

## CSCI 305, Homework # 2

YOUR NAME HERE

Due date: Tue, May 1, midnight

In all cases, we require that  $f(n)$  and  $g(n)$  be positive functions, *i.e.*  $f(n) > 0$  and  $g(n) > 0$  for all  $n > 0$ . Prove or disprove each of the following conjectures.

1.  $f(n) = O((f(n))^2)$

$$f(n) < c(f(n))^2$$

$$c = 1$$

$$f(n) = O(f(n) * f(n))$$

Provided the result of  $f(n)$  is equal to or greater than 1 this is always true

2.  $f(n) = \Theta(f(n/2))$

3.  $f(n) + o(f(n)) = \Theta(f(n))$

4. If  $f(n) = O(g(n))$  then  $f(n) + g(n) = O(f(n))$ .

Suppose  $f(n) = O(n)$  and  $g(n) = O(n^2)$

$f(n) = O(g(n))$  would be true,

but  $f(n) + g(n) = O(f(n))$  would not be true because  $g(n) < f(n)$ .