## CSCI 305, Homework # 4

## YOUR NAME HERE

Due date: Friday, May 11, Midnight

Explain the reasoning behind each answer.

- 1. Suppose we shuffle a deck of 10 cards, each bearing a distinct number from 1 to 10, to mix the cards thoroughly. We then remove three cards, one at a time, from the deck. What is the probability that we select the three cards in sorted (increasing) order?
  - Choose any 3 cards. There are 3! combinations of ways that you could have drawn. Of the those 6 only 1 is sorted. So 1/6.
- 2. Use indicator random variables to solve the following problem, known as the **hat-check problem**. Each of *n* customers gives a hat to a hat-check person at a restaurant. The hat-check person gives the hats back to the customers in a random order. What is the expected number of customers who get back their own hat?

$$X_h = I\{\text{Getting the correct hat back}\}$$

$$X_h = 1/n$$

$$E[X] = E\left[\sum_{k=1}^n X_h\right]$$

$$E[X] = \sum_{k=1}^n E[X_h]$$

$$E[X] = \sum_{k=1}^n 1/n$$

$$E[X] = n/n$$

$$E[X] = 1$$

The expected number of customers who get there hat back is 1 for any n.