i-1] * (x + -T(i-1));
           r[n - 1] = 1;
           for (int i = n - 2; i >= 0; i--)
               r[i] = r[i+1] * (x + -T(i+1));
```

```
if(!i or !j)
40
41
          T ans = 0;
                                                          12
                                                                            dp[i][j] = 1;
          for (int i = 0; i < n; i++) {
                                                                         else if(a[i][j] == a[i-1][j] and
42
                                                          13
              T num = 1[i] * r[i];
                                                                                 a[i][j] == a[i][j-1] and
43
                                                          14
               ans = ans + y[i] * num * den[i];
                                                                                 a[i][j] == a[i-1][j-1])
          }
                                                                             dp[i][j] = min(min(dp[i-1][j], dp[i][
45
                                                          16
                                                                j-1]),
46
          return ans;
                                                                                             dp[i-1][j-1]) + 1;
47
                                                                         else dp[i][j] = 1;
48 };
                                                          18
                                                          19
  6.2 Newton Raphson
                                                                         result = max(result, dp[i][j]);
                                                          20
                                                          21
                                                                     }
                                                                }
                                                          22
1 // Newton Raphson
                                                          23
                                                          24
                                                                 return result;
3 ld f(x) { return x*2 + 2; }
4 ld fd(x){ return 2; } // derivada
                                                                 Dp Digitos
                                                            7.2
6 ld root(ld x){
      // while(f(x)>EPS)
      for(int i=0;i<20;i++){
                                                          1 // dp de quantidade de numeros <= r com ate qt
          if(fd(x) < EPS)
                                                                digitos diferentes de 0
             x = LLINF;
10
                                                          2 ll dp(int idx, string& r, bool menor, int qt, vector<
                                                                vector < vi>> & tab) {
              x = x - f(x)/fd(x);
12
                                                                if(qt > 3) return 0;
13
                                                                if(idx >= r.size()) {
                                                          4
14
      return x;
                                                          5
                                                                     return 1;
15 }
                                                                if(tab[idx][menor][qt] != -1)
  6.3 Simpson's Formula
                                                                    return tab[idx][menor][qt];
                                                                11 \text{ res} = 0;
_{1} inline ld simpson(ld fl, ld fr, ld fmid, ld l, ld r){ ^{10}}
                                                                for(int i = 0; i <= 9; i++) {
      return (fl+fr+4*fmid)*(r-1)/6;
2
                                                                    if (menor or i <= r[idx]-'0') {
                                                                         res += dp(idx+1, r, menor or i < (r[idx]-
                                                                 '0') , qt+(i>0), tab);
5 ld rsimpson(ld slr, ld fl, ld fr, ld fmid, ld l, ld r
6 {
      1d \ mid = (1+r)/2;
                                                          16
      1d fm1 = f((1+mid)/2), fmr = f((mid+r)/2);
                                                          17
                                                                 return tab[idx][menor][qt] = res;
      ld slm = simpson(fl,fmid,fml,l,mid);
      ld smr = simpson(fmid,fr,fmr,mid,r);
                                                            7.3 Partition Problem
      if(fabsl(slr-slm-smr) < EPS) return slm+smr; //</pre>
      aprox. good enough
      return rsimpson(slm,fl,fmid,fml,l,mid)+rsimpson(
                                                          1 // Partition Problem DP O(n2)
      smr,fmid,fr,fmr,mid,r);
                                                           2 bool findPartition(vi &arr){
13 }
                                                                 int sum = 0;
14
                                                                int n = arr.size();
                                                           4
15 ld integrate(ld l, ld r)
16
                                                                for(int i=0;i<n;i++)</pre>
      1d \ mid = (1+r)/2;
                                                                    sum += arr[i];
      1d fl = f(1), fr = f(r);
1.8
      ld fmid = f(mid);
19
                                                                if(sum&1) return false:
      return rsimpson(simpson(fl,fr,fmid,l,r),fl,fr,
      fmid,1,r);
                                                                bool part[sum/2+1][n+1];
21 }
                                                                 for(int i=0;i<=n;i++)
                                                          13
       DP
                                                                    part[0][i] = true;
                                                          14
                                                                for(int i=1;i<=sum/2;i++)</pre>
                                                          16
  7.1
       Largest Ksubmatrix
                                                                    part[i][0] = false;
                                                          17
                                                          18
                                                                 for(int i=1;i<=sum/2;i++){</pre>
1 int n. m:
                                                          1.9
1 int a[MAX][MAX];
                                                                    for(int j=1;j<=n;j++){
                                                                         part[i][j] = part[i][j-1];
_3 // Largest K such that exists a block K*K with equal _{21}
                                                                         if(i >= arr[j-1])
4 int largestKSubmatrix(){
                                                                             part[i][j] |= part[i - arr[j-1]][j
      int dp[n][m];
                                                                 -1];
      memset(dp, 0, sizeof(dp));
                                                          24
                                                          2.5
      int result = 0;
                                                                 return part[sum / 2][n];
                                                          26
      for(int i = 0 ; i < n ; i++){
                                                          27 }
9
```

for(int j = 0 ; j < m ; j++){

10

7.4 Aliens

```
1 // Solves https://codeforces.com/contest/1279/problem 1 multiset<int> S;
3 // dado um vetor de inteiros, escolha k subsegmentos
       disjuntos de soma ámxima
4 // em vez de rodar a dp[i][k] = melhor soma éat i
      usando k segmentos,
_{5} // vc roda uma dp[i] adicionando um custo W toda vez ^{8} // size of the lis
      que usa um novo subsegmento,
6 // e faz busca ábinria nesse W pra achar o custo
      ímnimo que usa exatamente K intervalos
8 11 n, k, L;
9 pll check(ll w, vl& v){
       vector < pll > dp(n+1);
       dp[0] = \{0,0\};
11
12
       for (int i=1;i<=n;i++) {</pre>
           dp[i] = dp[i-1];
13
           dp[i].ff += v[i];
14
           if(i-L>=0){
               pll t = \{dp[i-L].ff + w, dp[i-L].ss + 1\};<sup>20</sup>
16
               dp[i] = min(dp[i], t);
17
           }
1.8
      }
19
20
21
      return dp[n];
22 }
23
24 ll solve(vl v){
      11 1=-1, r=n+1, ans=-1;
2.5
       while(1<=r){
26
           11 \text{ mid} = (1+r)/2;
27
           pll c = check(mid, v);
28
           if(c.ss <= k){
               r = mid - 1;
3.0
3.1
               ans = mid;
           }else{
32
               l = mid + 1;
33
      }
3.5
36
      pll c = check(ans, v);
3.7
3.8
       if(ans < 0) return 0;</pre>
40
       // we can simply use k insted of c.ss ~magic~
41
       return c.ff - ans*k;
42
43 }
45 int32_t main()
46 {sws;
47
48
       string s;
       cin >> n >> k >> L;
49
      cin >> s;
50
51
       vl upper(n+1, 0), lower(n+1, 0);
52
       for(int i=0;i<n;i++)</pre>
           if('A'<= s[i] and s[i] <= 'Z')
54
               upper[i+1] = 1;
5.5
       for(int i=0;i<n;i++)
56
           if('a' \le s[i] \text{ and } s[i] \le 'z')
5.7
               lower[i+1] = 1;
59
       cout << min(solve(lower),</pre>
6.0
                    solve(upper)) << endl;</pre>
61
62
       return 0;
63
64 }
```

7.5 Lis

```
2 for(int i=0;i<n;i++){</pre>
     auto it = S.upper_bound(vet[i]); // low for inc
       if(it != S.end())
          S.erase(it):
 5
       S.insert(vet[i]);
 6
 7 }
 9 int ans = S.size();
_{11} ////////////////////////// see that later
12 // https://codeforces.com/blog/entry/13225?#comment
       -180208
14 vi LIS(const vi &elements){
       auto compare = [&](int x, int y) {
           return elements[x] < elements[y];</pre>
1.6
17
18
       set < int, decltype(compare) > S(compare);
1.9
       vi previous( elements.size(), -1 );
       for(int i=0; i<int( elements.size() ); ++i){</pre>
21
           auto it = S.insert(i).first;
22
           if(it != S.begin())
2.3
               previous[i] = *prev(it);
24
           if(*it == i and next(it) != S.end())
25
               S.erase(next(it));
26
27
28
       vi answer;
29
30
       answer.push_back( *S.rbegin() );
       while ( previous[answer.back()] != -1 )
31
          answer.push_back( previous[answer.back()] );
32
       reverse( answer.begin(), answer.end() );
3.3
34
       return answer;
35 }
```

8 Strings

8.1Manacher

```
1 // O(n), d1 -> palindromo impar, d2 -> palindromo par
        (centro da direita)
_2 void manacher(string &s, vi &d1, vi &d2) {  
      int n = s.size();
      for(int i = 0, l = 0, r = -1; i < n; i++) {
          int k = (i > r) ? 1 : min(d1[l + r - i], r -
5
      i + 1);
          while (0 <= i - k && i + k < n && s[i - k] ==
      s[i + k]) {
7
              k++:
          }
8
9
          d1[i] = k - -;
          if(i + k > r) {
10
              1 = i - k;
11
12
               r = i + k;
13
14
15
16
      for(int i = 0, l = 0, r = -1; i < n; i++) {
          int k = (i > r) ? 0 : min(d2[l + r - i + 1],
1.7
      r - i + 1);
          while (0 <= i - k - 1 && i + k < n && s[i - k
18
      - 1] == s[i + k]) {
              k++;
19
2.0
           d2[i] = k--;
21
          if(i + k > r) {
22
              1 = i - k - 1;
23
```

```
r = i + k:
                                                                 while((1<<k) < n){
24
                                                          16
25
          }
                                                          17
                                                                     vector < pair < pii, int > > a(n);
      }
                                                                     for(int i=0;i<n;i++)</pre>
26
                                                          18
27 }
                                                          19
                                                                         a[i] = \{\{c[i], c[(i+(1<< k))%n]\}, i\};
                                                                     sort(a.begin(), a.end());
  8.2 Suffix Automaton
                                                          21
                                                                     for(int i=0;i<n;i++) p[i] = a[i].ss;</pre>
                                                                     c[p[0]]=0;
_{1} const int SA = 2*N; // Node 1 is the initial node of ^{23}
                                                                     for(int i=1;i<n;i++)</pre>
      the automaton
                                                                         c[p[i]] = c[p[i-1]] + (a[i].ff!=a[i-1].ff
2 int last = 1;
                                                                 ):
3 int len[SA], link[SA];
                                                                     k++:
4 array<int, 26> to[SA]; // maybe map<int, int>
                                                                 }
                                                          27
5 int lastID = 1;
                                                          28
                                                                 return p;
6 void push(int c) {
                                                          29 }
      int u = ++lastID;
      len[u] = len[last] + 1;
                                                           8.5 Suffix Array
      int p = last;
10
      last = u; // update last immediately
11
                                                          vector<int> suffix_array(string s) {
      for (; p > 0 && !to[p][c]; p = link[p])
12
                                                                s += "$";
                                                           2
          to[p][c] = u;
1.3
                                                                 int n = s.size(), N = max(n, 260);
                                                           3
14
                                                           4
                                                                 vector < int > sa(n), ra(n);
      if (p == 0) { link[u] = 1; return; }
                                                                 for (int i = 0; i < n; i++) sa[i] = i, ra[i] = s[
16
       int q = to[p][c];
      if (len[q] == len[p] + 1) { link[u] = q; return;
18
                                                                 for (int k = 0; k < n; k ? k *= 2 : k++) {
                                                                     vector < int > nsa(sa), nra(n), cnt(N);
19
      int clone = ++lastID;
20
                                                                     for (int i = 0; i < n; i++) nsa[i] = (nsa[i] -</pre>
      len[clone] = len[p] + 1;
21
                                                                 k+n) %n, cnt[ra[i]]++;
      link[clone] = link[q];
                                                                     for (int i = 1; i < N; i++) cnt[i] += cnt[i</pre>
22
      link[q] = link[u] = clone;
      to[clone] = to[q];
24
                                                                     for (int i = n-1; i+1; i--) sa[--cnt[ra[nsa[i
      for (int pp = p; to[pp][c] == q; pp = link[pp])
25
                                                                 ]]]] = nsa[i];
          to[pp][c] = clone;
26
                                                           13
27 }
                                                                     for (int i = 1, r = 0; i < n; i++) nra[sa[i]]
                                                           14
                                                                  = r += ra[sa[i]] !=
  8.3 Edit Distance
                                                                         ra[sa[i-1]] or ra[(sa[i]+k)%n] != ra[(sa[
                                                                 i -1]+k)%n];
                                                                     ra = nra:
int edit_distance(int a, int b, string& s, string& t) 16
                                                                     if (ra[sa[n-1]] == n-1) break;
      // indexado em 0, transforma s em t
                                                                 return vector < int > (sa.begin() +1, sa.end());
                                                          19
      if(a == -1) return b+1;
      if(b == -1) return a+1;
                                                          20 }
      if(tab[a][b] != -1) return tab[a][b];
                                                          21
                                                          22 vector < int > kasai(string s, vector < int > sa) {
                                                               int n = s.size(), k = 0;
      int ins = INF, del = INF, mod = INF;
                                                          2.3
                                                                 vector < int > ra(n), lcp(n);
      ins = edit_distance(a-1, b, s, t) + 1;
                                                                 for (int i = 0; i < n; i++) ra[sa[i]] = i;</pre>
                                                          25
      del = edit_distance(a, b-1, s, t) + 1;
      mod = edit_distance(a-1, b-1, s, t) + (s[a] != t[^{26}]
                                                                 for (int i = 0; i < n; i++, k -= !!k) {</pre>
                                                           27
      b]);
                                                                     if (ra[i] == n-1) { k = 0; continue; }
                                                                     int j = sa[ra[i]+1];
      return tab[a][b] = min(ins, min(del, mod));
12
                                                                     while (i+k < n and j+k < n and s[i+k] == s[j+
13 }
                                                          3.0
                                                                 kl) k++:
                                                                     lcp[ra[i]] = k;
  8.4 Suffix Array Old
                                                          3.1
                                                          32
                                                                 return lcp;
                                                          33
vi suffix_array(string s){
                                                          34 }
      s.pb('$');
      int n = s.size();
                                                             8.6 Lcs
      vi p(n), c(n);
      vector < pair < char, int > > a(n);
                                                          string LCSubStr(string X, string Y)
      for(int i=0;i<n;i++) a[i] = {s[i], i};</pre>
                                                          2 {
                                                                 int m = X.size();
      sort(a.begin(), a.end());
                                                                 int n = Y.size();
      for(int i=0;i<n;i++) p[i] = a[i].ss;
10
      c[p[0]]=0;
                                                                 int result = 0, end;
      for(int i=1;i<n;i++)</pre>
                                                                 int len[2][n];
12
          c[p[i]] = c[p[i-1]] + (a[i].ff!=a[i-1].ff);
                                                                 int currRow = 0;
14
      int k=0;
                                                                 for(int i=0;i<=m;i++){</pre>
1.5
```

```
for(int j=0;j<=n;j++){
                                                          4 void add_string(const char *str, int id){
12
              if(i==0 || j==0)
                                                                int p = 1;
                  len[currRow][j] = 0;
                                                                 for(int i = 0; str[i]; i++){
1.3
                                                                    int ch = str[i] - 'a'; // !
               else if(X[i-1] == Y[j-1]){
14
                                                                     if(!to[p][ch]) to[p][ch] = ne++;
                   len[currRow][j] = len[1-currRow][j-1]
                                                                     p = to[p][ch];
       + 1:
                   if(len[currRow][j] > result){
                       result = len[currRow][j];
                                                                 term[p]++;
                       end = i - 1;
                                                          12 }
18
                                                          13 void init(){
               }
                                                                 for(int i = 0; i < ne; i++) fail[i] = 1;</pre>
20
                                                          14
               else
                                                          15
                                                                 queue < int > q; q.push(1);
                                                                 int u, v; char c;
                   len[currRow][j] = 0;
                                                          16
          }
                                                          17
                                                                 while(!q.empty()){
24
                                                          18
                                                                     u = q.front(); q.pop();
           currRow = 1 - currRow;
                                                                     for(int i = 0; i < A; i++){
25
                                                          19
                                                          20
                                                                         if(to[u][i]){
                                                                             v = to[u][i]; q.push(v);
                                                          2.1
      if (result ==0)
                                                                             if(u!= 1){
          return string();
                                                                                 fail[v] = to[ fail[u] ][i];
29
                                                          23
                                                                                 term[v] += term[ fail[v] ];
30
                                                          24
      return X.substr(end - result + 1, result);
31
                                                          25
32 }
                                                          26
                                                                         else if(u != 1) to[u][i] = to[ fail[u] ][
  8.7
        Eertree
                                                                 i];
                                                                         else to[u][i] = 1;
                                                          28
                                                                     }
                                                          29
1 // heavily based on https://ideone.com/YQX9jv,
                                                                 }
                                                          30
2 // which adamant cites here https://codeforces.com/
      blog/entry/13959?#comment - 196033
3 struct Eertree {
                                                            8.9
                                                                  Kmp
      int s[N];
      int n, last, sz;
                                                          string p;
                                                           1 int neighbor[N];
      int len[N], link[N];
                                                           3 int walk(int u, char c) { // leader after inputting '
      int to[N][A];
                                                                 while (u != -1 \&\& (u+1 >= (int)p.size() || p[u +
      Eertree() {
1.0
                                                                 1] != c)) // leader doesn't match
          s[n++] = -1;
                                                                    u = neighbor[u];
          len[1] = -1, link[1] = 1; // "backspace" root 5
                                                                 return p[u + 1] == c ? u+1 : u;
          len[0] = 0, link[0] = 1; // empty root is 0
      (to[backspace root][any char] = empty root)
                                                           8 void build() {
                                                                neighbor[0] = -1; // -1 is the leftmost state
          last = 2;
                                                           9
                                                          10
                                                                 for (int i = 1; i < (int)p.size(); i++)</pre>
           sz = 2;
1.5
                                                                     neighbor[i] = walk(neighbor[i-1], p[i]);
                                                          11
16
      int get_link(int u) {
18
                                                            8.10 Z Func
           while (s[n - len[u] - 2] != s[n - 1]) u =
      link[u];
          return u;
                                                           vector<int> Z(string s) {
21
                                                               int n = s.size();
22
                                                                 vector < int > z(n);
      void push(int c) {
                                                                int x = 0, y = 0;
                                                           4
          s[n++] = c;
24
                                                                 for (int i = 1; i < n; i++) {
           int p = get_link(last);
                                                                     z[i] = max(0, min(z[i - x], y - i + 1));
          if (!to[p][c]) {
26
                                                                     while (i + z[i] < n \text{ and } s[z[i]] == s[i + z[i]]
              int u = ++sz:
27
                                                                 ]]) {
               len[u] = len[p] + 2;
                                                                         x = i; y = i + z[i]; z[i]++;
              link[u] = to[get_link(link[p])][c]; //
29
                                                          9
      may be 0 (empty), but never 1 (backspace)
                                                                 }
                                                          10
               to[p][c] = u;
3.0
                                                                return z;
31
          last = to[p][c];
32
      }
33
                                                            8.11 Lcsubseq
34 };
                                                           1 // Longest Common Subsequence
  8.8 Aho Corasick
                                                           2 string lcs(string x, string y){
                                                                int n = x.size(), m = y.size();
                                                                vector < vi > dp(n+1, vi(m+1, 0));
1 // https://github.com/joseleite19/icpc-notebook/blob/ 4
      master/code/string/aho_corasick.cpp
2 int to[N][A];
                                                                 for(int i=0;i<=n;i++){
                                                           6
3 int ne = 2, fail[N], term[N];
                                                                     for(int j=0;j<=m;j++){</pre>
```

```
if(!i or !j)
                                                                        return true:
                                                            43
                   dp[i][j]=0;
                                                            44
                                                                   }
                else if (x[i-1] == y[j-1])
                                                            45 };
1.0
                   dp[i][j]=dp[i-1][j-1]+1;
                                                               8.13
                                                                       Suffix Array Radix
                    dp[i][j]=max(dp[i-1][j], dp[i][j-1]);
13
           }
14
                                                             void radix_sort(vector<pii>& rnk, vi& ind) {
1.5
                                                                   auto counting_sort = [](vector<pii>& rnk, vi& ind
16
       // int len = dp[n][m];
                                                                        int n = ind.size(), maxx = -1;
       string ans="";
18
                                                                        for(auto p : rnk) maxx = max(maxx, p.ff);
                                                             4
19
                                                             5
       // recover string
20
                                                             6
                                                                        vi cnt(maxx+1, 0), pos(maxx+1), ind_new(n);
       int i = n-1, j = m-1;
21
                                                                        for(auto p : rnk) cnt[p.ff]++;
                                                             7
       while (i \ge 0 \text{ and } j \ge 0) {
22
                                                                        pos[0] = 0;
                                                             8
           if(x[i] == y[j]){
23
                                                             q
24
               ans.pb(x[i]);
                                                                        for(int i = 1; i <= maxx; i++) {</pre>
                                                            10
               i - -; i - -;
25
                                                                            pos[i] = pos[i-1] + cnt[i-1];
                                                            11
           }else if(dp[i][j+1]>dp[i+1][j])
                                                            1.2
27
               i - - ;
                                                            1.3
           else
28
                                                                        for(auto idx : ind) {
                                                            1.4
               j --;
29
                                                                            int val = rnk[idx].ff;
                                                            15
3.0
                                                                            ind_new[pos[val]] = idx;
                                                                            pos[val]++:
                                                            17
       reverse(ans.begin(), ans.end());
32
                                                            18
33
                                                            1.9
34
       return ans;
                                                                        swap(ind, ind_new);
                                                            2.0
35 }
                                                            21
                                                                   };
                                                            22
  8.12 Hash
                                                                    for(int i = 0; i < (int)rnk.size(); i++) swap(rnk</pre>
                                                                    [i].ff, rnk[i].ss);
1 struct Hash {
                                                                    counting_sort(rnk, ind);
                                                            24
                                                                    for(int i = 0; i < (int)rnk.size(); i++) swap(rnk</pre>
      vector < unordered_set <11>> h;
                                                            25
       vector<11> mods = {
                                                                    [i].ff, rnk[i].ss);
          1000000009,1000000021,1000000033,
                                                                    counting_sort(rnk, ind);
           1000000087,1000000093,1000000097,
                                                            27 }
           1000000103,1000000123,1000000181,
                                                            28
           1000000207,1000000223,1000000241,
                                                            29 vi suffix_array(const string& s) {
           1000000271,1000000289,1000000297
                                                                   int n = s.size();
                                                            30
      }:
                                                            31
                                                                   vector < pii > rnk(n, mp(0, 0));
9
      11 p = 31;
                                                                   vi ind(n):
1.0
                                                            32
       int num;
                                                                    forn(i, n) {
                                                            33
                                                                       rnk[i].ff = (s[i] == '$') ? 0 : s[i]-'a'+1;
                                                            34
       Hash(int qt) {
                                                                    // manter '$' como 0
13
           srand(time(0));
1.4
                                                            3.5
                                                                        ind[i] = i;
           num = qt;
15
                                                            36
16
           h.assign(num, unordered_set <11>());
                                                            37
                                                                    for(int k = 1; k <= n; k = (k << 1)) {</pre>
           random_shuffle(all(mods));
                                                            3.8
18
                                                            3.9
                                                                        for(int i = 0; i < n; i++) {</pre>
                                                                            if(ind[i]+k >= n) {
19
                                                             40
      11 compute_hash(string const& s, ll p, ll m) {
                                                                                rnk[ind[i]].ss = 0;
20
                                                            41
           ll res = 0, p_pow = 1;
21
                                                             42
                                                                            else {
22
                                                            43
                                                                                rnk[ind[i]].ss = rnk[ind[i]+k].ff;
           for(char c : s) {
                                                             44
               res = ( res + (c-'a'+1) * p_pow) % m;
24
                                                            45
               p_pow = (p_pow * p) % m;
2.5
                                                             46
                                                                        }
           }
                                                                        radix_sort(rnk, ind); // sort(all(rnk), cmp)
26
                                                             47
                                                                   pra n*log(n), cmp com rnk[i] < rnk[j]</pre>
27
           return res:
       }
                                                             48
29
                                                             49
                                                                        vector < pii > tmp = rnk;
       void add(string const& s) {
                                                                        tmp[ind[0]] = mp(1, 0); // rnk.ff comecar em
30
                                                            50
                                                                   1 pois '$' eh o 0
31
           forn(i, num) {
               ll value = compute_hash(s, p, mods[i]); 51
                                                                        for(int i = 1; i < n; i++) {
32
33
               h[i].insert(value);
                                                                            tmp[ind[i]].ff = tmp[ind[i-1]].ff;
                                                                            if(rnk[ind[i]] != rnk[ind[i-1]]) {
           }
34
                                                            5.3
       }
                                                                                 tmp[ind[i]].ff++;
35
36
                                                            5.5
       bool query(string const& s) {
37
                                                            56
           forn(i, num) {
                                                            57
                                                                        swap(rnk, tmp);
               11 val = compute_hash(s, p, mods[i]);
39
                                                            5.8
                if(!h[i].count(val))
                                                                    return ind;
                                                            59
                   return false;
                                                            60 }
41
           }
                                                            61
42
```

```
\verb|st.assign(n+1, vector < vi>(m+1, vi(k+1)));|\\
62 vi lcp_array(const string& s, const vi& sarray) {
                                                           47
63
      vi inv(s.size());
                                                                       for(int i = 0; i < n; i++)</pre>
                                                           48
                                                                           for(int j = 0; j < m; j++)
      for(int i = 0; i < (int)s.size(); i++) {</pre>
64
                                                           49
           inv[sarray[i]] = i;
                                                                               st[i][j][0] = mat[i][j];
66
                                                           51
      vi lcp(s.size());
                                                                       for(int j = 1; j <= k; j++) {
                                                           52
67
                                                                           for(int x1 = 0; x1 < n; x1++) {</pre>
68
       int k = 0;
                                                                               for(int y1 = 0; y1 < m; y1++) {
      for(int i = 0; i < (int)s.size()-1; i++) {</pre>
69
                                                           5.4
           int pi = inv[i];
                                                                                    int delta = (1 << (j-1));
70
                                                           55
           if(pi-1 < 0) continue;</pre>
                                                                                    if(x1+delta >= n or y1+delta >= m
                                                           56
           int j = sarray[pi-1];
                                                                  ) continue;
72
73
           while(s[i+k] == s[j+k]) k++;
7.4
                                                           5.8
                                                                                    st[x1][y1][j] = st[x1][y1][j-1];
                                                                                    st[x1][y1][j] = f(st[x1][y1][j],
75
           lcp[pi] = k;
           k = max(k-1, 0);
                                                                  st[x1+delta][y1][j-1]);
7.6
                                                                                    st[x1][y1][j] = f(st[x1][y1][j],
                                                                   st[x1][y1+delta][j-1]);
       return vi(lcp.begin()+1, lcp.end()); // LCP(i, j) _{61}
                                                                                    st[x1][y1][j] = f(st[x1][y1][j],
7.9
                                                                   st[x1+delta][y1+delta][j-1]);
        = min(lcp[i], ..., lcp[j-1])
80 }
                                                                               }
                                                                           }
                                                                       }
       ED
                                                           64
  9
                                                           6.5
                                                           66
       Sparse Table
  9.1
                                                                  // so funciona para quadrados
                                                           6.7
                                                           68
                                                                   int query(int x1, int y1, int x2, int y2) {
                                                                       assert(x2-x1+1 == y2-y1+1);
int logv[MAX+1];
                                                           6.9
                                                                       int k = logv[x2-x1+1];
void make_log() {
                                                           7.0
                                                                       int delta = (1 << k);</pre>
      logv[1] = 0; // pre-computar tabela de log
                                                           71
      for (int i = 2; i <= MAX; i++)</pre>
                                                           73
                                                                       int res = st[x1][y1][k];
          logv[i] = logv[i/2] + 1;
                                                                       res = f(res, st[x2 - delta+1][y1][k]);
6 }
                                                           7.4
                                                           7.5
                                                                       res = f(res, st[x1][y2 - delta+1][k]);
7 struct Sparse {
      int n;
                                                           76
                                                                       res = f(res, st[x2 - delta+1][y2 - delta+1][k]
                                                                  1):
      vector < vi > st;
                                                                       return res;
1.0
                                                                  }
                                                           7.8
      Sparse(vi& v) {
                                                           79
          n = v.size();
                                                           80
                                                                  int f(int a, int b) {
           int k = logv[n];
13
                                                                       return a | b;
                                                           81
           st.assign(n+1, vi(k+1, 0));
                                                           82
1.5
           forn(i, n) {
                                                           83
                                                           84 };
              st[i][0] = v[i];
18
                                                              9.2 Color Update
19
           for(int j = 1; j <= k; j++) {
20
               set<ti> inter; // 1, r, color
                   st[i][j] = f(st[i][j-1], st[i + (1 << 2
        (j-1)) [j-1]);
                                                            3
                                                                  vector < ti > update(int 1, int r, int c){
                                                                      if(inter.empty()){ inter.insert({1, r, c});
               }
                                                                  return {}; }
24
                                                                       vector<ti> removed;
                                                                       auto it = inter.lower_bound({1+1, 0, 0});
26
                                                            6
       int f(int a, int b) {
                                                                       it = prev(it);
27
          return min(a, b);
                                                                       while(it != inter.end()){
28
29
                                                            9
                                                                           auto [11, r1, c1] = *it;
                                                                           if ((1 \le 11 \text{ and } 11 \le r) \text{ or } (1 \le r1 \text{ and } r1 \le r)
30
      int query(int 1, int r) {
                                                                   or (11<=1 and r<=r1)){
31
           int k = logv[r-l+1];
                                                                               removed.pb({11, r1, c1});
           return f(st[l][k], st[r - (1 << k) + 1][k]); 12
33
                                                                           else if(11 > r)
                                                                               break;
34
                                                            13
35 };
                                                            14
                                                                           it = next(it);
36
                                                            15
37
                                                           16
                                                                       for(auto [11, r1, c1]: removed){
                                                                           inter.erase({11, r1, c1});
38 struct Sparse2d {
                                                                           if(l1<1) inter.insert({l1, min(r1, l-1),</pre>
39
      int n, m;
                                                           18
40
      vector < vector < vi>> st;
                                                                  c1}):
41
                                                                           if(r<r1) inter.insert({max(l1, r+1), r1,</pre>
      Sparse2d(vector < vi > mat) {
                                                                   c1});
          n = mat.size():
43
                                                           2.0
           m = mat[0].size();
                                                                       if(c != 0) inter.insert({1, r, c});
                                                           21
           int k = logv[min(n, m)];
                                                                       return removed;
45
                                                           22
                                                           23
46
```

```
1 struct Segtree {
24
25
      ti query(int i){
                                                                vector<ll> seg, lazy;
          if(inter.empty()) return {INF, INF, INF};
                                                                 int n, LOG;
26
           return *prev(inter.lower_bound({i+1, 0, 0})); 4
                                                                 Segtree(int n=0){
29 }:
                                                                     this -> n = n:
                                                                      LOG = ceil(log2(n));
  9.3 Segtree Pa
                                                                      seg.assign(2*n, 0);
                                                                      lazy.assign(2*n, 0);
                                                          10
1 int N:
2 vl t(4*MAX, 0);
                                                           11
                                                           12
                                                                 ll merge(ll a, ll b){
3 vl v(MAX, 0);
                                                                     return a + b;
4 vector < pll > lazy(4*MAX, {0,0});
                                                          13
                                                          14
5 // [x, x+y, x+2y...] //
                                                          15
                                                                 void poe(int p, ll x, int tam, bool prop=1){
                                                                      seg[p] += x*tam;
                                                           16
7 inline ll merge(ll a, ll b){
                                                           17
                                                                      if(prop and p < n) lazy[p] += x;</pre>
      return a + b;
                                                           1.8
9 }
                                                                 void sobe(int p){
                                                                     for(int tam = 2; p /= 2; tam *= 2){
void build(int l=0, int r=N-1, int no=1){
                                                          20
                                                                          seg[p] = merge(seg[2*p], seg[2*p+1]);
                                                          21
      if(1 == r){ t[no] = v[1]; return; }
                                                                          if(lazy[p]!=0)
                                                          22
      int mid = (1 + r) / 2;
1.3
                                                          23
                                                                             poe(p, lazy[p], tam, 0);
      build(1, mid, 2*no);
14
                                                                      }
      build(mid+1, r, 2*no+1);
15
                                                          2.5
      t[no] = merge(t[2*no], t[2*no+1]);
16
                                                                  void prop(int p){
                                                           26
                                                                     int tam = 1 << (LOG-1);
                                                           27
                                                                      for(int s = LOG; s; s--, tam /= 2){
19 inline pll sum(pll a, pll b){ return {a.ff+b.ff, a.ss^{28}}
                                                                          int i = p >> s;
      +b.ss}; }
                                                                          if(lazy[i]){
                                                           3.0
                                                           31
                                                                              poe(2*i, lazy[i], tam);
21 inline void prop(int 1, int r, int no){
                                                                              poe(2*i+1, lazy[i], tam);
      auto [x, y] = lazy[no];
                                                          3.2
22
                                                                              lazy[i] = 0;
                                                          3.3
       if(x==0 and y==0) return;
23
      11 len = (r-1+1);
24
                                                                     }
      t[no] += (x + x + y*(len-1))*len / 2;
                                                          35
      if(1 != r){
                                                                 void build(){
          int mid = (1 + r) / 2;
                                                           3.7
                                                                     for(int i = n-1; i; i--)
          lazy[2*no] = sum(lazy[2*no], lazy[no]);
                                                                          seg[i] = merge(seg[2*i], seg[2*i+1]);
          lazy[2*no+1] = sum(lazy[2*no+1], {x + (mid-1)}^{39}
29
                                                           40
      +1)*y, y});
                                                           41
                                                                 11 query(int a, int b){
3.0
                                                                     ll ret = 0;
                                                           42
31
      lazy[no] = {0,0};
                                                                      for(prop(a+=n), prop(b+=n); a <= b; ++a/=2,</pre>
32 }
                                                                  --b/=2) {
33
                                                                          if(a%2 == 1) ret = merge(ret, seg[a]);
34 ll query(int a, int b, int l=0, int r=N-1, int no=1){^{44}
                                                                          if(b\%2 == 0) ret = merge(ret, seg[b]);
35
      prop(l, r, no);
      if(r<a or b<l) return 0;</pre>
36
                                                                     return ret:
37
      if(a<=l and r<=b) return t[no];</pre>
      int mid = (1 + r) / 2;
                                                          48
38
                                                           49
                                                                  void update(int a, int b, int x){
      return merge(
                                                                     int a2 = a += n, b2 = b += n, tam = 1;
                                                          50
          query(a, b, 1, mid, 2*no),
40
                                                                      for(; a \le b; ++a/=2, --b/=2, tam *= 2){
                                                          51
           query(a, b, mid+1, r, 2*no+1)
41
                                                                          if(a%2 == 1) poe(a, x, tam);
42
                                                                          if(b\%2 == 0) poe(b, x, tam);
                                                           5.3
43 }
_{\rm 45} void update(int a, int b, ll x, ll y, int l=0, int r= ^{55}
                                                                      sobe(a2), sobe(b2);
                                                          56
      N-1, int no=1){
                                                           57 };
      prop(1, r, no);
      if(r<a or b<1) return;</pre>
47
                                                                   Segtree Recursive
                                                             9.5
      if(a<=1 and r<=b){
          lazy[no] = \{x, y\};
49
          prop(1, r, no);
                                                           1 int N;
                                                           vector<11> t(4*MAX, 0);
5.1
          return:
                                                           3 vector<ll> v(MAX, 0);
52
      int mid = (1 + r) / 2;
                                                           4 vector<ll> lazy(4*MAX, 0);
5.3
      update(a, b, x, y, 1, mid, 2*no);
54
       update(a, b, x + max((mid-max(1, a)+1)*y, OLL), y \in inline ll merge(ll a, ll b) \{ (mid-max(1, a)+1)*y, OLL) \} 
       , mid+1, r, 2*no+1);
                                                                 return a + b;
      t[no] = merge(t[2*no], t[2*no+1]);
                                                           8 }
57 }
                                                           void build(int l=0, int r=N-1, int no=1){
  9.4 Segtree Iterative Lazy
                                                           if(1 == r){ t[no] = v[1]; return; }
                                                                 int mid = (1 + r) / 2;
```

```
build(1, mid, 2*no);
                                                                 no query(int 1, int r){ // idx 0
1.3
                                                          3.0
14
      build(mid+1, r, 2*no+1);
                                                           31
                                                                      no a(0), b(0);
                                                                      for(l+=n, r+=n+1; l<r; l>>=1, r>>=1){
      t[no] = merge(t[2*no], t[2*no+1]);
15
                                                          3.2
16
                                                          3.3
                                                                          if(1&1)
                                                                              a=merge(a, t[1++]);
                                                          34
18 void prop(int 1, int r, int no){
                                                                          if(r&1)
                                                          35
      if(lazy[no] != 0){
                                                                              b = merge(t[--r], b);
19
          t[no] += lazy[no] * (r-l+1);
2.0
                                                          3.7
          if(1 != r){
                                                         38
                                                                      return merge(a, b);
21
               lazy[2*no] += lazy[no];
                                                          39
               lazy[2*no+1] += lazy[no];
23
                                                          40
                                                           41
                                                                  void update(int p, int value){
                                                                    for(t[p+=n] = no(value); p >>= 1;)
2.5
          lazy[no] = 0;
                                                          42
                                                                          t[p] = merge(t[p<<1], t[p<<1|1]);
                                                          43
                                                                 }
27 }
                                                          44
29 ll query(int a, int b, int l=0, int r=N-1, int no=1){46};
      prop(1, r, no);
3.0
                                                             9.7 Segtree Implicita Lazy
      if(r<a or b<1) return 0;</pre>
      if(a<=l and r<=b) return t[no];</pre>
32
      int mid = (1 + r) / 2;
33
                                                           1 struct node{
      return merge(
                                                               pll val;
34
          query(a, b, l, mid, 2*no),
3.5
                                                                 ll lazy;
           query(a, b, mid+1, r, 2*no+1)
                                                                11 1. r:
      ):
37
                                                                 node(){
38
                                                                      l = -1; r = -1; val = \{0, 0\}; lazy = 0;
39
40 void update(int a, int b, ll x, int l=0, int r=N-1, _{8});
      int no=1){
      prop(1, r, no);
4.1
                                                           10 node tree[40*MAX];
      if(r<a or b<1) return;</pre>
42
                                                           11 int id = 2;
      if(a<=l and r<=b){
                                                           12 11 N=1e9+10;
43
         lazy[no] += x;
44
                                                           13
          prop(l, r, no);
                                                          14 pll merge(pll A, pll B){
          return;
46
                                                                 if(A.ff==B.ff) return {A.ff, A.ss+B.ss};
                                                          16
                                                                 return (A.ff < B.ff ? A:B);</pre>
      int mid = (1 + r) / 2;
48
                                                          17 }
      update(a, b, x, 1, mid, 2*no);
49
                                                          18
      update(a, b, x, mid+1, r, 2*no+1);
                                                         19 void prop(ll l, ll r, int no){
50
      t[no] = merge(t[2*no], t[2*no+1]);
51
                                                         20
                                                                11 \text{ mid} = (1+r)/2;
52 }
                                                                 if(1!=r){
                                                          2.1
                                                                     if (tree [no].l == -1) {
                                                           22
  9.6 Segtree Maxsubarray
                                                                          tree[no].1 = id++;
                                                          23
                                                                          tree[tree[no].1].val = {0, mid-1+1};
                                                          24
1 // Subarray with maximum sum
                                                           2.5
                                                                      }
2 struct no{
                                                                      if (tree [no].r == -1) {
                                                           26
      ll p, s, t, b; // prefix, suffix, total, best
                                                           27
                                                                          tree[no].r = id++;
                                                                          tree[tree[no].r].val = {0, r-(mid+1)+1};
      no(11 x=0): p(x), s(x), t(x), b(x){}
                                                           28
5 } :
                                                           2.9
                                                                      tree[tree[no].1].lazy += tree[no].lazy;
                                                           3.0
7 struct Segtree{
                                                           31
                                                                      tree[tree[no].r].lazy += tree[no].lazy;
      vector < no > t;
                                                           32
      int n:
                                                                 tree[no].val.ff += tree[no].lazy;
9
                                                          33
                                                                  tree[no].lazy=0;
                                                          34
      Segtree(int n){
                                                          35
12
          this -> n = n;
                                                          36
           t.assign(2*n, no(0));
                                                          37 void update(int a, int b, int x, 11 1=0, 11 r=2*N, 11
13
                                                                  no=1){
14
                                                                 prop(l, r, no);
                                                          38
16
      no merge(no 1, no r){
                                                          3.9
                                                                  if(a<=l and r<=b){
17
          no ans;
                                                                     tree[no].lazy += x;
                                                           40
          ans.p = max(0LL, max(1.p, 1.t+r.p));
18
                                                           41
                                                                      prop(1, r, no);
          ans.s = max(0LL, max(r.s, l.s+r.t));
                                                                      return:
19
                                                          42
          ans.t = l.t+r.t;
                                                           43
                                                                 }
          ans.b = max(max(1.b, r.b), 1.s+r.p);
                                                                 if(r<a or b<1) return;
21
                                                          44
                                                                 int m = (1+r)/2;
          return ans;
23
                                                           46
                                                                 update(a, b, x, 1, m, tree[no].1);
24
                                                           47
                                                                 update(a, b, x, m+1, r, tree[no].r);
      void build(){
                                                           48
          for(int i=n-1; i>0; i--)
                                                                 tree[no].val = merge(tree[tree[no].1].val, tree[
26
                                                          49
               t[i]=merge(t[i<<1], t[i<<1|1]);
                                                                 tree[no].r].val);
      }
                                                           50 }
28
29
                                                           51
```

```
52 pll query(int a, int b, int l=0, int r=2*N, int no=1) 19 void update(int pos, int x, int i=1, int j=N, int no
                                                                   if(i==j){
       prop(1, r, no);
5.3
                                                            2.0
       if(a<=l and r<=b) return tree[no].val;</pre>
54
                                                            21
                                                                       t[no].val+=x;
       if(r<a or b<1) return {INF, 0};</pre>
                                                                       return;
       int m = (1+r)/2;
56
                                                            23
       int left = tree[no].1, right = tree[no].r;
                                                                   int meio = (i+j)/2;
                                                            24
                                                            2.5
       return tree[no].val = merge(query(a, b, 1, m,
                                                                   if(pos<=meio){</pre>
59
                                                            26
                                                                       if(t[no].1==0) t[no].1=idx++;
      left),
                                                            27
                                     query(a, b, m+1, r,
                                                                       update(pos, x, i, meio, t[no].1);
60
                                                            28
       right));
                                                            29
61 }
                                                            30
                                                                   else{
                                                                       if(t[no].r==0) t[no].r=idx++;
                                                            31
         Segtree Iterative
                                                            32
                                                                       update(pos, x, meio+1, j, t[no].r);
                                                            33
                                                            34
1 // Segment Tree Iterativa - Max
                                                                   t[no].val=merge(t[t[no].1].val, t[t[no].r].val);
                                                            3.5
                                                            36 }
struct Segtree{
                                                            3.7
      vi t;
                                                            38 int query(int A, int B, int i=1, int j=N, int no=1) {
      int n;
                                                            39
                                                                   if(B<i or j<A)</pre>
                                                                       return 0:
                                                            40
       Segtree(int n){
                                                                   if(A \le i \text{ and } j \le B)
                                                            41
           this -> n = n;
                                                                       return t[no].val;
                                                            42
           t.assign(2*n, 0);
9
                                                            43
10
                                                                   int mid = (i+j)/2;
                                                            44
                                                            45
      int merge(int a, int b){
12
                                                                   int ansl = 0, ansr = 0;
                                                            46
           return max(a, b);
                                                            47
14
                                                                   if(t[no].1!=0) ans1 = query(A, B, i, mid, t[no].1
15
       void build(){
16
                                                                   if(t[no].r!=0) ansr = query(A, B, mid+1, j, t[no
                                                            49
           for(int i=n-1; i>0; i--)
17
               t[i]=merge(t[i<<1], t[i<<1|1]);
                                                            50
19
                                                                   return merge(ansl, ansr);
                                                            51
20
                                                            52 }
       int query(int 1, int r){ // [1, r]
21
           int resl = - INF , resr = - INF ;
22
                                                              9.10 Mergesorttree
           for(l+=n, r+=n+1; l<r; l>>=1, r>>=1){
               if(1&1) resl = merge(resl, t[1++]);
24
                                                            struct ST { // indexado em 0, 0(n * log^2(n) )
                if(r&1) resr = merge(t[--r], resr);
                                                                   int size;
26
                                                                   vector < vl> v;
           return merge(resl, resr);
      }
28
                                                                   vl f(vl a, vl& b) {
29
                                                                       vl res = a;
       void update(int p, int value){
30
                                                                       for(auto val : b) {
           for(t[p+=n]=value; p >>= 1;)
3.1
                                                                            res pb(val);
               t[p] = merge(t[p<<1], t[p<<1|1]);
       }
33
                                                            10
                                                                       sort(all(res));
34
                                                                       return res;
35 };
                                                                   }
                                                            12
                                                            13
         Segtree Implicita
                                                                   ST(int n) {
                                                            14
                                                                       size = n;
                                                            1.5
1 // SegTree Implicita O(nlogMAX)
                                                            16
                                                                       v.assign(4*size, v1());
                                                            17
struct node{
                                                            18
      int val;
                                                                   void build(vector<11>& a, int lx=0, int rx=size
                                                            19
                                                                   -1, int x=1) {
      int 1, r;
      node(int a=0, int b=0, int c=0){
                                                            20
                                                                       if(lx==rx) {
           l=a;r=b;val=c;
                                                            21
                                                                           v[x].pb(a[lx]);
                                                                           return;
9 };
                                                            23
                                                                       }
                                                                       int m = (1x+rx)/2;
                                                            24
11 int idx=2; // 1-> root / 0-> zero element
                                                                       \verb|build(a, lx, m, 2*x);|\\
                                                            25
12 node t[8600010];
                                                            26
                                                                       build(a, m+1, rx, 2*x+1);
13 int N:
                                                            27
                                                                       v[x] = f(v[2*x], v[2*x+1]);
                                                            28
int merge(int a, int b){
                                                            29
                                                                   11 greaterequal(int 1, int r, int k, int lx=0,
       return a + b;
                                                            30
17 }
                                                                   int rx=size-1, int x=1) {
```

18

if(r < lx or l > rx) return 0;

```
if(1 <= 1x and rx <= r) {
                                                                  return 1:
32
                                                           5.5
               auto it = lower_bound(all(v[x]), k);
                                                           56 }
               return (v[x].end() - it);
34
           }
           int m = (1x + rx)/2;
                                                           59 int main()
           ll s1 = greaterequal(l, r, k, lx, m, 2*x);
                                                           60 {sws:
37
           11 	ext{ s2} = 	ext{greaterequal(1, r, k, m+1, rx, 2*x+1)} 	ext{61}
                                                                  int n, m, a, b, k;
                                                           62
                                                                  int v[MAX], aux[MAX];
                                                           63
           return s1 + s2;
                                                                  int root[MAX];
40
                                                           64
      }
                                                           65
41
                                                            66
                                                                   cin >> n >> m;
43 }:
                                                           6.7
                                                                   for(int i=0;i<n;i++){</pre>
                                                           68
          Segpersistente Mkthnum
                                                           6.9
                                                                       cin >> v[i]; aux[i]=v[i];
                                                            70
1 // kth number in range [1, r] if it was ordered
                                                                  sort(v, v+n);
2 struct node {
                                                            72
      int val;
      int 1, r;
                                                           74
                                                                  map < int , int > comp;
                                                           7.5
                                                                  for(int i=0, j=0;i<n;i++)</pre>
      node(int a=-1, int b=-1, int c=0){
                                                            76
                                                                       if(i == 0 or v[i]! = v[i-1])
          val=c;l=a;r=b;
6
                                                                           comp[v[i]]=j++;
8 }:
                                                                  root[0]=build(0, n-1);
                                                            7.9
node tree [8600010]; // 4*nlog(4*n) space = 8600010
                                                            8.0
11 int idx = 0;
                                                            81
                                                                  for(int i=1;i<=n;i++)
                                                                       root[i] = update(0, n-1, root[i-1], comp[aux[
                                                            82
int build(int 1, int r){
                                                                  i-1]]);
       if(l==r)
                                                           8.3
                                                                  for(int i=0;i<m;i++){</pre>
                                                           84
1.5
          return idx++;
                                                                       cin >> a >> b >> k;
                                                           8.5
16
                                                                       cout << v[query(0, n-1, root[a-1], root[b], k</pre>
                                                           86
      int mid = (1+r)/2;
                                                                  )] << endl;
18
       tree[idx].l = build(l, mid);
                                                           87
      tree[idx].r = build(mid+1, r);
20
                                                                  return 0:
                                                           89
21
                                                           90 }
22
       return idx++;
23 }
                                                              9.12 Cht
24
25 int update(int 1, int r, int root, int e){
       if(l>e or r<e)</pre>
                                                            const ll is_query = -LLINF;
                                                            2 struct Line{
27
          return root;
       if(l==e and r==e){
                                                                 11 m, b;
28
29
          tree[idx]=node(-1, -1, tree[root].val+1);
                                                                  mutable function < const Line *() > succ;
                                                                  bool operator < (const Line& rhs) const{</pre>
           return idx++;
30
31
                                                                       if(rhs.b != is_query) return m < rhs.m;</pre>
                                                                       const Line* s = succ();
      int mid = (1+r)/2;
32
                                                                       if(!s) return 0;
33
       tree[idx]=node(update(1, mid, tree[root].1, e),
                                                                       11 x = rhs.m;
                      update(mid+1, r, tree[root].r, e), 9
34
       tree[root].val+1);
                                                           10
                                                                       return b - s \rightarrow b < (s \rightarrow m - m) * x;
       return idx++;
36 }
                                                            12 };
                                                            13 struct Cht : public multiset < Line > { // maintain max m
38 int query(int 1, int r, int root1, int root2, int k){
                                                                  *x+b
3.9
       while(1!=r)
                                                                   bool bad(iterator y){
                                                            14
40
                                                                       auto z = next(y);
                                                                       if(y == begin()){
           int mid=(1+r)/2;
41
          if (tree [tree [root2].1].val-tree [tree [root1].1]
                                                                           if(z == end()) return 0;
      ].val>=k)
                                                           18
                                                                           return y->m == z->m && y->b <= z->b;
                                                                       }
          {
43
                                                            19
44
               r = mid;
                                                            20
                                                                       auto x = prev(y);
               root1 = tree[root1].1;
                                                                       if(z == end()) return y->m == x->m && y->b <=
45
                                                            21
               root2 = tree[root2].1;
                                                                       lelse
47
                                                                  )(y->b-z->b)*(y->m-x->m);
49
               1 = mid + 1;
               k-=tree[tree[root2].1].val-tree[tree[
50
                                                                  void insert_line(ll m, ll b){ // min -> insert (-
                                                            24
       root1].1].val;
                                                                  m,-b) -> -eval()
                                                                      auto y = insert({ m, b });
               root1 = tree[root1].r;
5.1
                                                            2.5
               root2 = tree[root2].r;
                                                                       y \rightarrow succ = [=] \{ return next(y) == end() ? 0 :
           }
                                                                   &*next(y); };
53
       }
                                                                       if(bad(y)){ erase(y); return; }
54
                                                            27
```

```
while(next(y) != end() && bad(next(y))) erase 1 bool initialized = false;
28
      (next(y));
                                                           2 int original_root = 1;
          while(y != begin() && bad(prev(y))) erase(
                                                           3 const int E = 2 * N;
29
                                                           4 vector <int> vt[N]; // virtual tree edges
      prev(y));
3.0
                                                           5 int in[N], out[N], T, t[E<<1];</pre>
      ll eval(ll x){
                                                           6 void dfs_time(int u, int p = 0) {
31
          auto 1 = *lower_bound((Line) { x, is_query })
                                                                 in[u] = ++T;
                                                                 t[T + E] = u;
                                                                 for (int v : g[u]) if (v != p) {
          return 1.m * x + 1.b;
33
                                                                      dfs_time(v, u);
34
                                                           10
35 };
                                                                      t[++T + E] = u;
                                                           11
                                                           12
                                                                 }
  9.13 Bit Kth
                                                          13
                                                                 out[u] = T;
                                                          14 }
                                                          15
1 struct FT {
                                                          int take(int u, int v) { return in[u] < in[v] ? u : v</pre>
      vector < int > bit; // indexado em 1
      int n;
                                                          17 bool cmp_in(int u, int v) { return in[u] < in[v]; }</pre>
                                                          18 void build_st() {
      FT(int n) {
                                                                 in[0] = 0x3f3f3f3f;
                                                          19
          this -> n = n + 1;
                                                          20
                                                                 for (int i = E-1; i > 0; i--)
           bit.assign(n + 1, 0);
                                                          21
                                                                      t[i] = take(t[i << 1], t[i << 1|1]);
                                                          22 }
      int kth(int x){
10
                                                          24 int query(int 1, int r) {
          int resp = 0;
                                                                 int ans = 0;
                                                          25
          x - -:
                                                                 for (1+=E, r+=E; 1 < r; 1>>=1, r>>=1) {
                                                          26
           for(int i=26; i>=0; i--){
13
                                                                      if (1&1) ans = take(ans, t[1++]);
                                                          27
              if(resp + (1<<i) >= n) continue;
14
                                                                      if (r&1) ans = take(ans, t[--r]);
                                                          28
               if(bit[resp + (1<<i)] <= x){</pre>
15
                                                          29
                   x -= bit[resp + (1<<i)];
16
                                                          30
                                                                 return ans;
                   resp += (1<<i);
17
                                                          31 }
               }
                                                          32
          }
19
                                                          33 int get_lca(int u, int v) {
          return resp + 1;
                                                                 if (in[u] > in[v]) swap(u, v);
                                                          34
      }
21
                                                                 return query(in[u], out[v]+1);
                                                          35
22
                                                          36 }
      void upd(int pos, int val){
23
                                                          37
          for(int i = pos; i < n; i += (i&-i))
24
                                                          38 int covers(int u, int v) { // does u cover v?
              bit[i] += val;
                                                                 return in[u] <= in[v] && out[u] >= out[v];
                                                          39
26
                                                           40 }
27 };
                                                           41
                                                          42 int build_vt(vector<int>& vnodes) {
  9.14 Bit
                                                          43
                                                                 assert(initialized);
                                                          44
                                                                 sort(all(vnodes), cmp_in);
                                                           45
1 struct FT {
                                                                 int n = vnodes.size();
      vi bit; // indexado em 1
                                                          46
                                                          47
                                                                 for (int i = 0; i < n-1; i++) {
      int n;
                                                                     int u = vnodes[i], v = vnodes[i+1];
                                                          48
                                                           49
                                                                      vnodes.push_back(get_lca(u, v));
      FT(int n) {
                                                          50
          this -> n = n+1;
                                                                 sort(all(vnodes), cmp_in);
                                                          51
          bit.assign(n+2, 0);
                                                                 vnodes.erase(unique(all(vnodes)), vnodes.end());
                                                          52
                                                          5.3
                                                          5.4
                                                                 for (int u : vnodes)
      int sum(int idx) {
                                                                      vt[u].clear();
                                                          5.5
          int ret = 0;
                                                          56
           for(++idx; idx > 0; idx -= idx & -idx)
12
                                                                 stack<int> s;
                                                          57
              ret += bit[idx];
13
                                                          58
                                                                 for (int u : vnodes) {
           return ret;
14
                                                                      while (!s.empty() && !covers(s.top(), u))
                                                          59
      }
                                                          60
                                                                          s.pop();
16
                                                                      if (!s.empty()) vt[s.top()].push_back(u);
                                                          61
      int sum(int 1, int r) { // [1, r]
                                                                      s.push(u);
          return sum(r) - sum(l - 1);
                                                          62
1.8
                                                          63
19
                                                          64
                                                                 return vnodes[0]; // root
                                                          65 }
      void add(int idx, int delta) {
21
                                                          66
           for(++idx; idx < n; idx += idx & -idx)</pre>
                                                          67 void initialize() {
               bit[idx] += delta;
23
                                                                  initialized = true;
                                                          68
24
                                                                 dfs_time(original_root);
                                                          69
25 };
                                                                 build_st();
                                                          70
                                                          71 }
  9.15 Virtual Tree
```

```
9.16 Treap
                                                                 X[en] = key;
                                                          5.0
                                                          51
                                                                 sz[en] = 1;
                                                                 L[en] = R[en] = 0;
                                                          52
1 // source: https://github.com/victorsenam/caderno/
                                                          53
                                                                 return en++;
      blob/master/code/treap.cpp
                                                          54 }
2 //const int N = ; typedef int num;
                                                          55 int query(int u, int l, int r){//0 index
3 num X[N]; int en = 1, Y[N], sz[N], L[N], R[N];
                                                          56
                                                                 unlaze(u);
4 void calc (int u) { // update node given children
                                                                 if(u! or r < 0 or 1 >= sz[u]) return
                                                          5.7
                                                                 identity_element;
      if(!u) return;
                                                                 if(1 \le 0 \text{ and } r \ge sz[u] - 1) \text{ return subt_data[}u
                                                          58
      sz[u] = sz[L[u]] + 1 + sz[R[u]];
6
                                                                 1:
      // code here, no recursion
                                                                 int ans = query(L[u], 1, r);
8 }
                                                                 if(1 \le sz[L[u]] and sz[L[u]] \le r)
                                                          6.0
9 void unlaze (int u) {
                                                          61
                                                                     ans = max(ans, st[u]);
      if(!u) return;
1.0
                                                                 ans = max(ans, query(R[u], l-sz[L[u]]-1, r-sz[L[u]])
                                                          62
11
      // code here, no recursion
                                                                 ]]-1));
12 }
_{13} void split_val(int u, num x, int &1, int &r) { //\ 1 ^{63}
                                                                 return ans;
                                                          64 }
      gets <= x, r gets > x
      unlaze(u); if(!u) return (void) (1 = r = 0);
14
                                                             9.17 Mingueue
      if(X[u] <= x) { split_val(R[u], x, 1, r); R[u] =</pre>
15
      1; 1 = u; }
      else { split_val(L[u], x, 1, r); L[u] = r; r = u; 1 struct MinQ {
16
                                                                 stack<pair<ll,ll>> in;
      calc(u);
1.7
                                                                 stack<pair<11,11>> out;
19 void split_sz(int u, int s, int &1, int &r) { // 1
                                                                 void add(ll val) {
      gets first s, r gets remaining
                                                                    11 minimum = in.empty() ? val : min(val, in.
      unlaze(u); if(!u) return (void) (1 = r = 0);
                                                                 top().ss);
20
      if(sz[L[u]] < s) \ \{ \ split\_sz(R[u], \ s \ - \ sz[L[u]] \ - \ \ \} 
                                                                     in.push(mp(val, minimum));
21
      1, 1, r); R[u] = 1; 1 = u; }
      else { split_sz(L[u], s, l, r); L[u] = r; r = u;
                                                                 11 pop() {
                                                           10
23
      calc(u):
                                                                     if(out.empty()) {
24 }
                                                                          while(!in.empty()) {
                                                          12
25 int merge(int 1, int r) { // els on l <= els on r</pre>
                                                                              11 val = in.top().ff;
                                                          13
      unlaze(1); unlaze(r); if(!1 || !r) return 1 + r; 14
26
                                                                              in.pop();
                                                                              11 minimum = out.empty() ? val : min(
      if(Y[1] > Y[r]) { R[1] = merge(R[1], r); u = 1; }
2.7
                                                                 val, out.top().ss);
      else { L[r] = merge(1, L[r]); u = r; }
                                                                              out.push({val, minimum});
28
                                                          1.6
29
       calc(u); return u;
30 }
31 void init(int n=N-1) { // XXX call before using other _{19}
                                                                     11 res = out.top().ff;
       funcs
                                                                      out.pop();
      for(int i = en = 1; i <= n; i++) { Y[i] = i; sz[i21]
                                                                      return res;
32
      ] = 1; L[i] = R[i] = 0; }
      random_shuffle(Y + 1, Y + n + 1);
33
                                                          23
34 }
                                                                 11 minn() {
                                                          24
35 void insert(int &u, int it){
                                                                     11 minimum = LLINF;
                                                          2.5
36
      unlaze(u):
                                                                      if(in.empty() || out.empty())
                                                          26
                                                                          minimum = in.empty() ? (11)out.top().ss :
3.7
      if(!u) u = it;
      else if(Y[it] > Y[u]) split_val(u, X[it], L[it],
38
                                                                  (11) in.top().ss;
      R[it]), u = it;
      else insert(X[it] < X[u] ? L[u] : R[u], it);</pre>
3.9
                                                                         minimum = min((11)in.top().ss, (11)out.
40
      calc(u):
                                                                 top().ss);
41 }
                                                           30
42 void erase(int &u, num key){
                                                                      return minimum:
                                                          31
      unlaze(u);
                                                                 }
      if(!u) return;
44
                                                          33
      if(X[u] == key) u = merge(L[u], R[u]);
45
                                                          34
                                                                 11 size() {
      else erase(key \langle X[u] ? L[u] : R[u], key);
46
                                                          35
                                                                      return in.size() + out.size();
47
      calc(u);
                                                          36
48
                                                          37 };
49 int create_node(num key){
```