

Notebook - Maratona de Programação

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1 Algoritmos

1.1 Mochila

```
int val[MAXN], peso[MAXN], dp[MAXN][MAXS]
3 int knapsack(int N, int M) // Objetos | Peso max
       for (i=0;i<=N;i++)</pre>
5
          for(j=0;j<=M;j++)</pre>
               if (i==0 || j==0)
9
                   dp[i][j] = 0;
               else if (peso[i-1] <= j)</pre>
                   dp[i][j] = max(val[i-1]+dp[i-1][j-
      peso[i-1]], dp[i-1][j]);
               else
13
                    dp[i][j] = dp[i-1][j];
14
15
      }
      return dp[N][M];
17
```

1.2 Kadane-DP

```
1 // Largest Sum Contiguous Subarray
2
3 int maxSubArraySum(vector<int> a)
4 {
5    int size = a.size();
6    int max_so_far = a[0];
7    int curr_max = a[0];
8
9    for (int i=1;i<size;i++)
10    {
11         curr_max = max(a[i], curr_max+a[i]);
12         max_so_far = max(max_so_far, curr_max);
13    }
14    return max_so_far;
15 }</pre>
```

1.3 Iterative-BS

```
1 int main()
       int l=1, r=N;
       int res=-1;
4
       while(1 \leq r)
            int m = (1 + r)/2;
9
            if(!ver(m))
10
            {
                1 = m+1;
11
            }
           else
13
14
15
                res = m;
                r = m-1;
16
            }
       }
18
       cout << res << endl;</pre>
19
20
21
       return 0;
22 }
```

2 Grafos

2.1 BFS

```
1 //BFS (Breadth First Search) O(V+A)
3 vector < vector < int >> adj; // adjacency list
     representation
 4 int n; // number of nodes
5 int s; // source vertex
7 queue < int > q;
 8 vector < int > d(n, INF);
9 d[s]=0;
10
11 q.push(s);
12 used[s] = true;
13 while (!q.empty()) {
14
   int v = q.front();
15
      q.pop();
16
       for (int u : adj[v]) {
           if (d[u] > d[v] + 1) {
17
               q.push(u);
               d[u] = d[v] + 1;
19
20
21
       }
22 }
```

2.2 Find-bridges

```
1 #define vi vector<int>
3 vector < vector <int> > grafo;
4 vector < bool > visited;
5 vi t, low;
6 int timer=0;
8 void find_bridges(int v, int p=-1)
9 {
       visited[v] = true;
10
       t[v] = low[v] = timer++;
11
       for(int i=0;i<(int)grafo[v].size();i++)</pre>
12
13
           int vert = grafo[v][i];
14
           if(vert == p)
16
               continue;
17
           if(visited[vert])
               low[v] = min(low[v], t[vert]);
18
           else
19
20
               find_bridges(vert, v);
21
               low[v] = min(low[v], low[vert]);
               if(low[to] > t[v])
23
                    IS_BRIDGE(v, vert);
24
25
       }
26
27 }
28
29 int main()
30 {
       timer = 0;
31
       visited.assign(N+1, false);
       t.assign(N+1, 0);
33
       low.assign(N+1, 0);
34
36
       for(int i=0;i<N;i++)</pre>
           if(!visited[i])
               find_bridges(1);
38
40
       return 0;
41 }
```

2.3 Dijkstra

```
1 // Dijkstra - Shortest Path
```

```
3 #define pii pair<int, int>
4 #define vi vector <int>
                                                            26
                                                                   return minimum;
5 #define vii vector< pair<int,int> >
                                                            27 }
6 #define INF 0x3f3f3f3f
                                                            28
                                                            29 int start[MAX+1], dfs_time;
8 vector<vii>> grafo(N+1, vii());
                                                            30 int tour[2*MAX+1], id[2*MAX+1];
9 vi distancia(N+1, INF);
                                                            31
10 priority_queue < pii, vii, greater <pii> > fila;
                                                            32 void dfs(int u, int pai=-1){
                                                                   start[u] = dfs_time;
                                                            33
12 void dijkstra(int k)
                                                                   id[dfs_time] = u;
                                                            34
                                                                   tour[dfs_time++] = start[u];
13 €
                                                            35
14
       int dist, vert, aux;
                                                            36
                                                                   for(int v : grafo[u]){
15
       distancia[k]=0;
                                                            37
                                                                       if(v==pai)
                                                                           continue;
16
                                                            38
      fila.push(mp(k, 0));
17
                                                            39
                                                                       dfs(v, u);
                                                                       id[dfs_time] = u;
18
                                                            40
19
       while(!fila.empty())
                                                            41
                                                                       tour[dfs_time++] = start[u];
20
                                                            42
           aux=fila.top().f;
                                                            43 }
22
           fila.pop();
                                                            44
                                                            45 int LCA(int u, int v)
23
           for(auto v: grafo[aux])
                                                            46 {
                                                            47
                                                                   if(start[u] > start[v])
25
               vert=v.f;
                                                                       swap(u, v);
               dist=v.s:
                                                                   return id[query(start[u], start[v])];
27
                                                            49
               if(distancia[vert]>distancia[aux]+dist)
                                                            50 }
28
29
                    distancia[vert] = distancia[aux] + dist; 52 int main()
30
                    fila.push(mp(vert, distancia[vert])); 53 {
                                                                   int N, k, a, b;
                                                            54
                                                                   cin >> N;
                                                            55
32
           }
33
                                                            56
       }
                                                            57
                                                                   for(int i=0;i<N-1;i++)</pre>
34
35 }
                                                            58
                                                                       cin >> a >> b:
36
                                                            59
37 int main()
                                                                       grafo[a].pb(b);
                                                            60
                                                                       grafo[b].pb(a);
38 €
                                                            61
39
       for(int i=0; i<M; i++)</pre>
                                                            62
                                                            63
                                                                   dfs(1);
40
           cin >> a >> b >> p;
                                                            64
41
42
           grafo[a].pb(mp(b, p));
                                                            65
                                                                   make();
           grafo[b].pb(mp(a, p));
                                                                   precompute(2*N, tour);
43
                                                            66
                                                            67
45 }
                                                            68
                                                                   cin >> k;
                                                            69
  2.4 LCA
                                                            70
                                                                   for(int i=0;i<k;i++)</pre>
                                                            71
                                                            72
                                                                       cin >> a >> b;
1 const int K = 100;
                                                                       cout << LCA(a, b) << endl;</pre>
2 int logv[MAX+1];
                                                            73
                                                            74
3 int st[MAX][K];
                                                            75
4 vector < vi > grafo(200010, vi());
                                                                   return 0;
                                                            76
6 void make(){
      logv[1] = 0; // pre-computar tabela de log
                                                                     Floyd-Warshall
      for (int i = 2; i <= MAX; i++)</pre>
9
           logv[i] = logv[i/2] + 1;
                                                            1 // Floyd Warshall
10 }
11
void precompute(int N, int array[]) { //
                                                             3 int dist[MAX][MAX];
13
   for (int i = 0; i < N; i++)
        st[i][0] = array[i];
                                                             5 void Floydwarshall()
14
15
                                                                   for(int k = 1; k \le n; k++)
    int k = logv[N];
16
                                                                       for(int i = 1;i <= n;i++)
    for (int j = 1; j <= k; j++)
                                                                            for(int j = 1; j <= n; j++)</pre>
         for (int i = 0; i + (1 << j) <= N; i++)
                                                             9
18
             st[i][j] = min(st[i][j-1], st[i + (1 << (j 10))]
                                                                                dist[i][j] = min(dist[i][j], dist[i][
19
                                                                   k] + dist[k][j]);
       - 1))][j - 1]);
20 }
21
                                                               2.6 Kruskal
22 int query(int L, int R) {
       int j = logv[R - L + 1];
       int \ minimum = min(st[L][j], \ st[R - (1 << j) + 1][\ _1 \ // \ deve-se \ ter \ dsu \ codada \ com \ as \ funcoes \ make\_set,
24
                                                                   find_set e union_sets
      i]);
```

```
2 struct Edge {
      int u, v, weight;
                                                           5
                                                                 vector< pair<int, int> > arestas;
3
      bool operator < (Edge const& other) {</pre>
                                                                 arestas.push_back(make_pair(1, 2));
                                                           6
          return weight < other.weight;</pre>
                                                                 arestas.push_back(make_pair(1, 3));
7 }:
                                                           9 // Adjacency Matrix
                                                          10
                                                                 int grafo[10][10];
9 int n:
                                                          11
10 vector < Edge > edges;
                                                          12
                                                                 grafo[1][2] = grafo[2][1] = 1;
                                                          13
12 int cost = 0;
                                                                 grafo[1][3] = grafo[3][1] = 2;
                                                          14
13 vector < Edge > result;
                                                          15
14 for (int i = 0; i < n; i++)
                                                          16 // Adjacency List
      make_set(i);
                                                          17
16
                                                          18
                                                                 vector < int > vizinhos[10];
17 sort(edges.begin(), edges.end());
                                                          19
                                                                 vizinhos[1].push_back(2);
                                                                 vizinhos[1].push_back(2);
19 for (Edge e : edges) {
      if (find_set(e.u) != find_set(e.v)) {
          cost += e.weight;
                                                             2.10 Centroid
21
          result.push_back(e); // vector com as arestas
22
       da MST
                                                           vi g[MAX];
          union_sets(e.u, e.v);
23
                                                           2 int size[MAX];
                                                           3 bool erased[MAX]; // vetor dos vertices apagados na
25 }
                                                                 decomp.
  2.7 DFS
                                                           5 int sz(int u, int p) {
                                                              int s = 1;
1 //DFS (Depth First Search) O(V+A)
                                                               for(auto prox : g[u]) {
                                                                 if(prox != p and !erased[prox])
3 void DFS(int x)
                                                                   s += sz(prox, u);
                                                           9
                                                               }
      for(int i=0; i<(int)vizinhos[x].size(); i++)</pre>
                                                               return size[u] = s;
                                                          11
6
                                                          12 }
           int v = vizinhos[x][i];
                                                          13
          if (componente[v] == -1)
                                                          14 int centroid(int u, int p, int n) {
                                                              // chamar funcao sz antes, n = size[u]
                                                          15
10
               componente[v] = componente[x];
                                                               for(auto prox : g[u]) {
                                                          16
11
               DFS(v):
                                                          17
                                                                 if(prox != p and !erased[prox]) {
12
          }
                                                                   if(size[prox] > n/2) {
                                                          18
      }
13
                                                                     return centroid(prox, u, n);
14 }
                                                          20
                                                                 }
                                                          21
  2.8 Kosaraju
                                                               }
                                                          22
                                                          23
                                                               return u;
_{1} // KOSARAJU - O(V+E) - encontra componentes
      fortemente conexos
                                                             2.11 Prim
_2 // g -> grafo, gt -> grafo tempo
3 // vis -> visitado, cor -> componente fortemente
      conexo ordenado topologicamente
                                                           1 // Prim Algorithm
4 vector<int> g[N], gt[N], S; int vis[N], cor[N];
                                                           2 #define MAXN 10100
5 void dfs(int u){
                                                           3 #define INFINITO 999999999
      vis[u] = 1; for(int v : g[u]) if(!vis[v]) dfs(v);
      S.push_back(u);
                                                           5 int n, m;
8 }
                                                           6 int distancia[MAXN];
9 void dfst(int u, int e){
                                                           7 int processado[MAXN];
      cor[u] = e;
                                                           8 vector < pii > vizinhos [MAXN];
      for(int v : gt[u]) if(!cor[v]) dfst(v, e);
11
12 }
                                                           10 int Prim()
13 void kosaraju(){
                                                          11 {
      for(int i = 1; i <= n; i++) if(!vis[i]) dfs(i);</pre>
14
                                                                 for(int i = 2;i <= n;i++) distancia[i] = INFINITO</pre>
      for(int i = 1; i <= n; i++) for(int j : g[i])</pre>
          gt[j].push_back(i);
16
                                                                 distancia[1] = 0;
      int e = 0; reverse(S.begin(), S.end());
17
                                                          14
18
      for(int u : S) if(!cor[u]) dfst(u, ++e);
                                                                 priority_queue < pii, vector < pii >, greater < pii > >
19 }
                                                                 fila.push( pii(distancia[1], 1) );
                                                          16
  2.9 Represent
                                                          17
                                                                 while(1)
                                                          18
1 // Grafos
                                                                      int davez = -1;
                                                          20
3 // List of edges
                                                          21
```

```
while(!fila.empty())
22
23
                int atual = fila.top().second;
24
               fila.pop();
               if(!processado[atual])
27
                    davez = atual:
29
                    break;
30
               }
           }
32
           if(davez == -1)
34
               break;
35
36
           processado[davez] = true;
37
           for(int i = 0;i < (int)vizinhos[davez].size() 21</pre>
39
       ;i++)
           {
40
41
                int dist = vizinhos[davez][i].first;
               int atual = vizinhos[davez][i].second;
43
               if( distancia[atual] > dist && !
45
      processado[atual])
46
               {
                    distancia[atual] = dist;
47
                    fila.push( pii(distancia[atual],
       atual));
49
           }
51
       int custo_arvore = 0;
53
       for(int i = 1;i <= n;i++)
           custo_arvore += distancia[i];
55
56
       return custo_arvore;
58 }
60 int main(){
61
62
       cin >> n >> m:
63
       for(int i = 1;i <= m;i++){
64
65
           int x, y, tempo;
           cin >> x >> y >> tempo;
67
68
           vizinhos[x].pb( pii(tempo, y) );
           vizinhos[y].pb( pii(tempo, x) );
70
72
       cout << Prim() << endl;</pre>
74
       return 0;
75
76 }
```

3 Geometria

3.1 Angle-adjacent-vertices-regular-polygon

a = 180/N

3.2 Inter-Retas

```
1 // Intersection between lines
2
3 typedef struct
4 {
```

```
int x. v:
6 } pnt;
8 bool collinear(pnt p, pnt q, pnt r)
9 {
       if(q.x<=max(p.x,r.x) && q.x>=min(p.x,r.x) && q.y
10
       <=max(p.y,r.y) && q.y>=min(p.y,r.y))
           return true;
12
13
       return false;
14 }
16 int orientation(pnt p, pnt q, pnt r)
17 {
       int val=(q.y-p.y)*(r.x-q.x)-(q.x-p.x)*(r.y-q.y);
18
19
       if(val==0)
          return 0;
       else if(val>0)
          return 1;
       else
24
25
           return 2;
26 }
28 bool intersect(pnt p1, pnt q1, pnt p2, pnt q2)
29 {
      int o1 = orientation(p1, q1, p2);
30
      int o2 = orientation(p1, q1, q2);
31
      int o3 = orientation(p2, q2, p1);
      int o4 = orientation(p2, q2, q1);
33
34
      if (o1!=o2 and o3!=o4)
35
           return true;
36
37
      if(o1==0 && collinear(p1, p2, q1))
38
           return true;
39
40
       if(o2==0 && collinear(p1, q2, q1))
41
42
           return true;
43
44
      if(o3==0 && collinear(p2, p1, q2))
           return true;
45
46
47
       if(o4==0 && collinear(p2, q1, q2))
           return true;
48
49
       return false;
50
52 }
```

3.3 Pick's-theorem

The area of a polygon with integer coordinates: $A = i + \frac{b}{2} - 1$ i is the number of points inside the polygon; b is the number of points on the boundry; 2A is necessarily an integer value.

3.4 Rotation

```
1 // Rotate clockwise 90 degree
2 (x, y) => (y, -x)
3
4 // Rotate counterclockwise 90 degree
5 (x, y) => (-y, x)
```

3.5 Inter-Retangulos

```
1 typedef struct
2 {
3 int x, y;
```

```
4 } Point:
                                                               // No caso de pontos tridimensionais, usar
                                                               produto vetorial.
6 bool doOverlap(Point 11, Point r1, Point 12, Point r2 59 }
                                                         61 // Dist entre ponto e reta
      if (11.x>r2.x or 12.x>r1.x or 11.y<r2.y or 12.y< 62 double distr(point a, line b){
                                                               double crs = cross(point(a - b.fp), point(b.sp -
      r1.y)
         return false:
                                                               b.fp));
      return true;
                                                               return abs(crs/dist(b.fp, b.sp));
10
                                                         64
11 }
                                                         65 }
                                                         66
                                                         67 void esq(point a, point b, point ext)
  3.6 Analytic-Geometry
                                                        68 { // Esquerda = 1; Direita = -1; Collinear = 0;
                                                              11 v = a.x*b.y+b.x*ext.y+ext.x*a.y - (a.y*b.x+b.y
1 struct point
                                                               *ext.x+ext.y*a.x);
                                                               if(v>0) return 1;
                                                         70
                                                               if(v==0) return 0;
      double x, y;
                                                         71
                                                               return -1;
      point(double _x=0, double _y=0) {
                                                         72
                                                        73 }
          x = _x; y = _y;
                                                        74
                                                        75 // Area de um poligono (pontos ordenados por
      void show(){
                                                               adjacencia)
                                                        76 double area(vector <point> p){
          cout << "x = " << x << endl;
          cout << "y = " << y << endl;
                                                        77 double ret = 0;
10
                                                            for(int i=2;i<(int)p.size();i++)</pre>
                                                        78
                                                         79
                                                              ret += cross(p[i] - p[0], p[i-1] - p[0])/2;
12
      point operator+(const point &o) const{
                                                        80
                                                             return abs(ret);
13
                                                        81 }
          return {x + o.x, y + o.y};
                                                        82 // Concavo ou Convexo
15
                                                        83 double ccw(point a, point b, point c){
     point operator-(const point &o) const{
                                                         84 double ret = cross(b - a, c - b);
17
         return {x - o.x, y - o.y};
                                                             return ret < 0;</pre>
                                                         85
18
                                                        86 }
      bool operator == (const point &o) const{
19
         return (x == o.x and y == o.y);
20
                                                                ED
22
23 }:
                                                           4.1
                                                                Range-query-bigger-than-k-BIT
24
25 struct line
                                                         1 // C++ program to print the number of elements
                                                         _{2} // greater than k in a subarray of range L-R.
27
      point fp, sp;
      line(point _fp=0, point _sp=0){
                                                         3 #include <bits/stdc++.h>
        fp=_fp;sp=_sp;
29
                                                         4 using namespace std;
30
                                                         6 // Structure which will store both
31
      //a = y1 - y2;
                                                         7 // array elements and queries.
32
33
      //b=x2-x1;
                                                         8 struct node {
      //c=x2*y1-y2*x1;
                                                              int pos;
34
                                                         Q
35
                                                         10
                                                              int 1:
36 };
                                                         1.1
                                                              int r;
                                                         12
                                                               int val;
38 // Produto Escalar
                                                         13 };
39 double dot(point a, point b){
                                                         14
      return a.x*b.x + a.y*b.y;
                                                        _{15} // Boolean comparator that will be used
41 }
                                                         _{16} // for sorting the structural array.
                                                         17 bool comp(node a, node b)
43 // Produto Vetorial
                                                         18 {
                                                               // If 2 values are equal the query will
44 double cross(point a, point b){
                                                        19
      return a.x*b.y - a.y*b.x;
                                                              // occur first then array element
                                                       20
                                                               if (a.val == b.val)
46 }
                                                        21
                                                                   return a.l > b.l;
                                                         22
48 // Dist entre dois pontos
                                                        23
49 double dist(point a, point b){
                                                               // Otherwise sorted in descending order.
                                                        24
     point c = a - b;
                                                       25
                                                               return a.val > b.val;
      return sqrt(c.x*c.x + c.y*c.y);
                                                        26 }
51
52 }
                                                        28 // Updates the node of BIT array by adding
                                                        _{29} // 1 to it and its ancestors.
54 // Colinearidade entre 3 pontos
55 bool collinear(point a, point b, point c){
                                                        30 void update(int* BIT, int n, int idx)
     return ((c.y-b.y)*(b.x-a.x)==(b.y-a.y)*(c.x-b.x))_{31} {
                                                               while (idx <= n) {
      // return (a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b33
                                                                BIT[idx]++;
```

34

idx += idx & (-idx);

.y)); // Triangle area

```
update(BIT, n, a[i].r);
35
                                                           103
36 }
                                                           104
37 // Returns the count of numbers of elements
                                                                  }
                                                           105
                                                                  // Output the answer array
38 // present from starting till idx.
                                                           106
                                                                  for (int i = 1; i <= q; ++i) {
39 int query(int* BIT, int idx)
                                                           107
40 {
                                                           108
                                                                      cout << ans[i] << endl;</pre>
       int ans = 0;
41
                                                           109
       while (idx) {
                                                           110
42
           ans += BIT[idx];
                                                          111
43
                                                          112 // Driver Code
           idx -= idx & (-idx);
                                                           113 int main()
45
46
       }
                                                           114 {
                                                                  int arr[] = { 7, 3, 9, 13, 5, 4 };
47
       return ans;
                                                           115
48 }
                                                                  int n = sizeof(arr) / sizeof(arr[0]);
                                                           116
49
                                                           117
50 // Function to solve the queries offline
                                                                  // 1-based indexing
                                                           118
51 void solveQuery(int arr[], int n, int QueryL[],
                                                                  int QueryL[] = { 1, 2 };
                                                           119
                   int QueryR[], int QueryK[], int q)
                                                                  int QueryR[] = { 4, 6 };
52
                                                           120
53 {
       // create node to store the elements
                                                                  // k for each query
54
                                                           122
                                                                  int QueryK[] = { 6, 8 };
55
       // and the queries
                                                           123
       node a[n + q + 1];
                                                           124
56
       // 1-based indexing.
57
                                                           125
                                                                  // number of queries
                                                                  int q = sizeof(QueryL) / sizeof(QueryL[0]);
                                                           126
       // traverse for all array numbers
                                                           127
59
60
       for (int i = 1; i <= n; ++i) {
                                                           128
                                                                  // Function call to get
           a[i].val = arr[i - 1];
                                                                  solveQuery(arr, n, QueryL, QueryR, QueryK, q);
61
                                                           129
           a[i].pos = 0;
                                                           130
62
           a[i].1 = 0;
                                                           131
                                                                  return 0:
63
           a[i].r = i;
                                                           132
64
65
                                                                   Iterative-SegTree
66
       // iterate for all queries
67
       for (int i = n + 1; i <= n + q; ++i) {
                                                           1 // Segment Tree Iterativa - Range maximum query
           a[i].pos = i - n;
69
           a[i].val = QueryK[i - n - 1];
70
                                                           3 #define N 100010
           a[i].1 = QueryL[i - n - 1];
71
           a[i].r = QueryR[i - n - 1];
72
                                                            5 struct Segtree
       7
73
                                                            6 {
74
                                                                  int t[2*N] = \{0\};
       // In-built sort function used to
75
       // sort node array using comp function.
76
                                                                  void build()
                                                            9
       sort(a + 1, a + n + q + 1, comp);
                                                           10
78
                                                                      for(int i=N-1; i>0; i--)
                                                           11
       // Binary Indexed tree with
79
                                                           12
                                                                           t[i]=max(t[i<<1], t[1<<1|1]);
80
       // initially 0 at all places.
                                                           13
       int BIT[n + 1];
81
                                                           14
                                                                  int query(int 1, int r)
                                                           1.5
       // initially 0
83
                                                           16
       memset(BIT, 0, sizeof(BIT));
                                                                      int ans=0:
                                                           17
                                                                      for (i+=N, r+=N; 1< r; 1>>=1, r>>=1)
85
                                                           18
       // For storing answers for each query( 1-based
86
       indexing ).
                                                                           if(1&1)
                                                           20
       int ans[q + 1];
87
                                                                               ans=max(ans, t[1++]);
                                                           21
88
                                                                           if (r&1)
                                                           22
       // traverse for numbers and query
89
                                                                               ans=max(ans, t[--r]);
       for (int i = 1; i <= n + q; ++i) {
90
                                                           24
                                                                      }
           if (a[i].pos != 0) {
91
                                                           25
92
                                                                      return ans;
               // call function to returns answer for
93
                                                                  }
                                                           27
       each query
               int cnt = query(BIT, a[i].r) - query(BIT, 29
94
                                                                  void update(int p, int value)
        a[i].1 - 1);
                                                           30
95
                                                                      for(t[p+=n]=value; p>1; p>>=1)
               // This will ensure that answer of each
                                                                          t[p>>1] = max(t[p], t[p^1]);
       auerv
               // are stored in order it was initially
                                                           34
       asked.
                                                           35 }:
               ans[a[i].pos] = cnt;
98
           }
                                                           37 int main()
           else {
100
               // a[i].r contains the position of the
                                                                  Segtree st;
                                                           39
               // element in the original array.
                                                           40
```

```
for(int i=0;i<n;i++)</pre>
41
                                                           57
42
                                                           58
                                                                  int resp_esq = consulta(esq, i, meio, A, B);
                                                                  int resp_dir = consulta(dir, meio+1, j, A, B);
           cin >> aux;
43
                                                           59
          st.t[N+i] = aux; //Leaves are stored in
                                                           60
44
       continuous nodes with indices starting with N
                                                                  if (resp_dir==-1)
                                                                      return resp_esq;
45
                                                           62
                                                                  if (resp_esq == -1)
                                                           63
      st.build();
                                                                      return resp_dir;
47
                                                           64
      x = st.query(inicio, fim);
48
                                                           65
      st.update(ind, value);
                                                           66
                                                                  if(resp_esq>resp_dir)
49
                                                           67
                                                                     return resp_esq;
50
51 }
                                                           68
                                                                  else
                                                           69
                                                                      return resp_dir;
  4.3 Recursive-SegTree
                                                           70 }
                                                           71
                                                           72 int main()
1 // Segment Tree Recursiva - Range maximum query
                                                           73 {
                                                                  monta(1, N, 1);
3 vector<int> val(MAX, 0);
                                                           74
4 vector < int > vet(N);
                                                                  atualiza(1, 1, N, pos, valor);
                                                                  x = consulta(1, 1, N, inicio, fim);
                                                           76
6 void monta(int i, int j, int no)
                                                           77
                                                           78 }
      if(i==j)
                                                                   Delta-Encoding
9
           val[no]=vet[i];
10
          return;
                                                            1 // Delta encoding
12
                                                           3 for(int i=0;i<q;i++)</pre>
      int esq = 2*no;
14
      int dir = 2*no+1;
                                                                  int l,r,x;
                                                           5
16
      int meio = (i+j)/2;
                                                                  cin >> 1 >> r >> x;
                                                            6
17
                                                                  delta[1] += x;
      monta(i, meio, esq);
                                                                  delta[r+1] = x;
      monta(meio+1, j, dir);
19
                                                           9 }
                                                           10
      val[no]=max(val[esq], val[dir]);
21
                                                           11 int atual = 0;
                                                           12
23
                                                           13 for (int i=0; i < n; i++)
24 void atualiza(int no, int i, int j, int pos, int
                                                           14 {
      novo_valor)
                                                                  atual += delta[i]:
                                                           1.5
25 {
                                                           16
                                                                  v[i] += atual;
      if(i==j)
                                                           17 }
27
           val[no]=novo_valor;
28
                                                              4.5 Seg-Tree-Farao
29
      }else
30
31
           int esq = 2*no;
                                                            1 typedef struct
          int dir = 2*no+1;
32
                                                            2 {
33
          int meio = (i+j)/2;
                                                                  pii prefix, sufix, total, maximo;
                                                            4 } no;
34
           if (pos <= meio)</pre>
35
               atualiza(esq, i, meio, pos, novo_valor); 6 int noleft[MAX], noright[MAX]; //Guarda os valores
                                                                dos nos para que nao sejam calculados novamente
37
               atualiza(dir, meio+1, j, pos, novo_valor)
                                                                 nas querys
38
                                                            7 int v[MAX]:
                                                            8 no arvore[MAX];
39
           if(val[esq]>val[dir])
40
              val[no]=val[esq];
                                                           10 pii somar(pii a, pii b) // une pairs
41
           else
43
               val[no]=val[dir];
                                                           12
                                                                  return mp(a.f+b.f, a.s+b.s);
      }
                                                           13 }
44
45 }
                                                           14
                                                           15 no une(no 1, no r)
47 int consulta(int no, int i, int j, int A, int B)
                                                           16 {
                                                                  if(1.total.s==0)
48 {
                                                           17
      if(i>B || j<A)</pre>
49
                                                           18
                                                                      return r:
50
          return -1;
                                                           19
                                                                  if(r.total.s==0)
       if(i>=A and j<=B)
51
                                                           20
                                                                      return 1;
          return val[no];
                                                           21
53
                                                           22
                                                                  no m:
      int esq = 2*no;
                                                           23
      int dir = 2*no+1;
                                                                  m.prefix = max(l.prefix, somar(l.total, r.prefix)
55
                                                           24
      int meio = (i+j)/2;
                                                                  ); //prefixo
```

```
scanf("%d%d", &A, &B); //Intervalo da
      m.sufix = max(r.sufix, somar(r.total, l.sufix)); 93
25
      //sufixo
                                                                  query
      m.total = somar(1.total, r.total); //Soma de
                                                                           aux = busca(1, A, B);
26
                                                                          printf("%d %d\n", aux.maximo.f, aux.
      todos os elementos da subarvore
                                                           95
      m.maximo = max(max(1.maximo, r.maximo), somar(1.
                                                                  maximo.s);
      sufix, r.prefix)); //Resultado para cada
                                                                      }
                                                           96
       subarvore
                                                           97
28
                                                           98
      return m;
29
                                                           99
30 }
                                                           100
                                                                  return 0;
                                                          101 }
31
32 no makenozero()
                                                                   BIT-2D
                                                              4.6
33 {
34
35
      m.prefix=m.sufix=m.total=m.maximo=mp(0,0);
                                                            1 // BIT 2D
      return m;
36
37 }
                                                            3 int bit[MAX][MAX];
38
39 no makeno(int k)
                                                            5 int sum(int x, int y)
40 {
                                                            6 {
41
      no m;
                                                                  int resp=0;
      m.prefix=m.sufix=m.total=m.maximo=mp(k,1);
42
      return m:
43
                                                                  for(int i=x;i>0;i-=i&-i)
                                                            9
44 }
                                                           10
                                                                      for(int j=y;j>0;j-=j&-j)
45
                                                                          resp+=bit[i][j];
                                                           11
46 void monta(int n)
                                                           12
47 {
                                                           13
                                                                  return resp;
      if(noleft[n] == noright[n])
48
                                                           14 }
49
                                                           15
           arvore[n]=makeno(v[noleft[n]]);
50
                                                           void update(int x, int y, int delta)
           return;
51
                                                           17 {
      }
52
                                                                  for(int i=x;i<MAX;i+=i&-i)</pre>
                                                           18
                                                                      for (int j=y; j < MAX; j+=j\&-j)
                                                           19
      int mid = (noleft[n]+noright[n])/2;
                                                                          bit[i][j]+=delta;
                                                           20
      noleft[2*n]=noleft[n]; noright[2*n]=mid;
55
                                                           21 }
      noleft[2*n+1]=mid+1; noright[2*n+1]=noright[n];
57
                                                           23 int query(int x1, y1, x2, y2)
58
      monta(2*n);
                                                           24 {
      monta(2*n+1);
59
                                                                  60
                                                                  (x1,y1);
61
       arvore[n]=une(arvore[2*n], arvore[2*n+1]);
                                                           26 }
62 }
63
                                                              4.7 BIT
64 no busca(int n, int esq, int dir)
65 {
66
       if(noleft[n]>=esq and noright[n]<=dir)</pre>
                                                            1 struct FT {
                                                                  vector < int > bit; // indexado em 1
           return arvore[n];
67
       if(noright[n] < esq or noleft[n] > dir)
                                                                  int n;
69
          return makenozero();
                                                                  FT(int n) {
70
       return une(busca(2*n, esq, dir),busca(2*n+1, esq,
71
                                                                      this -> n = n + 1;
                                                                      bit.assign(n + 1, 0);
       dir));
72 }
73
74 int main()
                                                                  int sum(int idx) {
                                                           10
75 {
                                                                      int ret = 0;
      int T, N, Q, A, B;
                                                                      for (++idx; idx > 0; idx -= idx & -idx)
76
                                                           12
      no aux;
                                                                          ret += bit[idx];
77
                                                           13
78
                                                           14
                                                                      return ret;
      scanf("%d", &T);
79
                                                           15
80
                                                           16
      while (T--)
                                                                  int sum(int 1, int r) {
81
                                                           17
                                                                      return sum(r) - sum(l - 1);
82
           scanf("%d", &N);
83
                                                           19
84
           for (int i=1; i <= N; i++)</pre>
               scanf("%d", &v[i]); //Elementos da arvore _{21}
                                                                  void add(int idx, int delta) {
85
                                                                      for (++idx; idx <= n; idx += idx & -idx)</pre>
86
                                                           22
           noleft[1]=1; noright[1]=N;
                                                                          bit[idx] += delta;
87
                                                           23
           monta(1);
88
                                                           24
                                                           25 };
           cin >> Q;
90
           while(Q--)
                                                                    Sparse-Table
91
92
           {
```

```
1 logv[1] = 0; // pre-computar tabela de log
                                                                   {
                                                            6
2 for (int i = 2; i <= MAXN; i++)</pre>
                                                                       return make_pair(1 / BLK, r) <</pre>
      logv[i] = logv[i/2] + 1;
                                                                       make_pair(other.1 / BLK, other.r);
                                                            8
                                                            9
5 int logv[MAXN+1];
                                                            10 };
6 int st[MAXN][K];
                                                            11
                                                            12 void add(); void remove() // implementar operacoes de
8 // operacao da sparse table deve ser idempotente ->
                                                                   acordo com o problema, cuidado com TLE ao
      op(x, x) = x
                                                                   utilizar MAP
9 void precompute(int N) { //
    for (int i = 0; i < N; i++)
                                                            14 vector < pair < int , ll >> mo() {
10
         st[i][0] = array[i];
                                                                   vector<pair<int,ll>> res;
12
                                                            16
                                                                   sort(queries.begin(), queries.end());
    int k = logv[N];
13
                                                            17
    for (int j = 1; j \le k; j++)
14
                                                                   int 1 = 0, r = -1;
        for (int i = 0; i + (1 << j) <= N; i++)
                                                                   for(Query q : queries) {
15
                                                            19
             st[i][j] = max(st[i][j-1], st[i + (1 << (j 20))]
                                                                       while(1 > q.1) {
                                                                               1--;
       - 1))][j - 1]);
                                                            21
                                                                                add(1);
18
                                                                       while(r < q.r) {
19 int query(int L, int R) {
                                                            24
      int j = logv[R - L + 1];
                                                                                r++:
      int maximum = \max(st[L][j], st[R - (1 << j) + 1][26]
                                                                                add(r):
21
                                                                       }
                                                                       while(1 < q.1) {
22
      return maximum;
                                                                                remove(1);
23
                                                            29
24 }
                                                            30
                                                                                1++;
                                                            31
  4.9
        Union-Find
                                                                       while(r > q.r) {
                                                            32
                                                            33
                                                                               remove(r);
                                                                                r--;
                                                            34
1 // Union-Find Functions
                                                            35
                                                                       res.pb(mp(q.idx, RESPOSTA)); // adicionar
                                                            36
3 int pai[MAX], peso[MAX];
                                                                   resposta de acordo com o problema
                                                            37
5 int find(int aux)
                                                                    return res; // ordernar o vetor pelo indice e
                                                            38
6 {
                                                                   responder queries na ordem
       if(pai[aux] == aux)
          return aux;
9
                                                                   Math
                                                              5
          return pai[aux]=find(pai[aux], pai);
10
11 }
12
                                                              5.1
                                                                     Totient
13 void join(int x, int y)
14 {
                                                            _{1} // phi(p^k) = (p^(k-1))*(p-1) com p primo
      x = find(x);
15
                                                            2 // O(sqrt(m))
      y = find(y);
16
                                                            3 ll phi(ll m) {
17
                                                                   11 \text{ res} = m;
      if(pesos[x]<pesos[y])</pre>
                                                            5
                                                                   for(11 d = 2; d*d <= m; d++) {
          pai[x] = y;
19
                                                                     if(m \% d == 0) {
                                                             6
       else if(pesos[x]>pesos[y])
20
                                                             7
                                                                         res = (res/d) * (d-1);
          pai[y] = x;
21
                                                                         while (m \% d == 0) {
       else if(pesos[x]==pesos[y])
22
                                                                          m /= d;
                                                            9
23
                                                            10
           pai[x] = y;
24
                                                                     }
                                                            11
25
           pesos[y]++;
                                                            12
26
                                                            13
                                                                   if(m > 1) {
27 }
                                                                    res /= m;
                                                            14
                                                                     res *= (m-1);
29 int main()
                                                            16
30 {
                                                            17
31
       for(int i=1;i<=N;i++)</pre>
                                                            18
                                                                   return res;
           pai[i]=i;
32
                                                            19 }
33 }
                                                            _{21} // modificacao do crivo, O(n*log(log(n)))
  4.10 Mo
                                                            22 vector<ll> phi_to_n(ll n) {
                                                                   vector < bool > isprime(n+1, true);
1 const int BLK = 500; // tamanho do bloco, algo entre 24
                                                                   vector<ll> tot(n+1);
      300 e 500 e nice
                                                                   tot[0] = 0; tot[1] = 1;
                                                                   for(ll i = 1; i <= n; i++) {</pre>
                                                            26
3 struct Query {
                                                                     tot[i] = i;
                                                            27
      int 1, r, idx;
                                                            28
      bool operator < (Query other) const</pre>
                                                            29
```

```
30 for(11 p = 2; p <= n; p++) {
31
    if(isprime[p]) {
        tot[p] = p-1;
32
        for(11 i = p+p; i <= n; i += p) {
33
             isprime[i] = false;
             tot[i] = (tot[i]/p)*(p-1);
35
37
38 }
39
      return tot;
40
41 }
```

5.2 Linear-Diophantine-Equation

```
1 // Linear Diophantine Equation
2 int gcd(int a, int b, int &x, int &y)
3 {
       if (a == 0)
5
       {
           x = 0; y = 1;
6
           return b;
      }
      int x1, y1;
      int d = gcd(b%a, a, x1, y1);
10
11
      x = y1 - (b / a) * x1;
      y = x1;
12
      return d;
13
14 }
15
16 bool find_any_solution(int a, int b, int c, int &x0,
       int &y0, int &g)
       g = gcd(abs(a), abs(b), x0, y0);
18
      if (c % g)
19
          return false;
21
      x0 *= c / g;
22
      y0 *= c / g;
      if (a < 0) x0 = -x0;
24
25
      if (b < 0) y0 = -y0;
      return true;
26
27 }
29 // All solutions
_{30} // _{x} = _{x0} + _{k*b/g}
_{31} // y = y0 - k*a/g
```

5.3 Sum-n2

Soma dos
n primeiros números ao quadrado = $\frac{(2N^3+3N^2+N)}{6}$

5.4 Factorization-sqrt

```
1 // Factorization of a number in sqrt(n)
3 int main()
4 {
       11 N:
5
       vector < int > div;
       cin >> N;
9
       for(11 i=2;i*i<=N;i++)</pre>
10
11
           if(N%i==0)
12
                vet.pb(i);
14
                while (N%i==0)
                    N/=i;
16
           }
```

```
18 }
19 if(N!=1)
20 vet.pb(N);
21
22 return 0;
23 }
```

5.5 Modular-Exponentiation

```
1 // Modular exponentiaion - (x^y)%mod in O(log y)
2 ll power(ll x, ll y, ll mod)
3 {
       ll res = 1;
      x\%=mod;
       while(v)
           if(y&1)
9
              res=(res*x)%mod;
10
11
           y = y >> 1;
12
13
           x=(x*x)%mod;
14
15
       return res;
16 }
```

5.6 Miller-Habin

```
1 ll llrand()
       11 tmp = rand();
       return (tmp << 31) | rand();</pre>
5 }
7 ll add(ll a, ll b, ll c)
8 {
       return (a + b)%c;
9
10 }
11
12 ll mul(ll a, ll b, ll c)
13 €
       ll ans = 0;
14
       while(b)
15
16
           if(b & 1)
17
               ans = add(ans, a, c);
           a = add(a, a, c);
20
           b /= 2;
       }
22
       return ans;
23 }
24
25 ll fexp(ll a, ll b, ll c)
26 {
       ll ans = 1;
27
28
       while(b)
       {
29
           if(b & 1)
31
               ans = mul(ans, a, c);
           a = mul(a, a, c);
32
           b /= 2;
33
34
35
       return ans;
36 }
37
38 bool rabin(ll n)
39 {
       if(n <= 1)
40
          return 1;
41
       if(n \le 3)
          return 1;
43
44
```

```
11 s=0, d=n-1;
45
                                                            13
46
       while (d\%2==0)
                                                            14 ll add(ll a, ll b, ll c)
                                                            15 {
47
           d/=2;
                                                                    return (a + b)%c;
                                                            16
48
           s++;
                                                            17 }
50
                                                            18
                                                            19 ll mul(ll a, ll b, ll c)
      for(int k = 0; k < 64*4; k++)
                                                            20 {
52
                                                                    11 \text{ ans} = 0;
53
                                                            21
           11 a = (11rand()\%(n - 3)) + 2;
                                                            22
                                                                    while(b)
           11 x = fexp(a, d, n);
                                                                    {
55
                                                            23
56
           if(x != 1 and x != n-1)
                                                            24
                                                                        if(b & 1)
                                                                         ans = add(ans, a, c);
57
                                                            25
               for(int r = 1; r < s; r++)</pre>
                                                                        a = add(a, a, c);
                                                            26
58
                                                                        b /= 2;
59
                                                            27
                    x = mul(x, x, n);
                                                            28
60
                    if(x == 1)
                                                            29
                                                                    return ans;
                                                            30 }
                        return 0;
62
                    if(x == n-1)
                                                            31
                                                            32 ll rho(ll n)
                        break;
64
                                                            33 {
65
               if(x != n-1)
66
                                                            34
                                                                    ll x, c, y, d, k;
                                                                    int i;
                   return 0;
                                                            35
67
           }
                                                                    do{
      }
                                                                        i = 1;
69
                                                            37
                                                            38
                                                                        x = llrand()%n;
70
                                                                        c = llrand()%n;
71
      return 1;
                                                            39
72 }
                                                                        y = x, k = 4;
                                                            40
73
                                                            41
                                                                        do{
                                                                            if(++i == k)
74
                                                            42
75 int main()
                                                             43
                                                                            {
                                                                                 y = x;
76 {
                                                            44
                                                                                 k *= 2;
                                                            45
      11 N;
                                                                            }
      cin >> N;
                                                                            x = add(mul(x, x, n), c, n);
                                                            47
79
                                                                            d = \_gcd(abs(x - y), n);
                                                             48
      cout << rabin(N) << endl;</pre>
81
                                                            49
                                                                        while(d == 1);
82
                                                            50
83
      return 0;
                                                            51
                                                                    while(d == n);
84
                                                            52
85 }
                                                            53
                                                                    return d;
                                                            54
  5.7 Inverso-Mult
                                                            55 }
                                                            56
                                                            57 int main()
1 // gcd(a, m) = 1 para existir solucao
                                                            58 {
_{2} // ax + my = 1, ou a*x = 1 (mod m)
                                                                    srand(time(0));
                                                            59
3 ll inv(ll a, ll m) { // com gcd
      11 x, y;
                                                                    11 N;
                                                            61
      gcd(a, m, x, y);
                                                            62
                                                                    cin >> N;
      return (((x % m) +m) %m);
                                                            63
7 }
                                                                    11 \text{ div} = \text{rho(N)};
                                                            64
                                                                    cout << div << " " << N/div << endl;
_{9} ll inv(ll a, ll phim) { // com phi(m), se m for primo _{66}^{\circ}
       entao phi(m) = p-1
      11 e = phim - 1;
10
                                                                    // Finding all divisors
                                                            68
      return fexp(a, e);
11
                                                            69
                                                                    vector < 11 > div;
                                                            70
                                                            71
  5.8 Pollard-Rho
                                                                    while(N>1 and !rabin(N))
                                                             72
                                                            73
                                                            74
                                                                        11 d = rho(N);
1 // Pollard Rho Algorithm
                                                            75
                                                                        div.pb(d);
                                                                        while (N%d==0)
                                                            76
3 #include <bits/stdc++.h>
                                                                            N/=d;
4 #define ll long long
                                                            78
                                                            79
                                                                    if(N!=1)
6 using namespace std;
                                                                        div.pb(N);
                                                            80
                                                            81
8 ll llrand()
                                                            82
                                                                    return 0;
9 {
       11 tmp = rand();
                                                            83
      return (tmp << 31) | rand();
                                                            84 }
11
12 }
```

5.9 Verif-primo

```
1 // prime verification sqrt(N)
2
3 bool eh_primo(long long N)
4 {
5     if(N==2)
6         return true;
7     else if(N==1 or N%2==0)
8         return false;
9     for(long long i=3;i*i<=N;i+=2)
10         if(N%i==0)
11         return false;
12     return true;
13 }</pre>
```

5.10 Crivo

5.11 FFT-golfbot

```
1 #include <bits/stdc++.h>
3 using namespace std;
5 const int N = (1<<19);</pre>
6 const double two_pi = 4 * acos(0);
8 struct cpx
9 {
10
       cpx(){}
       cpx(double aa): a(aa){}
11
       cpx(double aa, double bb):a(aa),b(bb){}
       double a:
13
14
       double b:
       double modsq(void) const
15
16
           return a*a+b*b;
      }
18
       cpx bar(void) const
19
20
           return cpx(a,-b);
21
       }
22
23 };
25 \text{ cpx b[N+100]};
26 cpx c[N+100];
27 cpx B[N+100];
28 cpx C[N+100];
29 int a[N+100];
30 int x[N+100];
31 double coss[N+100], sins[N+100];
32 int n,m,p;
34 cpx operator +(cpx a,cpx b)
35 €
       return cpx(a.a+b.a,a.b+b.b);
37 }
38
```

```
39 cpx operator *(cpx a,cpx b)
40 {
        return cpx(a.a*b.a-a.b*b.b,a.a*b.b+a.b*b.a);
41
42 }
43
44 cpx operator /(cpx a,cpx b)
45 {
        cpx r = a*b.bar();
46
        return cpx(r.a/b.modsq(),r.b/b.modsq());
47
48 }
49
50 cpx EXP(int i,int dir)
51 {
        return cpx(coss[i],sins[i]*dir);
52
53 }
54
55 void FFT(cpx *in,cpx *out,int step,int size,int dir)
56 €
57
        if(size<1) return;</pre>
        if(size==1)
58
        {
59
            out [0] = in [0];
60
            return:
61
        }
62
        FFT(in,out,step*2,size/2,dir);
63
64
        FFT(in+step,out+size/2,step*2,size/2,dir);
65
        for(int i=0;i<size/2;++i)</pre>
        {
66
67
            cpx even=out[i];
            cpx odd=out[i+size/2];
68
            out[i] = even+EXP(i*step,dir)*odd;
69
            \verb"out[i+size/2] = \verb"even+EXP" ((i+size/2)*step,dir)*
70
        odd:
71
72 }
74 int main()
75 {
76
        for(int i=0;i<=N;++i)</pre>
77
78
            coss[i]=cos(two_pi*i/N);
            sins[i]=sin(two_pi*i/N);
79
80
        while(cin >> n) // Numero de tacadas possiveis
81
82
            fill(x,x+N+100,0);
83
            fill(a,a+N+100,0);
84
            for (int i=0; i < n; ++i)</pre>
86
            {
87
                 cin >> p; // Distancia das tacadas
88
                 x[p]=1;
89
            for(int i=0;i<N+100;++i)</pre>
90
            {
91
92
                 b[i]=cpx(x[i],0);
93
            cin >> m; // Querys
94
95
            for (int i=0;i<m;++i)</pre>
96
            {
                 cin >> a[i]; // Distancia da query
97
98
            FFT(b,B,1,N,1);
99
            for(int i=0;i<N;++i)</pre>
100
                 C[i]=B[i]*B[i]:
101
            FFT(C,c,1,N,-1);
            for (int i=0; i < N; ++i)</pre>
103
                 c[i]=c[i]/N;
104
            int cnt=0;
105
            for(int i=0;i<m;++i)</pre>
106
                 if(c[a[i]].a>0.5 || x[a[i]])
107
                     cnt++:
108
             cout << cnt << endl;</pre>
110
        }
```

```
return 0;
                                                                    return res:
                                                             21
112 }
                                                             22 }
                                                             23
   5.12 Modular-Factorial
                                                             24 vector < vl > fexp(vector < vl > b, ll e, int n) {
                                                                    if(e == 0) {
                                                                        vector <vl> id:
                                                             26
 1 // C++ program to comput n! % p using Wilson's
                                                                        for(int i = 0; i < n; i++) {</pre>
                                                             27
                                                                             vl tmp;
                                                             28
 2 #include <bits/stdc++.h>
                                                                             for(int j = 0; j < n; j++) {</pre>
                                                             29
 3 using namespace std;
                                                                                 if(i == j)
                                                                                     tmp.pb(1);
                                                             31
 5 int power(int x, unsigned int y, int p)
                                                                                 else
                                                                                     tmp.pb(0);
                                                             33
       int res = 1;
                                                             34
       x = x \% p;
                                                             35
                                                                             id.pb(tmp);
 9
                                                             36
       while (y > 0)
10
                                                             37
11
                                                                        return id;
                                                             38
           if(y & 1)
12
                                                             39
               res = (res * x) % p;
13
                                                             40
14
                                                                    vector < vl > res = fexp(b, e/2, n);
                                                             41
           y = y >> 1;
15
                                                                    res = mult(res, res, n);
                                                             42
           x = (x * x) \% p;
16
                                                             43
17
                                                                    if(e%2)
                                                             44
18
       return res;
                                                                        res = mult(res, b, n);
                                                             45
19 }
                                                             46
20
                                                             47
                                                                    return res;
21 int modInverse(int a, int p)
                                                             48 }
22 {
                                                             49
       return power(a, p-2, p);
                                                             50 // k = tamanho da recorrencia/matriz, n = n-esimo
24 }
                                                             51 // f(n) = c1*f(n-1) + c2*f(n-2) + ... + ck*f(n-k)
26 int modFact(int n, int p)
                                                             _{52} // base -> [f(k-1), f(k-2), ..., f(0)]
27 {
                                                             53 // coeficientes -> [c1, c2, ..., ck]
       if (p \le n)
28
                                                            54 vl solve(int k, int n, vl base, vl coef) {
           return 0;
29
                                                                    vector < vl> inicial;
30
                                                                    inicial.pb(coef);
                                                             56
       int res = (p - 1);
31
                                                                    for(int row = 0; row < k-1; row++) {
                                                            57
32
                                                                        vl tmp;
                                                             58
33
       for(int i = n + 1; i < p; i++)
                                                                        for(int col = 0; col < k; col++) {</pre>
                                                             59
           res = (res * modInverse(i, p)) % p;
34
                                                                            if(col == row)
                                                             60
35
       return res;
                                                                                tmp.pb(1);
                                                             61
36 }
                                                             62
                                                             63
                                                                                 tmp.pb(0);
38 int main()
                                                             64
39 {
                                                             65
                                                                        inicial.pb(tmp);
       int n = 25, p = 29;
40
                                                             66
       cout << modFact(n, p);</pre>
41
       return 0;
                                                                    vector < vl > matexp = fexp(inicial, max(0, n-k+1),
                                                             68
43 }
                                                                    k);
                                                                    vl res(k);
   5.13 Recursao-linear
                                                                    for(int row = 0; row < k; row++) {</pre>
                                                                        ll val = 0;
 _{1} vector<vl> mult(vector<vl> a, vector<vl> b, int n) { ^{72}
                                                                        for(int aux = 0; aux < k; aux++) {</pre>
       vector < vl> res;
                                                             73
 2
                                                             74
                                                                             val += matexp[row][aux]*base[aux];
 3
       for(int i = 0; i < n; i++) {</pre>
                                                             75
           vl tmp;
           for(int j = 0; j < n; j++) {
                                                                        res[row] = val; // res = (f(n), f(n-1), ...,
                                                             76
                tmp.pb(0);
                                                                    f(n-k+1)
                                                             78
           res.pb(tmp);
 8
                                                             79
                                                                    return res;
       }
 9
                                                             80 }
10
       for(int row = 0; row < n; row++) {</pre>
                                                              5.14 Kamenetsky
            for(int col = 0; col < n; col++) {</pre>
12
                11 \text{ val} = 0;
13
                for(int k = 0; k < n; k++) {</pre>
                                                             1 // Number of digits in n! O(1)
14
                    val += (a[row][k]*b[k][col]);
15
                                                             3 #define Pi 3.14159265358979311599796346854
                res[row][col] = val;
                                                              4 #define Eul 2.71828182845904509079559829842
17
           }
       }
                                                              6 long long findDigits(int n)
19
                                                              7 {
20
```

```
double x;
                                                                       S == 40 //(101000)
                                                           36
                                                           37
      if (n < 0)
                                                                  // Check the j-th element
10
                                                           38
11
          return 0;
                                                           39
      if (n == 1)
                                                                       int S = 42; //(101010)
          return 1:
                                                                       int j = 3;
13
                                                           41
14
      x = ((n * log10(n / euler) + log10(2 * Pi * n))
                                                                       T = S & (1 << j); // T = 0
15
                                                           43
      /2.0));
                                                           44
                                                                  // Least significant bit (lsb)
16
                                                           45
      return floor(x) + 1;
17
                                                           46
18 }
                                                            47
                                                                       int lsb(int x){ return x&-x; }
                                                           48
                                                                  // Exchange o j-th element
                                                           49
       Misc
                                                           50
                                                                       S = (1 << j)
                                                           51
  6.1 LIS
                                                                  // Position of the first bit on
                                                           53
n multiset < int > S;
                                                                       T = (S \& (-S))
                                                           55
2 for(int i = 0; i < n; i++){</pre>
                                                                       T \rightarrow 4 bit ligado //(1000)
                                                           56
      auto it = S.upper_bound(vet[i]); // low for inc
                                                           57
      if(it != S.end())
                                                           58
                                                                  // Most significant digit of N
          S.erase(it);
                                                           59
      S.insert(vet[i]);
                                                                       double K = log10(N);
                                                           60
7 }
                                                           61
                                                                       K = K - floor(K);
8 // size of the lis
                                                                       int X = pow(10, K);
                                                           62
9 int ans = S.size();
                                                           63
                                                                  // Number of digits in N
                                                           64
  6.2 Bitwise
                                                           65
                                                                       X = floor(log10(N)) + 1;
1 // Bitwise
                                                           67
                                                                  // Power of two
      unsigned char a = 5, b = 9; // a = (00000101), b 69
3
                                                                       bool isPowerOfTwo(int x){ return x && (!(x&(x
      = (00001001)
                                                                  -1))); }
       AND -
                       a&b
                           // The result is 00000001
                                                           71
                                                                  // Turn off the first bit 1
                                                           72
       (1)
                             // The result is 00001101
                                                                      m = m \& (m-1);
      OR -
                       alb
                                                           73
       (13)
                                                           74
                       a^b
                             // The result is 00001100
                                                                  // Built-in functions
      XOR. -
       (12)
                                                           76
                                                                       // Number of bits 1
      NOT -
                             // The result is 11111010
                                                           77
                       ~a
                                                           78
                                                                       __builtin_popcount()
       (250)
                                                                       __builtin_popcountl1()
                      b<<1 // The result is 00010010
                                                           79
      Left shift -
                                                                      // Number of leading zeros
      Right shift - b >> 1 // The result is 00000100
                                                           81
                                                                       __builtin_clz()
       (4)
                                                                       __builtin_clzl1()
                                                           83
                                                           84
      // Exchange two int variables
12
                                                                       // Number of trailing zeros
                                                           85
13
                                                                       __builtin_ctz()
           a^=b;
                                                           86
14
                                                                       __builtin_ctzll()
           b^=a;
                                                           87
15
           a^=b;
                                                           88
16
                                                           89
                                                                  // floor(log2(x))
17
                                                           90
      // Even or Odd
18
                                                                       int flog2(int x){ return 32-1-__builtin_clz(x
                                                           91
19
           (x & 1)? printf("Odd"): printf("Even");
20
                                                           92
                                                                       int flog211(11 x){ return 64-1-
22
      // Turn on the j-th bit
                                                                   __builtin_clzll(x); }
23
           int S = 34; //(100010)
24
                                                              6.3
                                                                    Template
           int j = 3;
25
           S = S | (1 << j);
                                                            #include <bits/stdc++.h>
27
                                                            2 #define ff first
      // Turn off the j-th bit
29
                                                            3 #define ss second
                                                            4 #define ll long long
30
           int S = 42; //(101010)
                                                            5 #define ld long double
                                                            6 #define pb push_back
           int j = 1;
32
                                                            7 #define eb emplace_back
           S &= ~(1<<j)
                                                            8 #define mp make_pair
34
                                                            9 #define mt make_tuple
35
```

```
10 #define pii pair<int, int>
                                                                if(result==0)
11 #define vi vector<int>
                                                                    return string();
12 #define sws ios_base::sync_with_stdio(false);cin.tie(30
                                                                return X.substr(end - result + 1, result);
13 #define endl '\n'
14 #define teto(a, b) (a+b-1)/(b)
                                                                 Pal-int
                                                            7.3
16 const int MAX = 400010;
17 const int MOD = 1e9+7;
                                                         bool ehpalindromo(ll n)
18 const int INF = 0x3f3f3f3f;
                                                          2 {
19 const 11 LLINF = 0x3f3f3f3f3f3f3f3f3f3f;
                                                          3
                                                                if(n<0)
20 const ld EPS = 1e-7;
                                                                    return false;
22 using namespace std;
                                                                int divisor = 1;
                                                          6
                                                                while(n/divisor >= 10)
       Strings
                                                                    divisor *= 10;
                                                          9
                                                                while (n != 0)
  7.1 KMP
                                                         11
                                                                    int leading = n / divisor;
                                                         12
vector<int> preffix_function(const string &s){
                                                         13
                                                                    int trailing = n % 10;
      int n = s.size(); vector<int> b(n+1);
                                                         14
      b[0] = -1; int i = 0, j = -1;
                                                                    if(leading != trailing)
      while(i < n){
                                                                        return false;
                                                         16
          while(j >= 0 && s[i] != s[j]) j = b[j];
          b[++i] = ++j;
6
                                                                    n = (n \% divisor)/10;
                                                         18
      }
                                                         19
      return b:
                                                         20
                                                                    divisor = divisor/100;
9 }
                                                         21
void kmp(const string &t, const string &p){
                                                         22
      vector<int> b = preffix_function(p);
11
                                                                return true;
                                                         23
12
      int n = t.size(), m = p.size();
      int j = 0;
13
      for(int i = 0; i < n; i++){
                                                           7.4 Z-Func
          while(j >= 0 && t[i] != p[j]) j = b[j];
15
16
          j++;
          if(j == m){
                                                          vector < int > z_algo(const string &s)
17
                                                          2 {
18
                                                                int n = s.size();
                                                          3
              j = b[j];
                                                                int L = 0, R = 0;
          }
                                                          4
20
                                                                vector < int > z(n, 0);
                                                          5
      }
                                                                for(int i = 1; i < n; i++)
22 }
                                                          7
  7.2 LCS
                                                                    if(i <= R)
                                                                        z[i] = min(z[i-L], R - i + 1);
                                                          9
                                                                    while (z[i]+i < n \&\& s[z[i]+i] == s[z[i]])
                                                         10
string LCSubStr(string X, string Y)
                                                         11
                                                                        z[i]++:
2 {
                                                                    if(i+z[i]-1 > R)
      int m = X.size();
                                                         12
3
                                                         13
      int n = Y.size();
                                                                        L = i;
                                                         14
                                                                        R = i + z[i] - 1;
                                                         15
      int result = 0, end;
                                                                    }
                                                         16
      int len[2][n];
                                                         17
      int currRow = 0;
                                                         18
                                                                return z;
                                                         19 }
      for(int i=0;i<=m;i++){</pre>
10
          for(int j=0; j<=n; j++) {</pre>
11
                                                            7.5 Hash
              if(i==0 || j==0)
                  len[currRow][j] = 0;
13
               else if (X[i-1] == Y[j-1]){
14
                                                         1 ll compute_hash(string const& s) {
                  len[currRow][j] = len[1-currRow][j-1] 2
                                                                const ll p = 31; // primo, melhor = perto da
       + 1;
                                                                quantidade de caracteres
                   if(len[currRow][j] > result){
16
                                                                const 11 m = 1e9 + 9; // maior mod = menor
                       result = len[currRow][j];
                                                                probabilidade de colisao
17
                       end = i - 1;
                                                                11 hash_value = 0;
                   }
19
                                                                11 p_pow = 1;
              }
20
                                                                for (char c : s) {
                                                          6
21
               else
                                                                    hash_value = (hash_value + (c - 'a' + 1) *
                  len[currRow][j] = 0;
                                                                p_pow) % m;
          }
                                                                    p_pow = (p_pow * p) % m;
24
                                                          9
           currRow = 1 - currRow;
                                                                return hash_value;
                                                         10
      }
26
                                                         11 }
```

27