CSCI 305, Homework # 7

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Due date: Midnight, Tuesday, May 29

Quadratic probing. This is problem 11-3 in the book.

Suppose that we are given a key k to search for in a hash table with positions 0, 1, ..., m-1, and suppose that we have a hash function h mapping the key space into the set $\{0, 1, ..., m-1\}$. The search scheme is as follows:

- 1. Compute the value j = h(k) and set i = 0.
- 2. Probe in position j for the desired key k. If you find it, or if this position is empty, terminate the search.
- 3. Set i = i + 1. If i now equals m, the table is full, so terminate the search. Otherwise, set $j = (i + j) \mod m$ and return to step 2.

Assume that m is a power of 2.

- a. Show that this scheme is an instance of the general "quadratic probing" scheme by exhibiting the appropriate constants c_1 and c_2 for equation (11.5).
- b. Prove that this algorithm examines every table position in the worst case.